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Input: vector x, vector y
Output: coefitiens, Matrix A
begin cubicSpline
    if x or y has duplicates:
        return error
    end if
    if lenght of x is not equals to lenght of y:
        return error
    end if
    set n = lenght of x
    set m = (n - 1) * 4
    set A = matrix[m][m]
    set B = vector[m]
    set A[0][0] = x[0] ^3
    set A[0][1] = x[0]^{^2}
    set A[0][2] = x[0]
    set A[0][3] = 1
    set B[0] = y[0]
        #interpolation conditions
    For i = 0, \ldots, n
                          1
        set A[i+1][4*(i+1)-4] = \text{math.pow}(x[i+1], 3)
        set A[i+1][4*(i+1)-3] = \text{math.pow}(x[i+1], 2)
        set A[i+1][4*(i+1)-2] = x[i+1]
        set A[i+1][4*(i+1)-1] = 1
        set B[i+1] = y[i+1]
    #continuity conditions
    for i = 1, \ldots, n
        set A[n-1+i][4*i-4] = math.pow(x[i], 3)
        set A[n-1+i][4*i-3] = math.pow(x[i], 2)
        set A[n-1+i][4*i-2] = x[i]
        set A[n-1+i][4*i-1] = 1
        set A[n-1+i][4*i] = -math.pow(x[i], 3)
        set A[n-1+i][4*i+1] = -math.pow(x[i], 2)
        set A[n-1+i][4*i+2] = -x[i]
        {\rm set}\ A [\,n-1+i\,\,] \,[\,4*i\,+3] \,=\, -1
        set B[n-1+i] = 0
    #softness condition
    for i = 1, \ldots, n
                          1
        set A[2*n-3+i][4*i-4] = 3 * math.pow(x[i], 2)
        set A[2*n-3+i][4*i-3] = 2 * x[i]
        set set A[2*n-3+i][4*i-2] = 1
        set A[2*n-3+i][4*i-1] = 0
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set A[2*n-3+i][4*i] = -3 * math.pow(x[i], 2)
    set A[2*n-3+i][4*i+1] = -2 * x[i]
    set A[2*n-3+i][4*i+2] = -1
    set A[2*n-3+i][4*i+3] = 0
    set B[2*n-3+i] = 0
#concavity conditions
for i = 1, \ldots, n
    set A[3*n-5+i][4*i-4] = 6 * x[i]
    set A[3*n-5+i][4*i-3] = 2
    set A[3*n-5+i][4*i-2] = 0
    set A[3*n-5+i][4*i-1] = 0
    set A[3*n-5+i][4*i] = -6 * x[i]
    set A[3*n-5+i][4*i+1] = -2
    set A[3*n-5+i][4*i+2] = 0
    set A[3*n-5+i][4*i+3] = 0
    set B[n+5+i] = 0
#boundary conditions
set A[m-2][0] = 6 * x[0]
set A[m-2][1] = 2
set A[m-1][m-4] = 6 * x[n-1]
set A[m-1][m-3] = 2
x = solveSystem(A, B)
return x, A
```

 $end \ cubic Spline$