

numpy as np is python numpy library to converts to array a matrix
matrix_function.solution:
Method in matrix_function that do a progressive or backward substitution
to find an array

Input: matrix matrix
Output: solution array x

begin steppedMethod

```
dict dictionary
auxiliary_matrix <- np.array(matrix)
dictionary[0] <- matrix
int count = 0
array temporal_array
while (count < matrix.shape[0]-1) do:
    float pivot_number <- auxiliary_matrix
    if (count == 0):
        for row in auxiliary_matrix:
            pivot_column <- np.abs(row[-1])
            temporal_maxpivot <- np.max(pivot_column)
            temporal_array.add(temporal_maxpivot)
        end for
    end if
    sub_matrix <- auxiliary_matrix.T[0]
    division_colum = np.abs(sub_matrix)/temporal_array[count:]
    posmax_pivot <- np.where(division_colum ==
        np.max(division_colum))[0][0]
    if (posmax_pivot != 0):
        pivot_number <- auxiliary_matrix[posmax_pivot][0]
        temporal_matrix <- np.array(auxiliary_matrix[0])
        auxiliary_matrix[0] <- np.array(auxiliary_matrix[posmax_pivot])
        auxiliary_matrix[posmax_pivot] <- temporal_matrix
        temporal_matrix <- np.array(matrix[i])
        matrix[i] <- np.array(matrix[i+posmax_pivot])
        matrix[i+posmax_pivot] <- temporal_matrix
    end if
    if (pivot_number==0 and i == matrix.shape[0]-2):
        break;
    end if
    fj <- auxiliary_matrix[0]
    column_vector <- np.reshape(auxiliary_matrix.T[0][1:],
    (auxiliary_matrix.T[0][1:].shape[0], 1))
    multiplier <- column_vector/pivot_number
    fi <- auxiliary_matrix[1:]
```

```

fi <- fi - (multiplier*fj)
  if(count == 0):
    matrix[i+1:] <- fi
  else:
    auxiliary_fi <- fi
    while (auxiliary_fi.shape[1]+1 < matrix[i+1:].shape[1]):
      auxiliary_fi <- np.insert(auxiliary_fi ,
                                0, np.zeros(1), axis=1)
      matrix[i+1:] <- np.insert(auxiliary_fi , 0,
                                np.zeros(1), axis=1)
    auxiliary_matrix <- fi.T[1:].T
    dictionary[count+1] <- np.array(matrix)
  end while
a <- np.delete(matrix , matrix.shape[1]-1 , axis=1)
b <- matrix.T[matrix.shape[1]-1]
return matrix_function.soltion(a,b)

end steppedMethod

```