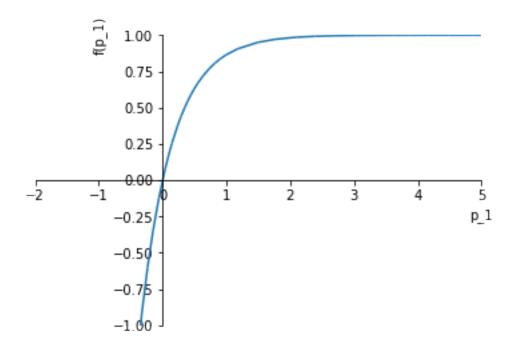
Sol_HW_8

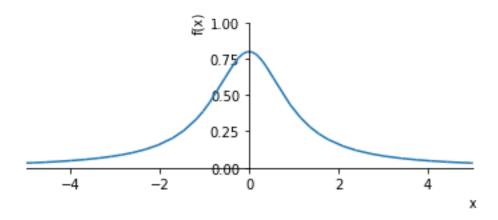
May 11, 2018

```
In [1]: from sympy import *
         init_printing()
         from IPython.display import display
         from sympy.functions import Abs
0.1 Problema 3
In [2]: p,x,k = symbols('p x k', \
                                   real=True)
         s, h, m, t, k0, p1 = symbols('sigma hbar m t k_0 p_1', real=True, \
                     positive=True)
         mom_repr = nsimplify(exp(-Abs(p)/(h*k0)))
         Nsq=integrate(mom_repr*mom_repr, (p,-oo,oo), conds='none')
         mom_repr/=sqrt(Nsq)
         mom\_repr\_t = exp(-I*(p**2/(2*m))*t/h)*mom\_repr
         display(simplify(mom_repr_t))
         abs(mom_repr)**2==abs(mom_repr_t)**2
                                     \frac{1}{\sqrt{\hbar}\sqrt{k_0}}e^{\frac{1}{\hbar}\left(-\frac{ip^2t}{2m}-\frac{|p|}{k_0}\right)}
Out[2]: True
In [3]: P_p1 = 2*integrate(exp(-2*p/(h*k0))/Nsq, (p, 0, p1), conds='none')
         pl=plot(P_p1.subs(h,1).subs(k0,1), xlim=(-2,5), ylim=(-1,1))
         display(P_p1)
<matplotlib.figure.Figure at 0x7f7f6deeb490>
                                           1 - e^{-\frac{2p_1}{\hbar k_0}}
<matplotlib.figure.Figure at 0x7f7f691f1f90>
```

In []: pl.show()



$$\frac{\sqrt{2}\sqrt{k_0}}{\sqrt{\pi}\left(k_0^2x^2+1\right)}$$



0

 $\frac{1}{k_0}$

 $\frac{\hbar k_0}{2}\sqrt{2}$

Out[5]:

