

boost

Basic Equations

$$I_{ref}(\theta) = \frac{2P_o \sin(\theta)}{V_{pk}} \quad (1)$$

$$\delta_Q(\theta) = 1 - \frac{V_{pk} \sin(\theta)}{V_o} \quad (2)$$

$$\delta_D(\theta) = \frac{V_{pk} \sin(\theta)}{V_o} \quad (3)$$

$$(4)$$

Bilateral Triangle Δ^B

A = triangle peak-to-peak

DT = time of triangle peak

$$\Delta_{rms}^B(A, B, D, T) = \frac{\sqrt{\int_0^{DT} \left(-\frac{A}{2} + \frac{At}{DT}\right)^2 dt + \int_0^{T(1-D)} \left(-\frac{A}{2} + \frac{At}{T(1-D)}\right)^2 dt}}{\sqrt{T}} \quad (5)$$

$$\Delta_{rms}^B(A, B, D, T) = \frac{A}{2\sqrt{3}} \quad (6)$$

$$\Delta_{avg}^B(A, B, D, T) = \frac{\int_0^{DT} \left(-\frac{A}{2} + \frac{At}{DT}\right) dt + \int_0^{T(1-D)} \left(-\frac{A}{2} + \frac{At}{T(1-D)}\right) dt}{T} \quad (7)$$

$$\Delta_{avg}^B(A, B, D, T) = 0 \quad (8)$$

$$(9)$$

Elevated Right Triangle Δ^R

B = Tri Y Midpoint

A = triangle height

DT = time of triangle peak

$$\Delta_{rms}^R(A, B, D, T) = \frac{\sqrt{\int_0^{DT} \left(-\frac{A}{2} + \frac{At}{DT} + B\right)^2 dt}}{\sqrt{T}} \quad (10)$$

$$\Delta_{rms}^R(A, B, D, T) = \frac{\sqrt{D}\sqrt{A^2 + 12B^2}}{2\sqrt{3}} \quad (11)$$

$$\Delta_{avg}^R(A, B, D, T) = \frac{\int_0^{DT} \left(-\frac{A}{2} + \frac{At}{DT} + B\right) dt}{T} \quad (12)$$

$$\Delta_{avg}^R(A, B, D, T) = BD \quad (13)$$

$$(14)$$

Inductor rms simple

$$I_{ref,rms} = \frac{\sqrt{\int_0^{\pi} \frac{4P_o^2 \sin^2(\theta)}{V_{pk}^2} d\theta}}{\sqrt{\pi}} \quad (15)$$

$$I_{ref,rms} = \frac{\sqrt{2}P_o}{V_{pk}} \quad (16)$$

$$I_{L,rms} = I_{ref,rms} \quad (17)$$

$$(18)$$

Inductor rms with ripple

$$\Delta i_{L,pp}(\theta) = v_{In}(\theta) \frac{\delta_Q(\theta)}{Lf} \quad (19)$$

$$\Delta i_{L,pp}(\theta) = \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{Lf} \quad (20)$$

$$\Delta i_{L,rms,t}(\theta) = \Delta_{rms}^B(A = i_{LR,pp}) \quad (21)$$

$$\Delta i_{L,rms,t}(\theta) = \frac{V_{pk} |V_o - V_{pk} \sin(\theta)| |\sin(\theta)|}{2\sqrt{3}LV_o f} \quad (22)$$

$$\Delta I_{L,rms} = \frac{\sqrt{\int_0^\pi \frac{V_{pk}^2 (V_o - V_{pk} \sin(\theta))^2 \sin^2(\theta)}{12L^2 V_o^2 f^2} d\theta}}{\sqrt{\pi}} \quad (23)$$

$$\Delta I_{L,rms} = \frac{V_{pk} \sqrt{12\pi V_o^2 - 64V_o V_{pk} + 9\pi V_{pk}^2}}{12\sqrt{2}\sqrt{\pi}LV_o f} \quad (24)$$

$$I_{L,rms} = \sqrt{I_{ref,rms}^2 + \Delta I_{L,rms}^2} \quad (25)$$

$$I_{L,rms} = \frac{\sqrt{576\pi L^2 P_o^2 V_o^2 f^2 + 12\pi V_o^2 V_{pk}^4 - 64V_o V_{pk}^5 + 9\pi V_{pk}^6}}{12\sqrt{2}\sqrt{\pi}LV_o V_{pk} f} \quad (26)$$

$$(27)$$

Bridge rms simple

$$I_{B,rms} = I_{L,rms} \quad (28)$$

$$I_{B,rms} = \frac{\sqrt{2}P_o}{V_{pk}} \quad (29)$$

$$(30)$$

Bridge rms with ripple

$$I_{B,rms} = I_{L,rms} \quad (31)$$

$$I_{B,rms} = \frac{\sqrt{576\pi L^2 P_o^2 V_o^2 f^2 + 12\pi V_o^2 V_{pk}^4 - 64V_o V_{pk}^5 + 9\pi V_{pk}^6}}{12\sqrt{2}\sqrt{\pi}LV_o V_{pk} f} \quad (32)$$

$$(33)$$

Bridge avg

$$I_{B,avg} = \frac{\int_0^\pi \frac{2P_o \sin(\theta)}{V_{pk}} d\theta}{\pi} \quad (34)$$

$$I_{B,avg} = \frac{4P_o}{\pi V_{pk}} \quad (35)$$

$$(36)$$

Switch rms simple

$$i_{Q,rms,t}(\theta) = \Delta_{rms}^R(B = i_{ref}, A = 0, D = \delta_Q) \quad (37)$$

$$i_{Q,rms,t}(\theta) = \frac{2P_o \sqrt{V_o - V_{pk} \sin(\theta)} |\sin(\theta)|}{\sqrt{V_o} V_{pk}} \quad (38)$$

$$I_{Q,rms} = \frac{\sqrt{\int_0^\pi \frac{4P_o^2 (V_o - V_{pk} \sin(\theta)) \sin^2(\theta)}{V_o V_{pk}^2} d\theta}}{\sqrt{\pi}} \quad (39)$$

$$I_{Q,rms} = \frac{P_o \sqrt{6\pi V_o - 16V_{pk}}}{\sqrt{3} \sqrt{\pi} \sqrt{V_o} V_{pk}} \quad (40)$$

$$(41)$$

Switch rms with ripple

$$i_{Q,rms,t}(\theta) = \Delta_{rms}^R (B = i_{ref}, A = i_{LR,pp}, D = \delta_Q) \quad (42)$$

$$i_{Q,rms,t}(\theta) = \frac{\sqrt{(V_o - V_{pk} \sin(\theta)) (48L^2 P_o^2 V_o^2 f^2 + V_o^2 V_{pk}^4 - 2V_o V_{pk}^5 \sin(\theta) + V_{pk}^6 \sin^2(\theta))} |\sin(\theta)|}{2\sqrt{3}LV_o^{\frac{3}{2}}V_{pk}f} \quad (43)$$

$$I_{Q,rms} = \frac{\sqrt{\int_0^\pi \frac{(V_o - V_{pk} \sin(\theta)) (48L^2 P_o^2 V_o^2 f^2 + V_o^2 V_{pk}^4 - 2V_o V_{pk}^5 \sin(\theta) + V_{pk}^6 \sin^2(\theta)) \sin^2(\theta)}{12L^2 V_o^3 V_{pk}^2 f^2} d\theta}}{\sqrt{\pi}} \quad (44)$$

$$I_{Q,rms} = \frac{\sqrt{2880\pi L^2 P_o^2 V_o^3 f^2 - 7680L^2 P_o^2 V_o^2 V_{pk} f^2 + 60\pi V_o^3 V_{pk}^4 - 480V_o^2 V_{pk}^5 + 135\pi V_o V_{pk}^6 - 128V_{pk}^7}}{12\sqrt{10}\sqrt{\pi}LV_o^{\frac{3}{2}}V_{pk}f} \quad (45)$$

