An executable formal semantics for PHP

Daniele Filaretti & Sergio Maffeis

www.phpsemantics.org



ECOOP 2014 Uppsala, Sweden















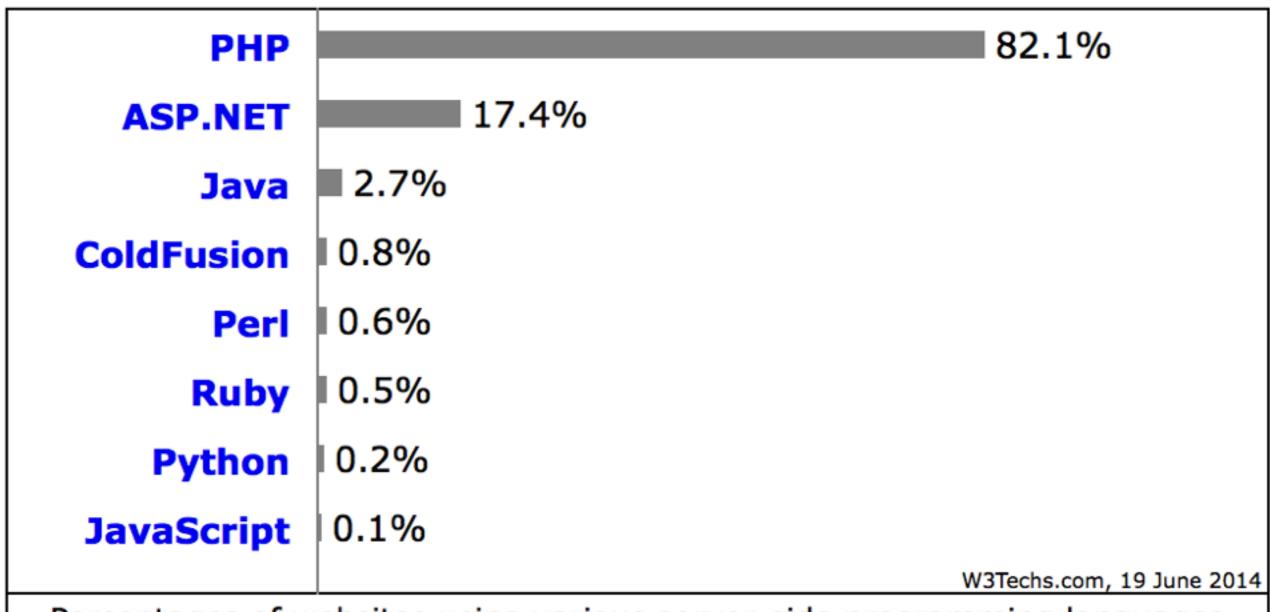












Percentages of websites using various server-side programming languages Note: a website may use more than one server-side programming language

http://w3techs.com/technologies/overview/programming_language/all

Analyzing PHP An introduction to PHP-Sat *

RIPS - A static source code analyser for vulnerabilities in PHP scripts

Eric Bouwers embouwer@cs.uu.nl

Center for Software Technology Universiteit Utrecht, The Netherlands

Johannes Dahse

Automated Security Review of PHP Web Applications with
Static Code Analysis

An evaluation of current tools and their applicability*

PHP Aspis: Using Partial Taint Tracking To Protect Against Injection Attacks

Ioannis Papagiannis Imperial College London

Matteo Migliavacca Imperial College London

Peter Pietzuch Imperial College London

Static Approximation of Dynamically Generated Web Pages

Yasuhiko Minamide
Department of Computer Science
University of Tsukuba
Tsukuba 305-8573, Japan
minamide@cs.tsukuba.ac.jp

Systematic Analysis of XSS Sanitization in Web Application Frameworks

Soft typing and analyses on PHP programs

On Using Static Analysis to Detect Type Errors in PHP Applications

EPFL-REPORT-147867

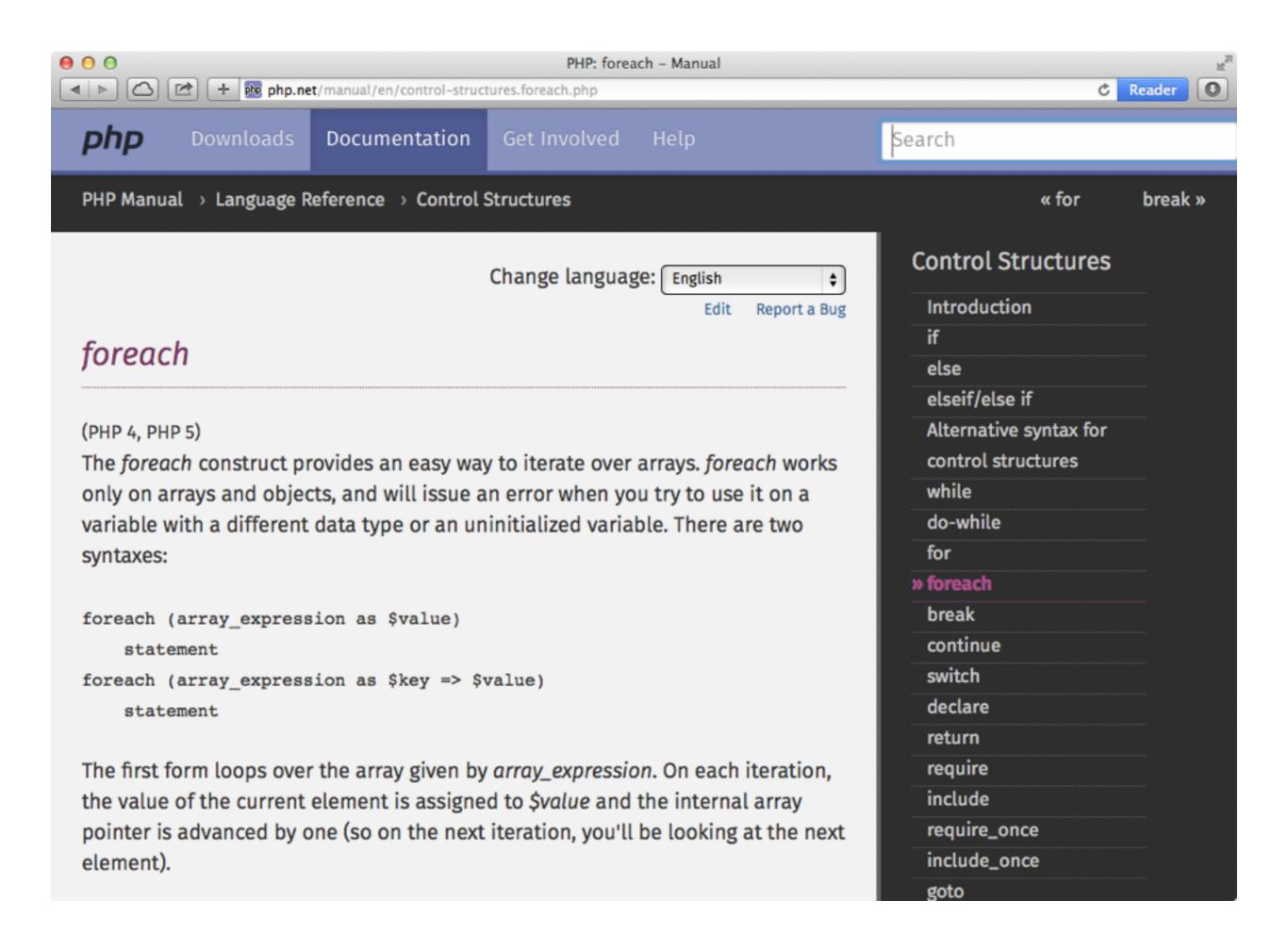
Patrick Camphuijsen

SAFERPHP:

Finding Semantic Vulnerabilities in PHP Applications

Limitations

- partial coverage of the language i.e. features ignored because "too hard" for analysis
- sometimes, features modelled incorrectly
- no formal guarantees of soundness



Absence of a specification

Absence of a specification

HHVM releases PHP spec on 30th July 2014

```
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c;
```

```
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // "onetwo"
```

```
a = array("one");
c = a[0] \cdot (a[0] = "two");
echo $c; // "onetwo"
$a = "one";
c = a . (a = "two");
echo $c;
```

```
a = array("one");
c = a[0] \cdot (a[0] = "two");
echo $c; // "onetwo"
$a = "one";
c = a . (a = "two");
echo $c; // "twotwo"
```

```
$a = array("a", "b", "c");
foreach($a as &$v) {};
foreach($a as $v) {};
var_dump($a);
```

```
a = array("a", "b", "c");
foreach($a as &$v) {};
foreach($a as $v) {};
var dump($a);
  array(3) {
     [0] \Rightarrow string(1)
                       "a"
     [1] \Rightarrow string(1)
                        "b"
     [2] \Rightarrow \&string(1)
```

```
$x = array(1, 2, 3);
$y = $x;
$x[0] = "updated";
echo $y[0];  // prints 1
```

```
$x = array(1, 2, 3);
$temp = &$x[1]; // aliasing!
$y = $x; // assign normally
$x[0] = "regular"; // no shared
$x[1] = "shared"; // shared
```

```
$x = array(1, 2, 3);
$temp = &$x[1]; // aliasing!
$y = $x; // assign normally
$x[0] = "regular"; // no shared
$x[1] = "shared"; // shared
```

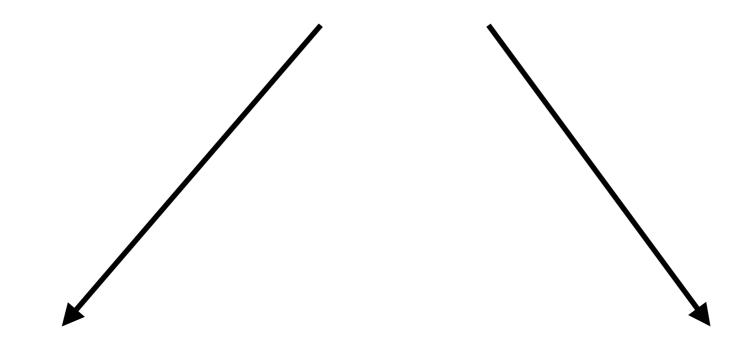
PHP tricky features

- Aliasing
- Complex array and object iteration
- Automatic type conversions
- Complex array copy
- Complex instance variable lookup
- Variable variables

Challenge

- Dynamic scripting language
- Not specified
- Documentation often incomplete
- Source of confusion for developers but also security specialists, tool designers etc.

