An executable formal semantics for PHP

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www.phpsemantics.org

Imperial College London

Dagstuhl 2014

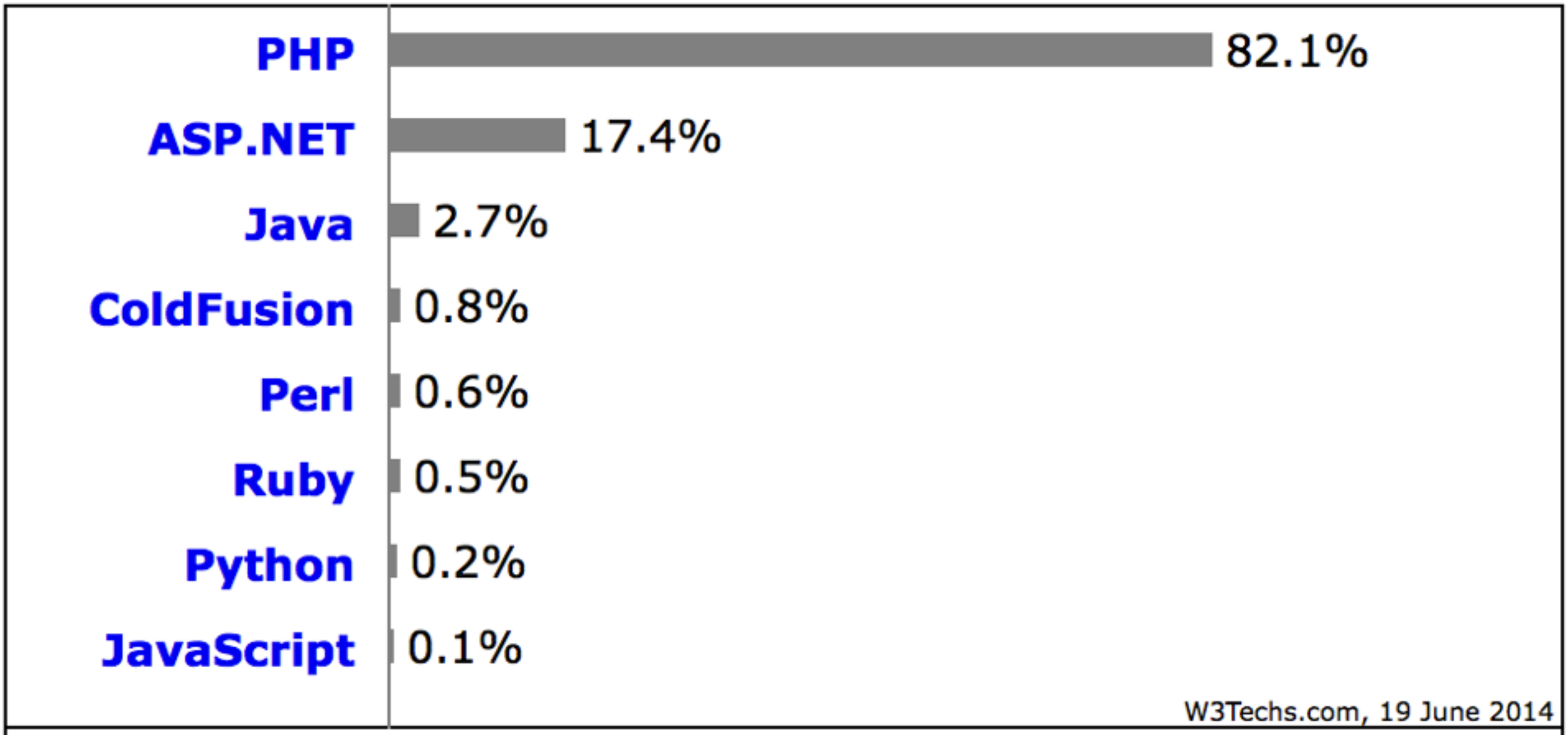

phpMyAdmin


YAHOO!


PHP


moodle


WordPress



http://w3techs.com/technologies/overview/programming_language/all

```php
$a = array("one");
```

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
```

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c;
```

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // “onetwo"
```

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // “onetwo"
```

```php
$a = "one";
$c = $a . ($a = "two");
echo $c;
```

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // “onetwo"
```

```php
$a = "one";
$c = $a . ($a = "two");
echo $c; // "twotwo"
```

PHP tricky features

- **Aliasing**
- Complex array and object **iteration**
- Automatic **type conversions**
- Complex **array copy**
- Complex instance variable **lookup**

Change language: English

Edit Report a Bug

Booleans

This is the simplest type. A boolean expresses a truth value. It can be either **TRUE** or **FALSE**.

Syntax

To specify a boolean literal, use the constants **TRUE** or **FALSE**. Both are case-insensitive.

```
<?php
$foo = True; // assign the value TRUE to $foo
?>
```

Typically, the result of an operator which returns a boolean value is passed on to a control structure.

