

A partially marginalized likelihood for exoplanet inference

David W. Hogg (NYU)

with help from Paul Baines (Davis) and everyone else at SAMSI Kepler

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abstract: We present a likelihood function for the time-series photometry that makes up a lightcurve from the *Kepler* mission (or similar experiment). The function includes parameters that describe stochastic stellar variability and parameters that describe periodic exoplanet (or other companion) transits. The stellar variability model is a Gaussian Process in a wavelet basis that is capable of modeling non-trivial time correlations with a diagonal covariance matrix. These choices make it possible to *marginalize out* all stellar-variability parameters, leaving the user with a flexible likelihood function parameterized only by exoplanet parameters. We show **something non-trivial**.

1 generalities

There are N observations Y_n of a single star taken at times t_n . The model is

$$Y_n = [1 - q(t_n | \omega)] F(t_n | \alpha) + e_n \quad , \quad (1)$$

where $q(\cdot | \omega)$ is a function that describes the attenuation of the starlight caused by the transiting exoplanet, ω is a blob of parameters describing an exoplanet's size and orbit, $F(\cdot | \alpha)$ is a function that describes the apparent brightness of the star as a function of time, α is a blob of parameters describing the stellar mean flux and variability, and e_n is the noise contribution to the n th datum (coming from photon and read noise, among other things). This description—plus a model for the noise—will lead to a justifiable likelihood function. If we model the noise contributions as being Gaussian and

independent with known variances σ_n^2 , the likelihood function becomes

$$p(\{Y_n\}_{n=1}^N \mid \omega, \alpha, \varphi) = \prod_{n=1}^N p(Y_n \mid \omega, \alpha, \varphi) \quad (2)$$

$$p(Y_n \mid \omega, \alpha, \varphi) = N(Y_n \mid \mu_n, \sigma_n^2) \quad (3)$$

$$\mu_n \equiv [1 - q(t_n \mid \omega)] F(t_n \mid \alpha) \quad , \quad (4)$$

where $\{Y_n\}_{n=1}^N$ is the set of all data, φ is an enormous blob of hyperparameters that includes all our decision-making and assumptions (and more, soon), the product in the likelihood encodes our “independent noise” assumption, and $N(x \mid m, V)$ is the Gaussian for x with mean m and variance V ,

By assumption, we care only about the exoplanet parameters ω and not in the least about the star parameters α .