Contribution: A *Trusted* Executable Formal Semantics of PHP

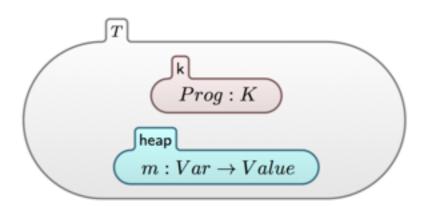


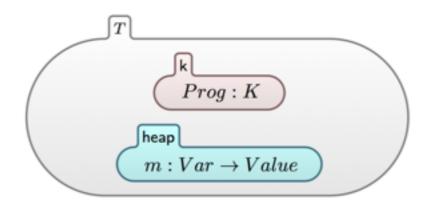
foundation for reliable tool development

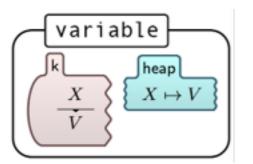
the missing specification

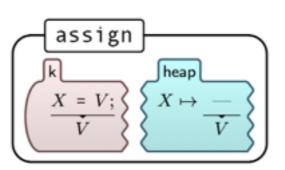
Methodology

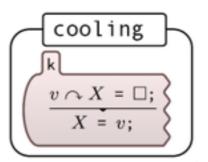
- Semantics must be based on experiments and testing against the "reference" implementation
 - Need a tight test-design loop
- We use the K Framework (UIUC)
 - amenable to formal proofs
 - executable
 - supports LTL model checking and symbolic execution





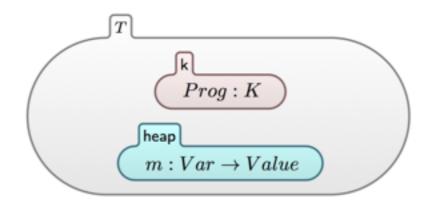


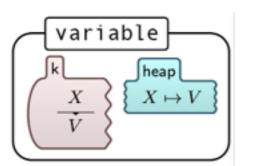


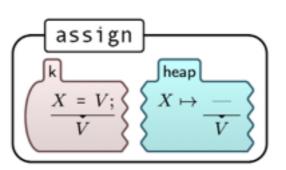


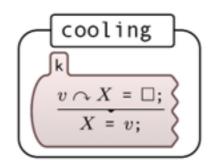
heating
$$X = E;$$

$$E \cap X = \square;$$





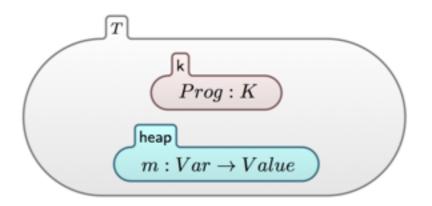




heating
$$X = E;$$

$$E \curvearrowright X = \square;$$

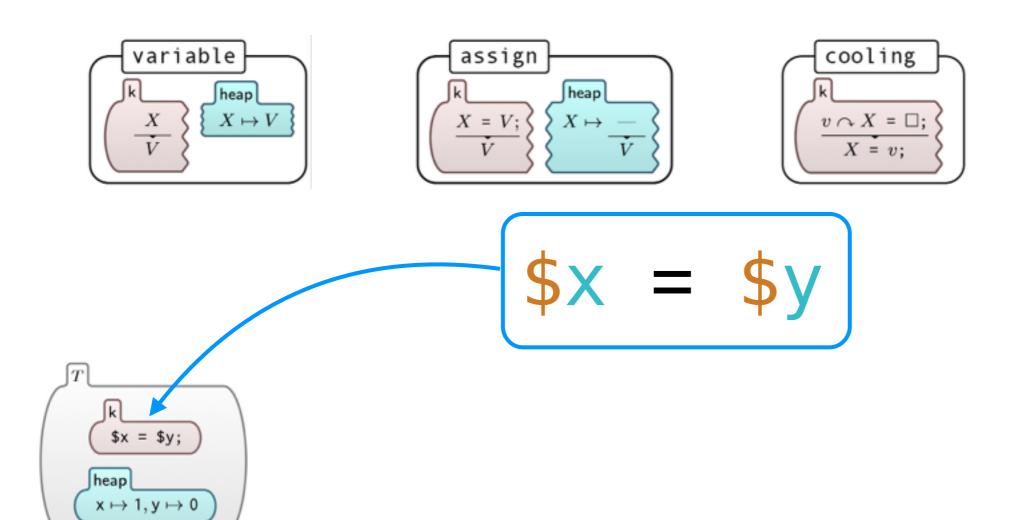
$$$x = $y$$

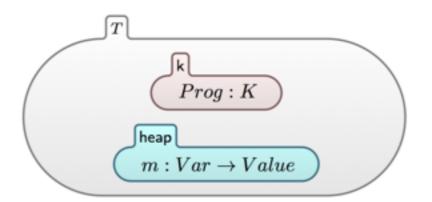


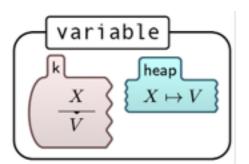
heating

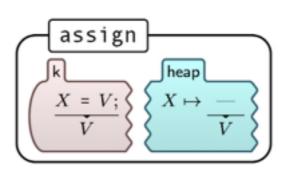
X = E;

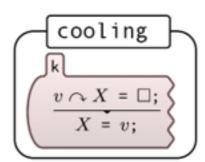
 $E \curvearrowright X = \square;$

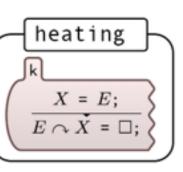


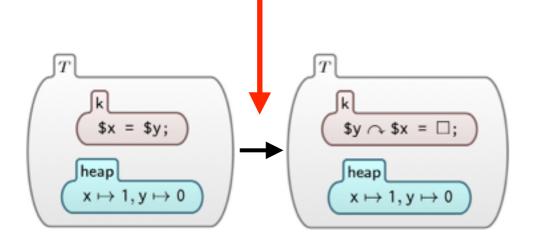


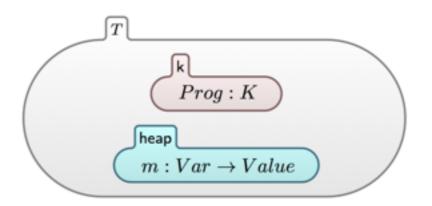








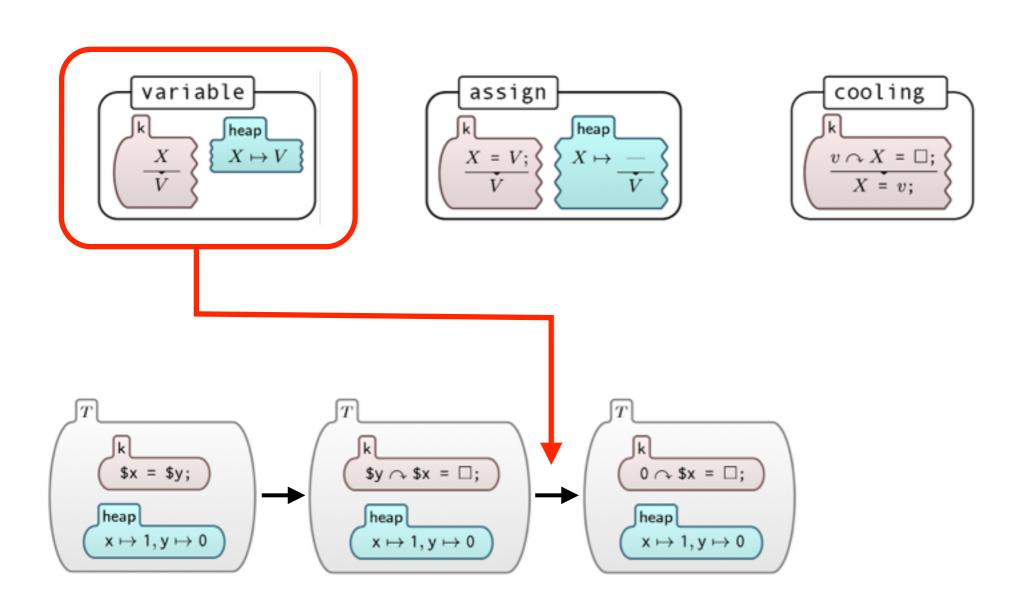


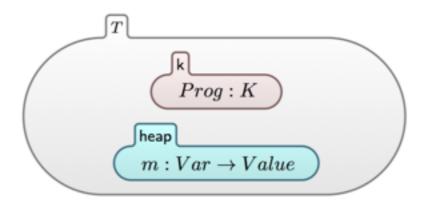


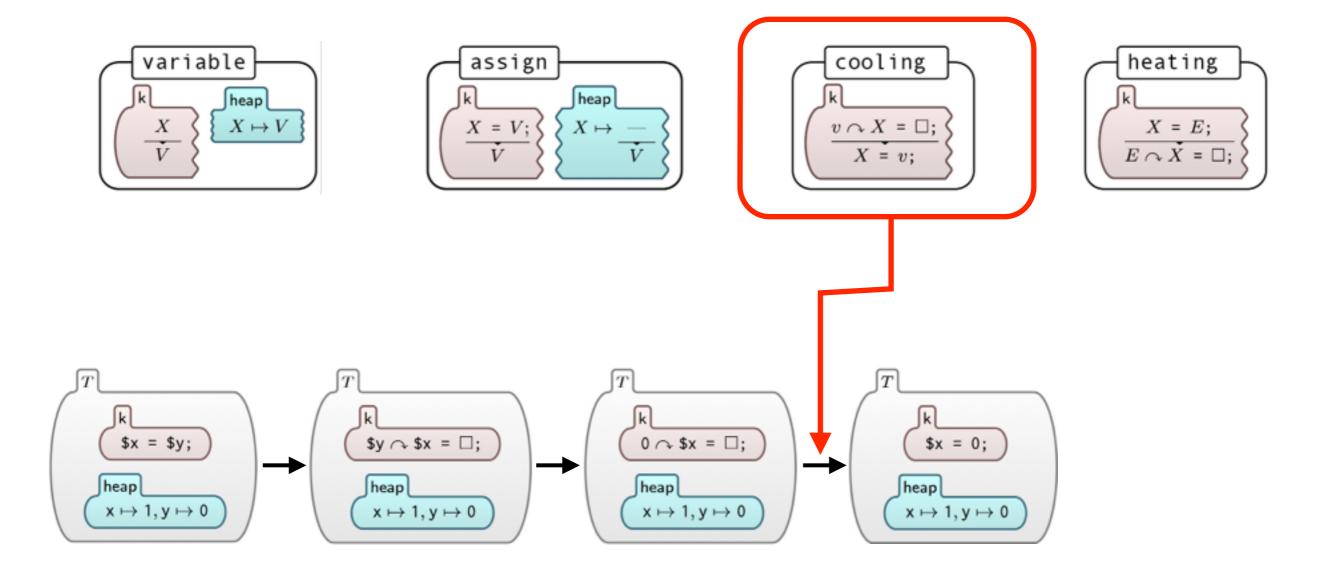
heating

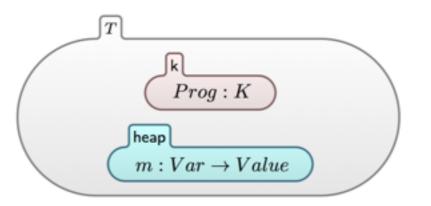
X = E;

