

## CS 4920/5920 Applied Cryptography Spring 2018

### Assignment 3

This assignment is due at the beginning of class on February 28. Please explain how you reached your answers.

#### Problem 1.

This problem provides a numerical example of encryption using a one-round version of DES. We start with the same bit pattern for the key  $K$  and the plaintext, namely:

**Hexadecimal notation:**      0 1 2 3 4 5 6 7 8 9 A B C D E F

**Binary notation:**              0000 0001 0010 0011 0100 0101 0110 0111

                                 1000 1001 1010 1011 1100 1101 1110 1111

- Derive  $K_1$ , the first-round subkey.
- Derive  $L_0, R_0$ .
- Expand  $R_0$  to get  $E[R_0]$ , where  $E[\cdot]$  is the expansion function, e.g., as given from: [https://en.wikipedia.org/wiki/DES\\_supplementary\\_material](https://en.wikipedia.org/wiki/DES_supplementary_material)
- Calculate  $A = E[R_0] \oplus K_1$ .
- Group the 48-bit result of (d) into sets of 6 bits and evaluate the corresponding S-box substitutions.
- Concatenate the results of (e) to get a 32-bit result,  $B$ .
- Apply the permutation to get  $P(B)$ .
- Calculate  $R_1 = P(B) \oplus L_0$ .
- Write down the ciphertext.

#### Problem 2.

Using the extended Euclidean algorithm, find the multiplicative inverse of

- 1234 mod 4321
- 24140 mod 40902
- 550 mod 1769

Note: Please explain the reason if the multiplicative inverse does not exist. Alternatively, provide a table similar to *Table 2.4* in the textbook; feel free to write a computer program to fill in the entries for the table.

**Problem 3.**

- a. Develop a set of tables similar to *Table 5.1* in the textbook for GF(5).
- b. Develop a table similar to *Table 5.5* in the textbook for GF(2<sup>4</sup>) with  $m(x) = x^4 + x + 1$ .

**Problem 4.**

Show the following:

- a. Show that the matrix given here, with entries in GF(2<sup>4</sup>), is the inverse of the matrix used in the MixColumns step of S-AES.

$$\begin{pmatrix} x^3 + 1 & x \\ x & x^3 + 1 \end{pmatrix}$$

- b. Verify *Equation (6.13)* in Appendix 6A in the textbook. That is, show that  $x^i \bmod (x^4+1) = x^{i \bmod 4}$ .

**Problem 5.**

Given the plaintext {000102030405060708090A0B0C0D0E0F} and the key {01010101010101010101010101010101}:

- a. Show the original contents of **State**, displayed as a 4 × 4 matrix.
- b. Show the value of **State** after initial AddRoundKey.
- c. Show the value of **State** after SubBytes.
- d. Show the value of **State** after ShiftRows.
- e. Show the value of **State** after MixColumns.