$$(46)$$

Switch avg

$$i_{Q,avg,t}(\theta) = \Delta_{avg}^R (B = i_{ref}, D = \delta_Q) \quad (47)$$

$$I_{Q,avg,t} = \frac{2P_o |V_o - V_{pk} \sin(\theta)| |\sin(\theta)|}{V_o V_{pk}} \quad (48)$$

$$I_{Q,avg} = \frac{\int_0^\pi \frac{2P_o \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{V_{pk}} d\theta}{\pi} \quad (49)$$

$$I_{Q,avg} = \frac{P_o |4V_o - \pi V_{pk}|}{\pi V_o V_{pk}} \quad (50)$$

$$(51)$$

Switch switching loss timings

$$t_{IR} = t_2 - t_1 = R_g C_{iss,test} \ln \left(\frac{V_{gs,max} - V_{th}}{V_{gs,max} - V_{gp}} \right) \quad (52)$$

$$t_{VF} = t_3 = \frac{R_g Q_{gd,test} V_{ds,max}}{V_{ds,test} (V_{gs,max} - V_{gp})} \quad (53)$$

$$t_{VR} = t_5 = \frac{R_g Q_{gd,test} V_{ds,max}}{V_{ds,test} V_{gp}} \quad (54)$$

$$t_{IF} = t_6 = R_g C_{iss,test} \ln \left(\frac{V_{gp}}{V_{th}} \right) \quad (55)$$

$$t_{ON} = t_{IR} + t_{VF} \quad (56)$$

$$t_{OFF} = t_{IF} + t_{VR} \quad (57)$$

$$(58)$$

Switch switching loss simple

$$P_{Q,sw,t}(\theta) = \frac{V_o f}{2} I_{ref}(\theta) (t_{ON} + t_{OFF}) \quad (59)$$

$$P_{Q,sw,t}(\theta) = \frac{P_o V_o f (T_{OFF} + T_{ON}) |\sin(\theta)|}{V_{pk}} \quad (60)$$

$$P_{Q,sw} = \frac{\int_0^\pi \frac{P_o V_o f (T_{OFF} + T_{ON}) |\sin(\theta)|}{V_{pk}} d\theta}{\pi} \quad (61)$$

$$P_{Q,sw} = \frac{2 P_o V_o f (T_{OFF} + T_{ON})}{\pi V_{pk}} \quad (62)$$

$$(63)$$

Switch switching loss with ripple

$$P_{Q,sw,t}(\theta) = \frac{V_o f}{2} \left((I_{ref}(\theta) - \Delta i_{L,pp}(\theta)) t_{ON} + (I_{ref}(\theta) + \Delta i_{L,pp}(\theta)) t_{OFF} \right) \quad (64)$$

$$P_{Q,sw,t}(\theta) = \frac{V_o f \left(T_{OFF} \left(\frac{2P_o \sin(\theta)}{V_{pk}} + \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o} \right) \sin(\theta)}{2Lf} \right) + T_{ON} \left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o} \right) \sin(\theta)}{2Lf} \right) \right)}{2} \quad (65)$$

$$P_{Q,sw} = \frac{\int_0^\pi \frac{V_o f \left(T_{OFF} \left(\frac{2P_o \sin(\theta)}{V_{pk}} + \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o} \right) \sin(\theta)}{2Lf} \right) + T_{ON} \left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o} \right) \sin(\theta)}{2Lf} \right) \right)}{2} d\theta}{\pi} \quad (66)$$

$$(67)$$

$$P_{Q,sw} = \frac{[16LP_o T_{OFF} V_o f + 16LP_o T_{ON} V_o f + 4T_{OFF} V_o V_{pk}^2 - \pi T_{OFF} V_{pk}^3 - 4T_{ON} V_o V_{pk}^2 + \pi T_{ON} V_{pk}^3]}{8\pi L V_{pk}} \quad (68)$$