```
<?php
// == is an operator which tests
// equality and returns a boolean
if ($action == "show_version") {
    echo "The version is 1.23";
```

dynamic language

dynamic language

+

no spec

dynamic language

+

no spec

+

poor documentation

dynamic language

+

no spec

+

poor documentation

=>

bugs, confusion, etc.

OWASP Top 10 – 2013 (New)
A1 – Injection
A2 – Broken Authentication and Session Management
A3 – Cross-Site Scripting (XSS)
A4 – Insecure Direct Object References
A5 – Security Misconfiguration
A6 – Sensitive Data Exposure
A7 – Missing Function Level Access Control
A8 – Cross-Site Request Forgery (CSRF)
A9 – Using Known Vulnerable Components
A10 – Unvalidated Redirects and Forwards
Merged with 2010-A7 into new 2013-A6

Analyzing PHP
An introduction to PHP-Sat *

Eric Bouwers
embouwer@cs.uu.nl

Center for Software Technology
Universiteit Utrecht, The Netherlands

RIPS - A static source code analyser for vulnerabilities in PHP scripts

Johannes Dahse

PHP Aspis: Using Partial Taint Tracking To Protect Against Injection Attacks

Ioannis Papagiannis
Imperial College London

Matteo Migliavacca
Imperial College London

Peter Pietzuch
Imperial College Lo

A Systematic Analysis of XSS Sanitization in Web Application Frameworks

On Using Static Analysis to Detect Type Errors in PHP Applications

EPFL-REPORT-147867

SAFERPHP:
antic Vulnerabilities in PHP Applications

Limitations

- partial coverage of the language - i.e. features ignored because “too hard” for analysis
- sometimes, features modelled incorrectly
- no formal guarantees of soundness

Our goal: A *Trusted* Executable Formal Semantics of PHP

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framework for
reliable tools
development

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framework for
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the missing
specification

Our tools and methodology:

The $\mathbb{K}$ Framework

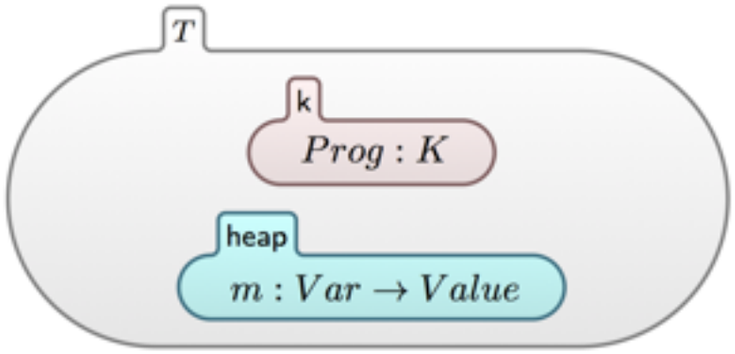
