# A Rodin Plug-in for Probabilistic Event-B based on a Rewriting Logic Approach

Daniel F. Osorio-Valencia

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### Abstract

# Acknowledgments

### Contents

1	Introduction Literature Review		4
<b>2</b>			5
	2.1	Event-B	5
	2.2	Probabilistic Event-B	7
	2.3	Maude	7
	2.4	Object-Based Programming	12
	2.5	PMaude	14
	2.6	PVeStA	17
	2.7	A Rewriting Logic Semantics and Statistical Analysis for Proba-	
		bilistic Event-B	18
	2.8	Rodin and Plugin Development	18
3	Methodology		19
4	Results		20
5	Discussion		21
6	Conclusions		22

# Introduction

### Literature Review

The main purpose of this chapter is to present the needed theoretical and technical background to understand how the plugin works. Therefore, a short but sufficient definition of various concepts and tools will be given. In terms of theoretical context, this chapter will discuss topics like Event-B, Maude and the rewriting logic approach to Event-B. Furthermore, this chapter will also provide some insight into plugin development in Rodin. To guide the reader through the different sections of this chapter and facilitate its reading, the following section dependency is given:

#### 2.1 Event-B

Event-B [1, 2] is a formal method for specifying and verifying properties about systems based on set theory and predicate logic. Specifications in Event-B are referred as models and they contain the mathematical development for a discrete transition system. The main components of an Event-B model are machines and contexts: machines contain the dynamic elements of the model, while contexts contain the static elements. Specifically, machines contain the system variables, invariants, theorems, variant and events. On the other hand, contexts contain carrier sets, constants, axioms and theorems. Both machines and contexts have different interactions between them. A machine can "see" one or several context, meaning that the machine includes the static elements specified in these contexts. Furthermore, machines can "refine" other machines, which means that if a machine  $M_2$  refines a machine  $M_1$ , then  $M_2$  can use all the dynamic elements specified in  $M_1$  and also create new ones that respect the properties defined in  $M_1$  (for example properties defined as invariants). This relation also occurs in the same way between contexts, when one context "extends" another one. Figure 2.1 illustrates how machines and contexts interact: In terms of syntax, the general structure for contexts is the one expressed in 2.2, such that:

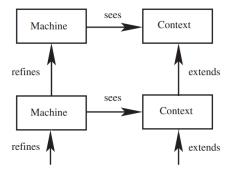


Figure 2.1: Machine and context relationship, taken from [1]

- context\_identifier is a string that identifies the context. The context identifier must be different to all the other components of the system (other machines or contexts).
- The "extends" clause lists all the contexts identifiers that the current context is extending.
- The clause "sets" takes a list of set identifiers. Each one of these set identifiers correspond to the name of one of the carrier sets of the model.
- The "constants" clause lists all the constants of the model.

```
< context\_identifier > \\ extends \\ < context\_identifier\_list > \\ sets \\ < set\_identifier\_list > \\ constants \\ < constant\_identifier\_list > \\ axioms \\ < label >: < predicate > \\ ... \\ theorems \\ < label >: < predicate > \\ ... \\ end
```

Figure 2.2: Context structure, taken from [1]

#### 2.2 Probabilistic Event-B

#### 2.3 Maude

Maude [3, 4, 5] is a high performance declarative language, that allows the specification of programs or systems, and their formal verification. Maude programs are represented as *functional modules* declared with syntax:

```
\begin{array}{c} \text{fmod MODULENAME is} \\ \text{BODY} \\ \text{endfm} \end{array}
```

where *MODULENAME* is the name of the functional module, and *BODY* is a set of declarations that specify the program. The body of the module contains *sorts* (written in Maude as sorts), where each sort correspond to an specific data type of the program. It also contains a set of function symbols or function declarations called *operators* (abbreviated as op in Maude), that specify the constructors of the different sorts, along with the syntax of the program functions. Finally, a set of *equations* (abbreviated as eq in Maude) is used to define the behavior of the functions. These equations use *variables* (abbreviated as var in Maude) to describe how each function works.

