Question 1

All we need is a counter example to see that the Hausdorff property does not carry through to quotient spaces. Consider \mathbb{R}^n as our topological space.