Scales to real languages
(C semantics - POPL'10)

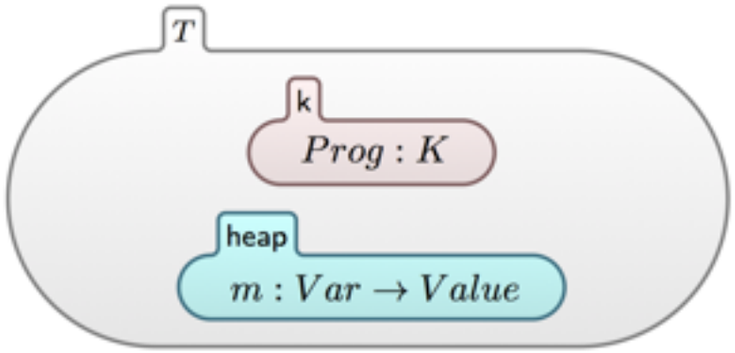
The $\mathbb{K}$ Framework

Formal
(rewriting)

Executable
(Maude/Java)

Verification
(deductive, LTL,
symbolic exec.)


T
k
Prog : K
heap
m : Var → Value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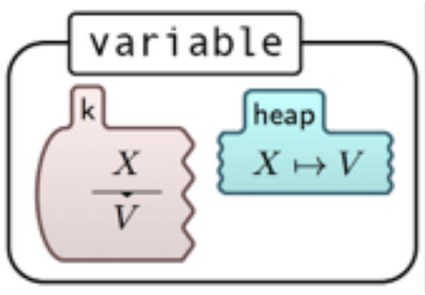
variable
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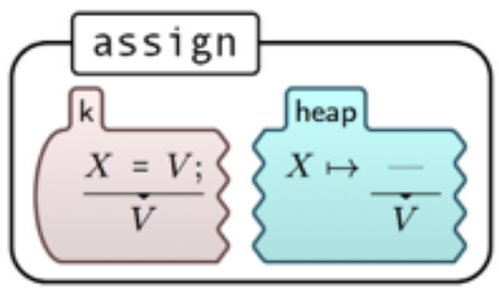
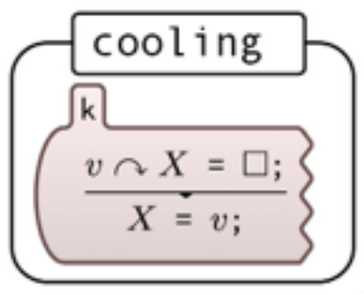
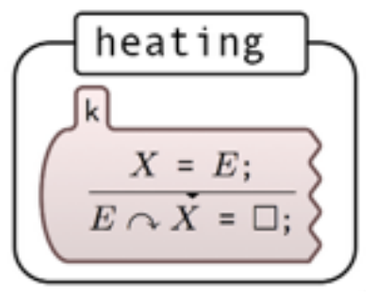

assign
k
X = V;
V
heap
X ↦ —
V


cooling
k
v ↷ X = □;
X = v;


heating
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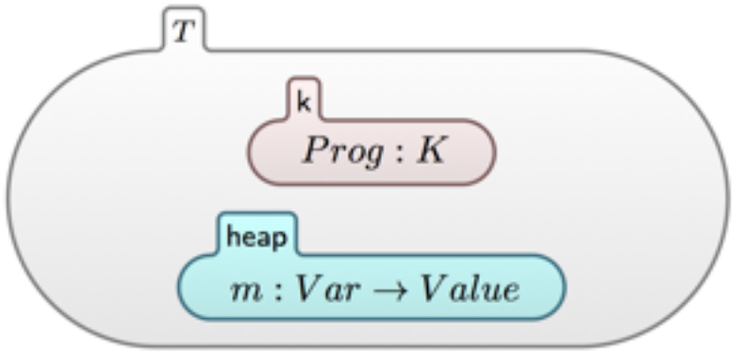
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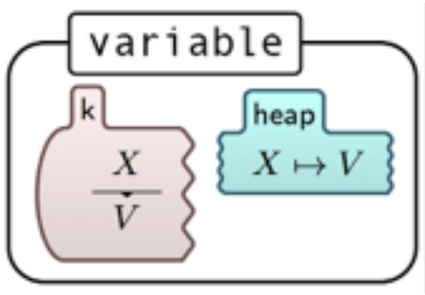
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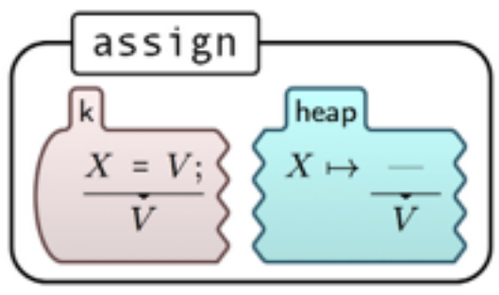
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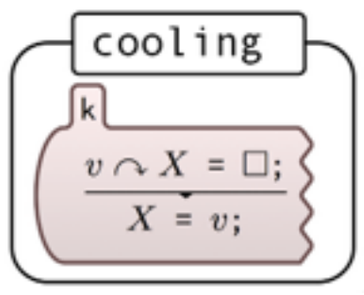
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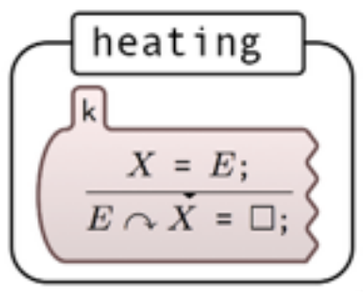
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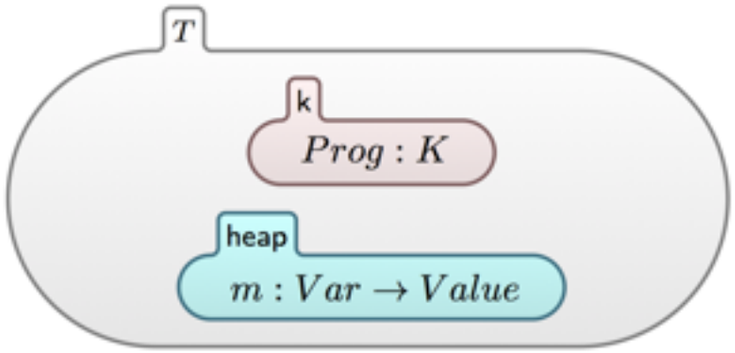
$x = $y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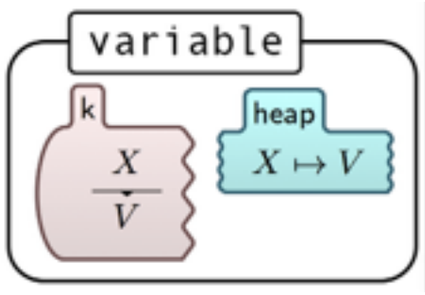
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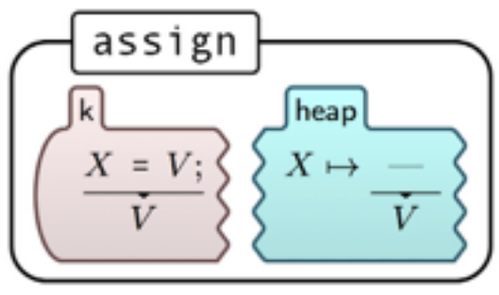
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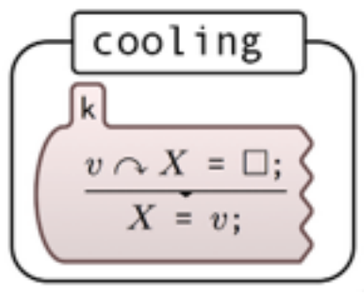
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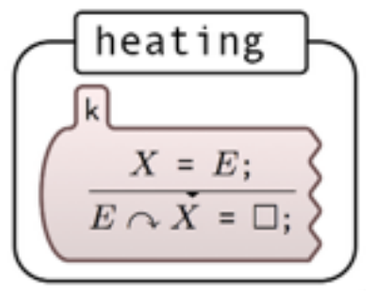
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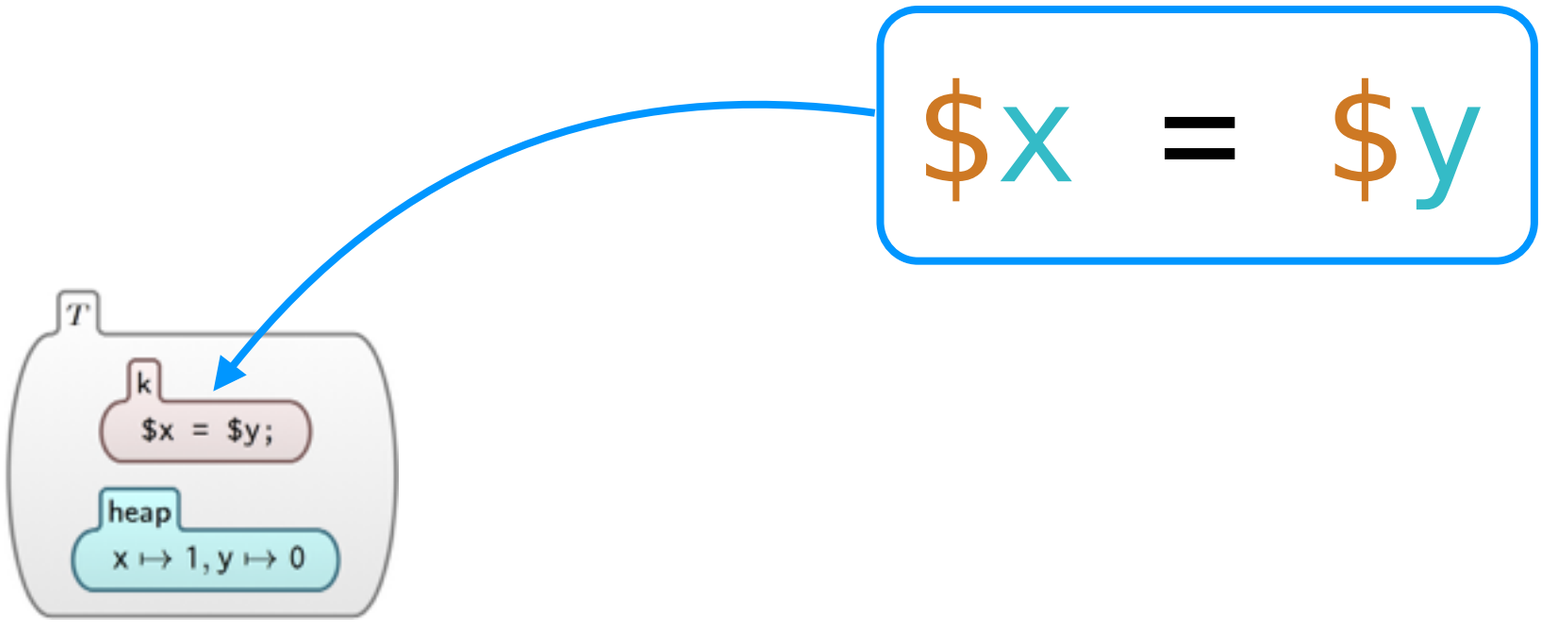
$x = $y
T
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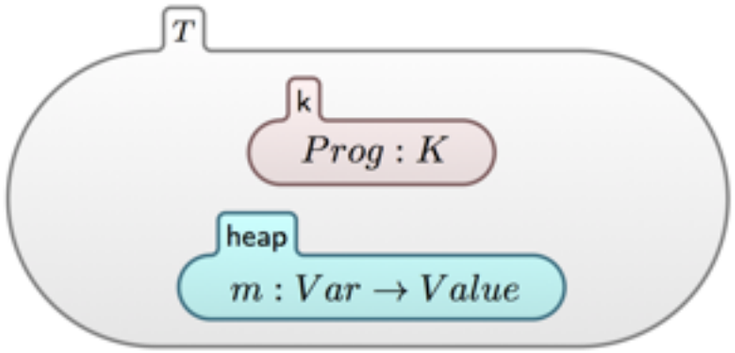
x ↦ 1, y ↦ 0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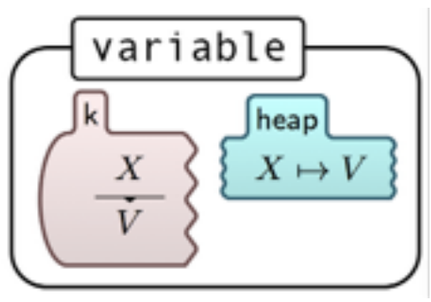
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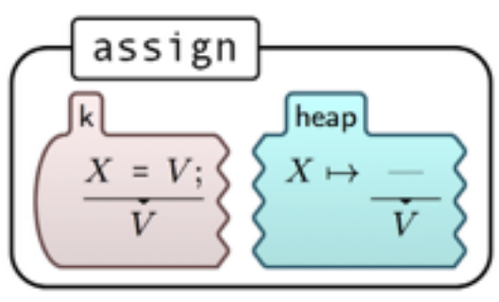
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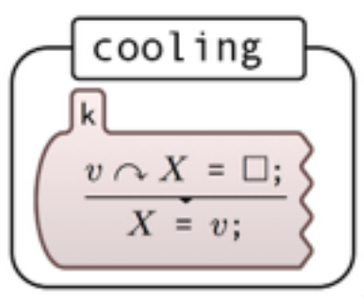
