PM-GroupProject

Dennis Goldenberg, Solomon Gao, Suleman Sadiq, Alana Berson

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```
library(readx1)
library(ggplot2)
suppressWarnings(library(zoo))
library(nlme)
suppressWarnings(library(forecast))
library(rpart)
suppressWarnings(library(rpart.plot))
suppressWarnings(library(tree))
suppressWarnings(library(randomForest))
suppressWarnings(library(olsrr))
```

1. Data Exploration and Preprocessing

Reading in USA fatality data:

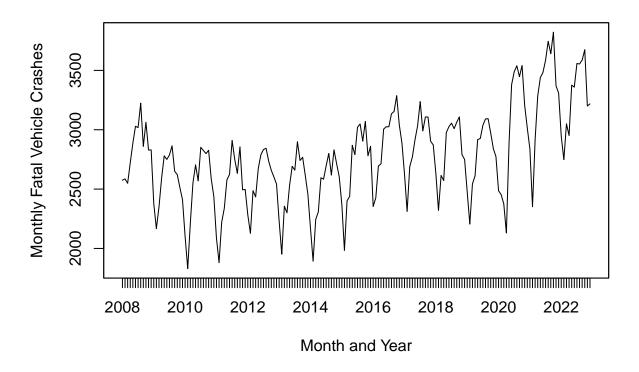
```
USAFat <- as.vector(t(as.matrix(read_excel("data/USA-FatalCrashes.xlsx",
    range = "B8:M22", col_names = FALSE,.name_repair = "unique_quiet"))))</pre>
```

Reading in USA population data (in hundreds of thousands):