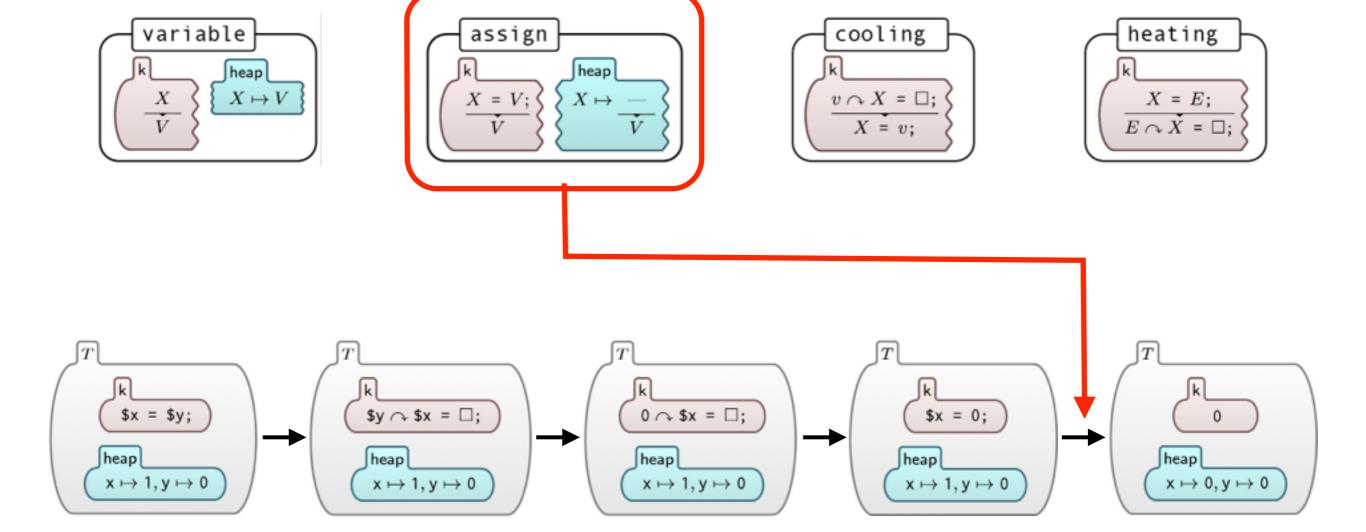
 $E \curvearrowright X = \square;$









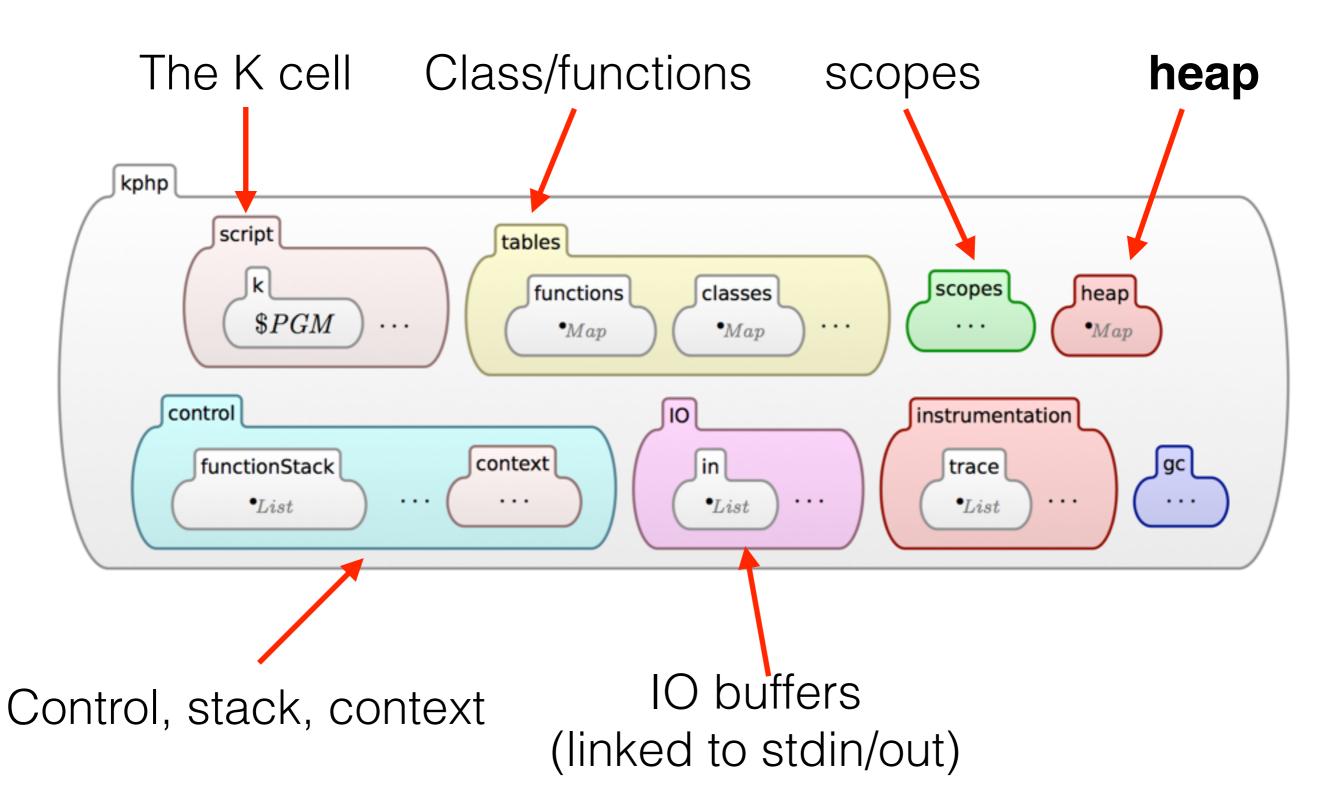


KPHP (Formalising PHP in K)

www.phpsemantics.org



Configuration (~30 cells)



Language Values

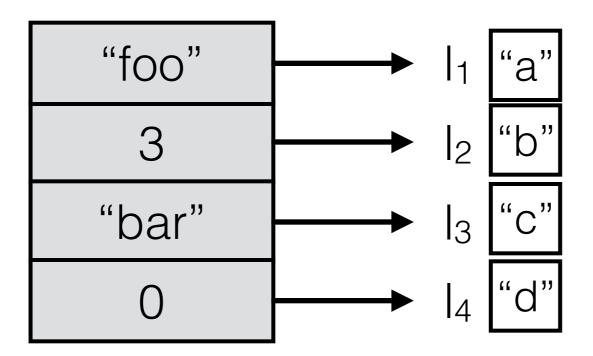
Scalar	Compound	Special
boolean	array	resource
integer	object	NULL
float		
string		

Language Values

Scalar	Compound	Special
boolean	array	resource
integer	object	NULL
float		
string		

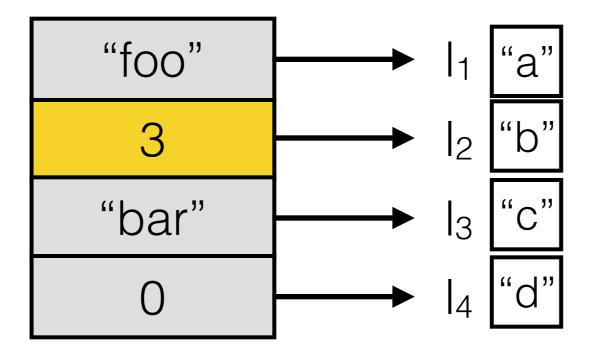
Arrays

Int U String —> Locations



Arrays

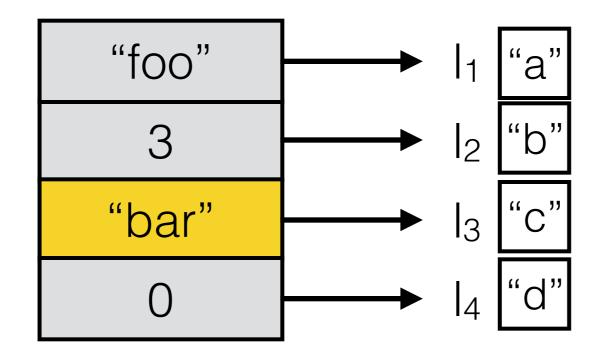
Int U String —> Locations



echo current(\$x) // "b"