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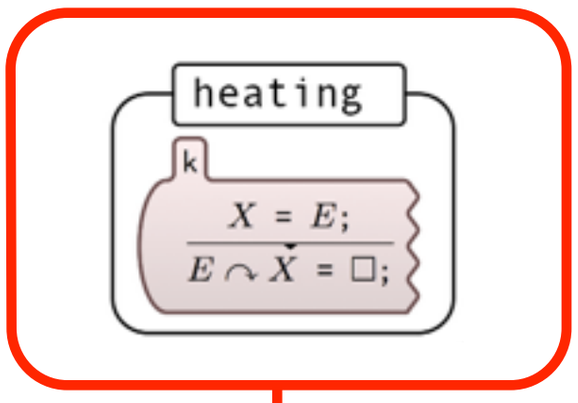
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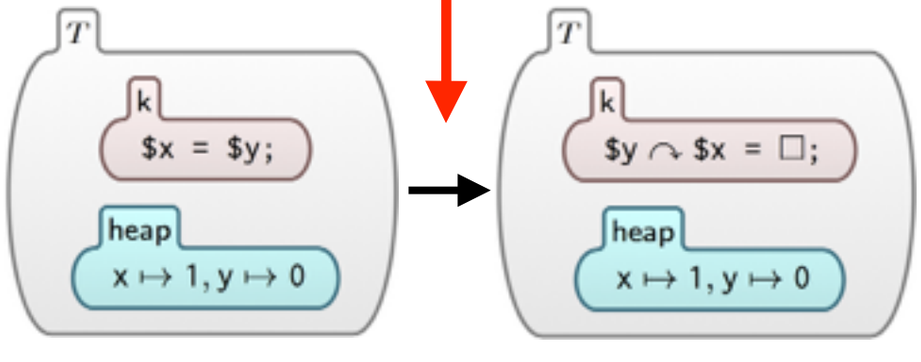
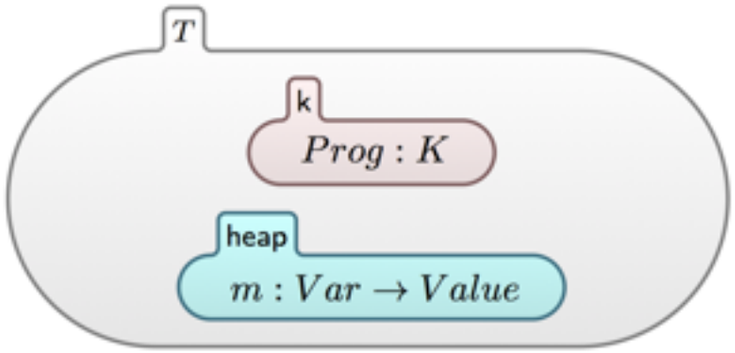

T
k
$x = $y;
heap
x ↦ 1, y ↦ 0
T
k
$y ↷ $x = □;
heap
x ↦ 1, y ↦ 0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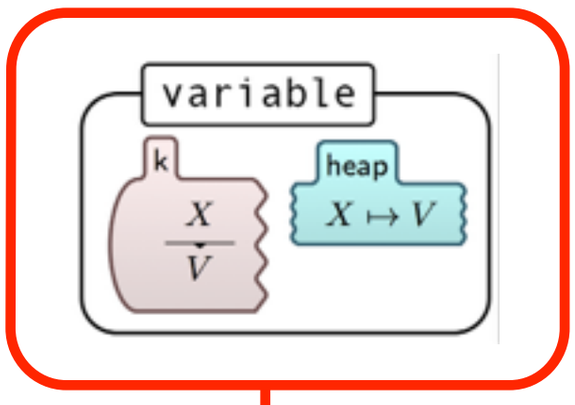
variable
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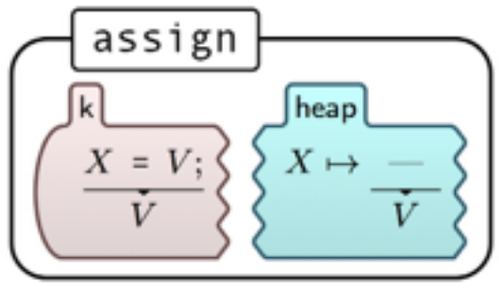
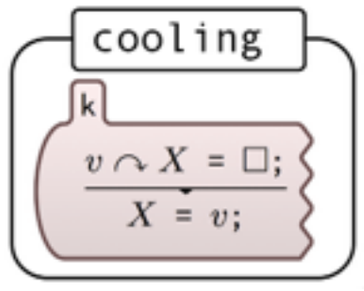
V
heap
X ↦ V


assign
k
X = V;
V
heap
X ↦ —
V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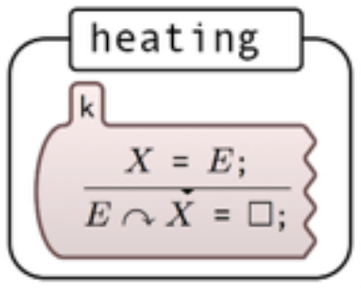
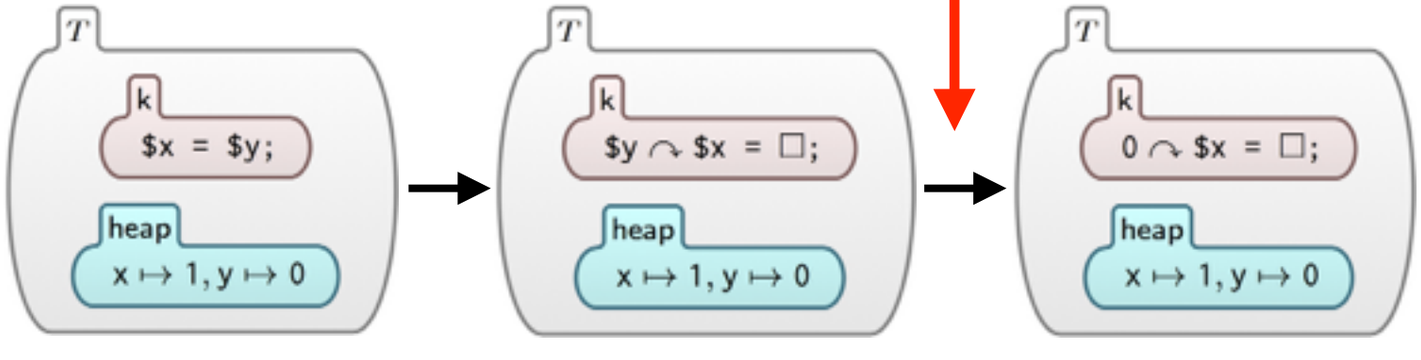

heating
k
X = E;
E ↷ X = □;


T
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heap
x ↦ 1, y ↦ 0
T
k
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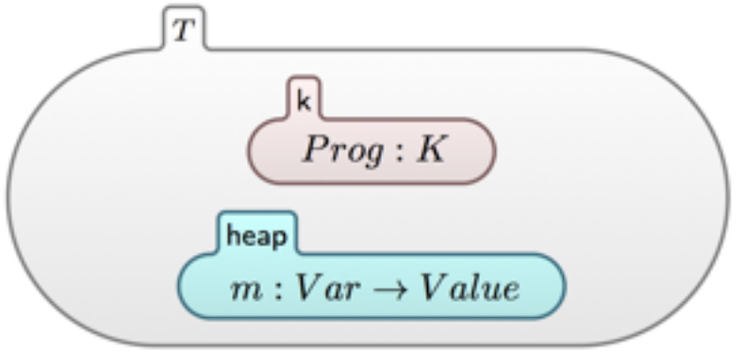
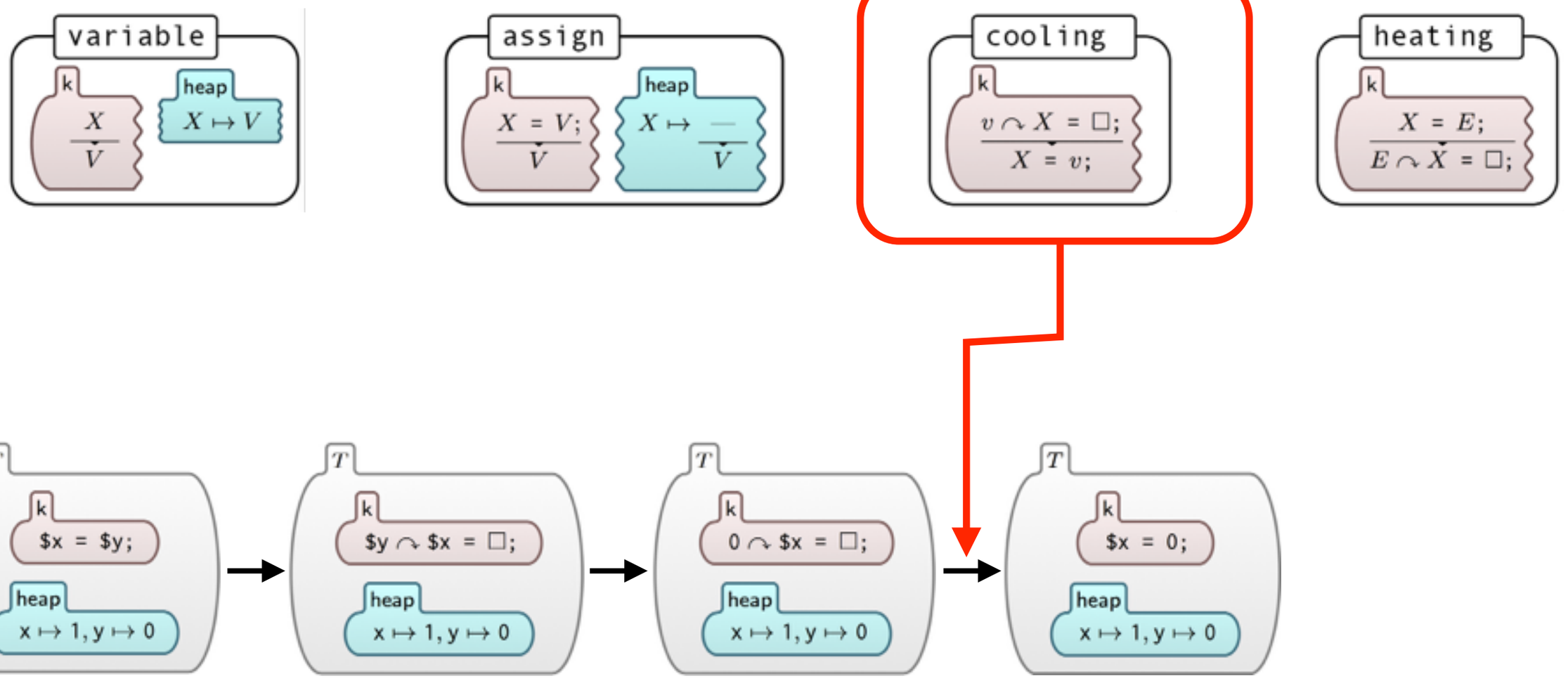

T
k
Prog : K
heap
m : Var → Value


variable
k
X
V
heap
X ↦ V
assign
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V
heap
X ↦ —
V
cooling
k
v ↷ X = □;
X = v;
heating
k
X = E;
E ↷ X = □;
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$x = $y;
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x ↦ 1, y ↦ 0
T
k
$y ↷ $x = □;
heap
x ↦ 1, y ↦ 0
T
k
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heap
x ↦ 1, y ↦ 0
T
k
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heap
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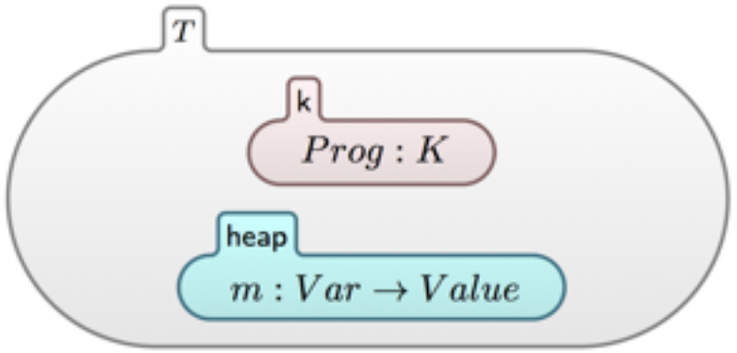
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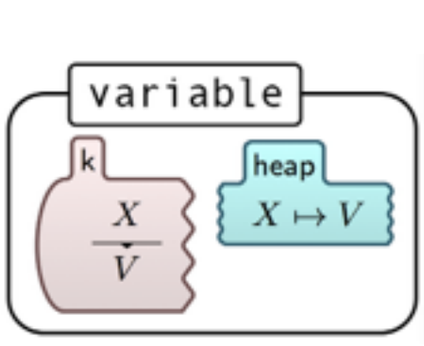
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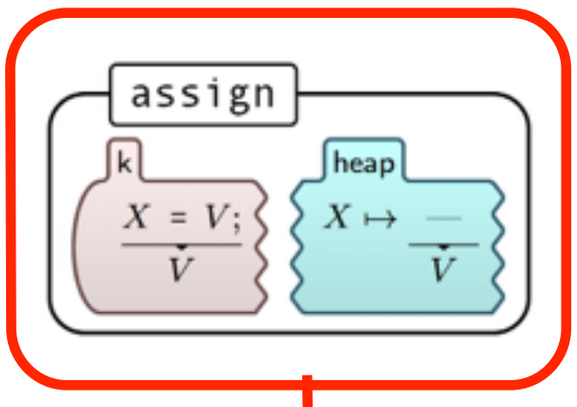
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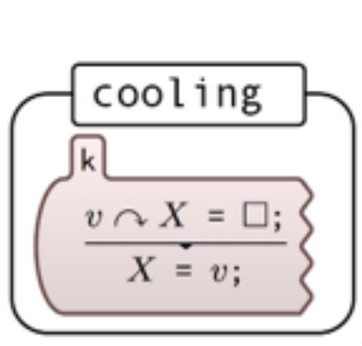
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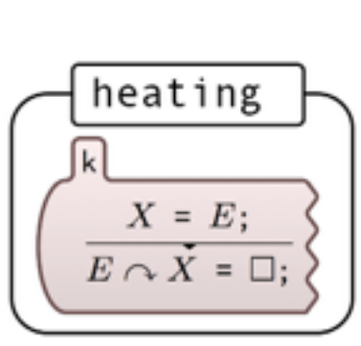
heating