```
USAPOP <- read_excel("data/USAPOP.xlsx")
colnames(USAPOP) <- c("Year", "Alabama","Alaska","Arizona","Arkansas",
    "California","Colorado","Connecticut","Delaware","D.C.","Florida","Georgia",
    "Hawaii","Idaho","Illinois","Indiana","Iowa","Kansas","Kentucky","Louisiana",
    "Maine","Maryland","Massachusetts","Michigan","Minnesota","Mississippi",
    "Missouri","Montana", "Nebraska","Nevada", "New Hampshire","New Jersey",
    "New Mexico","New York","North Carolina", "North Dakota","Ohio", "Oklahoma",
    "Oregon", "Pennsylvania", "Rhode Island","South Carolina", "South Dakota",
    "Tennessee","Texas", "Utah", "Vermont", "Virginia", "Washington",
    "West Virginia","Wisconsin", "Wyoming")
USAPOP$Year <- (2008:2023)*1000
USAPOP$Year <- as.integer(USAPOP$Year)</pre>
```

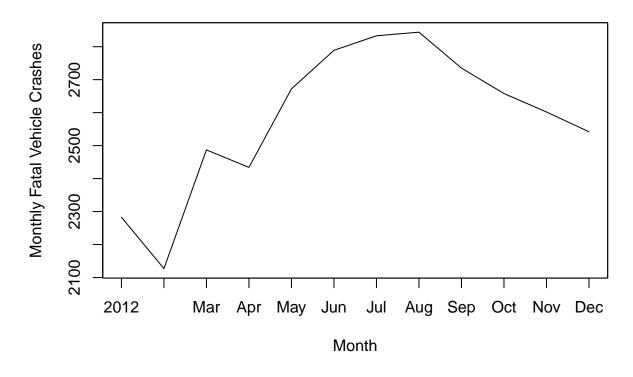
a. Seasonality of Data

USA Fatal Motor Vehicle Crashes by Month, 2008–2022



Examining a typical year:

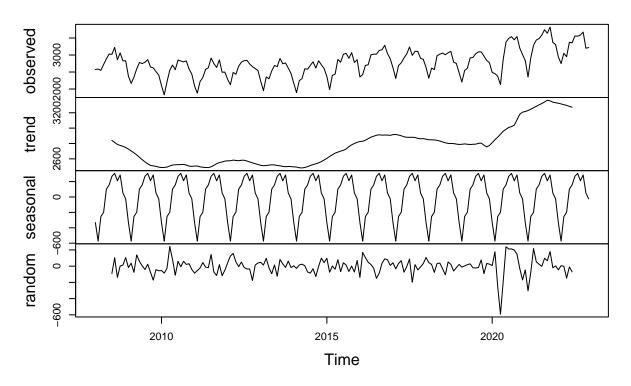
USA Fatal Motor Vehicle Crashes by Month, 2013



Looking at the Seasonality:

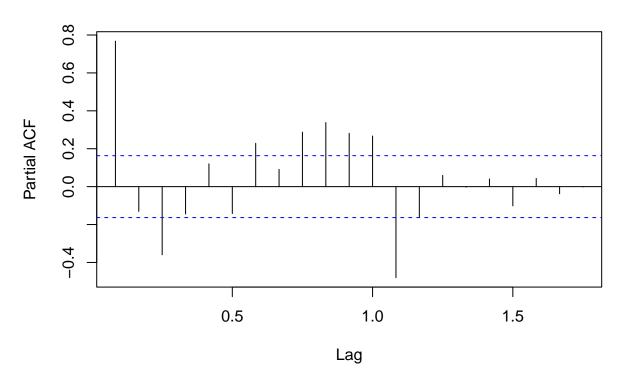
```
tsUSA <- ts(USAFat, start = 2008, freq = 12)
plot(decompose(tsUSA, type = "add"))</pre>
```

Decomposition of additive time series

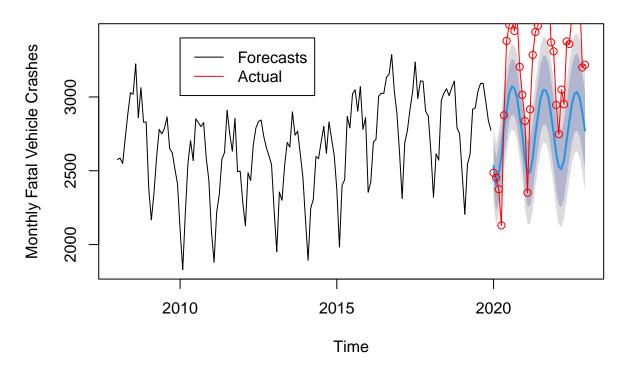


b. Autocorrelation and Autoregression

Partial Autocorrelation, 2008–2020 Data

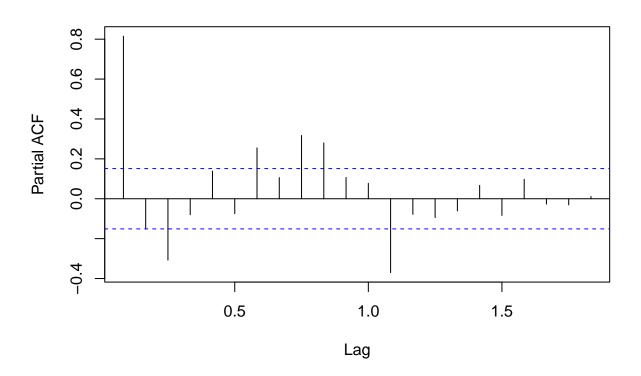


Forecasts From AR(12)

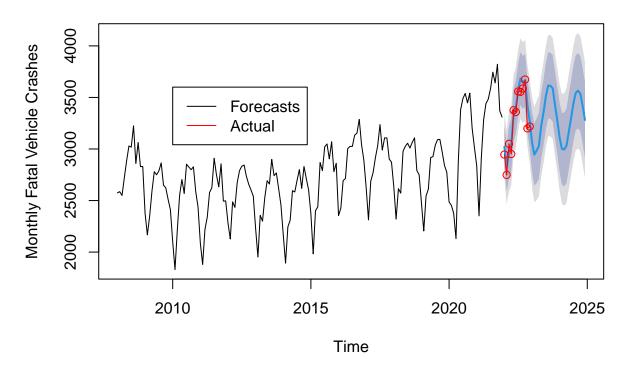