To illustrate how a Maude program is contructed, the following code corresponds to a program that defines the natural numbers and the addition operation, borrowed from [5]:

```
\begin{array}{l} \text{fmod NAT-ADD is} \\ \text{sort Nat} \end{array}. \\ \\ \text{op } 0 : \longrightarrow \text{Nat } [\text{ctor}] \ . \\ \\ \text{op } s : \text{Nat} \longrightarrow \text{Nat } [\text{ctor}] \ . \\ \\ \text{op } \_+\_: \text{Nat Nat} \longrightarrow \text{Nat} \ . \\ \\ \text{vars N M} : \text{Nat} \ . \\ \\ \text{*** Recursive Definition for addition} \\ \\ \text{eq N} + 0 = \text{N} \ . \\ \\ \text{eq N} + s (\text{M}) = s (\text{N} + \text{M}) \ . \\ \\ \text{endfm} \end{array}
```

The sort Nat is a data type that represents the natural numbers. This sort has two constructors (represented in the code with the key word ctor): 0 which is a constant and the operator s, which takes one argument of type Nat and represents the successor function in the natural numbers. With these two operators, it is possible to define arithmetic functions in the natural numbers, like addition or multiplication. In this module, both functions are defined inductively using equations. Using this module, it is possible to compute the

value for addition or multiplication for two natural numbers using the command red. For example, if the command red s(s(s(0))) + s(s(0)) is used, that represents the operation 3 + 2, the answer 5 is obtained represented as s(s(s(s(s(0))))):

```
***** equation
eq N + s(M) = s(N + M) .
N \longrightarrow s(s(s(0)))
M \longrightarrow s(0)
s(s(s(0))) + s(s(0))
s(s(s(s(0))) + s(0))
***** equation
eq N + s(M) = s(N + M) .
N \longrightarrow s(s(s(0)))
M \longrightarrow 0
s(s(s(0))) + s(0)
s(s(s(s(0))) + 0)
***** equation
eq N + 0 = N .
N \longrightarrow s(s(s(0)))
s(s(s(0))) + 0
s(s(s(0)))
result Nat: s(s(s(s(s(0)))))
```

Maude computes using equations from left to right. Therefore computation steps like the first one, the expression s(s(s(0))) + s(s(0)) is matched with the left side of the equation N + s(M) = s(N + M) and matching substitution  $\{N \mapsto s(s(s(0))), M \mapsto s(0)\}$ . The resulting expression s(s(s(0))) + s(s(0)), will be simplified again with the same equation, until it reduces to a simplified expression that can be matched with the equation N + 0 = N (as seen in the last step).

Semantically, functional modules in Maude are represented as equational theories [4, 5], that are represented as a pair  $(\Sigma, E)$  where:

- the signature  $\Sigma$  describes the syntax of the theory, which is the data types and operators symbols (sorts and operators).
- E is the set of equations between expressions written in the syntax of  $\Sigma$ .

As mentioned before, computations in Maude are done by using the equations over expressions constructed with operators. This method is called *term rewriting* [4, 5] and behaves in the following way:

• With the equations E of  $(\Sigma, E)$ , term rewriting rules are defined as  $\vec{E} = \{u \to v \mid (u = v) \in E\}$ .

- A term t, which are expressions formed using the syntax in  $\Sigma$ , is rewritten to t' in one step  $t \to_{\overrightarrow{E}} t'$  if and only if, the following conditions are suffice:
  - there is a subterm w in t, expressed as t[w].
  - there is a rule  $(u \to v) \in \overrightarrow{E}$  and a substituon  $\theta$  s.t. :  $w = u\theta$ ,  $w' = v\theta$ ,  $t' = t[w'] = t[v\theta]$ .

for example, in the previous computation red s(s(s(0))) + s(s(0)) the term rewriting process in the second step, is the following:

- E = N+s(M) = s(N + M)
- t = s(s(s(s(0))) + s(0))
- $\theta = \{ N \mapsto s (s (s (0))), M \mapsto 0 \}$
- $w = N + s(M) \theta = s(s(s(0))) + s(0)$
- $\bullet \ w' = \mathrm{s} \, (\mathrm{N+M}) \, \theta = \mathrm{s} \, (\mathrm{s} \, (\mathrm{s} \, (\mathrm{O}) \,)) \ + \ \mathrm{O})$
- t' = s([w']) = s(s(s(s(0))) + 0))

the resulting term rewriting is  $t \to_{\overrightarrow{E}} t'$ . Aside from building programs in Maude using functional modules, it is also possible to model concurrent systems. This is done with *system modules*, which permits the construction of system states and transitions. Semantically, a system module is a *rewrite theory* [5, 6]  $\mathcal{R} = (\Sigma, E, L, R)$  where:

- $(\Sigma, E)$  is an equational theory.
- L is a set of labels.
- R is a set of unconditional labeled rewrite rules of the form  $l: t \to t'$ , and conditional labeled rewrite rules fo the form  $l: t \to t'$  if cond, where  $l \in L$ , t, t' are terms in  $\Sigma$  and cond is a condition or system guard.

The syntax for system modules in Maude is:

```
\begin{array}{c} \operatorname{mod} \ \operatorname{MODULENAME} \ \operatorname{is} \\ \operatorname{BODY} \\ \operatorname{endm} \end{array}
```

Where the body represents a rewrite theory  $\mathscr{R}$ . The syntax for unconditional rewriting rules is

```
rl [l] : t \Rightarrow t'.
```

and for conditional rewriting rules is

$$\operatorname{crl}[l]: t \Longrightarrow t' \text{ if } \operatorname{cond}.$$

to exemplify this, lets consider the following simple model of a bus: A transport bus has capacity for 60 people. The bus can be moving or stationary and can

only drop or lift passengers when the bus is stationary. Finally, at any time the bus driver can use the brake to stop or use the gas pedal to move. The corresponding Maude system module for this model is:

In this model the states of the system are represented with instances of the sort Bus, and it contains a natural number that represents the number of people inside the bus and a Status, which represents the state of the bus (it can be stationary or moving). In this case, no equations are used, therefore the set of equations  $E = \emptyset$  and  $\Sigma$  will contain the sorts Bus and Status with their respective operators. To model the different events in the model, 4 rewriting rules were used:

- An unconditional rule labeled move, that represents the event of using the gas pedal to move the bus by changing the status from stationary to moving. Note that this rule can only be applied when the bus is stationary, as stated by the rule first term bus (N, stationary).
- An unconditional rule labeled stop, that represents the event of using the brakes to stop the bus. This changes the status of the bus from moving to stationary. As the previous rule, it can only be applied when the first term is matched, i.e. when the bus status is moving.
- An unconditional rule labeled drop, that represents the event of dropping people off the bus. The subterm s (N) assures that the it can only drop a person when the number of people in one or more. This rule rewrites the state of the system, by reducing the number of passengers in the bus by one.
- A conditional rule labeled lift, that represents the event of lifting a

passenger. When this rules is applied, the number of passengers inside the bus is increased by one. To prevent exceeding the maximum capacity of the bus, the condition if  $s(N) \le 60$  is used.

With this system module, that represents a rewrite theory  $\mathscr{R}$ , the simple bus model can be specified and verified using other functionalities in Maude like model checking with the commands rewrite and search. The rewrite command or rew takes an initial state of the system and uses the rewriting rules until termination, i.e. until no other rewriting rule can be applied to the system state. In the case of the bus example, the rules move and stop can be applied infinitely. Therefore, to be able to simulate this system Maude also allows to use bounded rewriting. With this method it is possible to specify the number of rewriting rules to be applied to the initial state of the system. For example, the command rew [3] bus(0, stationary) . will apply 3 rewriting rules to to the state bus(0, stationary), which refers to a stationary bus with no passengers. The resulting execution is:

\*\*\*\*\* rule

```
rl bus(N, stationary) \Rightarrow bus(N, moving) [label move].
bus (0, stationary)
 ——>
bus(0, moving)
***** rule
rl bus(N, moving) \Rightarrow bus(N, stationary) [label stop].
bus(0, moving)
bus (0, stationary)
***** rule
crl bus(N, stationary) => bus(s N, stationary) if s N <= 60 = true [label lift]
bus (0, stationary)
<del>----></del>
bus (1, stationary)
result Bus: bus(1, stationary)
Lastly, with the search command it is possible to verify if a given state is
reachable. For example, to check if the state bus (10, stationary) can
be reached from the initial state bus (0, moving), the command search
bus (0, stationary) =>* bus (10, moving) . can be used. The result
of this command is:
search in BUS: bus(0, stationary) =>* bus(10, moving).
Solution 1 (state 21)
states: 22
            rewrites: 50 in 0ms cpu (0ms real) (~ rewrites/second)
```

empty substitution

No more solutions.