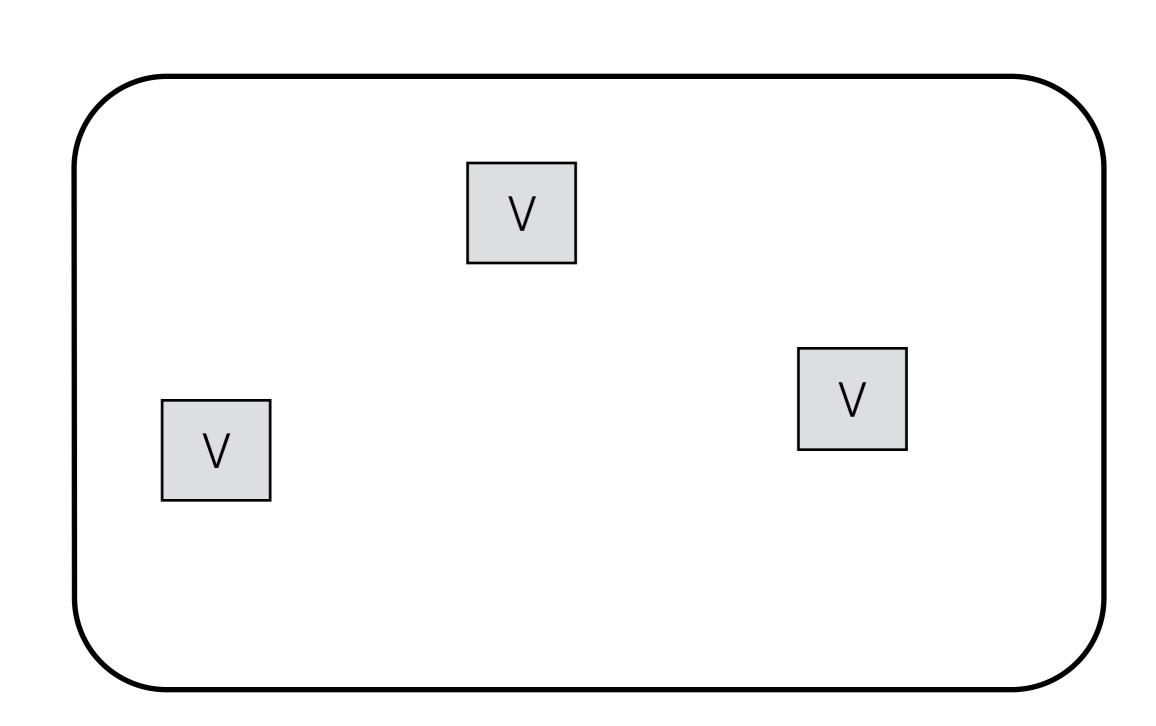
Arrays

Int U String —> Locations

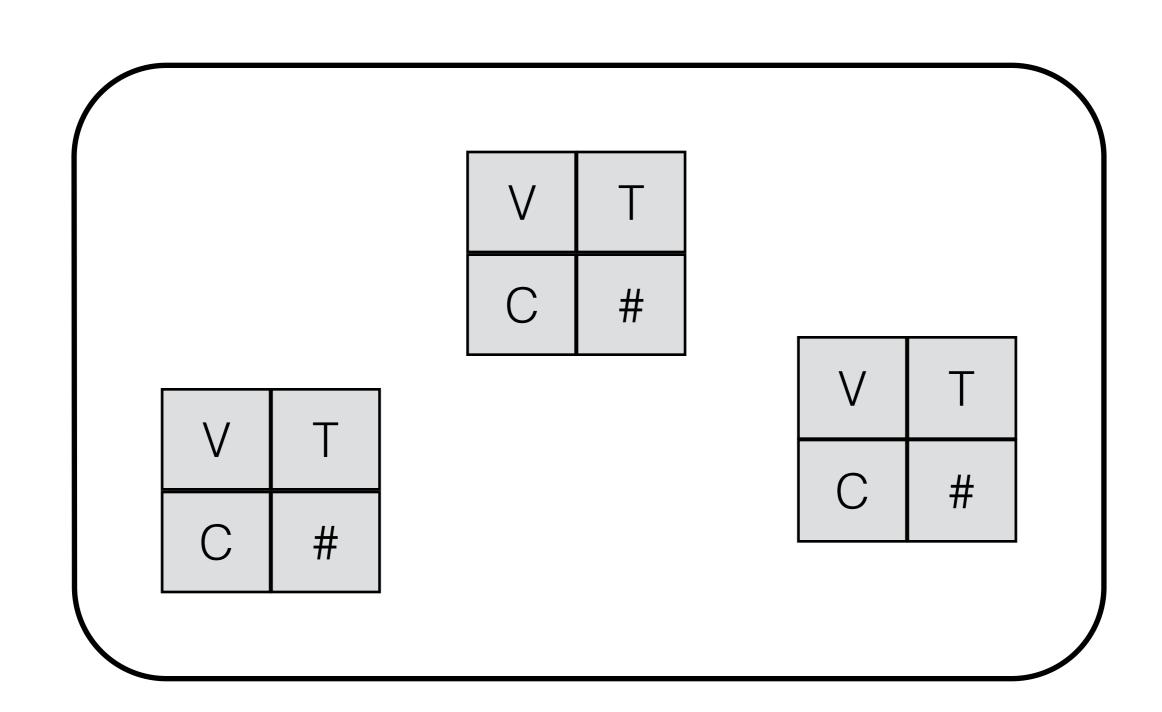


```
echo current($x) // "b"
next($x);
echo current($x) // "c"
```