```
# Now use data of 2008-2021 as training set and 2022 data as testing set.
train_set2 <- ts(USAFat[1:(length(USAFat) - 12)], start = 2008, freq = 12)
test_set2 <- ts(USAFat[(length(USAFat) - 11):length(USAFat)], start = 2022, freq = 12)
pacf(train_set2, main = "Partial Autocorrelation, 2008-2021 Data")</pre>
```

Partial Autocorrelation, 2008–2021 Data



Forecasts From AR(12), Include 2021 in Train



c. Collecting fatality dates on states that legalized pre-2022

2. Modeling

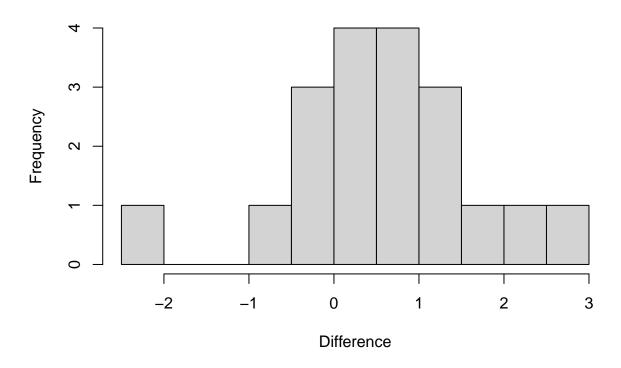
a. Difference of Means on Panel Data

I do a difference of means test to see if there is a change in the average number of fatal crashes per 100,000 in the year pre-legalization vs. the year when legalization went into effect. I linearly interpolate between population estimates to get the population estimate to divide by (i.e. if legalization went into effect at March 2015, I take 2/12 of the population of 2015 and add 10/12 of the population of 2014 for the pre-legalization population):

```
effDatefracs <- as.numeric(legEffDate) - as.integer(legEffDate)
yearsLeg <- as.integer(legEffDate)
avgs_pre <- c()
avgs_post <- c()
for(i in 1:length(legStates)){
   stateInfo <- as.vector(t(as.matrix(read_excel())))</pre>
```

```
paste("data/",legStates[i],".xlsx",sep = ""),range = "B9:M23",
    col names = FALSE,.name_repair = "unique_quiet"))))
  #linear interpolation
  pop_est_pre <- effDatefracs[i] * USAPOP[yearsLeg[i] - 2007,legStates[i]] +</pre>
    (1 - effDatefracs[i]) * USAPOP[yearsLeg[i] - 2008,legStates[i]]
  pop_est_post <- (1-effDatefracs[i])*USAPOP[yearsLeg[i] - 2007,legStates[i]]+</pre>
    effDatefracs[i] * USAPOP[yearsLeg[i] - 2006,legStates[i]]
  #find point in state info, calculate averages
  index_Leg <- (as.numeric(legEffDate[i]) - 2008)*12 + 1</pre>
  pre_per_HT <- mean(stateInfo[(index_Leg - 12):(index_Leg - 1)])/pop_est_pre</pre>
  post_per_HT <- mean(stateInfo[(index_Leg):(index_Leg + 12)])/pop_est_post</pre>
  avgs_pre <- append(avgs_pre,pre_per_HT)</pre>
  avgs_post <- append(avgs_post, post_per_HT)</pre>
hist(avgs_post - avgs_pre, breaks = 10,
     main = "Differences of Average Fatal Crash Number, Pre/Post Legalization",
     xlab = "Difference")
```

Differences of Average Fatal Crash Number, Pre/Post Legalization



I generate the data-frame with data, and run a paired sample t-test:

```
pairedData <- as.data.frame(cbind(legStates,avgs_pre,avgs_post))
colnames(pairedData) <- c("State", "avg_pre_Leg","avg_post_Leg")
pairedData$avg_pre_Leg <-round(as.numeric(pairedData$avg_pre_Leg),6)
pairedData$avg_post_Leg <- round(as.numeric(pairedData$avg_post_Leg),6)</pre>
```

```
testMeans <- t.test(pairedData$avg_post_Leg, pairedData$avg_pre_Leg,</pre>
       paired = TRUE, alternative = "greater")
```

The test statistic is $t = \frac{m}{\frac{s}{\sqrt{s}}}$, where m is the mean difference, s is the sample standard deviation of the