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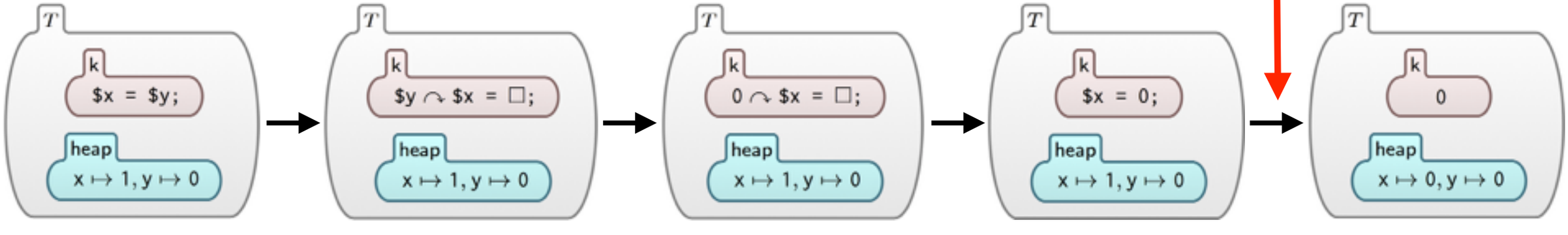
X = E;
E ↷ X = □;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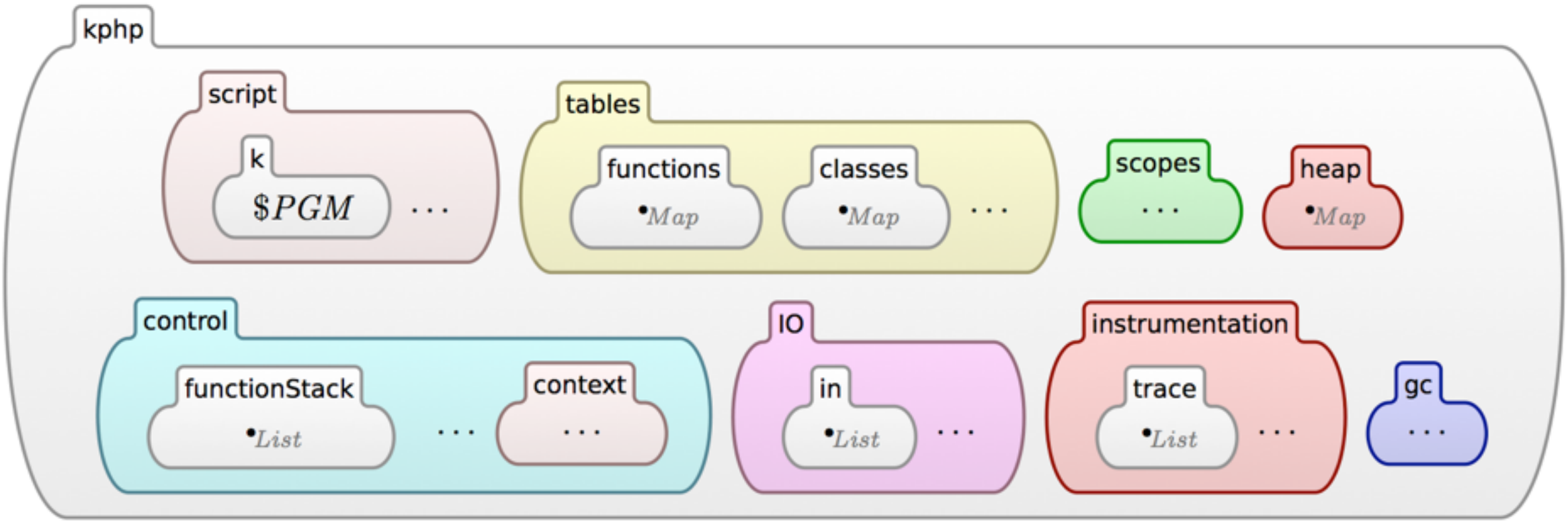
T
k
$x = 0;
heap
x ↦ 1, y ↦ 0
T
k
0
heap
x ↦ 0, y ↦ 0

KPHP

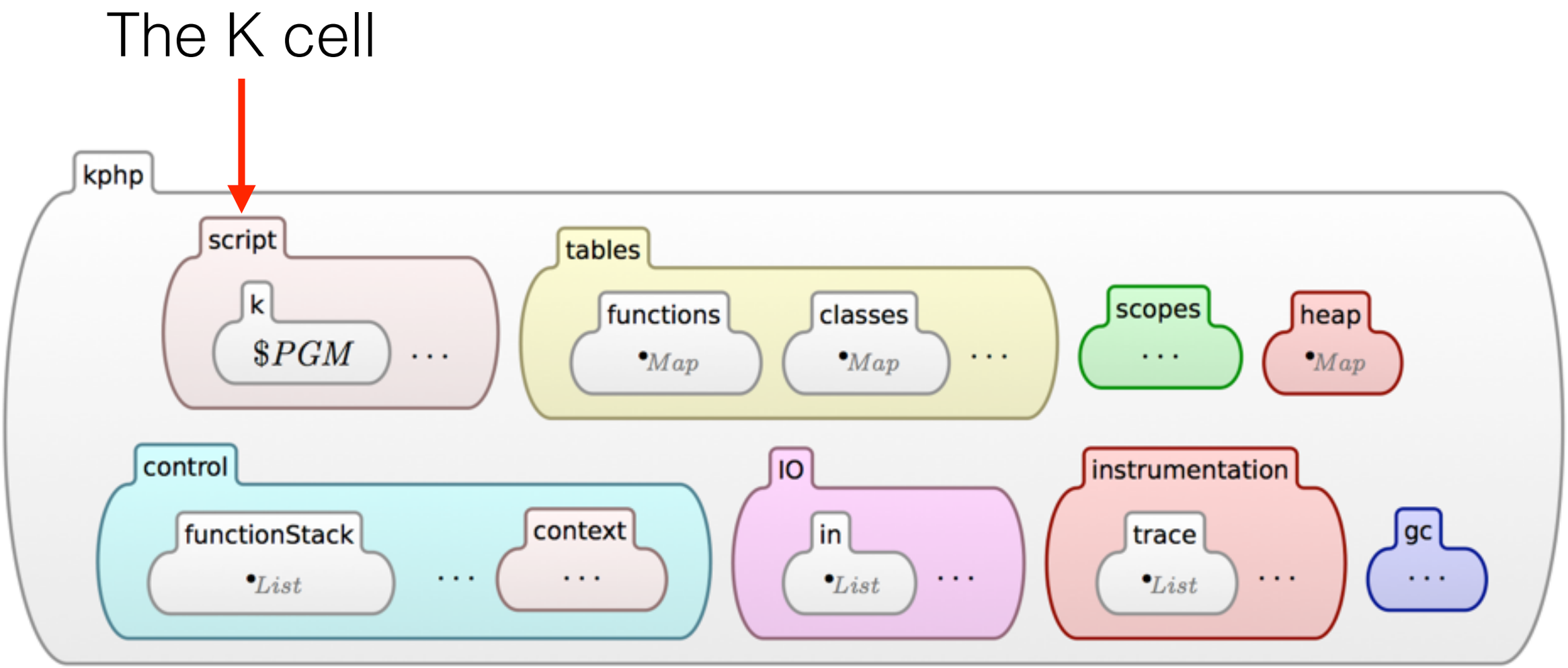
(Formalising PHP in K)

[ECOOP 2014]

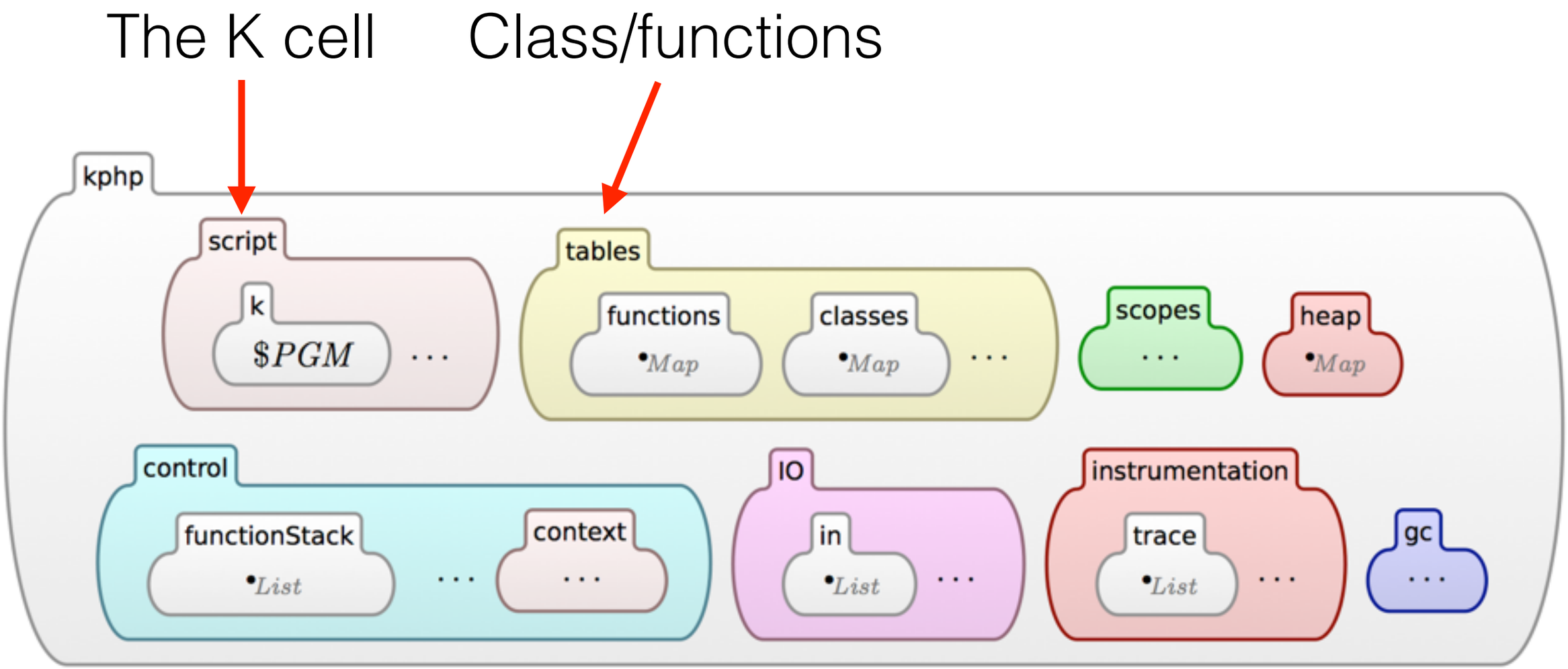
Configuration (~30 cells)



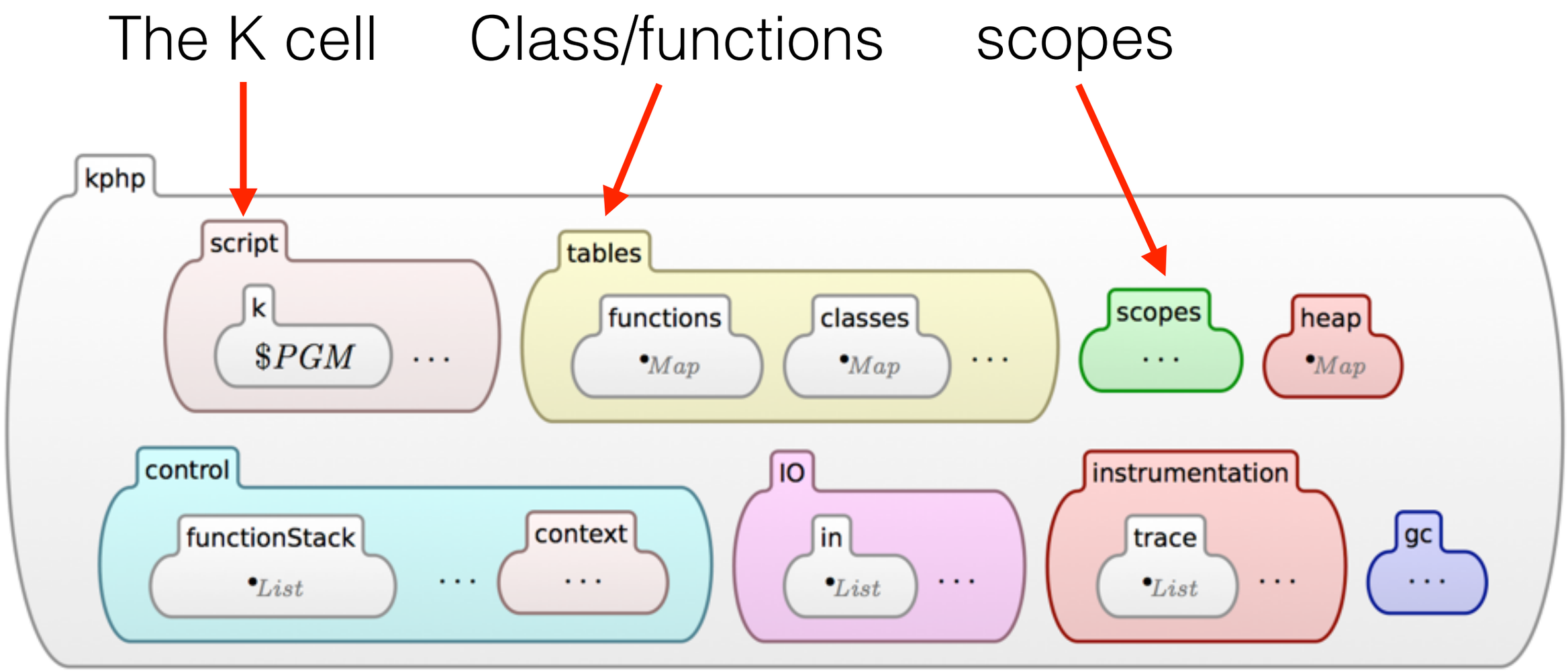
Configuration (~30 cells)



Configuration (~30 cells)



Configuration (~30 cells)



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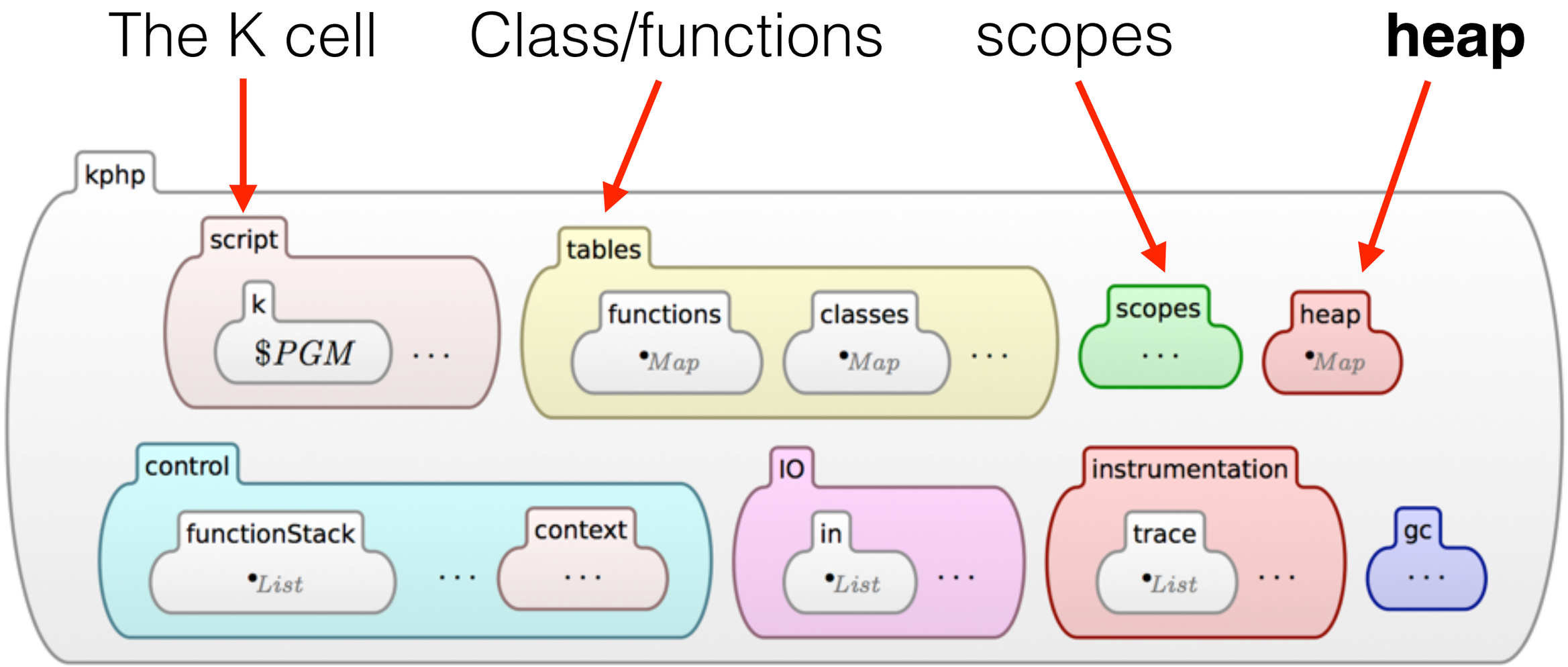
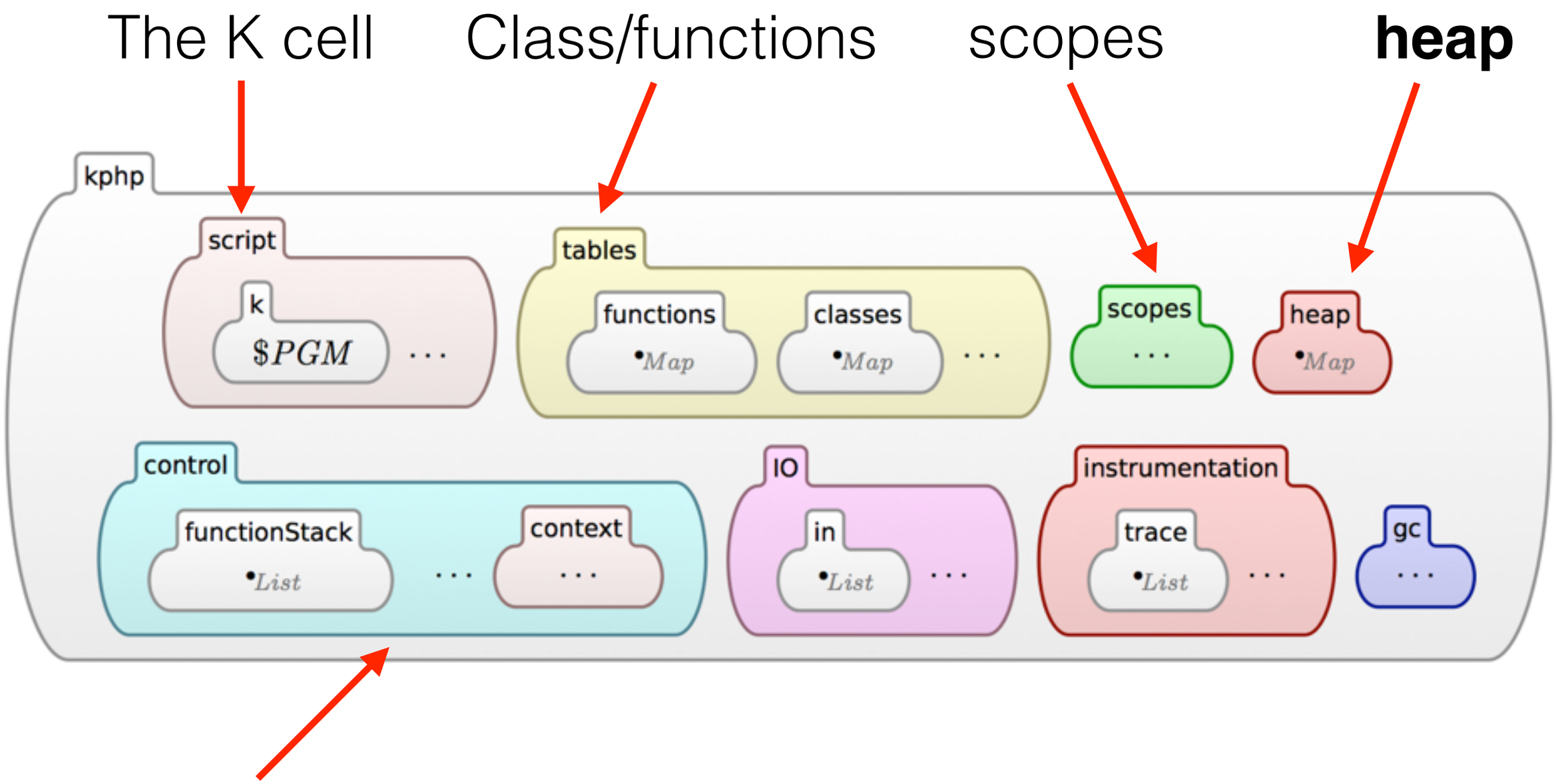


Configuration (~30 cells)



Control, stack, context

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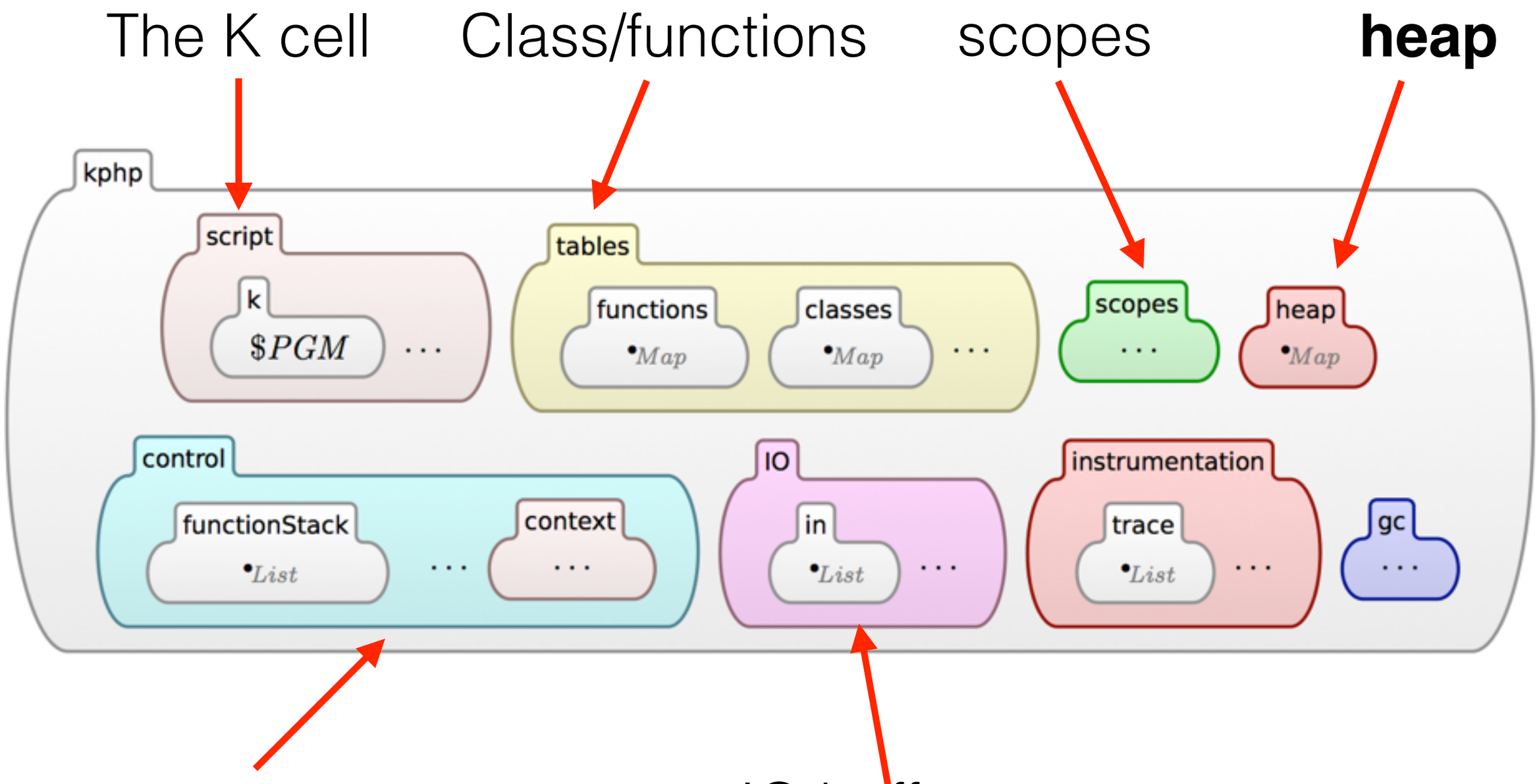

Control, stack, context

IO buffers
(linked to stdin/out)

Memory Layout

Language Values

Scalar	Compound	Special
boolean	array	resource
integer	object	NULL
float		
string		

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Scalar	Compound	Special
boolean	array	~~resource~~
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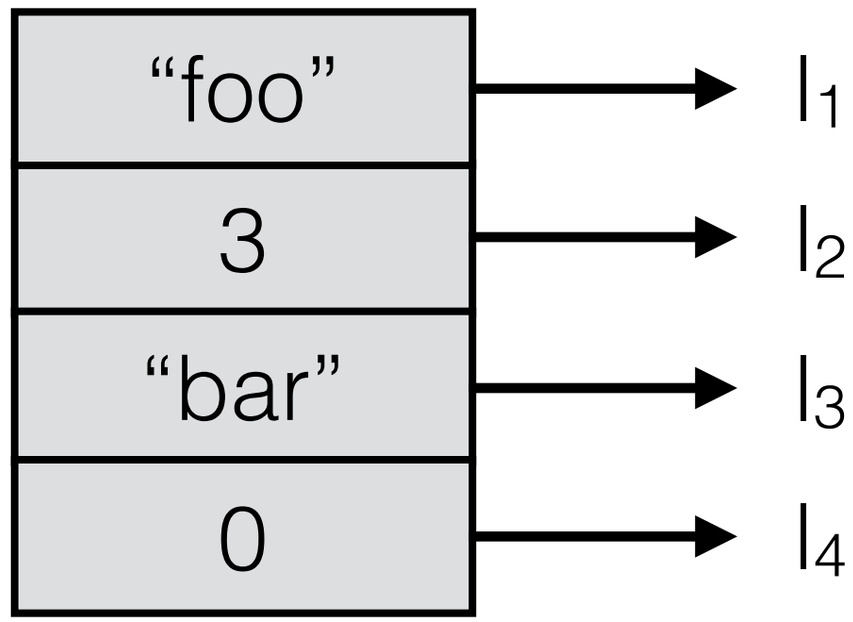
Arrays

Int U String —> Locations



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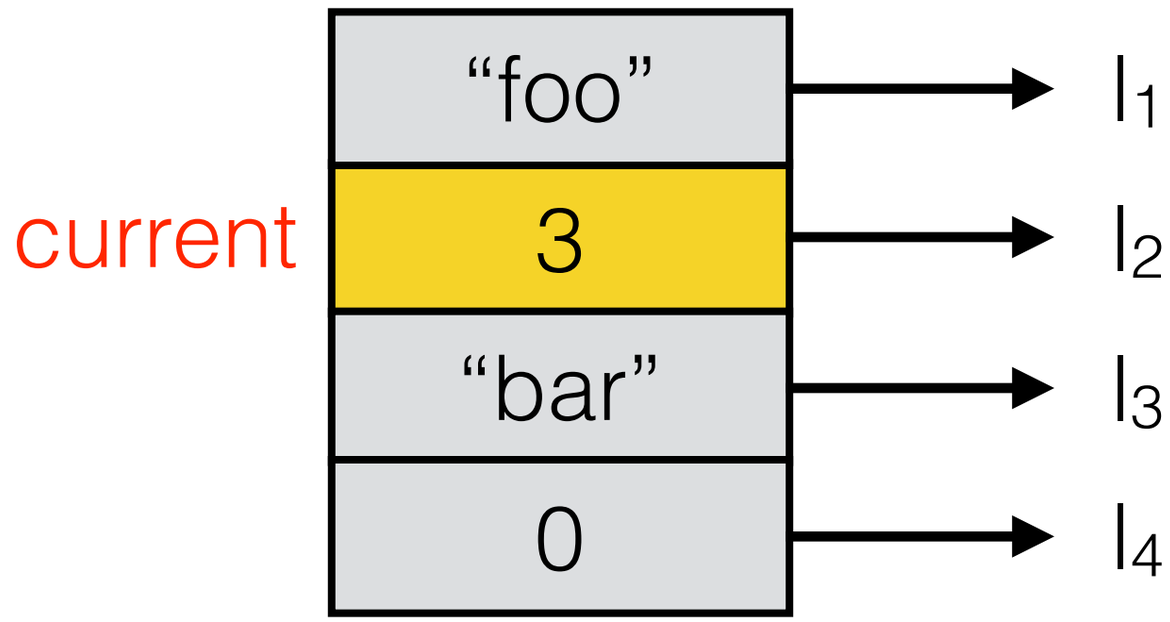
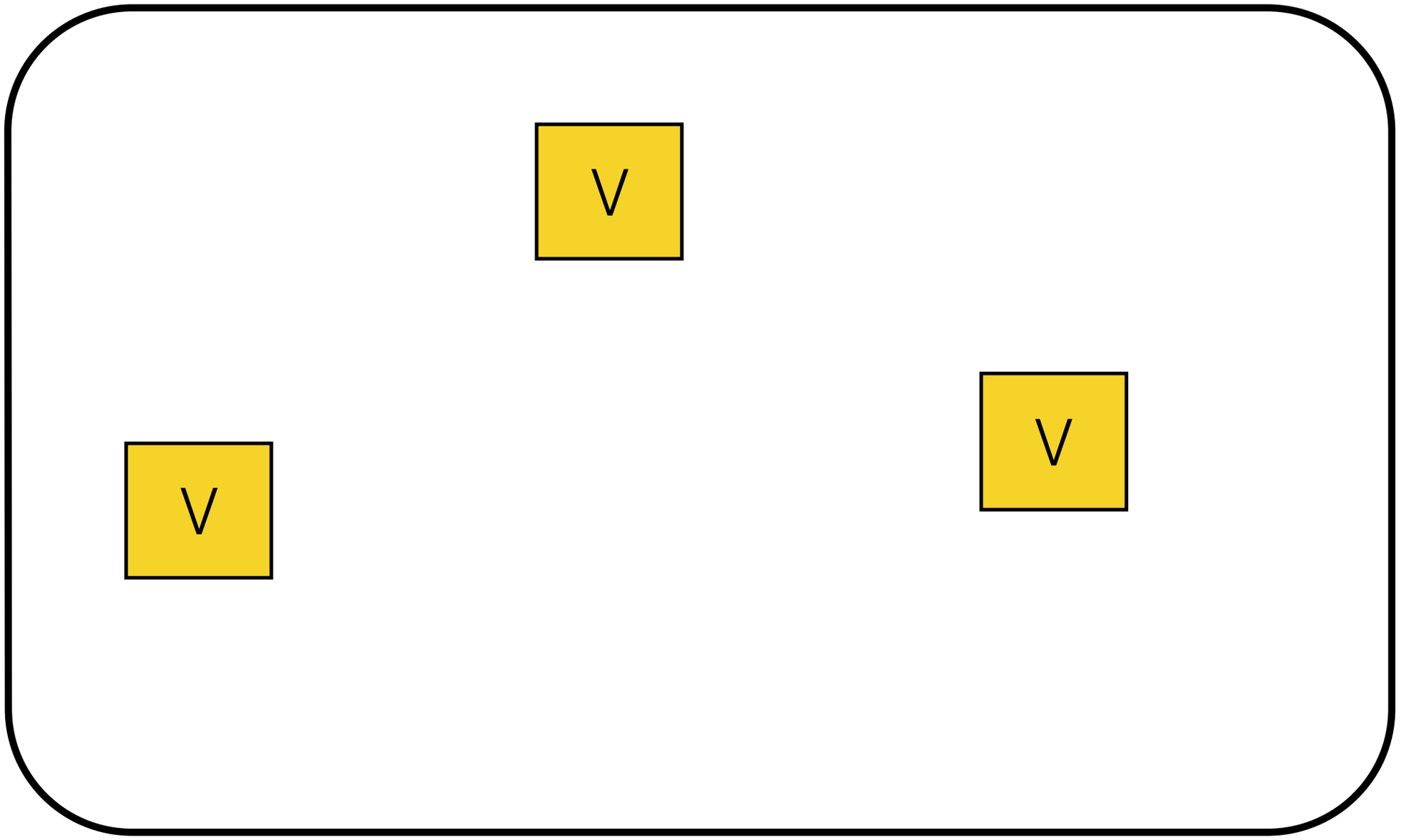
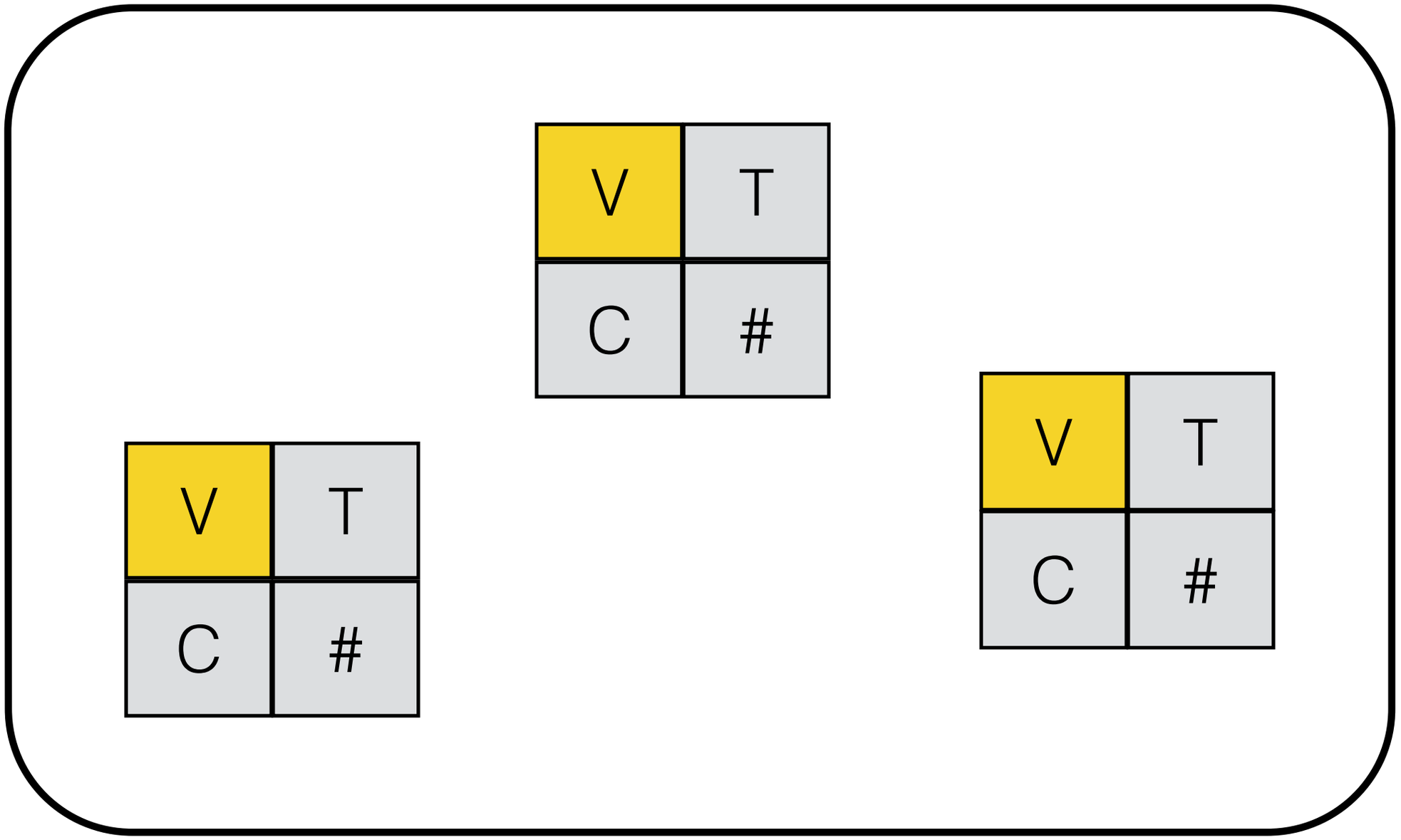


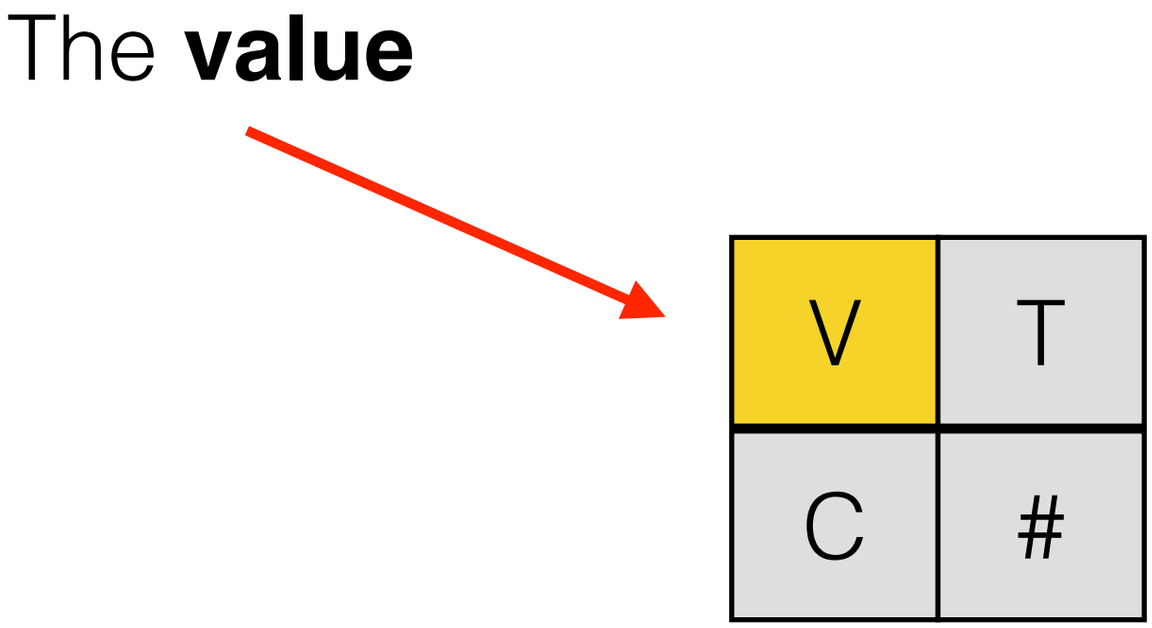
Values and Z-Values



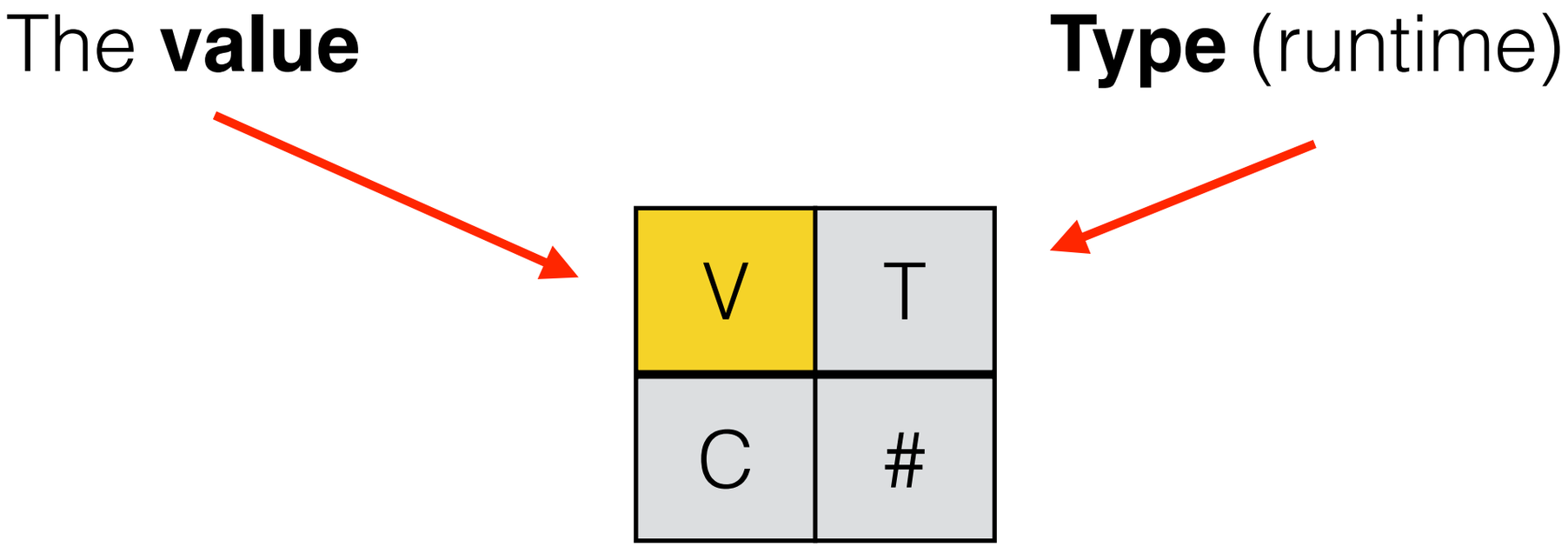
Values and **Z-Values**



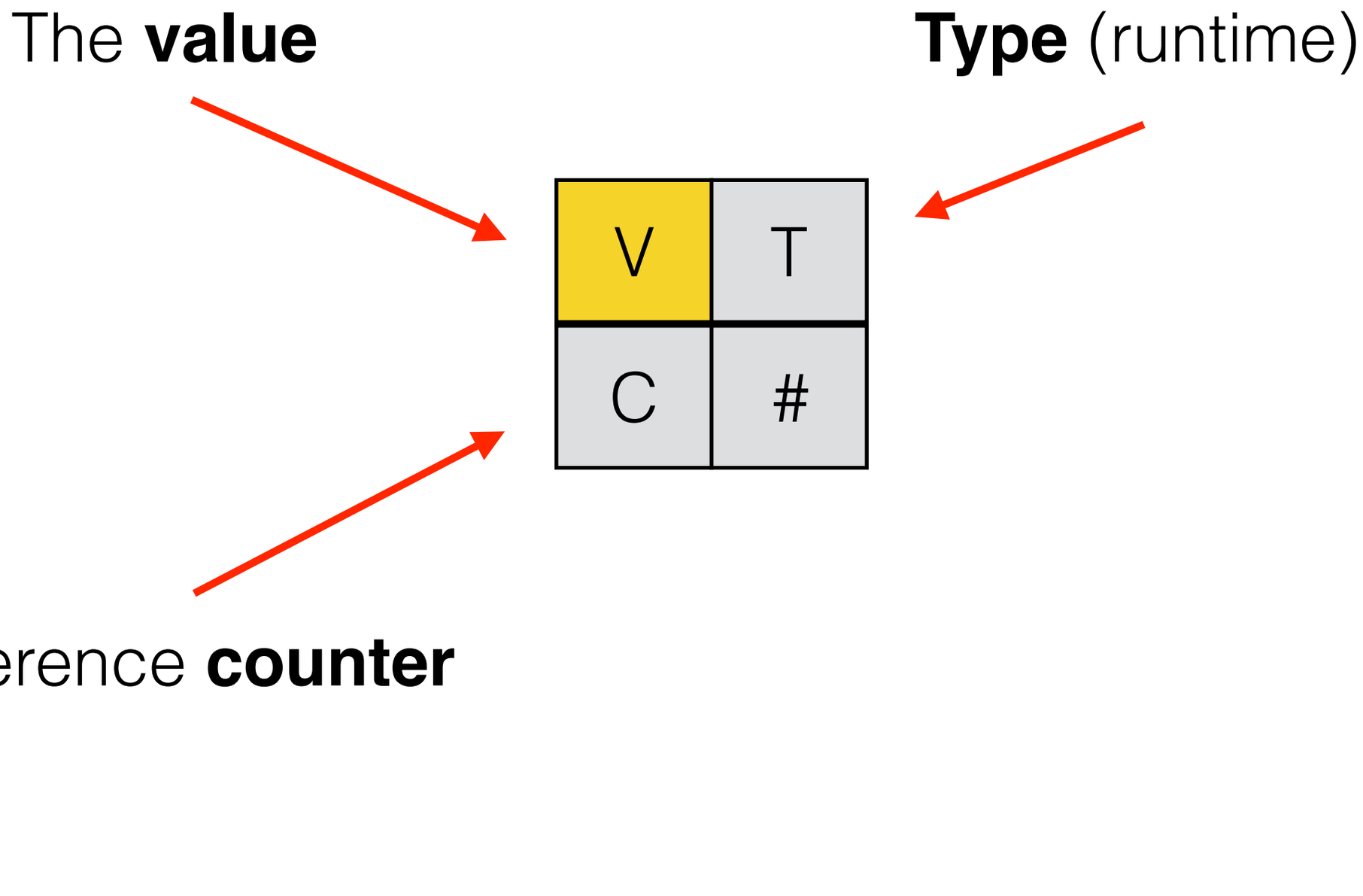
Z-Values



Z-Values



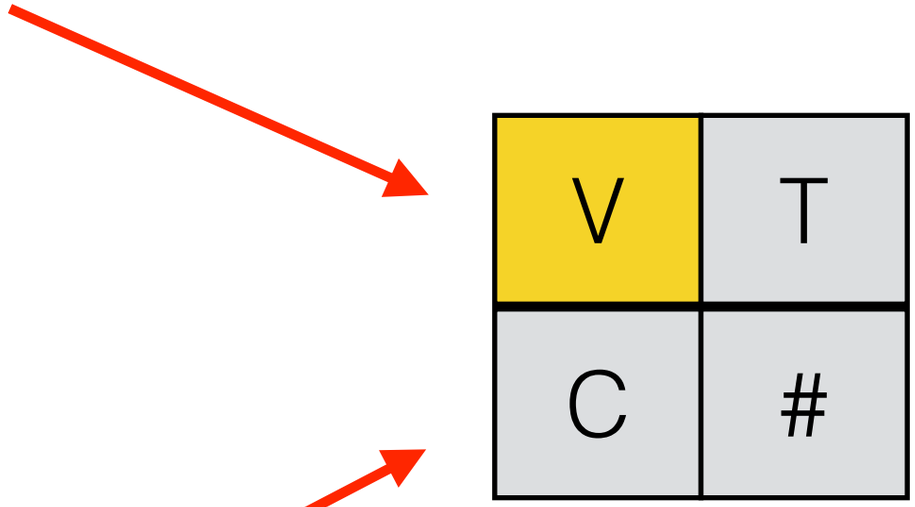
Z-Values



Z-Values

The **value**

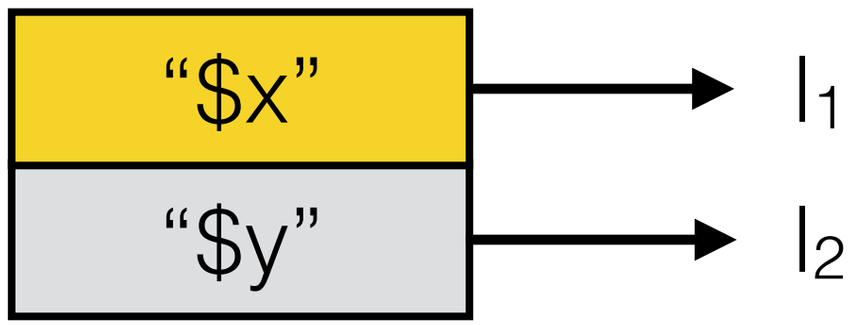
Type (runtime)



Reference **counter**

used for optimisation purposes in Zend

Environments via arrays



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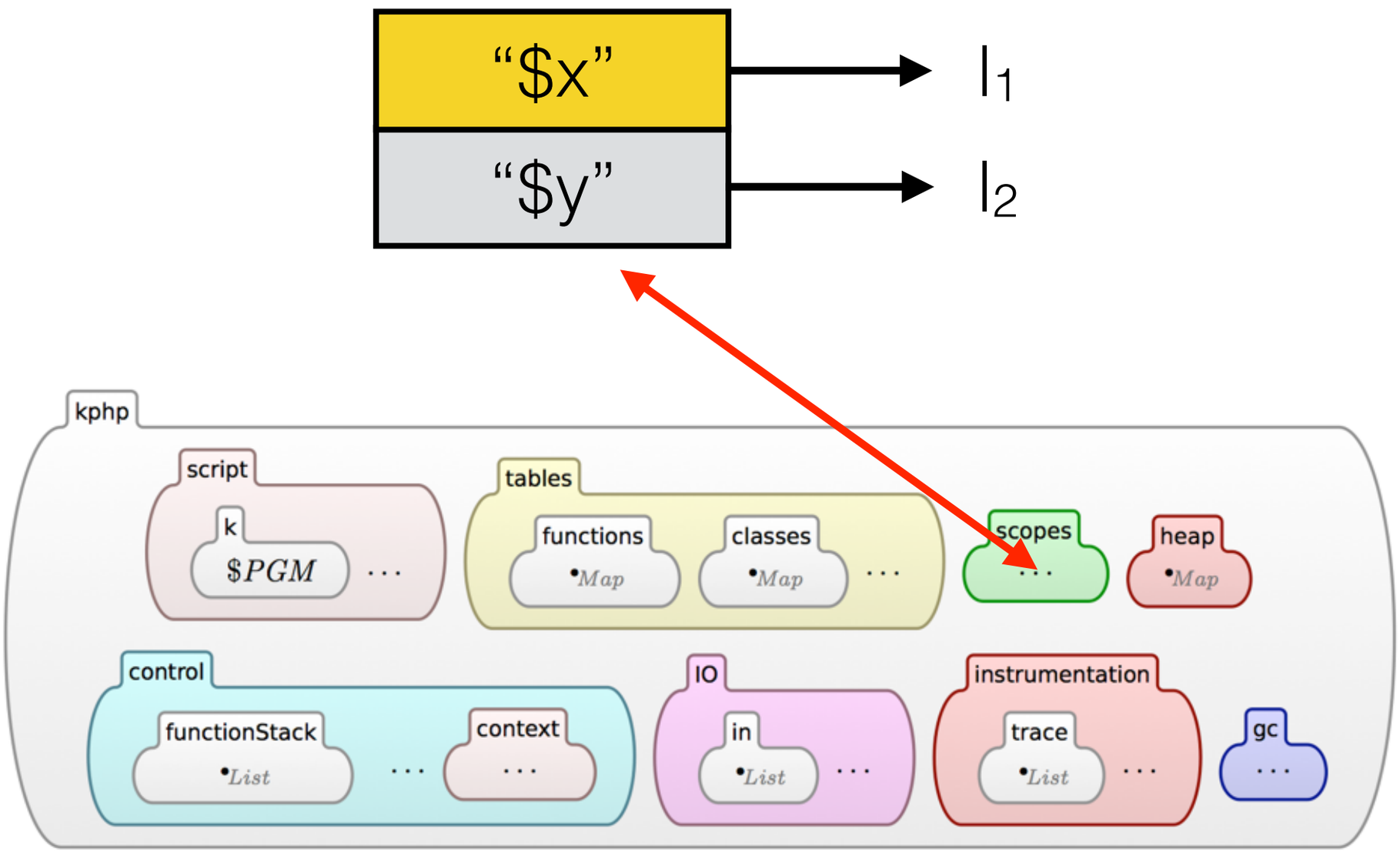
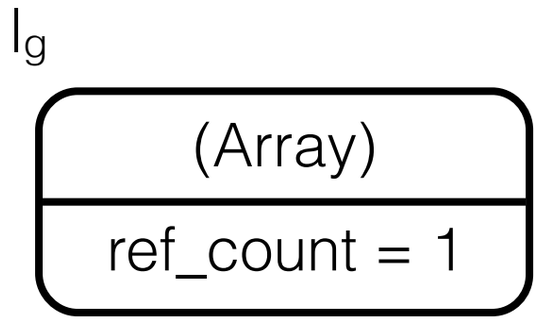


Put it all together