No solution.

If the search returns a solution, it means that the state is reachable. Furthermore it is also possible to check if the system will exceed the maximum capacity defining an system invariant I that states this property. This can be done, by adding the following code to the bus module:

```
*** Define predicates  \begin{array}{l} var \ X : \ Bus \ . \\ op \ predicate : \ Bus \rightarrow Bool \ . \\ eq \ predicate (bus(N,S)) = if \ N <= 60 \ then \ true \ else \ false \ fi \ . \end{array}
```

This invariant can be checked with the search command using:

```
search bus(0,stationary) =>* X s.t. predicate(X) =/= true .
```

which searches for a state X where the bus has more than 60 passengers. The resulting execution of the command returns no solution:

```
search \ in \ BUS : \ bus(0\,, \ stationary) \implies X \ such \ that \ predicate(X) = /= \ true = \ true
```

This means that the bus system can not exceed the maximum capacity of the bus.

### 2.4 Object-Based Programming

Object-based programming in Maude [3, 6, 5] is supported by a predefined module CONFIGURATION. This module contains the necessary sorts and syntax to define the objects, messages, system configurations and objects interactions, of an object-based system. This module is defined as:

```
mod CONFIGURATION is
  *** basic object system sorts
  sorts Object Msg Configuration .
  *** construction of configurations
  subsort Object Msg < Configuration .
  op none : -> Configuration [ctor] .
  op __ : Configuration Configuration -> Configuration
[ctor config assoc comm id: none] .
```

The basic sorts are Object, Msg and Configuration. A term of sort Object represents an instance of a system object, a term of sort Msg represents a message shared by the system objects and a term of sort Configuration represents a snapshot of the current system state, represented as a multiset of objects

and messages. These configurations are built with the multiset union operation (defined with syntax  $_{--}$ ) between objects, messages or other configurations, and the empty configuration is defined as none. The module configuration also implements a predefined syntax for object construction. They have the form:

$$\langle O:C \mid a_1:v_1,...a_n:v_n \rangle$$

Where O is the objects identifier, C is its class,  $a_1...a_n$  are attribute identifiers and  $v_1...v_n$  are the values of each one of the attributes. This defined syntax in Maude is implemented as:

```
*** Maude object syntax
sorts Oid Cid .
sorts Attribute AttributeSet .
subsort Attribute < AttributeSet .
op none : -> AttributeSet [ctor] .
op _,_ : AttributeSet AttributeSet -> AttributeSet
[ctor assoc comm id: none] .
op <_:-|-> : Oid Cid AttributeSet -> Object [ctor object] .
endm
```

Where Oid corresponds to the object identifier O, Cid is the class identifier C and the attributes of the object are represented as a multiset. Messages' syntax is defined by the user. To understand how systems are modeled in Maude with configurations, the bank account example in [3] can be examined:

```
mod BANK-ACCOUNT is
    protecting INT .
    protecting CONFIGURATION .
    op Account : -> Cid [ctor].
    op bal : _ : Int -> Attribute [ctor gather (&)] .
    op from_to_transfer_ : Oid Oid Nat -> Msg [ctor] .
    vars AB: Oid.
    vars M N L : Nat .
    *** Definition of transfer rewriting rule
    crl [transfer]
      (from A to B transfer M)
      < A : Account | bal : N >
      < B : Account | bal : L >
      \Rightarrow < A : Account | bal : N - M >
         < B : Account | bal : L + M >
      if N >= M.
```

\*\*\* Definition of the initial configuration

The system consists of different bank accounts, that can transfer money to each other. The bank account class is named as Account, and it contains the attribute bal which corresponds to the amount of money available in an account. The message from\_to\_transfer\_simulates the transfer request from one account to another, by specifying the the two account object identifiers or Oid (one for the account that sends the money and the other one for the account that receives the money) and the amount of money to be sent as an integer. The rewrite rule transfer matches a system configuration where the message from A to B transfer M and the two accounts with Oid A and B are present. After that, the rule modifies the attribute bal of both accounts according to the transaction parameters and erases the message from the configuration. For example, if the initial configuration of the system is the one defined by bankConf, the result after using the rewriting command rew in BANK-ACCOUNT: bankConf. would be:

```
result Configuration: < A-001 : Account | bal : 550 > < A-002 : Account | bal : 950 >
```

