Project 2

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Problem 1

Problem 3

a)

ii) 10-fold Cross-Validation

Model Accuracy

```
# Predict outcome using model from training data based on testing data
predictions <- predict(cvmodel, newdata=test)

# Create confusion matrix to assess model fit/performance on test data
con_matx <- confusionMatrix(data=predictions, test$COMMIT)
con_matx</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction no yes
##
         no 13
##
          yes 2 11
##
##
                  Accuracy: 0.8
##
                    95% CI: (0.6143, 0.9229)
       No Information Rate: 0.5
##
##
       P-Value [Acc > NIR] : 0.0007155
##
                     Kappa: 0.6
##
##
   Mcnemar's Test P-Value: 0.6830914
##
##
##
               Sensitivity: 0.8667
               Specificity: 0.7333
##
##
            Pos Pred Value: 0.7647
##
            Neg Pred Value: 0.8462
##
                Prevalence: 0.5000
##
            Detection Rate: 0.4333
##
     Detection Prevalence: 0.5667
         Balanced Accuracy: 0.8000
##
```

```
##
## 'Positive' Class : no
##
b)
c)
```

```
compute_weibull_stats <- function(shape, scale) {</pre>
  # Compute the mean
  mean_value <- scale * gamma(1 + (1/shape))</pre>
  # # Compute the median
  # median_value <- scale * qweibull(0.5, shape, scale)</pre>
  # Compute the median
  median_value <- scale * (log(2)^(1/shape))</pre>
  # Compute the mode
  if (shape > 1)
    mode_value <- scale * ((shape - 1) / shape)^(1/shape)</pre>
    mode_value <- 0
  # Compute the variance
  variance_value \leftarrow scale<sup>2</sup> * (gamma(1 + (2/shape)) - (gamma(1 + (1/shape)))<sup>2</sup>)
  # Return the computed statistics as a named list
  return(list(mean = mean_value,
               median = median_value,
               mode = mode_value,
               variance = variance_value))
}
# lambda = scale
# K = shape
# Example usage
scale_param <- 6</pre>
shape_param <- 1
stats <- compute_weibull_stats(shape_param, scale_param)</pre>
# Accessing the computed statistics
mean_value <- stats$mean</pre>
median_value <- stats$median</pre>
mode_value <- stats$mode</pre>
variance_value <- stats$variance</pre>
```

Printing the computed statistics
cat("Mean:", mean_value, "\n")

Mean: 6

cat("Median:", median_value, "\n")

Median: 4.158883

cat("Mode:", mode_value, "\n")

Mode: 0

cat("Variance:", variance_value, "\n")

Variance: 36

Maximum likelihood estimator (MLE) of the parameters from the Weibull distribution

Maximum Likelihood Estimator (MLE) of σ from the normal distribution assuming μ is constant.

Step 1: Probability Density Function for a normal distribution.

$$f(x; \lambda, k) = \begin{cases} \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} e^{-\left(\frac{x}{\lambda}\right)^{k}}, & x \ge 0\\ 0, & x < 0 \end{cases}$$

Step 2: The likelihood function (L).

$$L_{\hat{x}}(\lambda, k) = \prod_{i=1}^{n} \frac{k}{\lambda} \left(\frac{x_i}{\lambda}\right)^{k-1} e^{-\left(\frac{x_i}{\lambda}\right)^k}$$

$$= \left(\frac{k}{\lambda}\right)^n \left(\frac{1}{\lambda^{k-1}}\right)^n \left(\prod_{i=1}^n x_i^{k-1}\right) \left(e^{-\sum_{i=1}^n \left(\frac{x_i}{\lambda}\right)^k}\right)$$

$$= \frac{k^n}{\lambda^{nk}} e^{-\sum_{i=1}^n \left(\frac{x_i}{\lambda}\right)^k} \prod_{i=1}^n x_i^{k-1}$$

Step 3: The log-likelihood function (ln(L)).

$$\ln L_{\hat{x}}(\lambda, k) = n \ln(k) - nk \ln(\lambda) - \sum_{i=1}^{n} \left(\frac{x_i}{\lambda}\right)^k + (k-1) \sum_{i=1}^{n} \ln x_i$$

Step 4: Derivative of the log-likelihood function (ln(L)).

$$\frac{d \ln L_{\hat{x}}(\lambda, k)}{d\lambda} = -\frac{nk}{\lambda} + k \sum_{i=1}^{n} \frac{x_i^k}{\lambda^{k+1}}$$

MAYBE COMBINE STEP 4 AND 5!!!!!!!!!!!!

Step 5: Solving for the desired parameters.

Therefore the estimator $\hat{\lambda}$ is:

$$\hat{\lambda} = \left(\frac{1}{n} \sum_{i=1}^{n} x_i^k\right)^{\frac{1}{k}}$$

Plugging in $\hat{\lambda}$ into the log-likelihood function (ln(L)) and then differentiating with respect to k:

$$\frac{d\ln L_{\hat{x}}(\lambda, k)}{dk} = \frac{d}{dk} \left[n\ln(k) - nk\ln(\lambda) - \sum_{i=1}^{n} \left(\frac{x_i}{\lambda}\right)^k + (k-1)\sum_{i=1}^{n} \ln x_i \right]$$

$$= r$$

Therefore the estimator \hat{k} is: