

- a) **Approach & Pseudocode:** Let the length of the input string, `str`, be  $n$ . Let `maxwordlength` be the length of the longest word in the dictionary.
- I. First, I constructed a `ArrayList<String>` of the dictionary words.
  - II. Then I created a `DPtable[n][maxwordlength]`. The  $(i,j)$ th entry in this table will be a 1 if `str(i:i+j+1)` is a word in the dictionary.
  - III. Then I recursively called `getsentences(str,i)` on `str`. This function looks for words starting from the  $i$ th position in the `str` using the  $i$ th row in the DP table. Once it finds a word, it calls `getsentences(str-str(i+j+1))`. This function keeps track of the words in the sentence prior to  $i$ . It prints all the words once it reaches the end of the `str`.
- b) **Time Complexity:** The worst case time complexity is when the dictionary contains all possible words in the string i.e.  $2^n$  words. The complexity of lookup for `ArrayList` is  $O(2^n)$ . All the elements in the DP table are 1 and `maxwordsize=n`. In this case, time to fill the DP table is  $O(n \cdot n \cdot 2^n)$ . Each row in the table indicates that `getsentences` will be called  $O(n)$  times and this is same for all rows. Number of times we end up at start of any row is max of  $n \cdot n$ . So, the number of times `getsentences` is called is  $O(n \cdot n \cdot n)$  and lookup in each case is  $O(2^n)$ . So the total complexity is  $O(n^3 2^n)$ . **Its exponential in worst case.**
- c) **Correctness:** The algorithm looks for all possible combinations of words. It starts at the beginning and looks for words up to size `maxwordlength` and calls the recursive function on rest of the string. I only print sentences when the end of the `str` is reached. If the last remaining letters in the `str` don't make a word, then the algo doesn't print that sentence.
- d) **Loop Invariant:** The algorithm finds breaks in the input `str` such that the substring before the break and substring after the break make meaningful sentences. So, the loop invariant is `substring[0,break-1] + substring[break,end]` make a sentence.