```
difference, and n is the number of observations (in this case, 19). I calculate:
sprintf("Sample Mean Difference: %.5f", testMeans$estimate)
## [1] "Sample Mean Difference: 0.60166"
sprintf("Test statstic: %.5f",testMeans$statistic["t"])
## [1] "Test statstic: 2.41257"
sprintf("Degrees of Freedom: %.0f", testMeans$parameter)
## [1] "Degrees of Freedom: 18"
sprintf("p-value: %.5f", testMeans$p.value)
## [1] "p-value: 0.01336"
print("95% Confidence Interval:")
## [1] "95% Confidence Interval:"
print(testMeans$conf.int[1:2])
## [1] 0.1692114
                         Inf
So, \mathbb{P}(T_{18} > 2.41257) = 0.01336 < 0.05; I reject H_0 at \alpha = 0.05.
```

b. Decision Tree and Random Forest to Predict Crashes

i. Collecting Data

Features to split on: (Note Rhode Island legalized on 05/22/2022 so it should probably be excluded)

- Marijuana Legal? (Pre-2022)
- Billions of Highway Miles-driven per 100,000 (2022)
- Proportion of Population in Urban Areas (2020)
- Speed Limits on Urban Interstates (as of 2024)
- % of Population Above 70 (2022)
- Damage in Millions of Dollars per 100,000 by Hazardous Weather (2022)
- % of Binge Drinking by State (2022)

```
#Create response variable:
avg2022 <- as.vector(t(as.matrix(read_excel("rfdata/2022StateData.xlsx",</pre>
    range = "B7:AZ8",col_names = TRUE,.name_repair = "unique_quiet"))))/12
pop2022 <- as.vector(t(as.matrix(USAPOP[2022 - 2007,2:dim(USAPOP)[2]])))</pre>
resp <- avg2022/pop2022
#Getting Percent Urban Population
urbRaw <- read_excel("rfdata/UrbanRural.xlsx", sheet = "Data", range = "B1:AZ4")
urb <- as.vector(t(urbRaw[2,]))/as.vector(t(urbRaw[1,]))</pre>
#Speed Limits on Urban Interstates
```

```
55, 75, 65, 70, 75, 70, 65, 70, 65, 70, 60, 65, 70, 65, 65, 55, 75, 65,
        70, 75, 65, 70, 55, 70, 55, 70, 80, 70, 75, 70, 55, 70, 60, 55, 70, 75)
#Marijuana Legalized?
legMar \leftarrow as.integer(c(0,1,1,0,1,1,0,1,0,0,0,0,1,0,0,0,0,1,0,
            1,1,0,0,0,1,0,1,0,1,1,1,0,0,0,0,1,0,0,0,0,0,0,0,1,1,1,0,0,0))
#% Population Over 70 by State, 2022
over 70 <- as.numeric(read excel("rfdata/USAAge700ver.xlsx")[1, ])
#Total Damage (in millions of $) from Hazardous Weather Events, 2022
hazard <- c(18.25, 30.97, 26.33, 44.48, 86.33, 1.1, 0.19, 0.26, 0, 17004.67,
            4.26, 1.33, 311.26, 25.70, 15.98, 24.97, 105.49, 8.22, 191.57,
            0.9, 7.84, 32.83, 75.24, 73.41, 183.68, 63.23, 4.27, 30.98,
            70.07, 443.28, 11, 0.17, 183.12, 10.59, 57.63, 20.17, 44.83,
            9.83, 8.08,1.12, 2.08, 499.83, 3.5, 1527.29, 36.76, 69.56,5.69,
            358.53, 11.48, 24.11, 25.17)
hazard <- hazard/pop2022
#Binge Drinking Prevalence among Adults
binge <- as.vector(t(as.matrix(read_excel("rfdata/BingeDrinking.xlsx",</pre>
                                sheet = "Data",range="C6:C57")))/100
#Billions of Highway-Miles Driven per 100,000 people
hMiles <- t(as.matrix(read excel("rfdata/hMiles.xlsx", range = "C1:C53")))
#remove Puerto Rico
hMiles <- hMiles[-c(40)]
#take billions of Miles per 100,000 people
hperHT <- (hMiles/1000)/pop2022
#Final Data Gathering
finData <- as.data.frame(cbind(resp,legMar,hperHT,urb,spL,over_70,hazard,binge))</pre>
corMat <- cor(finData)</pre>
finData$legMar <- factor(finData$legMar)</pre>
finData$spL <- factor(finData$spL)</pre>
finData$hperHT <- round(finData$hperHT, 6)</pre>
finData$urb <- round(finData$urb, 6)</pre>
finData$over_70 <- round(finData$over_70, 6)</pre>
finData$hazard <- round(finData$hazard, 6)</pre>
finData$states <- colnames(USAPOP)[2:52]</pre>
finData \leftarrow finData[,c(1,9,2:8)]
colnames(finData) <- c("resp", "State", "Legal", "HW_travel",</pre>
                         "Urban", "Speed_Lim", "over_70", "hazard", "binge")
finData <- finData[which(finData$State != "Rhode Island"),]</pre>
ii. 1 tree (for example)
set.seed(1)
train_index <- sample(1:nrow(finData),.8 * nrow(finData),replace = FALSE)</pre>
test_index <- setdiff(1:50, train_index)</pre>
```

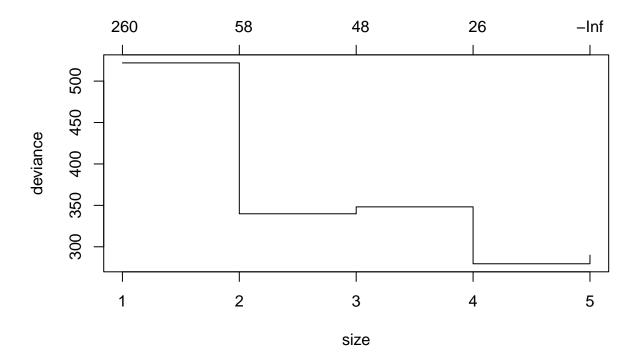
spL <- c(70, 55, 65, 65, 65, 55, 55, 55, 55, 65, 70, 60, 75, 55, 55,

rtree <- tree(resp ~ ., data = finData[train_index,-c(2)])</pre>

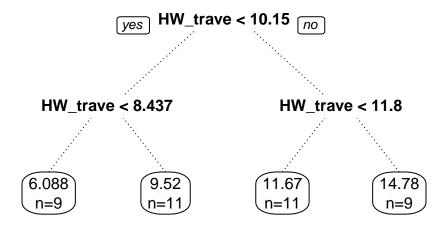
cv <- cv.tree(rtree, K = 5, FUN = prune.tree)</pre>