$$(69)$$

Switch switching loss output capacitance

$$P_{Q,sw,c}(\theta) = \frac{C_{oss} V_o^2 f}{2} \quad (70)$$

$$P_{Q,sw,c} = \frac{\int_0^\pi \frac{C_{oss} V_o^2 f}{2} d\theta}{\pi} \quad (71)$$

$$P_{Q,sw,c} = \frac{C_{oss} V_o^2 f}{2} \quad (72)$$

$$(73)$$

Boost Diode simple

$$i_{D,rms,t}(\theta) = \Delta_{rms}^R(B = i_{ref}, A = 0, D = \delta_D) \quad (74)$$

$$i_{D,rms,t}(\theta) = \frac{2P_o \sqrt{\sin^3(\theta)}}{\sqrt{V_o} \sqrt{V_{pk}}} \quad (75)$$

$$I_{D,rms} = \frac{\sqrt{\int_0^\pi \frac{4P_o^2 \sin^3(\theta)}{V_o V_{pk}} d\theta}}{\sqrt{\pi}} \quad (76)$$

$$I_{D,rms} = \frac{4P_o}{\sqrt{3} \sqrt{\pi} \sqrt{V_o} \sqrt{V_{pk}}} \quad (77)$$

$$(78)$$

Boost Diode with ripple

$$i_{D,rms,t}(\theta) = \Delta_{rms}^R(B = i_{ref}, A = i_{LR,pp}, D = \delta_D) \quad (79)$$

$$i_{D,rms,t}(\theta) = \frac{\sqrt{(48L^2 P_o^2 V_o^2 f^2 + V_o^2 V_{pk}^4 - 2V_o V_{pk}^5 \sin(\theta) + V_{pk}^6 \sin^2(\theta)) \sin^3(\theta)}}{2\sqrt{3} L V_o^{\frac{3}{2}} \sqrt{V_{pk}} f} \quad (80)$$

$$I_{D,rms} = \frac{\sqrt{\int_0^\pi \frac{(48L^2 P_o^2 V_o^2 f^2 + V_o^2 V_{pk}^4 - 2V_o V_{pk}^5 \sin(\theta) + V_{pk}^6 \sin^2(\theta)) \sin^3(\theta)}{12L^2 V_o^3 V_{pk} f^2} d\theta}}{\sqrt{\pi}} \quad (81)$$

$$I_{D,rms} = \frac{\sqrt{3840L^2 P_o^2 V_o^2 f^2 + 80V_o^2 V_{pk}^4 - 45\pi V_o V_{pk}^5 + 64V_{pk}^6}}{12\sqrt{5} \sqrt{\pi} L V_o^{\frac{3}{2}} \sqrt{V_{pk}} f} \quad (82)$$

$$(83)$$

Boost Diode avg

$$i_{D,avg,t}(\theta) = \Delta_{avg}^R(B = i_{ref}, D = \delta_D) \quad (84)$$

$$I_{D,avg,t} = \frac{2P_o \sin^2(\theta)}{V_o} \quad (85)$$

$$I_{D,avg} = \frac{\int_0^\pi \frac{2P_o \sin^2(\theta)}{V_o} d\theta}{\pi} \quad (86)$$

$$I_{D,avg} = \frac{P_o}{V_o} \quad (87)$$

$$(88)$$

Boost Diode switching loss timings

$$K_Q = \frac{I_{rr,0} T_{rr,0}}{2\sqrt{I_{F,0}}} \quad (89)$$

$$S = \frac{T_{rr,0} \frac{dI_{D,0}}{dt}}{I_{rr,0}} - 1 \quad (90)$$

$$I_{rr} = \sqrt{\frac{2 \frac{dI_D}{dt} K_Q \sqrt{I_F}}{1 + S}} \quad (91)$$

$$T_a = \frac{I_{rr}}{\frac{dI_D}{dt}} \quad (92)$$

$$T_b = S T_a \quad (93)$$

$$E_Q = V_{DS} \left(\frac{I_{rr}}{2} T_a + \frac{I_{rr}}{4} T_b \right) \quad (94)$$