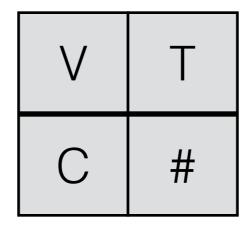
Values and Z-Values

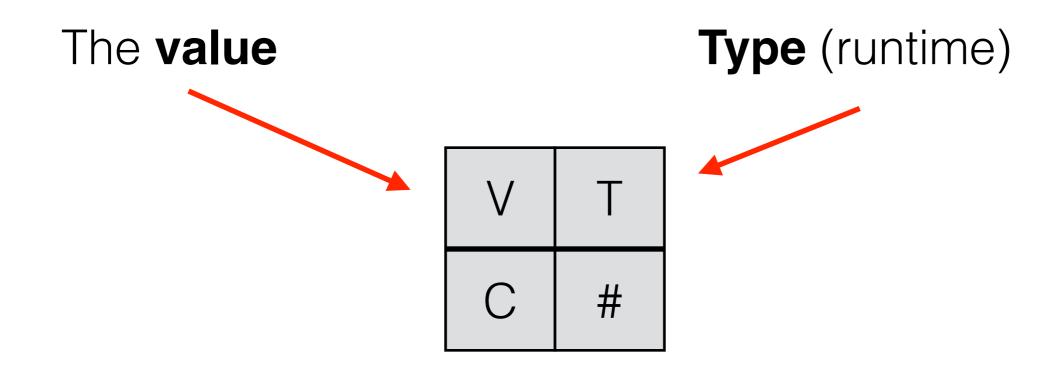


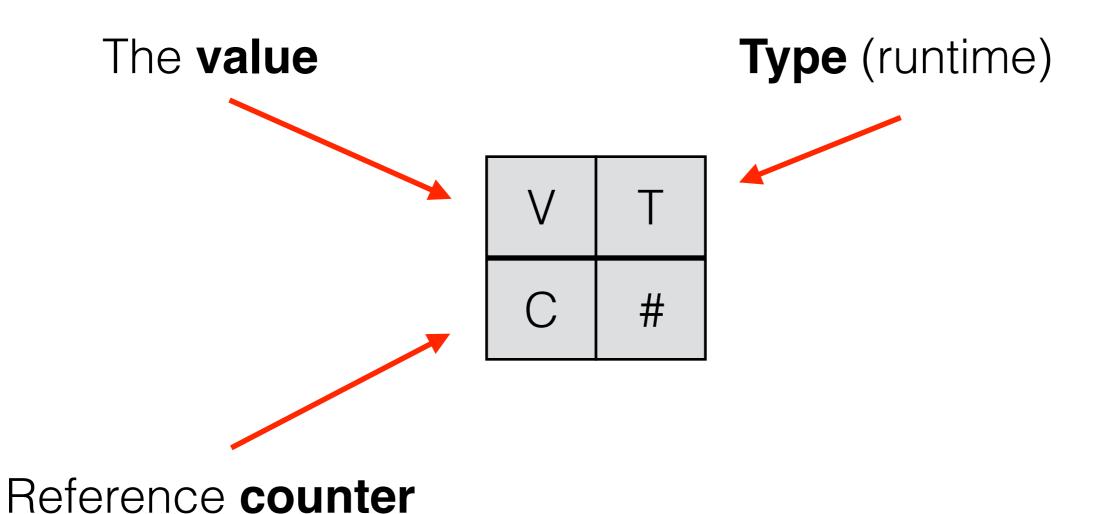
Values and **Z-Values**

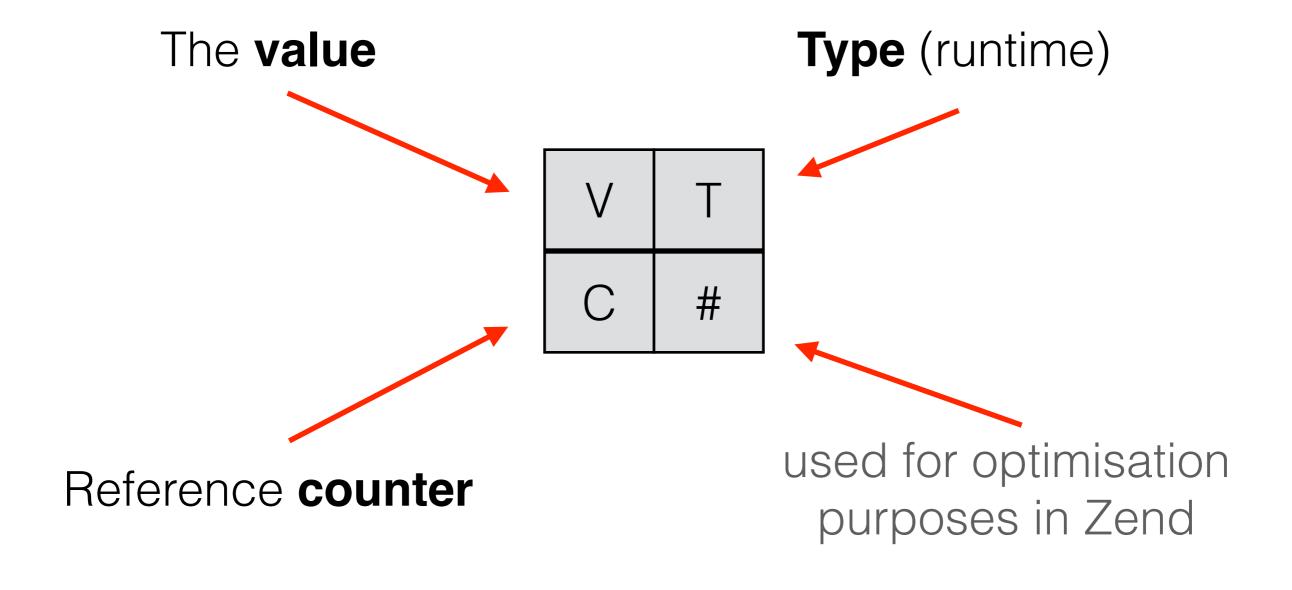






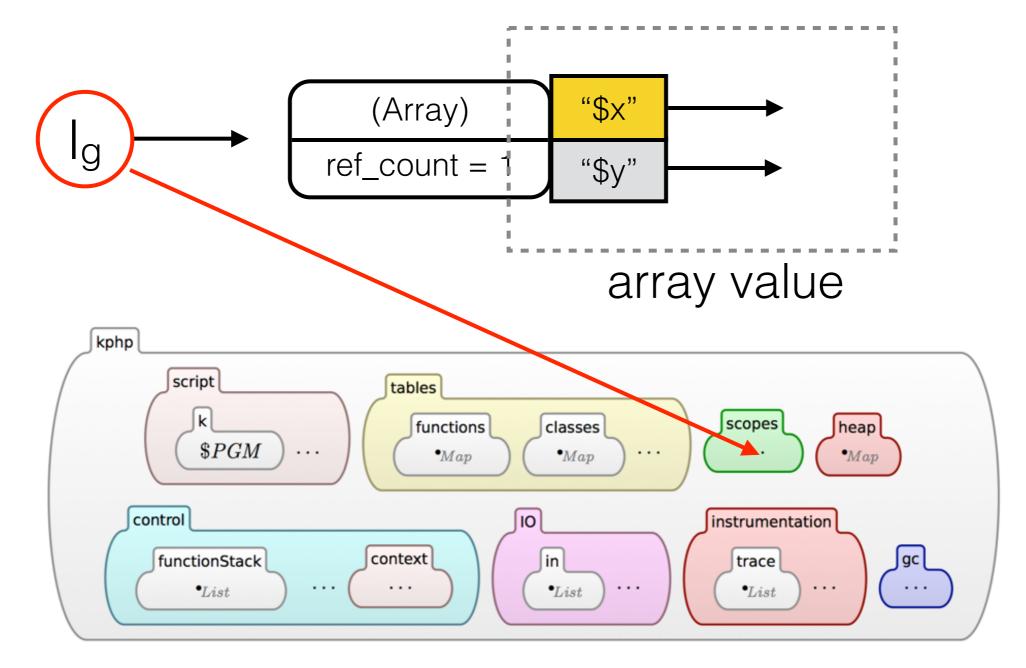






Scopes via arrays

heap: Loc -> Z-Value



```
$x = array("foo" => 5, "bar" => 5); $y = 5;
next($x);
$x["baz"] = &$x["bar"];
$x [12] = 5;
```

```
(Array)
ref\_count = 1
```

```
x = array("foo" => 5, "bar" => 5);  y = 5;
next($x);
x["baz"] = &x["bar"];
x [12] = 5;
                                                          (Int) 5
                                                       ref_count = 1
                                            "foo"
                                (Array)
  I_g
                                            "bar"
                                                          (Int) 5
                              ref_count = 1
                   "$x"
       (Array)
                                                       ref_count = 1
     ref_count = 1
```

```
x = array("foo" => 5, "bar" => 5);  y = 5;
next($x);
x["baz"] = &x["bar"];
x [12] = 5;
                                                            (Int) 5
                                                         ref_count = 1
                                             "foo"
                                  (Array)
  I_g
                                             "bar"
                                                            (Int) 5
                               ref_count = 1
                    "$x"
        (Array)
                                                         ref_count = 1
     ref_count = 1
                    "$y"
                                  (Int) 5
                               ref_count = 1
```

```
x = array("foo" => 5, "bar" => 5);  y = 5;
next($x);
x["baz"] = &x["bar"];
x [12] = 5;
                                                            (Int) 5
                                                         ref_count = 1
                                              "foo"
                                  (Array)
  I_g
                                             "bar"
                                                            (Int) 5
                               ref_count = 1
                    "$x"
        (Array)
                                                         ref_count = 1
     ref_count = 1
                    "$y"
                                  (Int) 5
                               ref_count = 1
```

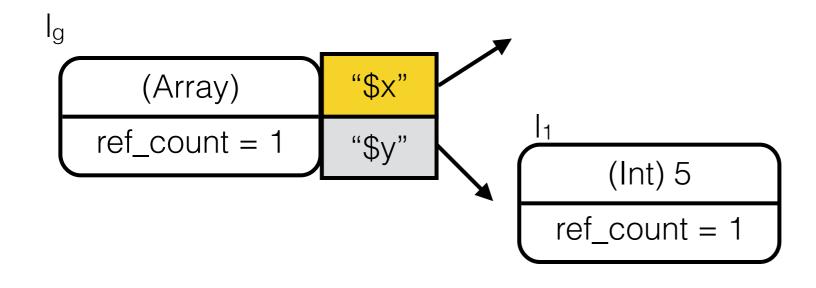
```
x = array("foo" => 5, "bar" => 5);  y = 5;
next($x);
x["baz"] = &x["bar"];
x [12] = 5;
                                                              (Int) 5
                                                          ref_count = 1
                                               "foo"
                                   (Array)
  I_g
                                              "bar"
                                                              (Int) 5
                                ref_{count} = 1
                    "$x"
        (Array)
                                              "baz"
                                                           ref_{count} = 2
     ref_count = 1
                    "$y"
                                   (Int) 5
                                ref_count = 1
```

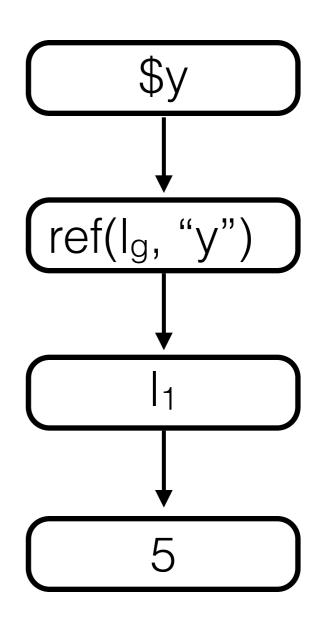
```
x = array("foo" => 5, "bar" => 5);  y = 5;
next($x);
x["baz"] = &x["bar"];
x [12] = 5;
                                                               (Int) 5
                                                            ref_count = 1
                                                "foo"
                                   (Array)
  I_g
                                                "bar"
                                                               (Int) 5
                                 ref_{count} = 1
                     "$x"
        (Array)
                                                "baz"
                                                            ref_count = 1
     ref_count = 1
                     "$y"
                                                 12
                                                               (Int) 5
                                                            ref_{count} = 1
                                    (Int) 5
                                 ref_count = 1
```

Internal values

• Locations: **I₁, I₂, I_{3....}**

References: ref(I, "x")





Semantic rules: numbers

- Covering most of the core language (except interfaces, abstract classes, some minor features)
- ~ 800 rules
- ~ 8000 LOC
- 29 *.k files

Layers

Low-level rules

(copy values, inc. ref. counter, update scope etc.)

Layers

Language **features** (e.g.: assignment, function call)

Low-level rules (copy values, inc. ref. counter, update scope etc.)

Layers

Derived Construct

(e.g.
$$x++ \longrightarrow x = x + 1$$
)

Language features

(e.g.: assignment, function call)

Low-level rules

(copy values, inc. ref. counter, update scope etc.)

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(_:KResult,□)
(C) 'Assign \left(\frac{R:Ref}{convertToLoc(R)}, -\right) [intermediate]
(D) 'Assign(L:Loc, V:Value) [step]
(E) 'Assign \left( -: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)} \right)
     when ¬ isLiteral(V) [intermediate]
(F) <sup>'Assign(L:Loc,L1:Loc)</sup>
reset(L1) → 'Assign(L, L1)
     when currentOverflow(L1) [intermediate]
when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(\_:KResult,\square)
(C) 'Assign \left(\frac{R:Ref}{convertToLoc(R)}, -\right) [intermediate]
(D) \frac{'Assign(L:Loc, V:Value)}{copvValueToLoc(V, L) \sim V} [step]
(E) 'Assign \left( -: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)} \right)
       when ¬ isLiteral(V) [intermediate]
(F) \frac{\text{'Assign}(L:Loc,L1:Loc)}{\text{reset}(L1)} \curvearrowright \text{'Assign}(L,L1)
       when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
       when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(\_:KResult,\Box)
(C) 'Assign \left(\frac{\mathsf{R:Ref}}{\mathsf{convertToLoc(R)}}, -\right)
                                                  [intermediate]
(D) \frac{'Assign(L:Loc, V:Value)}{copyValueToLoc(V, L) \sim V}
                                           [step]
(E) 'Assign \left( -: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)} \right)
      when ¬ isLiteral(V) [intermediate]
(F) <sup>'Assign(L:Loc,L1:Loc)</sup>/<sub>reset(L1) → 'Assign(L. L1)</sub>
      when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
      when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(_:KResult,\Box)
(C) 'Assign \left(\frac{\mathsf{R:Ref}}{\mathsf{convertToLoc(R)}}, -\right)
                                                 [intermediate]
     'Assign(L:Loc, V:Value) copyValueToLoc(V, L)~V
                                           [step]
(E) 'Assign \left( -: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)} \right)
      when ¬ isLiteral(V) [intermediate]
(F) <sup>'Assign(L:Loc,L1:Loc)</sup>/<sub>reset(L1) → 'Assign(L, L1)</sub>
      when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
      when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(\_:KResult,\Box)
(\mathrm{C}) 'Assign \left(rac{\mathsf{R}:\mathsf{Ref}}{\mathsf{convertToLoc}(\mathsf{R})}, 
ight.
                                          [intermediate]
     'Assign(L:Loc, V:Value)
                                     [step]
     copyValueToLoc(V, L)~V
(E) 'Assign \left(-: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)}\right)
     when ¬ isLiteral(V) [intermediate]
    when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
     when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(\mathrm{B}) CONTEXT 'Assign(\_:KResult,\Box)
              R:Ref convertToLoc(R), -
                                       [intermediate]
(\mathrm{C}) 'Assign (
     'Assign(L:Loc, V:Value)
                                  [step]
     copyValueToLoc(V, L)~V
(E) 'Assign \left(-: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)}\right)
     when ¬ isLiteral(V) [intermediate]
    when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
     when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(\_:KResult,\Box)
(\mathrm{C}) 'Assign \left(rac{\mathsf{R}:\mathsf{Ref}}{\mathsf{convertToLoc}(\mathsf{R})}, -
ight.
                                          [intermediate]
     'Assign(L:Loc, V:Value)
                                     [step]
     copyValueToLoc(V, L)~V
(E) 'Assign \left(-: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)}\right)
     when ¬ isLiteral(V) [intermediate]
    when currentOverflow(L1) [intermediate]
(G) 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
     when ¬ currentOverflow(L1) [intermediate]
```

