3. Matching methods (I)

LPO 8852: Regression II

Sean P. Corcoran

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Lecture

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Treatment effects

Treatment effect for unit *i* using the potential outcomes framework:

$$\tau_i = Y_i(1) - Y_i(0)$$

where $Y_i(D_i)$ is the potential outcome for unit i. $D_i=1$ if i is treated and $D_i=0$ if not. Two *estimands* that may be of interest:

Population average treatment effect (ATE):

$$\tau_{ATE} = E(\tau) = E[Y(1) - Y(0)]$$

Average treatment effect on the treated (ATT):

$$au_{ATT} = E(\tau|D=1) = E[Y(1)|D=1] - \underbrace{E[Y(0)|D=1]}_{ ext{not observed}}$$

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Treatment effects

When we use the mean of Y for the *untreated* in place of E[Y(0)|D=1]:

$$E[Y(1)|D=1] - E[Y(0)|D=0] = \tau_{ATT} + \underbrace{E[Y(0)|D=1] - E[Y(0)|D=0]}_{\text{selection bias}}$$

Selection bias reflects the difference in the average Y in the untreated state (Y(0)) between the treatment and control group.

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Example 1: job training program

Person	Treat	Educ.	Age	Y(0)	Y(1)	Υ
1	1	1	26	10	14	14
2	1	1	21	8	12	12
3	1	1	30	12	16	16
4	1	1	19	8	12	12
5	1	0	25	6	10	10
6	1	0	22	4	8	8
7	0	0	21	4	8	4
8	0	0	26	6	10	6
9	0	0	28	8	12	8
10	0	0	20	4	8	4
11	0	1	26	10	14	10
12	0	1	21	8	12	8
13	0	0	16	2	6	2
14	0	0	15	1	5	1

Source: Jennifer Hill (2011) lecture notes. Assume Y is earnings and D_i indicates participation in job training program.

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Example 1: job training program

In the above example, ATE = ATT = 4. But:

$$E[Y(1)|D=1] - E[Y(0)|D=0] = \tau_{ATT} + \underbrace{E[Y(0)|D=1] - E[Y(0)|D=0]}_{\text{selection bias}}$$

$$12.0 - 5.4 = 4.0 + \underbrace{8.0 - 5.4}_{\text{selection bias}}$$

The treated group has a higher Y(0) than the untreated group. Notice the treated group also has a higher average education and age, two things associated with higher earnings. Their Y would likely have been higher even in the absence of treatment.

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Example 2: private vs. public colleges

			Private		-		Public		
		lvy	Leafy	Smart		All State	Tall State	Altered State	Earnings
A	1 2 3		Reject Reject Reject	Admit Admit Admit			Admit Admit Admit		110000 100000 110000
В	4 5	Admit Admit		71411111		Admit Admit	/ tunne	Admit Admit	60000 30000
С	6 7		Admit Admit						115000 75000
D	8 9	Reject Reject				Admit Admit	Admit Admit		90000 60000

Source: Angrist & Pischke MM (2015). Shaded cell represents the student's chosen college, from those they were admitted to. Based on Dale & Krueger (2002).

Example 2: private vs. public colleges

In the private vs. public colleges example:

$$E[Y(1)|D=1] - E[Y(0)|D=0] = 92,000 - 72,500 = 19,500$$

$$= \tau_{ATT} + \underbrace{E[Y(0)|D=1] - E[Y(0)|D=0]}_{\text{selection bias}}$$

It is likely the treated group has a higher Y(0) than the untreated group. This is suggested above by the higher mean earnings for students who applied and were admitted to private colleges (esp. groups A and C).

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Treatment effects

What if we could create equivalent groups by $\underline{\text{conditioning}}$ on some X? For example, what if:

$$\underbrace{E[Y(0)|D=1,X]}_{\text{unobserved}} = \underbrace{E[Y(0)|D=0,X]}_{\text{observed}!}$$

In other words, there is no difference in potential outcomes Y(0) between D=0 and D=1, once we condition on X. Then we could contrast the mean Y for each set of X and then average them.