```
par(oma = c(0,0,2,0))
plot(cv)
title(main = "Deviance of Tree vs. Number of Leaves, corresponding alpha",
outer = TRUE)
```

Deviance of Tree vs. Number of Leaves, corresponding alpha



Regression Tree for Fatal Crashes per 100,000



```
oneTree <- tree(resp ~ ., data = finData[train_index, -c(2)], method = "anova")
oneTree <- prune.tree(oneTree, k = 30)
predOneTree <- predict(oneTree, newdata = finData[test_index,3:9])
mseOneTree <- mean((predOneTree - finData$resp[test_index])^2)
pseudoROneTree <- 1 - (mseOneTree * 50)/(var(finData$resp) * 49)</pre>
```

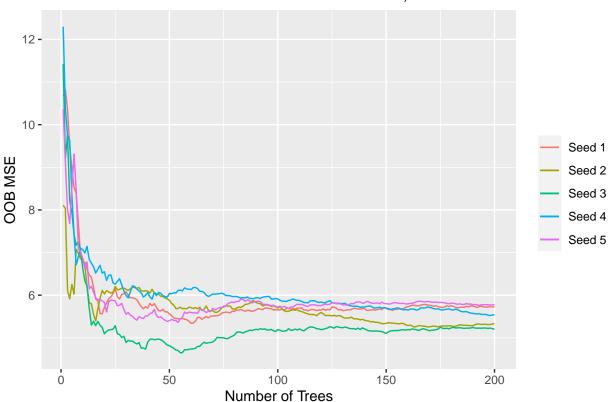
iii. Bagging

I generate 5 different iterations of the random Forest for bagging in order to try and optimize for the number of trees:

```
num_tree = 200
mseRBs <- c()
for(j in 1:5){
 set.seed(j)
 rB_raw <- randomForest(resp ~., data = finData[,-c(2)], ntree = num_tree,
      mtry = dim(finData)[2] - 2, importance = TRUE, keep.inbag = TRUE)
  mseRBs <- append(mseRBs, rB_raw$mse)</pre>
}
mseRBs <- as.data.frame(matrix(mseRBs, nrow = num_tree, ncol = j))</pre>
colnames(mseRBs) <- c(1:5)</pre>
plotMSE <- ggplot(data = mseRBs, aes(x = 1:200)) +</pre>
  geom_line(aes(y = `1`, color = "Seed 1")) +
  geom_line(aes(y = `2`, color = "Seed 2")) +
  geom_line(aes(y = `3`, color = "Seed 3")) +
  geom line(aes(y = `4`, color = "Seed 4")) +
  geom_line(aes(y = `5`, color = "Seed 5")) +
```