$$E_D = \frac{V_R I_{rr}}{4} T_b \quad (95)$$

$$(96)$$

Boost Diode switching loss reverse recovery simple

$$I_F = \frac{2P_o \sin(\theta)}{V_{pk}} \quad (97)$$

$$\frac{dI_D}{dt} = \frac{2P_o \sin(\theta)}{T_{IR} V_{pk}} \quad (98)$$

$$I_{rr} = \frac{2\sqrt[4]{2}\sqrt{K_Q}P_o^{\frac{3}{4}}\sqrt{\sin^{\frac{3}{2}}(\theta)}}{\sqrt{T_{IR}}V_{pk}^{\frac{3}{4}}\sqrt{S+1}} \quad (99)$$

$$T_a = \frac{\sqrt[4]{2}\sqrt{K_Q}\sqrt{T_{IR}}\sqrt[4]{V_{pk}}\sqrt{\sin^{\frac{3}{2}}(\theta)}}{\sqrt[4]{P_o}\sqrt{S+1}\sin(\theta)} \quad (100)$$

$$T_b = \frac{\sqrt[4]{2}\sqrt{K_Q}S\sqrt{T_{IR}}\sqrt[4]{V_{pk}}\sqrt{\sin^{\frac{3}{2}}(\theta)}}{\sqrt[4]{P_o}\sqrt{S+1}\sin(\theta)} \quad (101)$$

$$E_{Qrr} = \frac{\sqrt{2}K_Q\sqrt{P_o}V_o(S+2)\sqrt{\sin(\theta)}}{2\sqrt{V_{pk}}(S+1)} \quad (102)$$

$$E_{Drr} = \frac{\sqrt{2}K_Q\sqrt{P_o}SV_o\sqrt{\sin(\theta)}}{2\sqrt{V_{pk}}(S+1)} \quad (103)$$

$$P_{D,sw,rr}(\theta) = \frac{\sqrt{2}K_Q\sqrt{P_o}V_o f \sqrt{\sin(\theta)}}{\sqrt{V_{pk}}} \quad (104)$$

$$P_{D,sw,rr} = \frac{\int_0^\pi \frac{\sqrt{2}K_Q\sqrt{P_o}V_o f \sqrt{\sin(\theta)}}{\sqrt{V_{pk}}} d\theta}{\pi} \quad (105)$$

$$P_{D,sw,rr} = \frac{\sqrt{2}K_Q\sqrt{P_o}V_o f \int_0^\pi \left(1 - \frac{(\theta - \frac{\pi}{2})^2}{4}\right) d\theta}{\pi\sqrt{V_{pk}}} \quad (106)$$

$$P_{D,sw,rr} = \frac{K_Q\sqrt{P_o}V_o f (48 - \pi^2)}{24\sqrt{2}\sqrt{V_{pk}}} \quad (107)$$

$$(108)$$

Boost Diode switching loss reverse recovery with ripple

$$I_F = \frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf} \quad (109)$$

$$\frac{dI_D}{dt} = \frac{\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}}{T_{IR}} \quad (110)$$

$$I_{rr} = \frac{\sqrt{2}\sqrt{K_Q} \sqrt{\left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}\right)^{\frac{3}{2}}}}{\sqrt{T_{IR}}\sqrt{S+1}} \quad (111)$$

$$T_a = \frac{\sqrt{2}\sqrt{K_Q}\sqrt{T_{IR}} \sqrt{\left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}\right)^{\frac{3}{2}}}}{\sqrt{S+1} \left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}\right)} \quad (112)$$

$$T_b = \frac{\sqrt{2}\sqrt{K_Q}S\sqrt{T_{IR}} \sqrt{\left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}\right)^{\frac{3}{2}}}}{\sqrt{S+1} \left(\frac{2P_o \sin(\theta)}{V_{pk}} - \frac{V_{pk} \left(1 - \frac{V_{pk} \sin(\theta)}{V_o}\right) \sin(\theta)}{2Lf}\right)} \quad (113)$$