In the private vs. public college example, assume there is no difference in Y(0) conditional on application/admitted group A-D:

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Example 2: private vs. public colleges

		lvy	Leafy	Smart	All State	Tall State	Altered State	Earnings
A	1 2 3		R R R	A A A		A A A		110000 100000 110000
В	4 5	A A			A A		A A	60000 30000
С	6 7		A A					115000 75000
D	8 9	R R			A A	A		90000 60000

Avg(Y|D=1, Group=A)=105,000

Avg(Y|D=0, Group=A)=110,000. Difference = 105,000 - 110,000 = -5,000

Avg(Y|D=1, Group=B)=60,000

Avg(Y|D=0, Group=B)=30,000. Difference = 60,000 - 30,000 = 30,000

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Example 2: private vs. public colleges

The simple average of the within-group differences (groups A and B) is:

$$(-5,000+30,000)/2 = $12,500$$

A weighted average gives more weight to the group with more individuals:

$$(-5,000)*(3/5)+(30,000)*(2/5)=$$
\$9,000

The weighted average uses the data more efficiently, and also generalizes appropriately to the groups included in the calculation. Note groups C and D are either all treated (private college) or all untreated (public college). There is no **common support** here.

Example 2: private vs. public colleges

Note in this case that neither the weighted nor unweighted average estimates the ATE or ATT. This is due to the lack of common support.

- Without a counterfactual for the treated in group C, we can't estimate τ_{ATT}
- Without a counterfactual for the untreated in group D, we can't estimate τ_{ATF} (or τ_{ATII})

An illustration of the importance of being attentive to the population to which you are able to generalize with the data you have.

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Example 2: private vs. public colleges

Angrist & Pischke MM (2015) explain how regression estimates are weighted averages of multiple matched comparisons. E.g., consider the regression:

$$Y_i = \alpha + \beta P_i + \gamma A_i + e_i$$

where $P_i=1$ if the student attended a private college and $A_i=1$ if the student was in group A (versus B). Students in groups C and D are excluded.

Using the Example 2 data, $\hat{\beta}=10,000$. This is comparable to the averages on the previous slide, but not identical to either. Regression effectively applies different weights, but the idea is the same. (See $\it MM$ for details).

We will return later to the differences between matching and regression.

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Subclassification

The above example is a case of **subclassification**: grouping treated and untreated observations into strata, calculating differences within strata, and then weighting those differences to get a treatment effect estimate.

Subclassification is an example of a **selection on observables** design. Other examples include matching, weighting (and multiple regression!)

For these methods to yield valid estimates of an ATE/ATT, selection bias must be due entirely to the covariates you are conditioning on. Once you account for these, potential outcomes are no longer related to treatment—a big assumption, but reasonable in some applications.

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Conditional independence assumption (CIA)

A setting in which potential outcomes are independent (\perp) of treatment status is called *unconfoundedness, ignorability, selection on observables, exogeneity,* or the **conditional independence assumption** (CIA).

$$Y(0), Y(1) \perp \!\!\!\perp D|X$$

Note this is an <u>assumption</u> that is not easily validated. Another requirement of these methods is **common support** or *overlap*:

$$0 < P(D = 1|X) < 1$$

This is something that can be examined in the data.

Example 3: Subclassification

Murnane & Willett (ch. 12) stratify the NELS sample by family income to estimate the effect of Catholic high school attendance on 12th grade math achievement:

Stratum					Cell Frequencies		Average Mathematics Achievement (12th grade)		
Label	Income	Sample	Sample	Mean	Public	Catholic	Public	Catholic	Diff.
Range	Range	Variance	Public	Catholic		(% of stratum total)			
Hi_Inc	\$35,000 to \$74,999	0.24	11.38	11.42	1,969	344 (14.87%)	53.60	55.72	2.12***.†
Med_ Inc	\$20,000 to \$34,999	0.22	9.65	9.73	1,745	177 (9.21%)	50.34	53.86	3.52***.†
Lo_Inc	≤\$19,999	3.06	6.33	6.77	1,365	71 (4.94%)	46.77	50.54	3.76***.†
							Weighte Average		3.01
							Weight Average		2.74

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Example 3: Subclassification

The weighted average ATE uses total cell sizes as weights; the ATT uses counts of treated cases in each cell as weights. These TEs are smaller than the unconditional mean differences in math scores ($\hat{\beta}_{CATH}=3.895$), suggesting upward bias.

Note income is a continuous variable. M&W created three strata with the aim of (1) creating balance in family income within each strata; (2) maintaining common support.

Example 3: Subclassification

Can also stratify on multiple covariates, as M&W do here with income and a measure of prior achievement (12 total cells):

Stratum		Cell Fre	equencies	Average Mathematics Achievement (12th Grade)			
Base-Year Family Income	Base-Year Mathematics Achievement	Public	Catholic	Public	Catholic	Diff.	
Hi_Inc	Hi_Ach	1,159	227	58.93	59.66	0.72	
	MHi_Ach	432	73	49.18	50.71	1.53**	
	MLo_Ach	321	38	42.75	44.23	1.48	
	Lo_Ach	57	6	39.79	40.40	0.62	
Med_Inc	Hi_Ach	790	93	57.42	59.42	2.00**-	
	MHi_Ach	469	49	47.95	50.14	2.19**	
	MLo_Ach	390	33	41.92	44.56	2.64**	
	Lo_Ach	96	2	37.94	39.77	1.83	
Lo_Inc	Hi_Ach	405	36	56.12	56.59	0.47	
	MHi_Ach	385	13	47.12	48.65	1.53	
	MLo_Ach	433	21	40.99	41.70	0.71	
	Lo_Ach	142	1	36.81	42.57	5.76	
				Weighted Av	erage ATE	1.50	
				Weighted Av	erage ATT	1.31	

p < 0.10; p < 0.05; p < 0.01; p < 0.001; p < 0.001 One-sided test.

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Curse of dimensionality

Finer strata may provide a stronger argument for the conditional independence assumption that treatment group membership is unrelated to potential outcomes (within strata), but they make it more and more difficult to achieve common support—the **curse of dimensionality**.

Matching methods

A closely related approach to subclassification is **matching**. Rather than group observations into strata and averaging over strata, we "impute" counterfactuals by matching each treated (untreated) case to a similar untreated (treated) case based on one or more covariates.

- Exact matching
- Approximate matching (e.g., nearest neighbor, coarsened exact matching, propensity score)

Need not match to only one "counterfactual"—can match to multiple cases. It is also possible to match *with replacement* to promote better matches.

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Exact matching

As the name suggests, **exact matching** entails pairing each treated (untreated) observation with one or more untreated (treated) observations with the same X. Estimate the ATT with:

$$\widehat{\tau_{ATT}} = \frac{1}{N_T} \sum_{D_i=1} (Y_i - Y_{j(i)})$$

where $Y_{j(i)}$ represents the Y for the matched case(s) for treated observation i. If multiple exact matches are used, $Y_{j(i)}$ stands in for the average of these.

Approximate matching

Approximate matching relaxes the demand for an exact match and identifies "nearest neighbors" based on one or more covariates. How do we measure distance to find nearest neighbors?

- Easy with one covariate: absolute distance between x's
- With multiple covariates: Euclidean distance $||X_i X_j|| = \sqrt{\sum_{m=1}^k (X_{mi} X_{mj})^2}$, though variables are on different scales
- Normalized Euclidean distance—scales each variable by its variance: $\sqrt{\sum_{m=1}^{k} \frac{(X_{mi} X_{mj})^2}{\sigma_x^2}}$
- Mahalanobis distance–accounts for covariance between x's

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Stata's teffects nnmatch

Stata's teffects implements a wide array of treatment effect estimators using matching, weighting, regression adjustment, etc. teffects nnmatch can use exact or approximate matching, or a combination of these.

teffects nnmatch $(y\ x)\ (t)$, options

Here y is the outcome, x are the covariates, and t is the treatment indicator. In the options can specify ate or atet, and $\operatorname{ematch}(\mathit{vars})$ to specify a list of variables on which you desire an exact match. For nearest neighbor matching you can specify the distance metric used, e.g., $\operatorname{metric}(\operatorname{euclidean})$. There are lots of other options.

See simple matching examples on Github using simulated data.

Stata's teffects nnmatch

Treatment-erre Estimator Outcome model	cts estimation: : nearest-ne		hing		obs = requested = min =	200
Distance metri		ls			max =	15
У	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
ATET treat						
(1 vs 0)	31.00002	.8976628	34.53	0.000	29.24063	32.7594

See the teffects documentation for standard error calculations, which are based on Abadie & Imbens (2006, 2011, 2012).

Abadie & Imbens (2008) do *not* recommend bootstrap estimation of standard errors when doing nearest neighbor matching.

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Stata's tebalance

By design, nearest neighbor matching seeks to balance the confounding covariate(s) in the treated and untreated groups. You can see how you did in this regard using tebalance summarize following teffects:

tebalance summar: te: refitting the		using	the ge	nerate() option	
Covariate balance	e summa:	У			Raw	Matched
		Numbe	r of ob	5 =	200	168
		Treat	ed obs	=	84	84
		Contr	ol obs	-	116	84
	Standar	dized	differ	ences	Vari	ance ratio
		Raw	Mat	ched	Raw	Matched
age educ		4947	.009	5797 0222	.8829962 1.038685	1.011965

Note: the raw standardized difference is like the difference in z-scores, but with an adjustment (see the teffects manual). The matched standardized difference takes into account any weights that are used.

Stata's tebalance

Try tebalance summarize, baseline following teffects to see baseline differences in covariates in original units.

. tebalance summarize, baseline note: refitting the model using the generate() option

Covariate balance summary

		Raw	Matched
Number of obs	=	750	556
Treated obs	=	278	278
Control obs	=	472	278

	Me	ans	Variances		
	Control	Treated	Control	Treated	
age	27.49364	30.3705	41.56259	38.57342	

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Bias corrections

Recall that in this genre of estimators—in which the CIA is assumed to hold—the only source of bias comes from imbalance in the covariates (i.e., imperfect matches).

When there is imperfect matching, the treatment effect estimator is a combination of the "true" effect and differences in Y that are a byproduct of the imbalance in covariates.

Abadie & Imbens (2011) propose a consistent bias-corrected estimator. The idea here is that one can use OLS to estimate the relationship between Y and covariates X. The difference in (predicted) Y due to the differences in X (between the perfect and actual match) is used to adjust the treatment effect estimate. In teffects: use biasadj(varnames) option with varnames the list of continuous covariates.

Propensity scores

Rosenbaum & Rubin (1983) showed that if Y(0), Y(1) are independent of D conditional on X, then they are also independent of D conditional on a **propensity score** constructed using X.

- Rather than stratifying or matching on all of the variables in X, it is sufficient to use the "one-number summary" of the relationship between treatment and X: P(X) = Pr(D = 1|X)
- P(X) can be estimated using a logit, probit, or LPM regression from which one can obtain predicted probabilities $\widehat{P(X)}$

Stata also refers to the propensity score as the estimated probability of treatment

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Propensity scores

The propensity score estimator for ATT can be written as:

$$E_{P(X)|D=1}\left(\underbrace{E[Y(1)|D=1,P(X)]}_{\text{treated}}-\underbrace{E[Y(0)|D=0,P(X)]}_{\text{untreated}}\right)$$

Effectively, for each propensity score we calculate the difference in mean outcomes for the treated and untreated with that P(X). We then take a weighted average of these over the different propensity score values. The subscript P(X)|D=1 means we are taking a weighted average over the area of common support.

Compare logic to Example 2 where we averaged the group differences in earnings across two groups with common support (A and C), weighting as appropriate.

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Propensity scores

In practice P(X) takes on a continuum of values and thus stratifying on P(X) itself—in the manner we did with subclassification—is not feasible.

Thus, we can do other things with the propensity score, including matching and re-weighting. Even when propensity scores are not used to estimate treatment effects, they can be useful diagnostic tools since they force you to think about the model of selection into treatment.

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Propensity scores

We will look at several uses for propensity scores:

- Matching
- Inverse probability weighting (IPW)

Note: King & Nelson (2019) critique of using propensity scores for matching. (See link to seminar video on Github). Preferred use these days is IPW.