#### 2.5 PMaude

Probabilistic Maude or PMaude [7], is a Maude extension that introduces probabilities to the language. The underlying theory behind PMaude are probabilistic rewrite theories which correspond to an extension of rewrite theories: probabilistic rewrite theories can be expressed as tuple  $\mathscr{R}_p = (\Sigma, E, L, R, \pi)$ , where  $(\Sigma, E, L, R, \gamma)$  is a rewrite theory and  $\pi$  is a function that assigns to each rewrite rule  $r \in R$  a probability, given the current model state or configuration. This probability will determine if a rule may or may not be executed in the following system transition. The general form of probabilistic rewrite rules, for unconditional and conditional respectively is:

```
l: t(\overrightarrow{x}) \to t'(\overrightarrow{x}, \overrightarrow{y}) \text{ if } C(\overrightarrow{x}) \text{ with probability } \overrightarrow{y} := \pi_r(\overrightarrow{y})
l': t(\overrightarrow{x}) \to t'(\overrightarrow{x}, \overrightarrow{y}) \text{ with probability } \overrightarrow{y} := \pi_r(\overrightarrow{y})
```

Where  $\overrightarrow{x}$  is the set of variables of the current model state,  $\overrightarrow{y}$  is the set of new variables accessible in the following model state and  $C(\overrightarrow{x})$  is the conjunction of conditions over the set  $\overrightarrow{x}$ . Moreover, l, l' are labels in L, t, t' are terms written with  $\Sigma$  and  $\pi_r$  corresponds to the probability function assigned to the specific rule  $r \in R$ . Lets consider the PMaude module, presented in [7]:

```
pmod EXPONENTIAL-CLOCK is
  *** the following imports positive real number module
  protecting POSREAL .
  *** the following imports PMaude module that defines
  *** the distributions EXPONENTIAL, BERNOULLI, GAMMA, etc.
  protecting PMAUDE .
  *** declare a sort Clock
  sort Clock .
  *** declare a constructor operator for Clock
  op clock : PosReal PosReal => Clock
  *** declares a constructor operator for a broken clock
  op broken : PosReal PosReal => Clock .
  *** T is used to represent time of clock,
  *** C represents charge in the clocks battery,
  *** t represents time increment of the clock
  vars T C t : PosReal . var B : Bool .
  rl [advance]: clock(T,C) \Rightarrow
                         if B then
                               \operatorname{clock}\left(\mathrm{T+t},\mathrm{C}-\frac{\mathrm{C}}{1000}\right)
                         else
                              broken (T,C -\frac{C}{1000})
                  with probability B:=BERNOULLI(\frac{C}{1000})
                                     t := EXPONENTIAL(1.0).
  rl [reset]: clock(T,C) \Rightarrow clock(0.0,C).
endpm
```

This model represents a clock that works with a battery. The idea is to model the behavior of the clock, when the battery starts depleting: when the charge of the battery is high, then the probability that the clock breaks is low. Conversely, when the clock's battery is low, the clock has a higher probability of breaking. In this probabilistic system module, the clock is represented as a term clock(T,C), where T is the time and C is the charge of the clock. The main probabilistic rewrite rule advance represents the "ticks" of the clock. If the boolean value B is true, then the clocks ticks normally and the new time will be the current time T plus an increment t. Also, the charge of the clock will be reduced by a thousandth of the currents clock's charge. If B is false, then the clock will break and change to the state broken  $(T,C-\frac{C}{1000})$ . The constructor broken of sort Clock, represents the broken state of the clock. To incorporate

the probabilistic choice of event for the clock's state (either ticking or breaking), the value B is chosen probabilistically, based on the charge of the clock. This is done by the BERNOULLI function, which receives a float number and returns a boolean value that is distributed according to the Bernoulli distribution with mean  $\frac{C}{1000}$ . Therefore, the lesser the charge left in the battery, the greater is the probability that the clock will break. The value t is also probabilistically determined, in this case by a exponential distribution function. There is also a second rewriting rule, that resets the clock to its initial state clock (0.0, C). It is important to remark that this model has both probabilistic and non-deterministic choice: The state of the clock depends on a probability function but the choice of rewriting rules is done non-dereministically by Maude's fair scheduler.