```
(A) CONTEXT 'Assign(\square,_)
(B) CONTEXT 'Assign(\_:KResult,\Box)
(C) 'Assign \left(\frac{\mathsf{R:Ref}}{\mathsf{convertToLoc(R)}}, -\right)
                                         [intermediate]
     'Assign(L:Loc, V:Value)
                                   [step]
     copyValueToLoc(V, L)~V
(E) 'Assign \left(-: KResult, \frac{V:ConvertibleToLoc}{convertToLoc(V,r)}\right)
     when ¬ isLiteral(V) [intermediate]
    when currentOverflow(L1) [intermediate]
^{(G)} 'Assign(L,L1)
'Assign(L, convertToLanguageValue(L1))
     when ¬ currentOverflow(L1) [intermediate]
```

Example: function call

```
\left\langle \frac{\text{runFunction(FN:String, f(FP:K, FB:K, RT:RetType, LS:Loc), Args:K)} \land K}{\text{processFunArgs(FP, Args)} \land} \right\rangle k
\left\langle \frac{\text{pushStackFrame(FN, K, L, CurrentClass, CurrentObj, RT, D)} \land K}{\text{ArrayCreateEmpty(L1)} \land \text{setCrntScope(L1)} \land \text{incRefCount(L1)} \land K} \right\rangle k
                                                                                   copyFunArgs 	→ FB 	→ 'Return(NULL)
                                                                                                                          (CurrentObj:Loc)object
                                                          \langle CurrentClass:Id \rangle_{class}
  \(\( L \: Loc \)\) currentScope
  \langle \frac{D:K}{.} \rangle functionArgumentDeclaration
  when fresh(L1) [internal]
```

Example - revisited

Evaluation order: LR or RL?

Example - revisited

PHP bug 61188

Evaluation order: LR or RL?

[2012-02-26 19:04 UTC] <u>rasmus@php.net</u>

I do see your argument, but you are making assumptions about how PHP handles sequence points in expressions which is not documented and thus not stricly defined.

[2012-09-01 19:01 UTC] avp200681 at gmail dot com

```
[...]
I've found in PHP documentation:
"Operators on the same line have equal precedence, in which
case associativity decides the order of evaluation."
```

Example - explained

- evaluation order is left-to-right
- array access evaluates to values
- variables evaluate to references
- references are resolved lazily

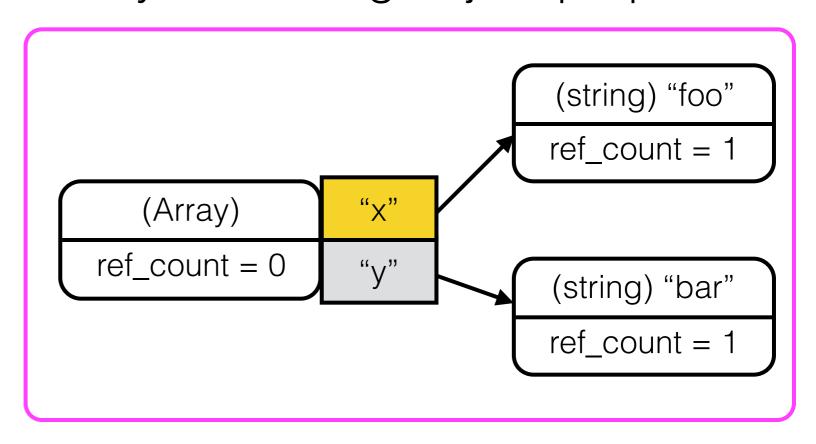
What about objects?

```
Class A {public $x = "one"; private $y = "two" }
$x = new A();
```

What about objects?

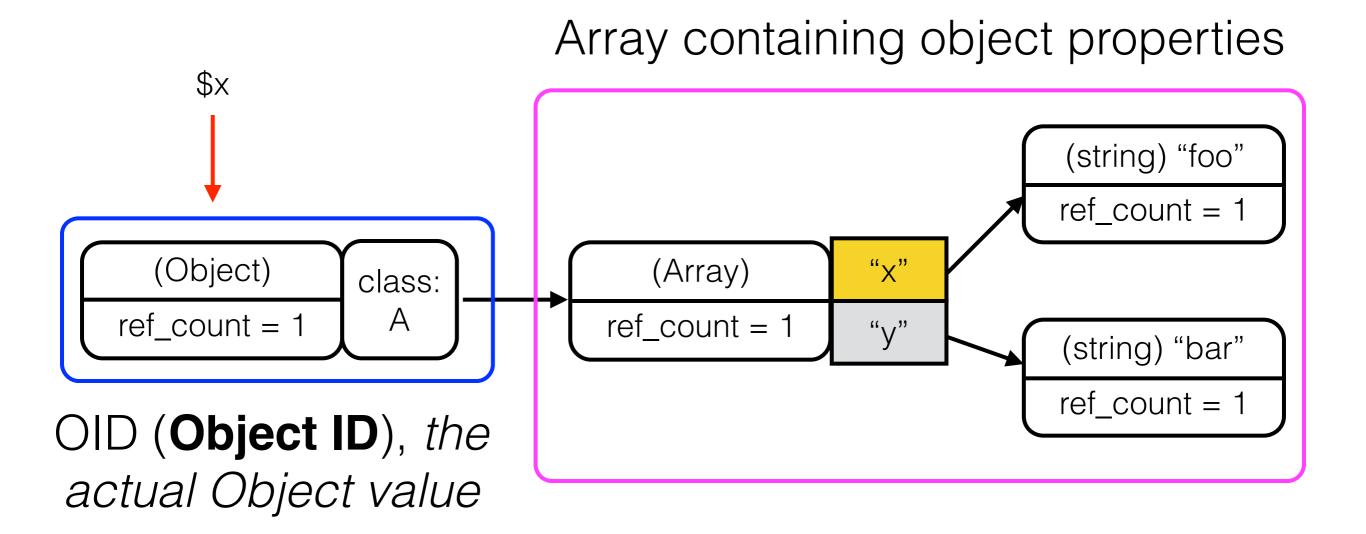
```
Class A {public $x = "one"; private $y = "two" }
$x = new A();
```

Array containing object properties



What about objects?

```
Class A {public $x = "one"; private $y = "two" }
$x = new A();
```



Objects as arrays

- Object properties have visibilities (public, protected, private)
- We attach visibility attributes to all arrays
 - "Normal" arrays are always accessible, so all their elements are public
 - Arrays associated to objects may have protected or private visibility
 - Objects as "guarded arrays"
- Generalisation in semantic rules

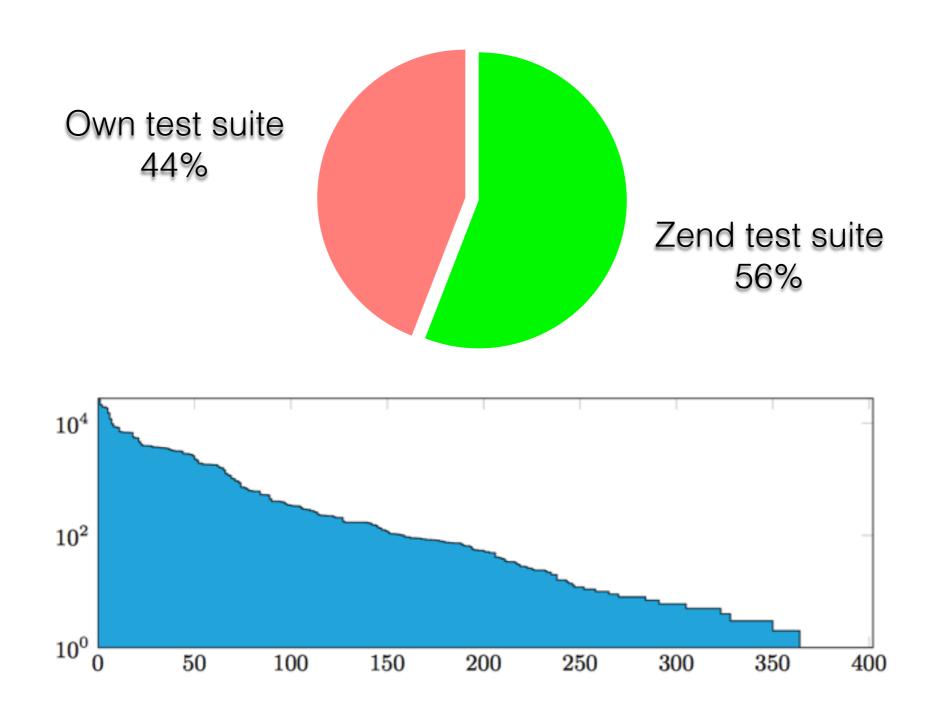
Validation

- Testing against the Zend test suite.
- focusing on core language section of test suite
- passing all tests supported by our semantics