```
$x = array("foo" => 5, "bar" => 5); $y = 5;
next($x);
$x["baz"] = &$x["bar"];
$x [12] = 5;
```



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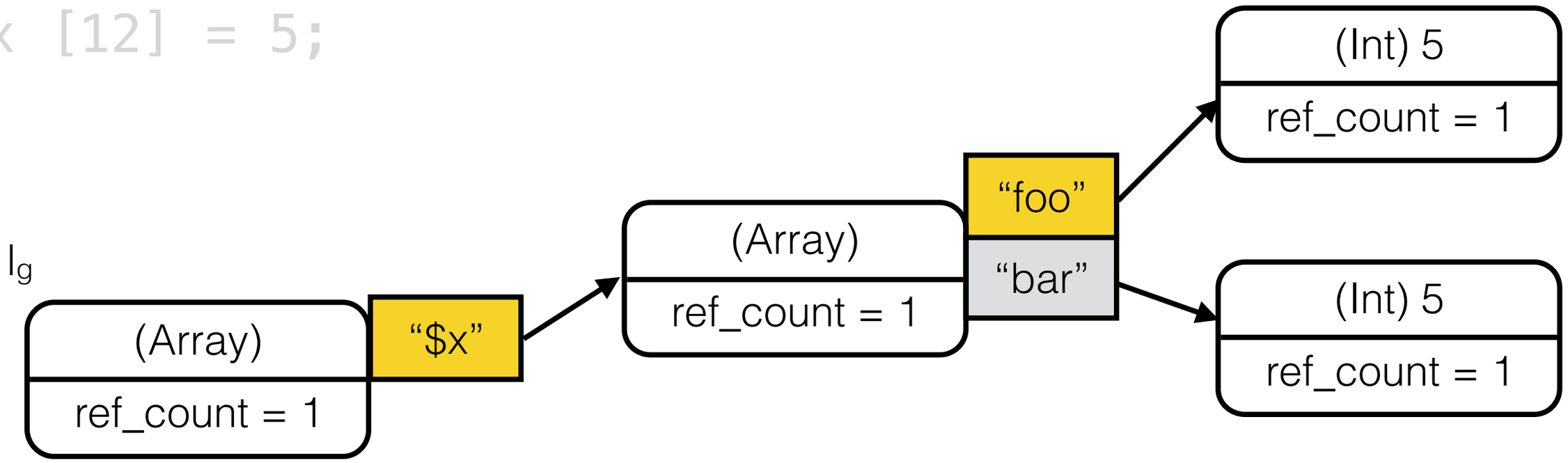

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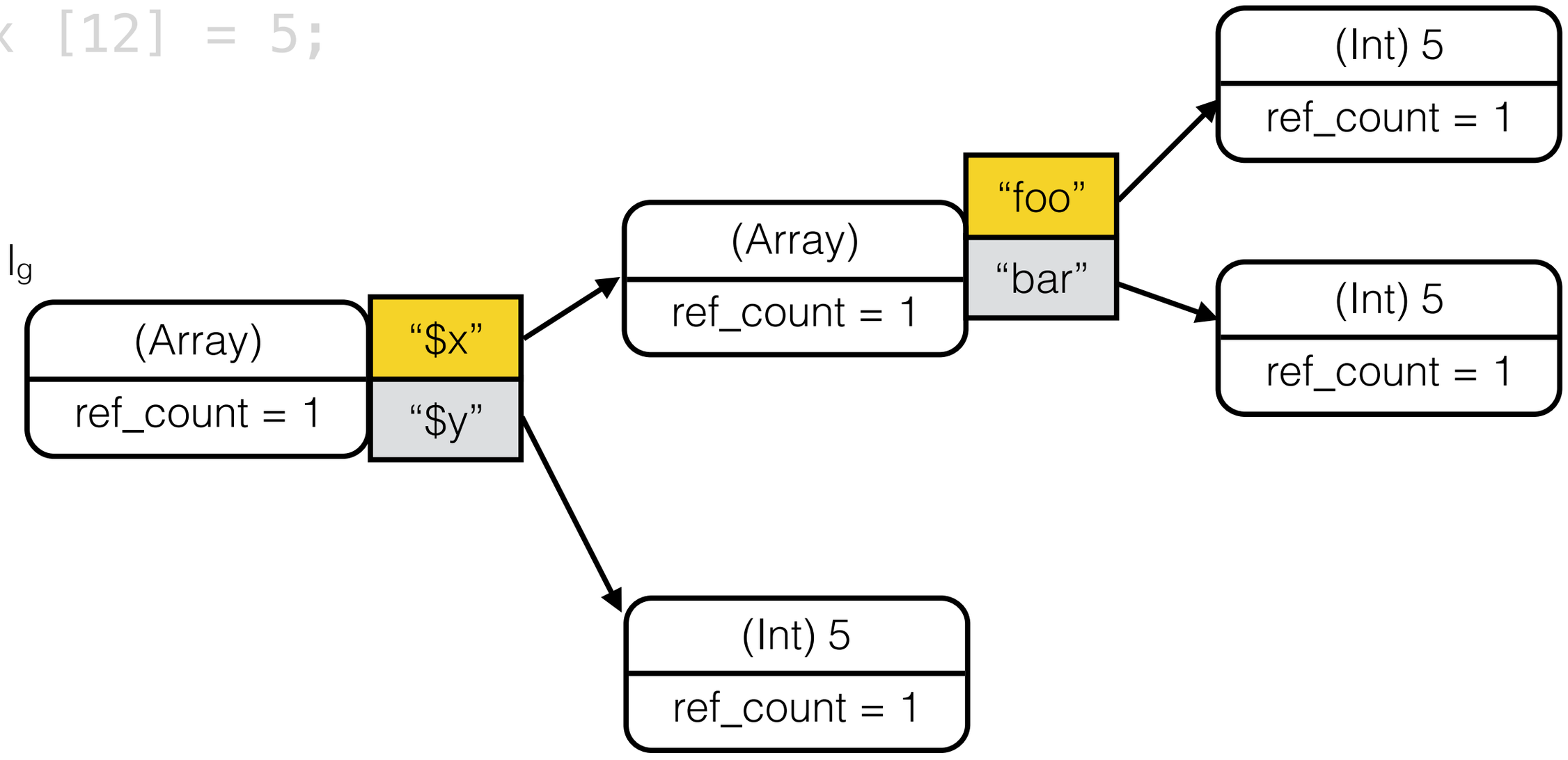

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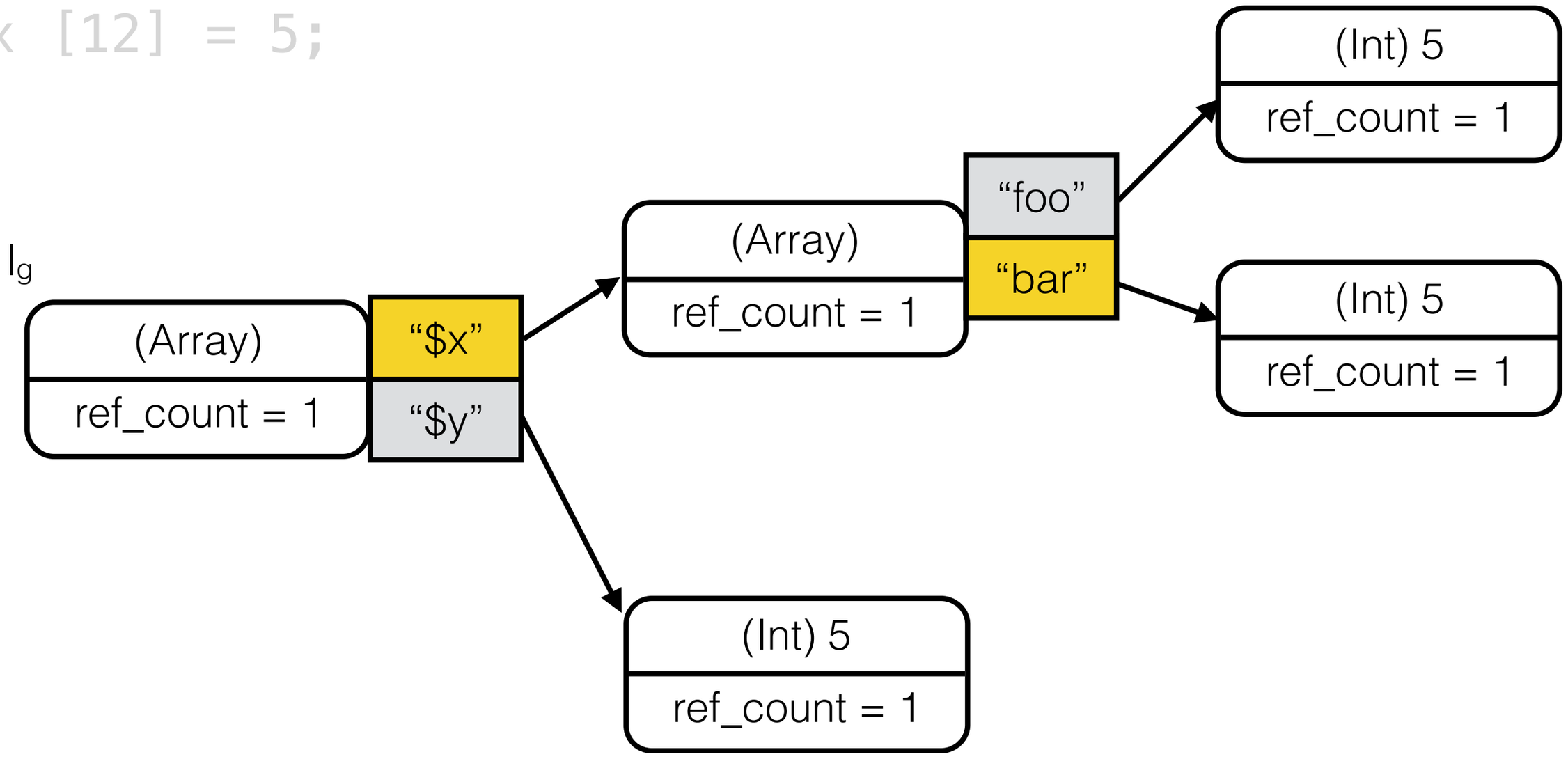

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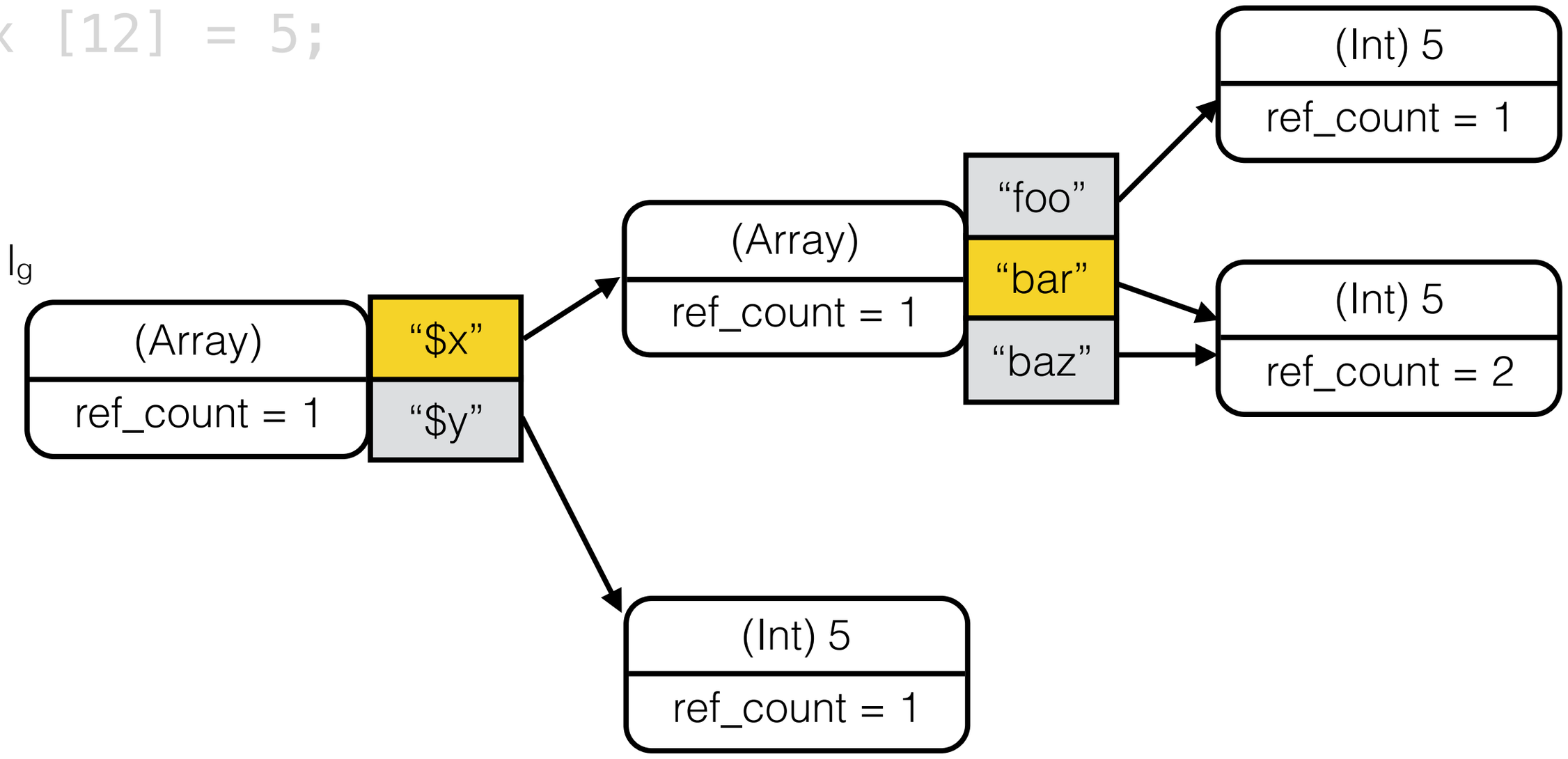

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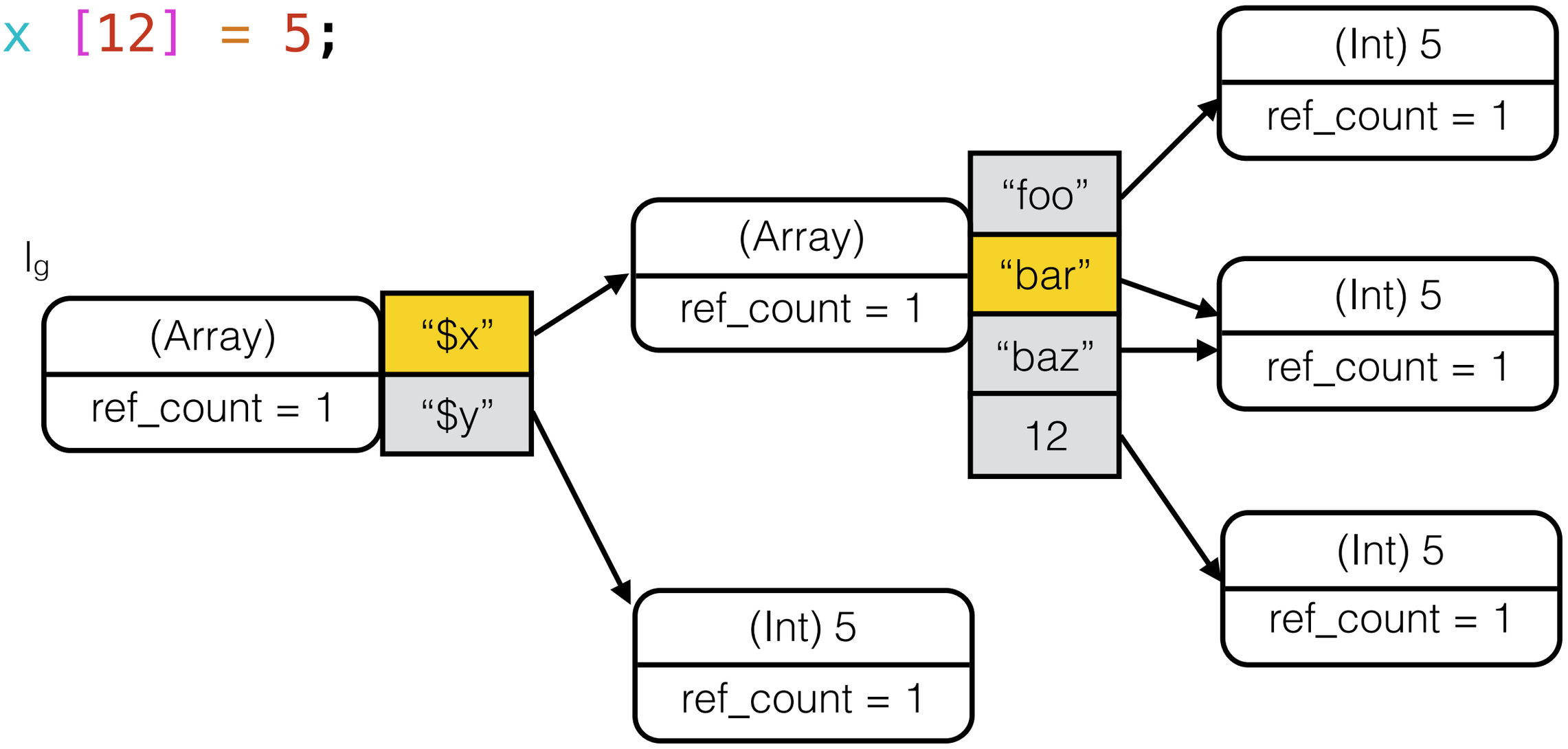


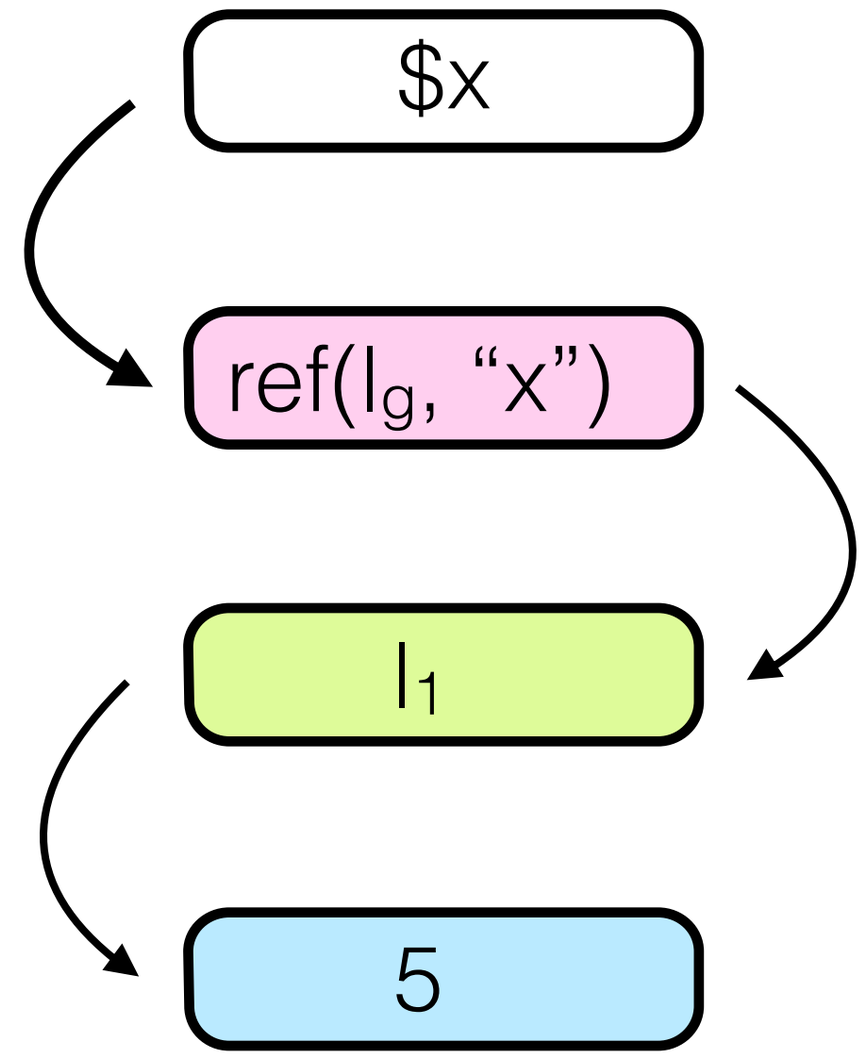
Internal values

- Locations: **l_1, l_2, l_3**....

- References: **ref(l, “x”)**

Internal values

evaluation to a reference



convert to location

convert to language value

Semantic rules: numbers

- ~ 800 rules
- ~ 8000 LOC
- 29 *.k files

Layers

Low-level rules
(copy values, inc. ref. counter, update scope etc.)

Layers

Language **features**
(e.g.: assignment, function call)

Low-level rules
(copy values, inc. ref. counter, update scope etc.)

Layers

Derived Construct
(e.g. x++ —> x = x + 1)

Language **features**
(e.g.: assignment, function call)

Low-level rules
(copy values, inc. ref. counter, update scope etc.)

Example: assignment

(A) CONTEXT 'Assign(□,_)

(B) CONTEXT 'Assign(_:KResult,□)

(C) $$\text{'Assign}\left(\frac{\text{R:Ref}}{\text{convertToLoc(R)}}, \_\right)$$ [intermediate]

(D) $$\frac{\text{'Assign(L:Loc, V:Value)}}{\text{copyValueToLoc(V, L)} \curvearrowright \text{V}}$$ [step]

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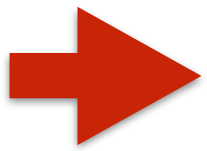
Example: assignment



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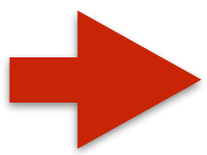

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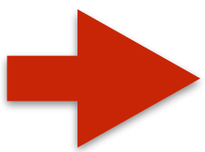

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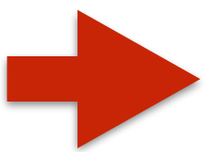

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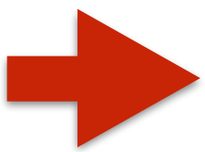

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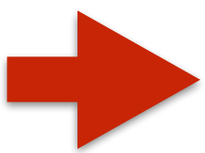

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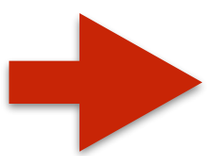

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Example - revisited

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // “onetwo"
```

```php
$a = "one";
$c = $a . ($a = "two");
echo $c; // "twotwo"
```