PMaude modules can be transformed into regular system modules in Maude. This is done with three key modules: COUNTER, RANDOM and SAMPLER. The built-in COUNTER module in Maude consists of the rewriting rule

```
rl counter \Rightarrow N:Nat.
```

that rewrites the constant counter to a natural number. The module is built to guarantee that every time the constant counter is replaced with a natural number N, this natural number corresponds to the successor of the natural number obtained in the previous use of the rule. The built-in RANDOM module provides a random number generator function, called random. Lastly, the SAMPLER module specifies the sampling functions for different probability functions. For example, for the previous clock example, the needed functions will be:

```
op EXPONENTIAL : PosReal \Rightarrow PosReal . op BERNOULLI : PosReal \Rightarrow Bool .
```

that are defined as:

```
rl EXPONENTIAL(R) \Rightarrow (- log(rand)) / R . rl BERNOULLI(R) \Rightarrow if rand < R then true else false fi .
```

The value rand in both of the rules is defined as:

```
rl [rnd] : rand \Rightarrow float(random(counter + 1) / 4294967296).
```

and it is rewritten in each step to a random number between 0 and 1. The number 4294967296 is used to divide the number returned by random, since it is the maximum number the function can return. The resulting Maude system module [7] is:

```
\mod \ EXPONENTIAL\!-\!CLOCK\!-\!TRANSFORMED \ is
```

```
*** The SAMPLER mode includes the COUNTER and RANDOM modules protecting SAMPLER . protecting POSREAL .
```

```
\begin{array}{l} \text{sort Clock} : \\ \text{op clock} : \text{Nat Float} \rightarrow \text{Clock [ctor]} : \\ \text{op broken} : \text{Nat Float} \rightarrow \text{Clock [ctor]} : \\ \\ \text{vars T C} : \text{PosReal} : \\ \\ \text{rl clock}(\text{T,C}) \Rightarrow \text{if BERNOULLI}(\frac{\text{C}}{1000}) \text{ then} \\ \\ \text{clock}(\text{T} + \text{EXPONENTIAL}(1.0)), \text{ C} - \frac{\text{C}}{1000}) \\ \\ \text{else} \\ \\ \text{broken}(\text{T,C} - \frac{\text{C}}{1000}) \\ \\ \text{fi} : \\ \\ \text{rl [reset]: clock}(\text{T,C}) \Rightarrow \text{clock}(0.0\text{,C}) : \\ \\ \text{endm} \end{array}
```

#### 2.6 PVeStA

PVeStA [8] is a statistical model checking tool for probabilistic-real time systems, that are specified either as discrete or continuous Markov chains, or probabilistic rewrite theories in Maude. It permits the verification of properties expressed in quantitative temporal logics like QuaTex [7] using Monte Carlo simulations. PVeStA is implemented in Java and consists of two executable programs: a client pvesta-client and a server pvesta-server. The pvesta-client program takes as input the Maude probabilistic model, a list of formulas written in QuaTex, multiple execution parameters for the model checking simulation and a server list. Then it sends to every one of the running pvesta-servers (PVeStA's model checking supports parallelism) a simulation request for the specified probabilistic Maue model and QuaTex formulas. After that, the servers return the results back to the pvesta-client program. This previously explained process can be viewed in the following figure: To demonstrate how PVeStA works, a variation of the clock model shown

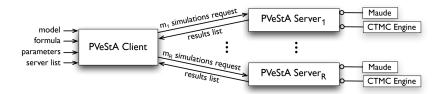


Figure 2.3: Components and interactions of PVeStA, taken from [8]

in the previous section will be used.

- 2.7 A Rewriting Logic Semantics and Statistical Analysis for Probabilistic Event-B
- 2.8 Rodin and Plugin Development

Methodology

Results

Discussion

### Conclusions

### **Bibliography**

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