```
xlab("Number of Trees") + ylab("00B MSE") +
ggtitle("00B MSE as a function of the number of Trees, 5 Simulations") +
theme(legend.title = element_blank(), plot.title = element_text(hjust = 0.5))
plotMSE
```

OOB MSE as a function of the number of Trees, 5 Simulations



It seems as though around 50 is where the OOB MSE finishes decreasing. For the sake of bias-variance trade-off, I select 50 as the number of trees, and fit a random forest model:

```
set.seed(6)
RB <- randomForest(resp ~., data = finData[,-c(2)], ntree = 50,
      mtry = dim(finData)[2] - 2, importance = TRUE, keep.inbag = TRUE)
mseRB <- RB$mse[50]</pre>
pseudoRRB <- 1 - (mseRB * 50)/(var(finData$resp) * 49)</pre>
RB$importance
##
                  %IncMSE IncNodePurity
              0.04685631
## Legal
                               1.713326
## HW travel 11.59499367
                             426.179536
## Urban
             -0.19137532
                              24.914778
## Speed_Lim -0.21115978
                              27.582473
## over_70
             -0.33457491
                              31.267251
```

28.871072

34.615816

I generate summary statistics:

-0.01103727

0.34190161

hazard

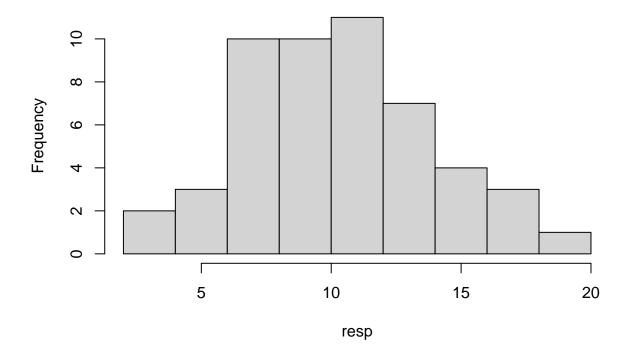
binge

c. Regression Analysis

i. Testing distribution of Response

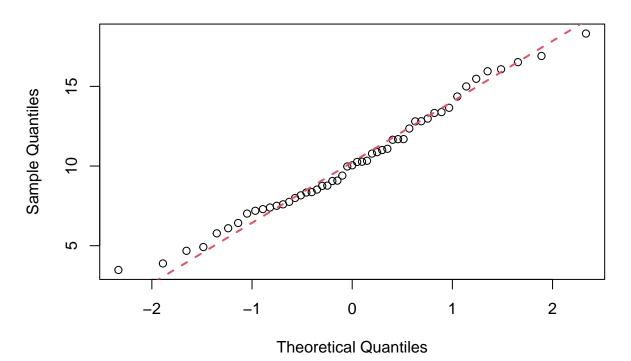
```
set.seed(1)
lambdaMLE <- mean(resp)
#hist(resp, breaks = 20)
#qqplot(resp, distribution = "poisson")
PoissonDist <- rpois(length(resp), lambdaMLE)
title <- sprintf("QQ Plot, Poisson Dist. with lambda = %.4f",lambdaMLE)
#qqplot(resp * 12, PoissonDist, main = title)
#abline(0,1,col = 'red')
hist(resp, breaks = 10)</pre>
```

Histogram of resp



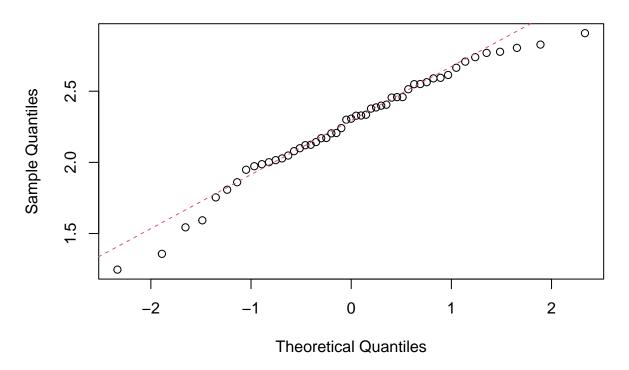
I examine the distribution of resp via qq-plots:

QQ Plot, Normal Dist. with mean = 10.2553 and SD = 3.5458