Evaluation order: LR or RL?

Example - revisited

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```

PHP bug 61188

Evaluation order: LR or RL?

[2012-02-26 19:04 UTC] rasmus@php.net

I do see your argument, but you are making assumptions about how PHP handles sequence points in expressions which is not documented and thus not stricly defined.

[2012-09-01 19:01 UTC] avp200681 at gmail dot com

[...]
I've found in PHP documentation:
"Operators on the same line have equal precedence, in which
case associativity decides the order of evaluation."

Example - explained

```php
$a = array("one");
$c = $a[0] . ($a[0] = "two");
echo $c; // “onetwo"
```

```php
$a = "one";
$c = $a . ($a = "two");
echo $c; // "twotwo"
```

- evaluation order **is left-to-right**
- array access evaluates to values
- variables evaluate to references
- references are resolved lazily

Validation

- Testing against the **Zend test suite.**

- Tests **categorised** (HTTP, date/time, crypto…)

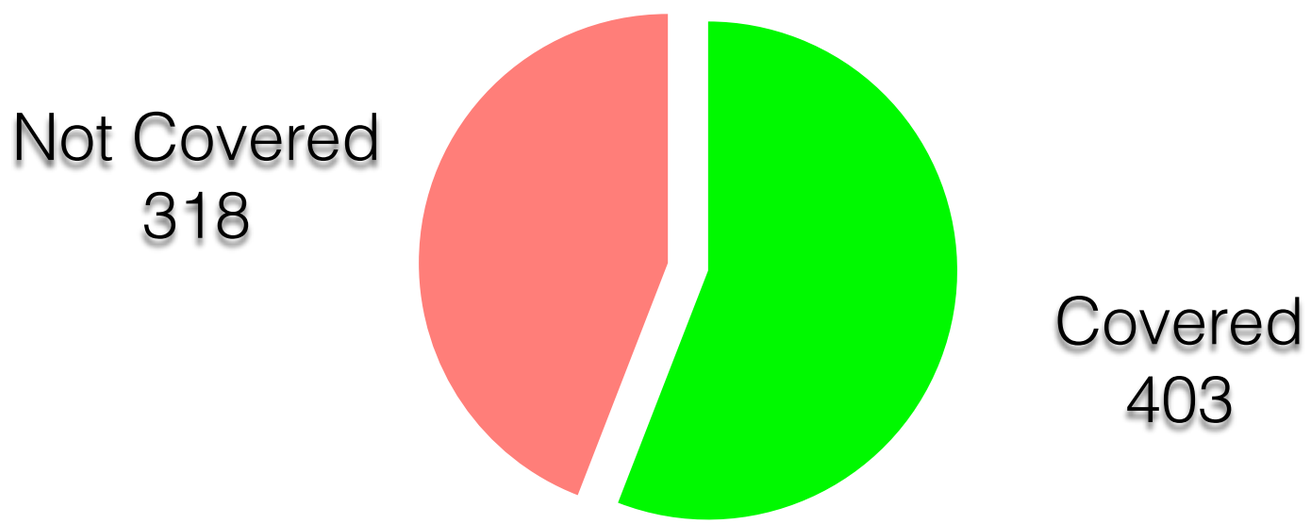
- focusing on **core language** section of test suite

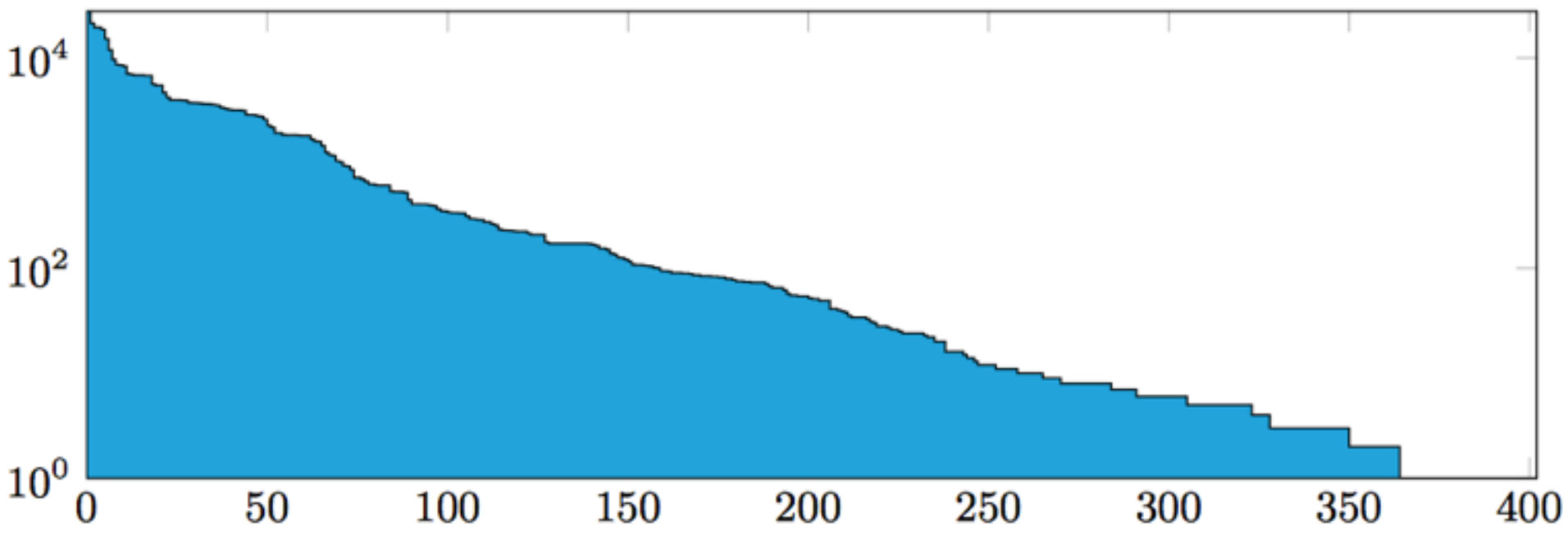
- passing all tests supported by our semantics

zend/lang/002.phpt

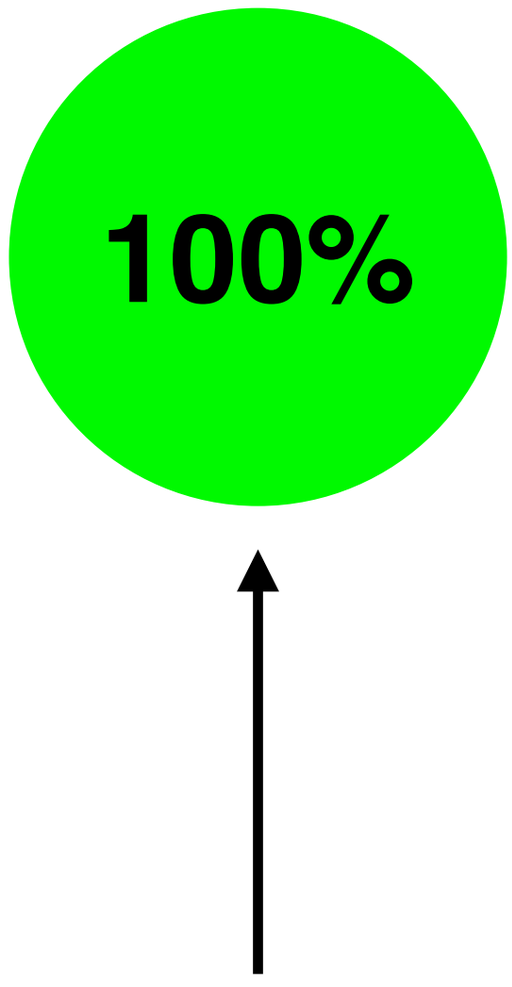
```
--TEST--
Simple While Loop Test
--FILE--
<?php
    $a=1;
    while ($a<10) {
        echo $a;
        $a++;
    }
?>
--EXPECT--
123456789
```

Coverage


Not Covered
318
Covered
403


10^4
10^2
10^0
0
50
100
150
200
250
300
350
400

Coverage



(Zend + **Own test suite**)

Temporal verification of PHP programs

Extension of LTL with predicates over KPHP configurations

LTL example

```
function foo() {
    global $y;
    $x = &$y;
}
```

LTL example

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
```

LTL example

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
foo();
```

LTL example

```
function foo() {
    global $y;
    $x = &$y;
}
$y = #symbolic_input();
foo();
```

◊alias(fv('foo',var('x')),gv(var('y')))

Future Work

Add language features

Fix bugs

Future Work

Add language features

Fix bugs

Deductive verification (**Reachability Logic**)

Add language features

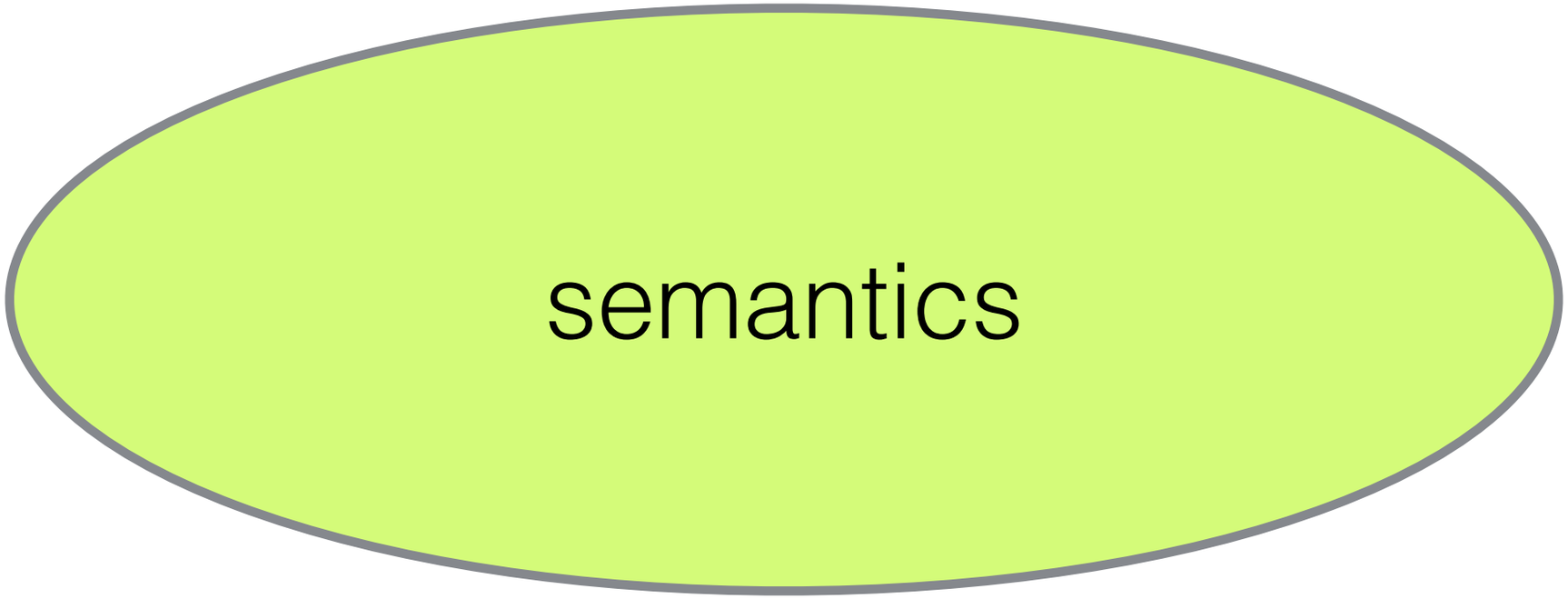
Fix bugs

Future Work

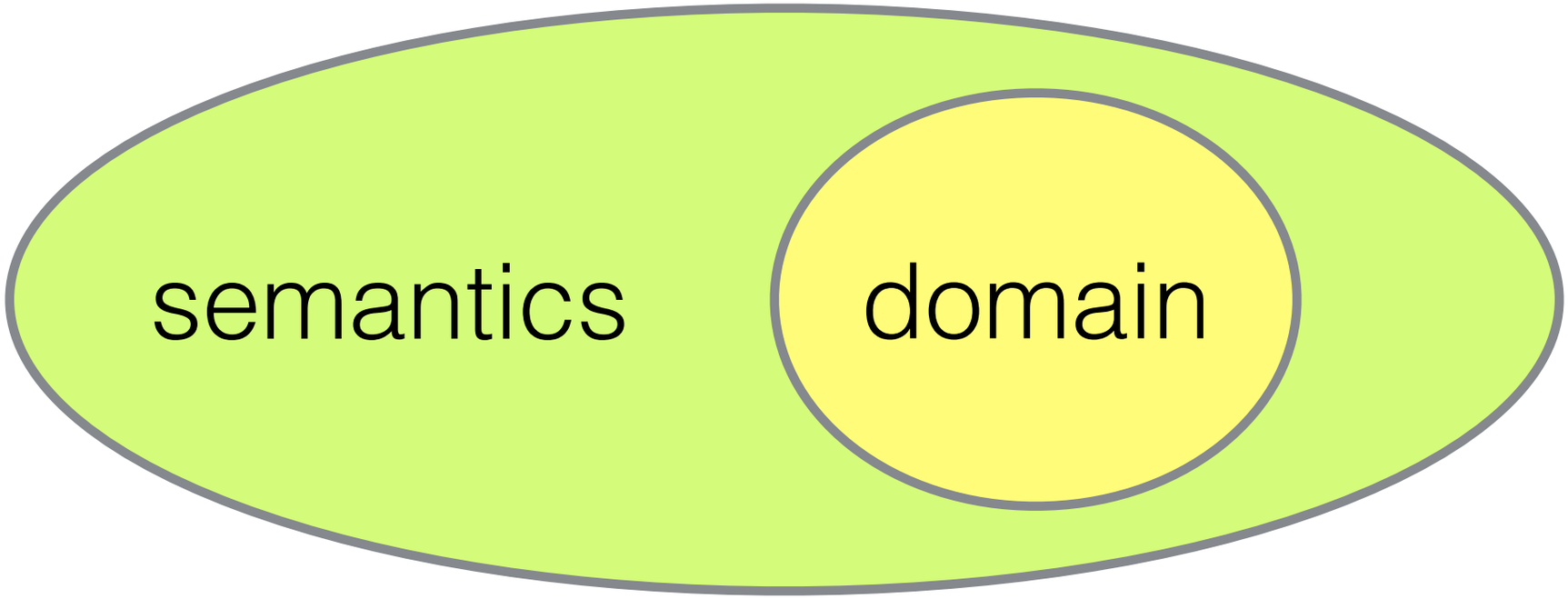
Deductive verification (**Reachability Logic**)