```
1 --TEST--
 2 Child public element should not
      override parent private element
      in parent methods
 3 --FILE--
 4 <?php
   class par {
       private $id = "foo";
       function displayMe()
            print $this->id;
11
12 };
13
14 class chld extends par {
15
       public $id = "bar";
       function displayHim()
17
            parent::displayMe();
18
19
20 };
21
22
23 \cdot \text{sobj} = \text{new chld()};
24 $obj->displayHim();
25 ?>
26 --EXPECT--
27 foo
```

Coverage

"How many times each rule is used by the test suite?"



Application: temporal verification of PHP programs

- Using K's builtin support for LTL model checking and symbolic execution
- Extension of LTL with predicates over KPHP configurations
- Real-world case studies: input validation (PHPMyAdmin) and hashing function (PHP library)

Case study: hashing

```
34 function pbkdf2($algorithm, $password, $salt, $count, $key_length, $raw_output = false)
35 {
36
       $algorithm = strtolower($algorithm);
       if(!in_array($algorithm, hash_algos(), true))
37
38
           die('PBKDF2 ERROR: Invalid hash algorithm.');
       if($count <= 0 || $key length <= 0)
39
           die('PBKDF2 ERROR: Invalid parameters.');
40
41
42
       $hash_length = strlen(hash($algorithm, "", true));
       $block count = ceil($key length / (float) $hash length);
43
44
45
       echo "key len: $key_length\n";
46
       echo "hash len: $hash length\n";
       echo "block count: $block count\n";
47
48
       $output = ""; //"";
49
       for($i = 1; $i <= $block_count; $i++) {</pre>
50
51
           // $i encoded as 4 bytes, big endian.
52
           $last = $salt . pack("N", $i);
53
           // first iteration
54
           $last = $xorsum = hash_hmac($algorithm, $last, $password, true);
55
           // perform the other $count - 1 iterations
           for ($j = 1; $j < $count; $j++) {
56
57
               $xorsum ^= ($last = hash hmac($algorithm, $last, $password, true));
58
59
           $output .= $xorsum;
       }
60
61
62
       if($raw output)
63
           return substr($output, 0, $key length);
64
       else
65
           return bin2hex(substr($output, 0, $key length));
66 }
```

Case study: hashing

Lemma: For all \$password, \$salt and for given \$algo, \$count and \$key_len:

- (i) The result is a string: ♦has_type(gv(var('result')),string)
- (ii) The length of the output is as requested

```
$\delta eqTo(gv(var('key_len')),len(gv(var('result'))))
```

(iii) The length of the string stored in \$output grows and eventually becomes greater then the expected output length