```
set.seed(1)
meanLogResp <- mean(log(resp))
sdLogResp <- sd(log(resp))
LogNormalDist <- rlnorm(length(resp), meanLogResp, sdLogResp)
title <- sprintf("QQ Plot, Log-Normal Dist. with mu = %.4f and sigma = %.4f", meanLogResp, sdLogResp)
qqnorm(log(resp), main = title)
qqline(log(resp), col = 2, lty = 2)</pre>
```

QQ Plot, Log-Normal Dist. with mu = 2.2634 and sigma = 0.3760



ii. Best Subset Selection

```
train_data <- finData[train_index,-c(2)]</pre>
test_data <- finData[test_index, -c(2)]</pre>
linmodel <- lm(resp ~., data = train_data)</pre>
best_sub <- ols_step_best_subset(linmodel)$metrics[,c("predictors", "rsquare",</pre>
                                                     "adjr", "cp", "aic", "sbic")]
best_sub
##
                                                 predictors
                                                              rsquare
## 1
                                                  HW travel 0.6475114 0.6382354
## 2
                                           HW_travel binge 0.6817754 0.6645740
## 3
                                 HW_travel Speed_Lim binge 0.6876043 0.6192678
## 4
                         HW_travel Speed_Lim over_70 binge 0.6906085 0.6107656
## 5
                 HW_travel Speed_Lim over_70 hazard binge 0.6912330 0.5986029
## 6
           Legal HW_travel Speed_Lim over_70 hazard binge 0.6919939 0.5857849
## 7 Legal HW_travel Urban Speed_Lim over_70 hazard binge 0.6919940 0.5709916
##
                    aic
            ср
## 1 -3.956205 179.2986 66.65335
## 2 -5.071050 177.2081 65.69632
## 3 4.399053 186.4687 67.88781
## 4 6.125951 188.0821 70.43232
## 5 8.069183 190.0013 73.22550
## 6 10.000012 191.9026 76.02018
## 7 12.000000 193.9026 78.87731
```

iii. Running best Model

```
linBestModel <- lm("resp ~ HW_travel + binge", data = train_data)</pre>
predlinBest <- predict(linBestModel, newdata = test data)</pre>
linBestMSE <- mean((test_data$resp - predlinBest)^2)</pre>
summary(linBestModel)
##
## Call:
## lm(formula = "resp ~ HW_travel + binge", data = train_data)
##
## Residuals:
##
                1Q Median
       Min
                                3Q
                                        Max
## -5.3293 -0.9234 -0.1180 1.5654 4.1128
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.7993
                         3.0577 0.588 0.5598
                                     7.821 2.35e-09 ***
## HW_travel
                1.2838
                            0.1641
## binge
               -25.2905
                           12.6708 -1.996 0.0533 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.086 on 37 degrees of freedom
## Multiple R-squared: 0.6818, Adjusted R-squared: 0.6646
## F-statistic: 39.64 on 2 and 37 DF, p-value: 6.318e-10
MSEFin <- c(mseOneTree, mseRB, linBestMSE)</pre>
prop_var_explained <- c(pseudoROneTree, pseudoRRB,</pre>
                        best_sub$rsquare[which.min(best_sub$aic)])
fin_stats <- as.data.frame(cbind(MSEFin, prop_var_explained))</pre>
fin_stats$Algorithm <- c(sumstats$Algorithm, "Multiple Linear Regression")
fin_stats <- fin_stats[,c(3,1,2)]</pre>
colnames(fin_stats) <- c("Algorithm", "MSE", "Proportion of Variance Explained")</pre>
fin_stats
##
                      Algorithm
                                     MSE Proportion of Variance Explained
## 1
                  Decision Tree 6.605976
                                                                 0.4375485
## 2
                  Bagged Forest 5.609170
                                                                 0.5224193
## 3 Multiple Linear Regression 3.652816
                                                                 0.6817754
```