Static Analysis **(Abstract Interpretation)**

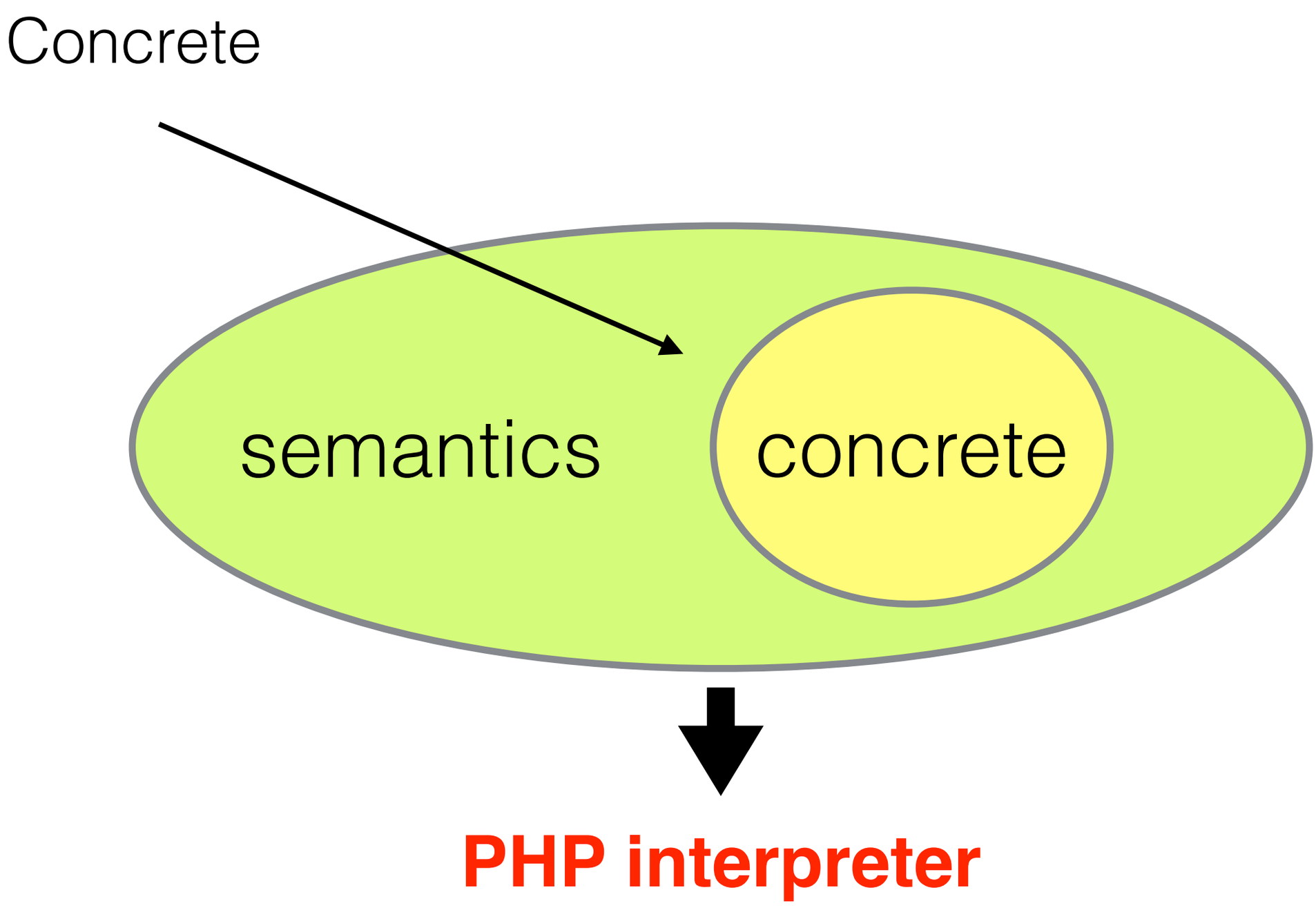
Abstract Interpretation



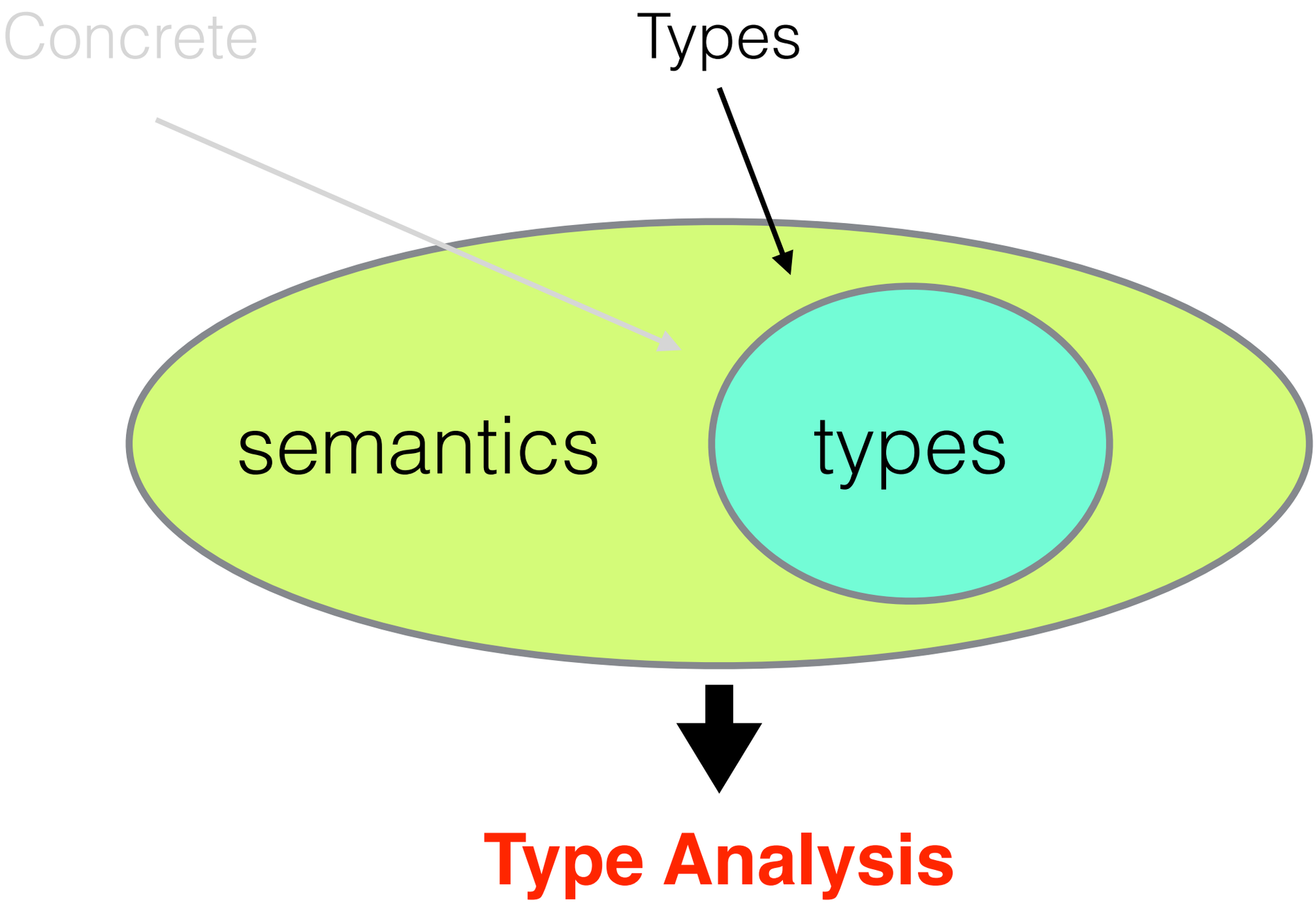
Abstract Interpretation



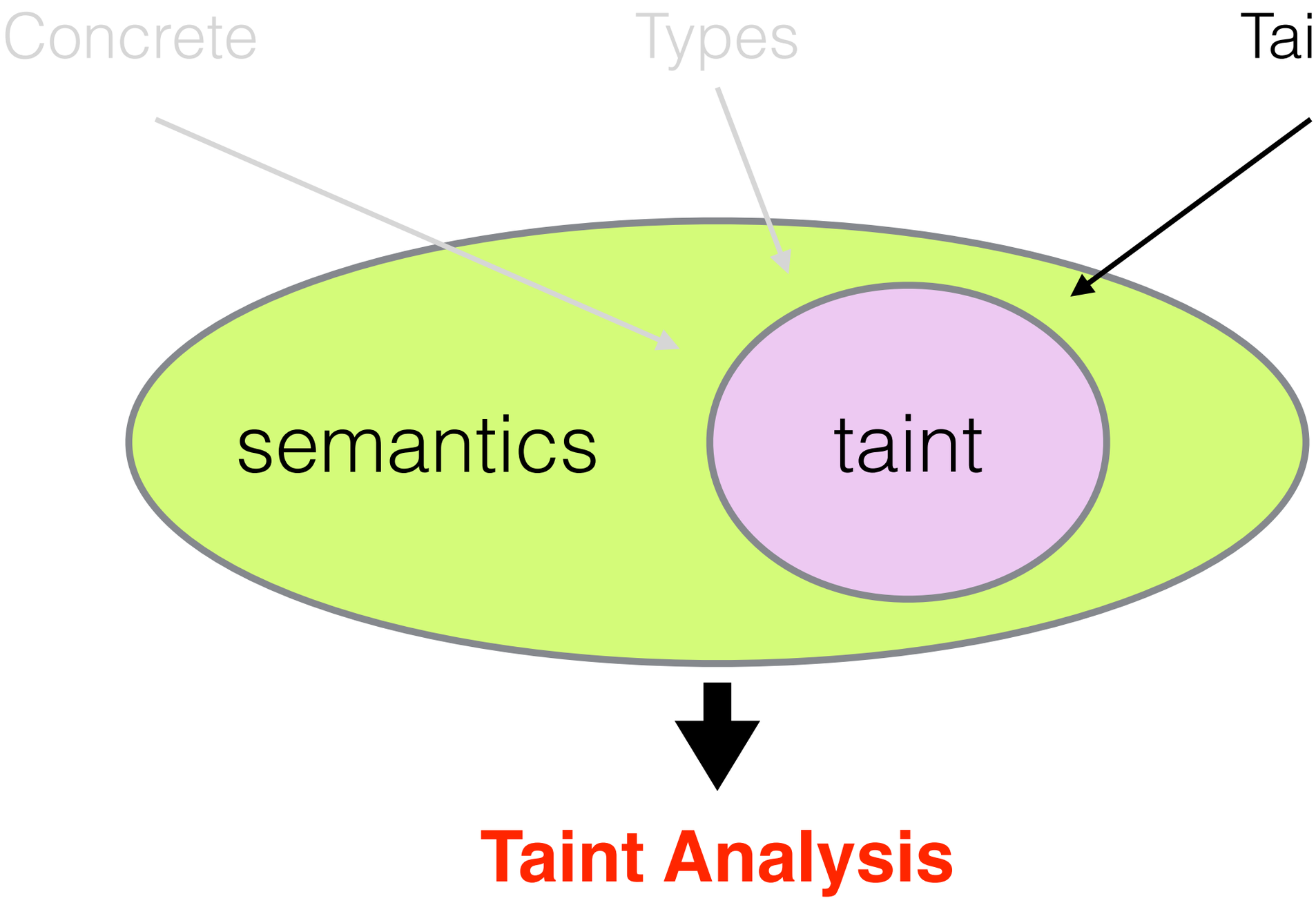
Abstract Interpretation



Abstract Interpretation

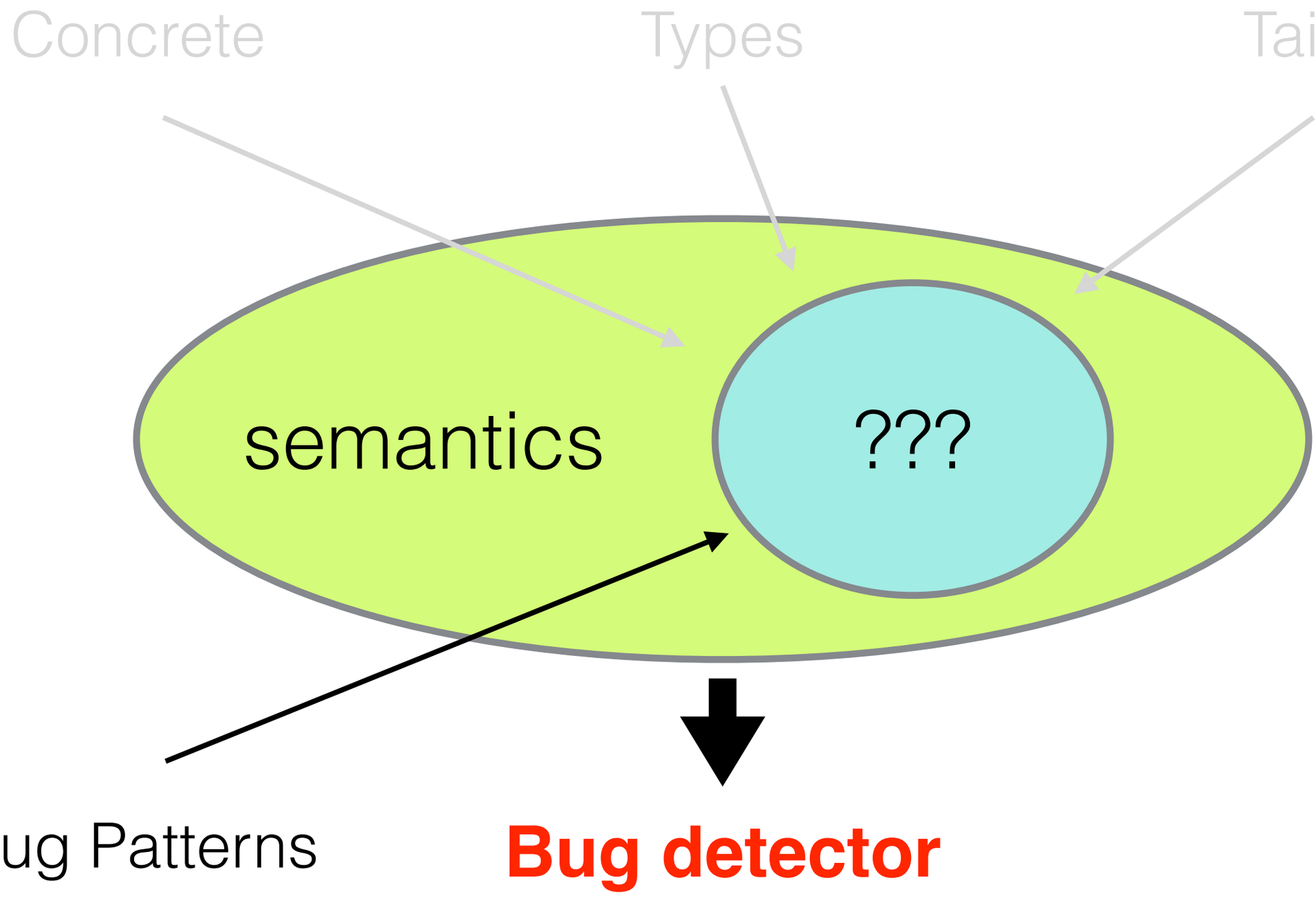


Abstract Interpretation



Taint Analysis

Abstract Interpretation

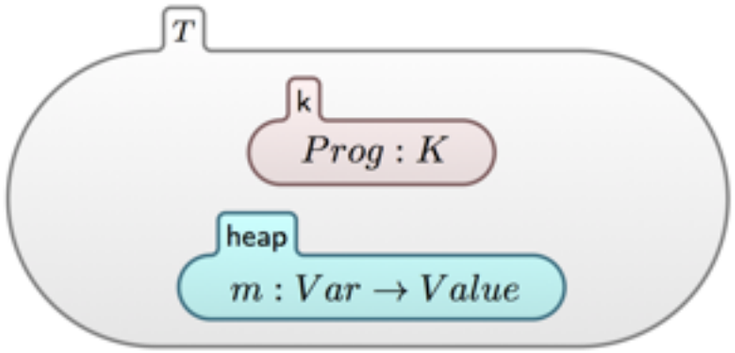


Thank you!

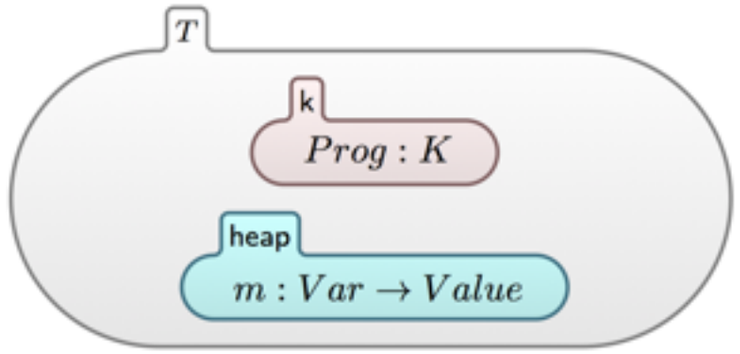
www.phpsemantics.org

paper, sources, web interface

Appendix/misc/old

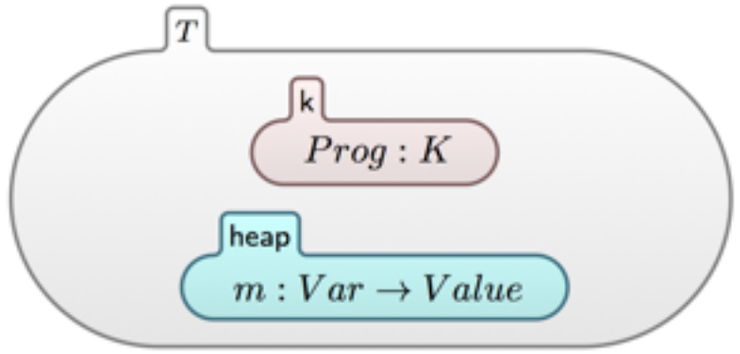


Komputations



Komputations

(i) the K cell holds **a list of computations separated by** ↷

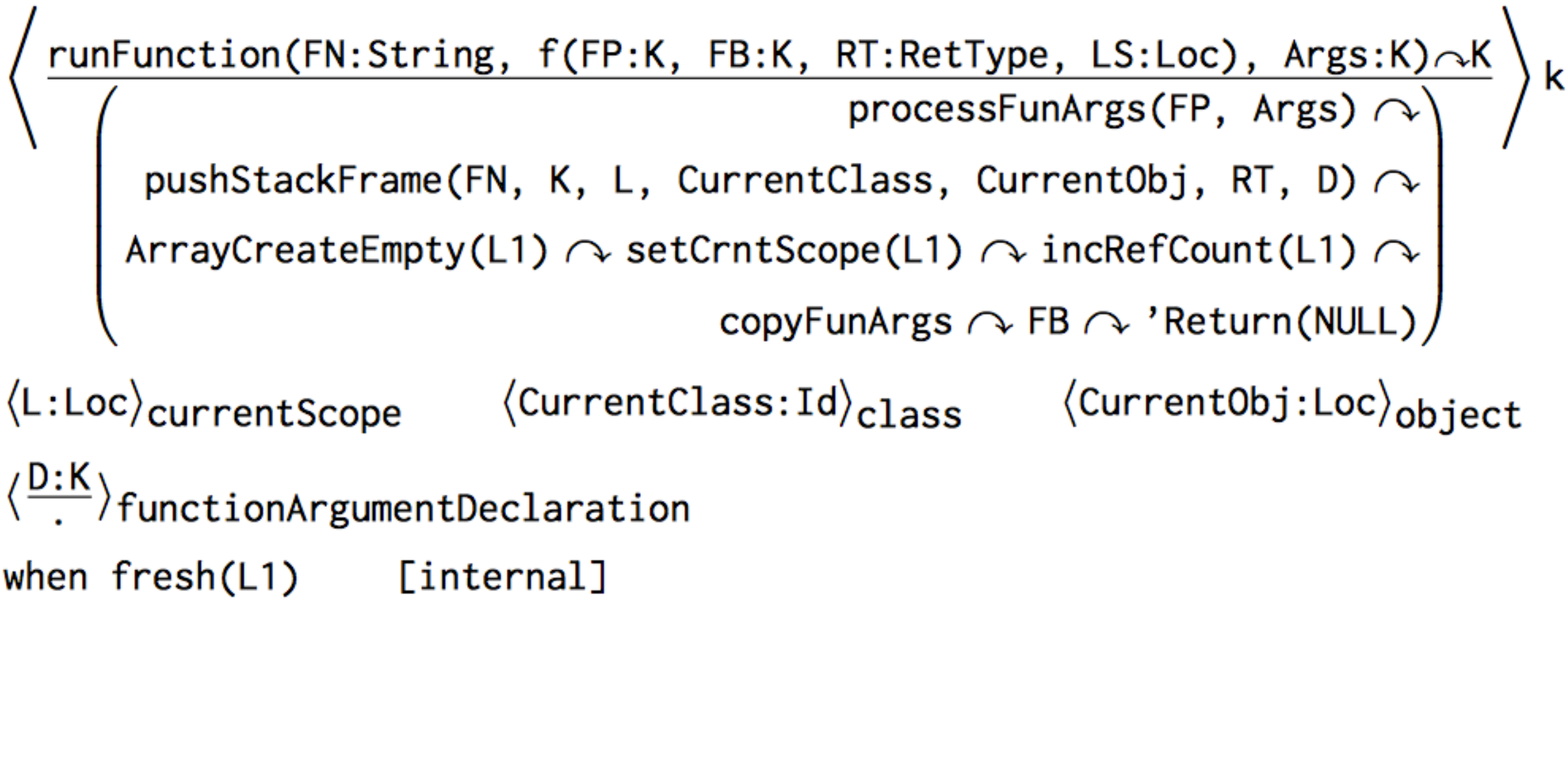


Komputations

(i) the K cell holds **a list of computations separated by** ↷

(ii) the input program goes into the k cell

Example: function call



```php
$a = array("a", "b", "c");
```

```php
$a = array("a", "b", "c");
foreach($a as &$v) {};
```

```php
$a = array("a", "b", "c");
foreach($a as &$v) {};
foreach($a as $v) {};
```

```php
$a = array("a", "b", "c");
foreach($a as &$v) {};
foreach($a as $v) {};
var_dump($a);
```

```php
$a = array("a", "b", "c");
foreach($a as &$v) {};
foreach($a as $v) {};
var_dump($a);
```

```
array(3) {
   [0]=> string(1) "a"
   [1]=> string(1) "b"
   [2]=> &string(1) "b"
}
```