$$E_{Qrr} = \frac{\sqrt{2}K_Q\sqrt{V_o} \sqrt{(4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3 \sin(\theta)) \sin(\theta) (S+2)}}{4\sqrt{L}\sqrt{V_{pk}}\sqrt{f} (S+1)} \quad (114)$$

$$E_{Drr} = \frac{\sqrt{2}K_QS\sqrt{V_o} \sqrt{(4LP_oV_of - V_{pk}^2 (V_o - V_{pk} \sin(\theta))) \sin(\theta)}}{4\sqrt{L}\sqrt{V_{pk}}\sqrt{f} (S+1)} \quad (115)$$

$$(116)$$

$$P_{D,sw,rr}(\theta) = \frac{\sqrt{2}K_Q\sqrt{V_o}\sqrt{f}\sqrt{(4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3 \sin(\theta)) \sin(\theta)}}{2\sqrt{L}\sqrt{V_{pk}}} \quad (117)$$

$$P_{D,sw,rr} = \frac{\int_0^\pi \frac{\sqrt{2}K_Q\sqrt{V_o}\sqrt{f}\sqrt{(4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3 \sin(\theta)) \sin(\theta)}}{2\sqrt{L}\sqrt{V_{pk}}} d\theta}{\pi} \quad (118)$$

$$P_{D,sw,rr} = \frac{\sqrt{2}K_Q\sqrt{V_o}\sqrt{f} \int_0^\pi \left(-\frac{(\theta - \frac{\pi}{2})^2 (4LP_oV_of - V_oV_{pk}^2 + 2V_{pk}^3)}{4\sqrt{4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3}} + \sqrt{4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3} \right) d\theta}{2\pi\sqrt{L}\sqrt{V_{pk}}} \quad (119)$$

$$P_{D,sw,rr} = \frac{K_Q\sqrt{V_o}\sqrt{f} \left| -4\pi^2 LP_oV_of + 192LP_oV_of - 48V_oV_{pk}^2 + \pi^2 V_oV_{pk}^2 - 2\pi^2 V_{pk}^3 + 48V_{pk}^3 \right|}{48\sqrt{2}\sqrt{L}\sqrt{V_{pk}}\sqrt{4LP_oV_of - V_oV_{pk}^2 + V_{pk}^3}} \quad (120)$$

$$(121)$$

Boost Diode switching loss junction capacitance

$$P_{D,sw,c}(\theta) = \frac{C_j V_{D,bl}^2(\theta) f}{2} \quad (122)$$

$$P_{D,sw,c}(\theta) = \frac{C_j V_o^2 f}{2} \quad (123)$$

$$P_{D,sw,c} = \frac{\int_0^\pi \frac{C_j V_o^2 f}{2} d\theta}{\pi} \quad (124)$$

$$P_{D,sw,c} = \frac{C_j V_o^2 f}{2} \quad (125)$$

$$(126)$$

Cap rms simple

$$I_{C,rms} = \sqrt{I_{D,rms}^2 - \left(\frac{P_o}{V_o}\right)^2} \quad (127)$$

$$I_{C,rms} = \frac{P_o \sqrt{16V_o - 3\pi V_{pk}}}{\sqrt{3}\sqrt{\pi}V_o\sqrt{V_{pk}}} \quad (128)$$

$$(129)$$

Cap rms with ripple

$$I_{C,rms} = \sqrt{I_{D,rms}^2 - \left(\frac{P_o}{V_o}\right)^2} \quad (130)$$

$$I_{C,rms} = \frac{\sqrt{3840L^2P_o^2V_o^2f^2 - 720\pi L^2P_o^2V_oV_{pk}f^2 + 80V_o^2V_{pk}^4 - 45\pi V_oV_{pk}^5 + 64V_{pk}^6}}{12\sqrt{5}\sqrt{\pi}LV_o^{\frac{3}{2}}\sqrt{V_{pk}}f} \quad (131)$$

$$(132)$$