$$\frac{\sqrt{2}\hbar}{2}\geq\frac{\hbar}{2}$$

$$\frac{\hbar^2 k_0^2}{2}$$

1 Punto 14

```
In [7]: from sympy.physics.matrices import msigma
           a,b, w = symbols('a b omega_0', real=True)
           H = h*w*diag(1, 2, 2)
           A = a*diag(1,msigma(1))
           B = b*diag(msigma(1), 1)
In [8]: display(H.eigenvects())
           Psi_0 = nsimplify(1/sqrt(2))*H.eigenvects()[0][2][0]+nsimplify(0.5)*H.eigenvects()[1][2]
           display(Psi_0)
           display('avg E', nsimplify(0.5*H.eigenvects()[0][0] + 2*0.25*H.eigenvects()[1][0]))
           display('delta E', sqrt(simplify(nsimplify(0.5*H.eigenvects()[0][0]**2 + 2*0.25*H.eigenv
                      nsimplify(0.5*H.eigenvects()[0][0] + 2*0.25*H.eigenvects()[1][0])**2))
                      \left[ \left( \hbar \omega_0, \quad 1, \quad \left| \begin{array}{c} 1 \\ 0 \\ 0 \end{array} \right| \right), \quad \left( 2\hbar \omega_0, \quad 2, \quad \left[ \begin{array}{c} 0 \\ 1 \\ 0 \end{array} \right], \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{array} \right] \right) \right]
'avg E'
                                                         \frac{3\omega_0}{2}\hbar
'delta E'
                                                         \frac{\hbar |\omega_0|}{2}
In [9]: A.eigenvects()
           #Note que los vectores propios de A son u1 (vp a), N*(u2+u3) (vp a) y N*(-u2+u3) (vp -a)
    Out [9]:
                        \left[ \begin{pmatrix} -a, & 1, & \begin{bmatrix} 0 \\ -1 \\ 1 \end{bmatrix} \right], \quad \begin{pmatrix} a, & 2, & \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, & \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \right] \right]
In [10]: Psi_t = Matrix([[exp(-I*t*H.eigenvects()[0][0])*Psi_0[0]], \
                                     [exp(-I*t*H.eigenvects()[1][0])*Psi_0[1]], [exp(-I*t*H.eigenvects()[1][0]
             display(Psi_t)
             Psi_t_T = adjoint(Psi_t)
             display(Psi_t_T)
```

$$\begin{bmatrix} \frac{\sqrt{2}}{2}e^{-i\hbar\omega_0t} \\ \frac{1}{2}e^{-2i\hbar\omega_0t} \\ \frac{1}{2}e^{-2i\hbar\omega_0t} \end{bmatrix}$$
$$\begin{bmatrix} \frac{\sqrt{2}}{2}e^{i\hbar\omega_0t} & \frac{1}{2}e^{2i\hbar\omega_0t} & \frac{1}{2}e^{2i\hbar\omega_0t} \end{bmatrix}$$

In [11]: display(Psi_t_T*A*Psi_t) display(Psi_t_T*B*Psi_t)

[a]

$$\left[\frac{\sqrt{2}b}{4}e^{i\hbar\omega_0t} + \frac{b}{4} + \frac{\sqrt{2}b}{4}e^{-i\hbar\omega_0t}\right]$$

In [12]: $simplify((A*Psi_t))$ #Se mide a, note que $A*Psi_t = a*Psi_t$

Out[12]:

$$\begin{bmatrix} \frac{\sqrt{2}a}{2}e^{-i\hbar\omega_0t} \\ \frac{a}{2}e^{-2i\hbar\omega_0t} \\ \frac{a}{2}e^{-2i\hbar\omega_0t} \end{bmatrix}$$

In [13]: B.eigenvects()

Out[13]:

$$\left[\begin{pmatrix} -b, & 1, & \begin{bmatrix} \begin{bmatrix} -1\\1\\0 \end{bmatrix} \end{bmatrix} \right), & \begin{pmatrix} b, & 2, & \begin{bmatrix} \begin{bmatrix} 1\\1\\0 \end{bmatrix}, & \begin{bmatrix} 0\\0\\1 \end{bmatrix} \end{bmatrix} \right) \right]$$

In $\lceil 14 \rceil$: #Medir -b

display(simplify((abs((nsimplify(1/sqrt(2))*adjoint(B.eigenvects()[0][2][0])*Psi_t)[0])

display(simplify((abs(nsimplify(1/sqrt(2))*adjoint(B.eigenvects()[1][2][0])\ *Psi_t)[0]**2+abs(adjoint(B.eigenvects()[1][2][1])*Psi_t)[0]**2).r

$$-\frac{\sqrt{2}}{4}\cos\left(\hbar\omega_0t\right) + \frac{3}{8}$$

$$\frac{\sqrt{2}}{4}\cos\left(\hbar\omega_0t\right) + \frac{5}{8}$$