Propensity scores in practice

Kev considerations:

- Choice of model for estimating propensity score (logit, probit)
- Selection of covariates for estimating treatment model
- Algorithm used for matching, if matching: how matches are made, how many, how close
- Checking for overlap and common support
- Assessing match quality (balanced distribution of covariates)
- Treatment effect calculation
- Estimating standard errors for treatment effects

Source: Caliendo & Kopeinig (2008), a good guide for practice. Also see the text by Guo & Fraser (2015), *Propensity Score Analysis*.

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Estimating the propensity score

Choice of model:

- For binary treatment, whether one uses a logit, probit, or LPM model is probably not that consequential.
- For multiple treatments, the choice may be more important (see Caliendo & Kopeinig, 2008)

Covariate selection:

- Goal: choose X's such that the unconfoundedness holds—should promote covariate balance.
- Should be correlated with treatment (D_i) and the outcome Y.
- Selection should be based on theory and contextual knowledge.
- X should be measured before treatment, and not affected by it (or by the anticipation of treatment).
- X's should not be "too good" at predicting treatment—we are relying on common support.

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Matching algorithms

There are many approaches to identifying matches for treated cases:

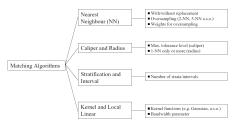


Figure 2. Different Matching Algorithms.

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Matching algorithms

Nearest neighbor (NN):

- Treated cases are paired with one or more nearest (untreated) neighbors based on their $\widehat{P(X)}$.
- Matches can be with or without replacement
 - With replacement: better matches, possibly less bias, but higher standard errors (re: repeated use of same observations)
 - Without replacement: worse matches, possibly more bias, but lower standard errors (re: using more variation)
 - If matching without replacement, order matters, so sort randomly (and preserve sort order if you wish to replicate)
- "Oversampling": choosing > 1 match for each treated case

Matching algorithms

Caliper and radius matching:

- A "caliper" is a tolerance level for how different $\widehat{P(X)}$ can be for matched observations
- "Radius" matching defines a caliper and then uses all untreated neighbors in the caliper

Stratification and interval matching:

 This method partitions the common support into intervals (strata) and then calculates mean differences within these strata

Kernel (KM) and local linear matching (LLM):

• Weighting algorithm that uses weighted average of nearly all untreated observations. Weights may depend on how different the $\widehat{P(X)}$ are.

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Checking for overlap and common support

Given $\widehat{P(X)}$, one can inspect the distributions for the treated and untreated observations to look for common support.

- Can compare the maxima and minima of $\widehat{P(X)}$ for the two groups
- Can formally compare the density distributions for each

The command teffects overlap (following teffects psmatch) produces densities of propensity scores.

Stata's teffects psmatch

teffects psmatch can estimate propensity scores and produce ATT and ATE via nearest neighbor matching using propensity scores.

teffects psmatch (y) (t x, tmodel), options

Again y is the outcome, x are the covariates, and t is the treatment indicator. tmodel is the type of propensity score model you would like to estimate (e.g., logit, probit). In the options can specify ate or atet, the number of nearest neighbors, the caliper, etc.

I also recommend the older user-written package psmatch2, which is useful for refining your propensity score model before requesting the ATE estimate. Alternatively, can "quietly" run teffects and then diagnose balance with tebalance. NOTE, however, that the treatment effect standard errors are incorrect in psmatch2.

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Stata's teffects psmatch

Can obtain predicted propensity scores after teffects psmatch using the predict command. Requires the gen() option in the teffects psmatch command which creates variables containing the index of the nearest neighbor:

predict (newvar), ps options

Can also predict *potential outcomes* (po), individual treatment effects given potential outcomes (te), and distance to nearest neighbor (distance).

In-class exercise

Using NSW data matched to CPS and PSID (Lalonde 1983 and others):

quietly teffects psmatch (re78) (treat age educ black hisp re74 re75, probit), atet gen(mvar)

or

psmatch2 treat age educ black hisp re74 re75

- Estimates propensity scores (default for psmatch2 is probit regression)
- Identifies nearest neighbor matches (default in psmatch2 is matching with replacement).