```
\Box \big( (\text{inFun('pbkdf2')} \land \neg \text{inFun('top')} \land \Diamond \text{inFun('top')} ) \Longrightarrow \\ (\Diamond (\text{geq(len(fv('pbkdf2',var('output'))}), fv('pbkdf2', var('key_len'))}) \\ \mathcal{U} \text{ inFun('top')} \big) \big)
```

Improving language support

Fix bugs

Future Work

Deductive verification (Reachability Logic)

Static
Analysis
(Abstract
Interpretation)

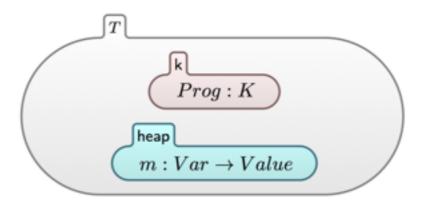
Conclusions

- The first formal semantics for PHP
- Semantics is directly executable
- Validated by passing all supported tests from the Zend test suite
- Full coverage of rules by adding our own tests
- Proof of concept infrastructure for verification of PHP programs
- A first step toward defining semantics based static analysis tools for PHP

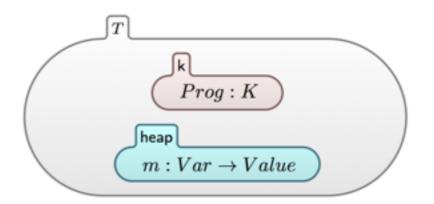
Thank you!

www.phpsemantics.org paper, sources, web interface

Appendix/misc/old

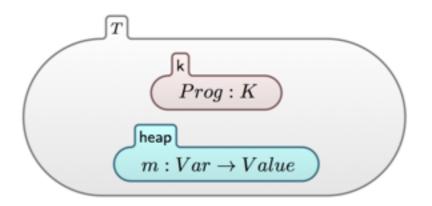


Komputations



Komputations

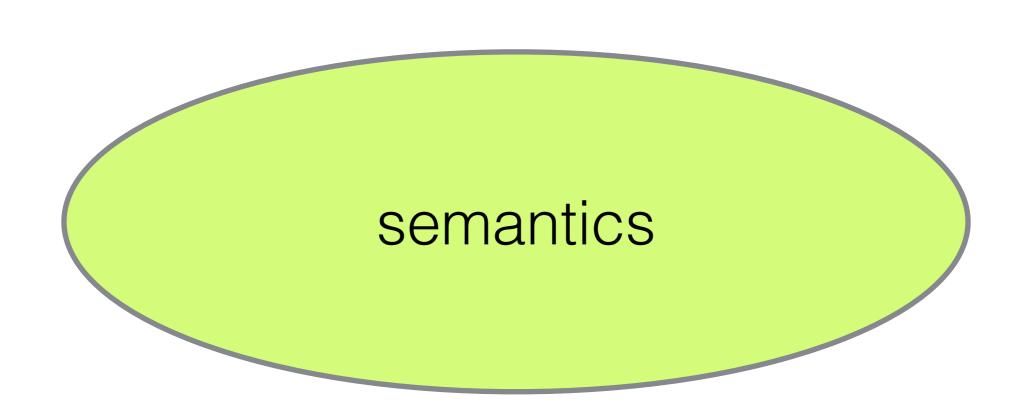
(i) the K cell holds a list of computations separated by

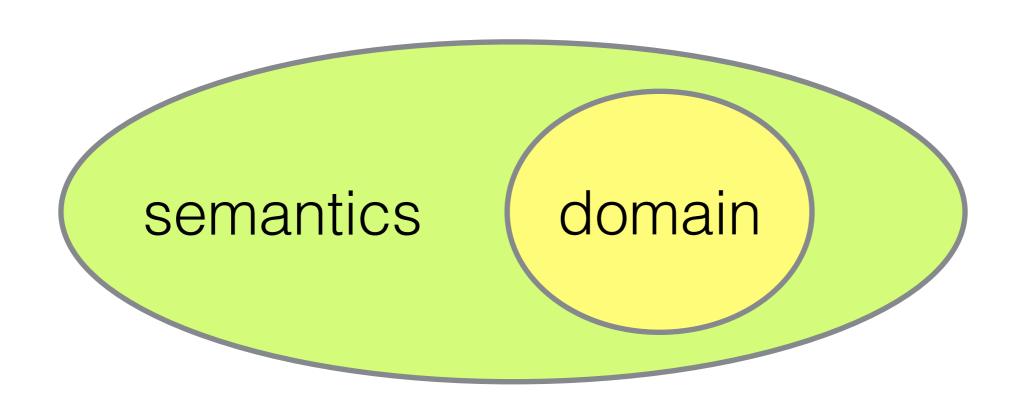


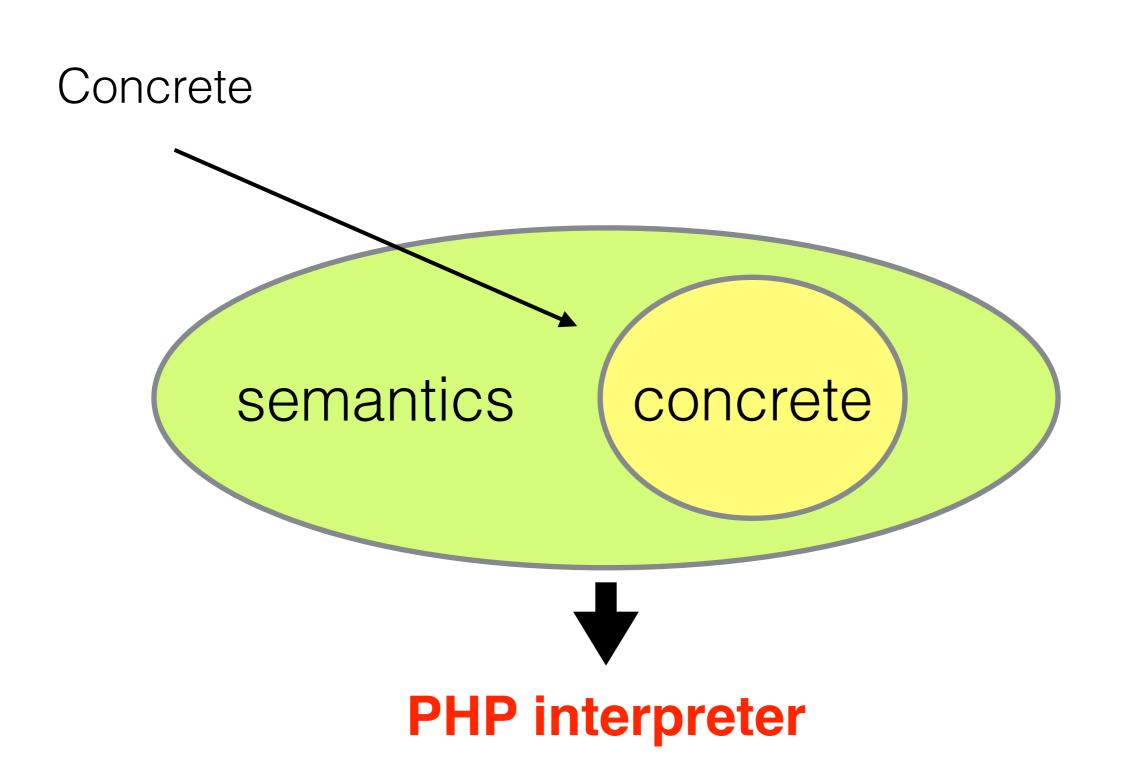
Komputations

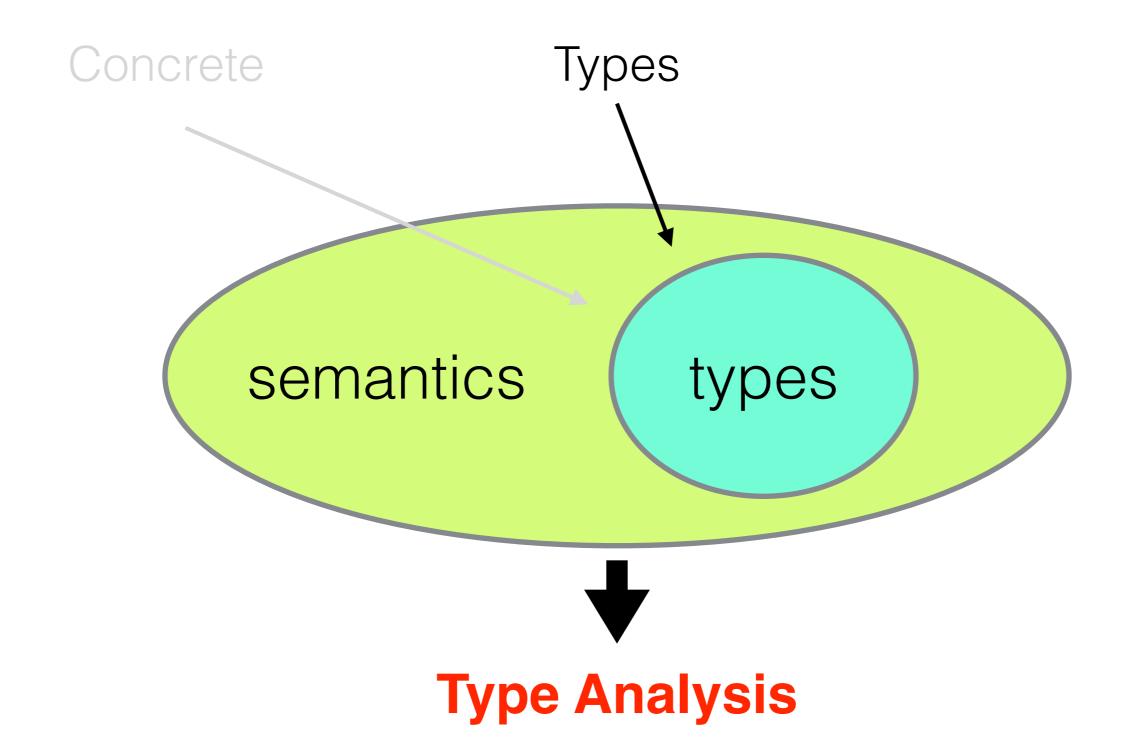
(i) the K cell holds a list of computations separated by

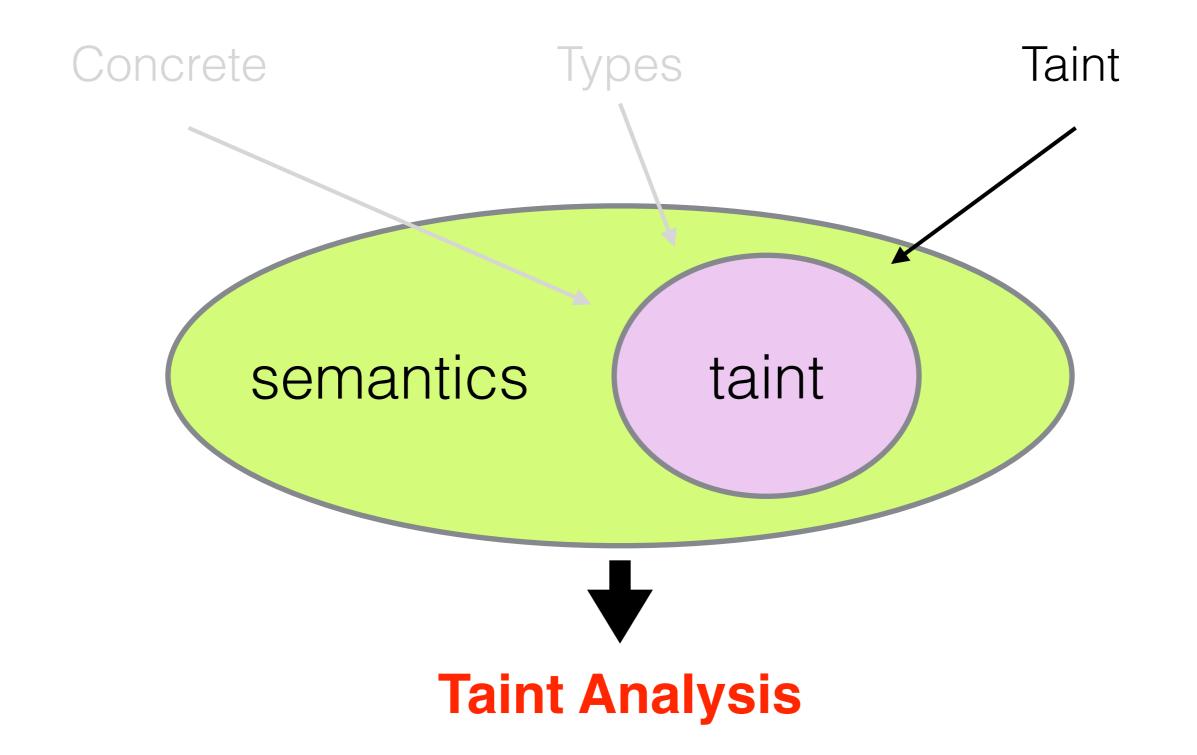
(ii) the input program goes into the k cell

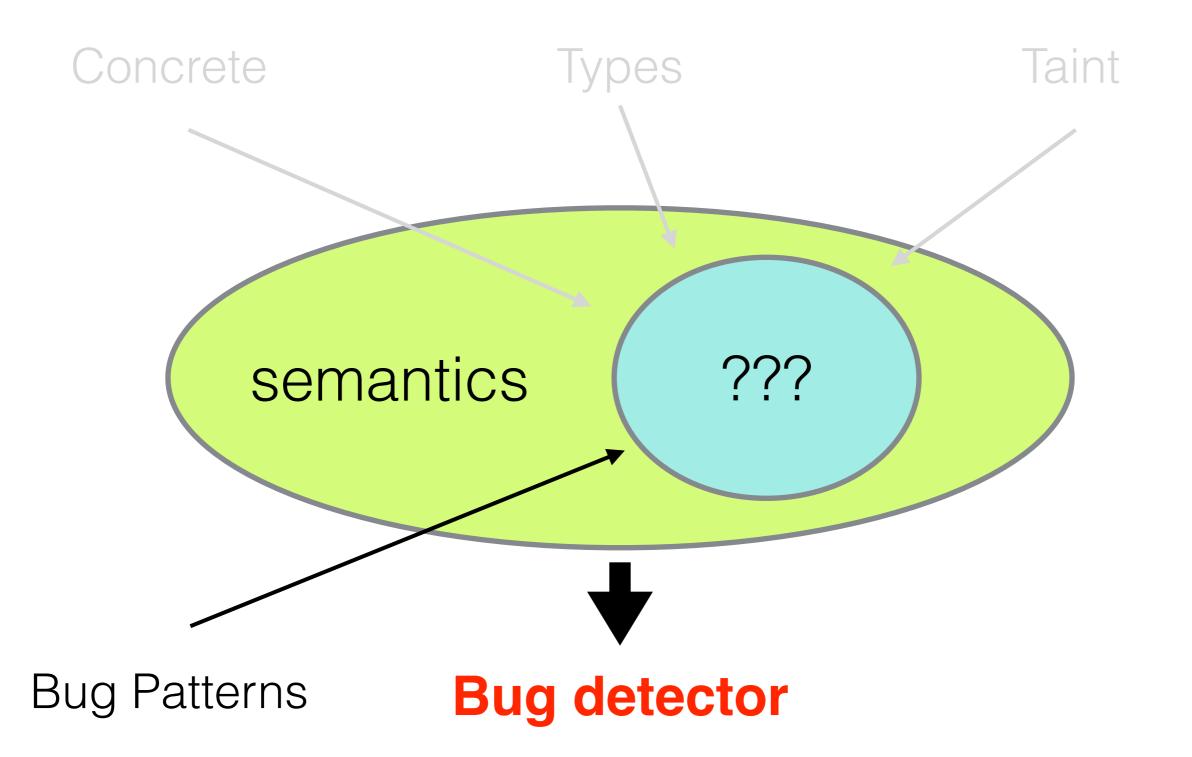












```
1 --TEST--
 2 Child public element should not
      override parent private element
      in parent methods
 3 --FILE--
 4 <?php
 5 class par {
       private $id = "foo";
       function displayMe()
       {
10
           print $this->id;
11
12 };
13
14 class chld extends par {
15
       public $id = "bar";
       function displayHim()
16
17
           parent::displayMe();
18
19
20 };
21
22
23 sobj = new chld();
24 $obj->displayHim();
25 ?>
26 --EXPECT--
27 foo
```

zend/lang/036.phpt

- chld extends par
- both classes has member
 \$id private for parent,
 public for child
- instance of child calls parent's displayMe method, which outputs "foo"
- if par's \$id was public, then output would be "bar"
- Implication: members indexed by (key, visibility) pair!

```
function foo() {
   global $y;
   $x = &$y;
}
```

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
```

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
foo();
```

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
foo();
```

```
$\dar(\'\text{roo', var('x')), gv(var('y'))}
```

```
1 --TEST--
 2 Child public element should not
      override parent private element
      in parent methods
 3 --FILE--
 4 <?php
 5 class par {
       private $id = "foo";
       function displayMe()
       {
10
           print $this->id;
11
12 };
13
14 class chld extends par {
15
       public $id = "bar";
       function displayHim()
16
17
           parent::displayMe();
18
19
20 };
21
22
23 sobj = new chld();
24 $obj->displayHim();
25 ?>
26 --EXPECT--
27 foo
```

zend/lang/036.phpt

- chld extends par
- both classes has member
 \$id private for parent,
 public for child
- instance of child calls parent's displayMe method, which outputs "foo"
- if par's \$id was public, then output would be "bar"
- Implication: members indexed by (key, visibility) pair!