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Example

psmatch2 will show you the probit estimates. Alternatively, could just use probit (or logit) command.

. psmatch2 treat age educ black hisp re74 re75

treat	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
age	0171489	.0041262	-4.16	0.000	0252362	0090616
education	0301524	.015144	-1.99	0.046	0598342	0004707
black	1.589191	.0958607	16.58	0.000	1.401308	1.777075
hispanic	.6522818	.1525644	4.28	0.000	.353261	.9513026
re74	000023	.0000105	-2.19	0.029	0000436	-2.40e-06
re75	000082	.0000133	-6.14	0.000	0001081	0000558
_cons	-1.677663	.2261594	-7.42	0.000	-2.120927	-1.234399

Note: 346 failures and 0 successes completely determined.

Example

psmatch2 creates several variables in your dataset: _pscore, _treated, _support, _weight, _id, _n1, _nn, _pdif

_pscore: estimated P(X)

_treated: flags observations Stata recognized as treated

_support: flags observations on common support

• _weight: weight for matched controls (untreated obs only)

• _id: id number assigned for identifying matches

_n1: id of nearest neighbor (treated obs only)

_nn: number of matched neighbors

• _pdif: absolute value of diff between P(X) and P(X) of NN

As noted earlier, teffects psmatch can be augmented with options (and used with the predict command to get similar information)

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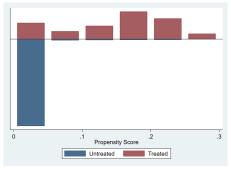
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Example

Inspect the histograms of propensity scores for the treated and untreated observations: psgraph



Assessing balance on covariates

In this step we check whether the X have similar distributions in the matched sample (treated and untreated observations). Why? If the groups are "exchangeable" we would expect similar distributions of X.

- For this test there must be one control for every treatment observation. If there are multiple control observations for a given treatment observation, they should be weighted so that the sum of the weights is equal to 1.
- If the covariates are not balanced, this suggests the propensity score needs to be re-estimated, perhaps with interaction terms, quadratic, or higher-order terms, or by including additional covariates.
- Stata: can use pstest following psmatch2, or teffects balance

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Example

pstest age educ black hisp re74 re75

. pstest age educ black hisp re74t re75t,both

	Unmatched	M	ean		%reduct	t-t	est	V(T)/
Variable	Matched	Treated	Control	%bias	bias	t	p> t	V(C)
age	U	25.816	33.444	-82.3		-9.43	0.000	0.42*
	н	25.816	24.989	8.9	89.2	0.95	0.342	0.58*
education	U	10.346	12.04	-67.9		-7.92	0.000	0.48*
	М	10.346	10.811	-18.6	72.6	-1.95	0.053	0.62*
black	U	.84324	.09739	224.5		33.96	0.000	
	н	.84324	.84865	-1.6	99.3	-0.14	0.886	
hispanic	ū	.05946	.06671	-3.0		-0.39	0.694	
	н	.05946	.03784	8.9	-198.1	0.97	0.335	
re74t	U	2.0956	14.746	-156.5		-16.63	0.000	0.22*
	Н	2.0956	1.7488	4.3	97.3	0.79	0.433	1.96*
re75t	σ	1.5321	14.38	-170.9		-17.24	0.000	0.10*
	М	1.5321	1.5778	-0.6	99.6	-0.14	0.891	1.03

^{*} if variance ratio outside [0.75; 1.34] for U and [0.75; 1.34] for M

Sample	Ps R2	LR chi2	p>chi2	MeanBias	MedBias	В	R	%Var
Unmatched Matched					119.4 6.6	266.1* 27.0*		

* if B>25%, R outside [0.5; 2]

pstest %bias

The column %bias provides the standardized percent bias: the difference in sample means between the treated and untreated observations as a percentage of the square root of the average of the sample variances in the treated and untreated groups.

$$\Delta_X = rac{ar{X}_1 - ar{X}_0}{\sqrt{(s_0^2 + s_1^2)/2}}$$

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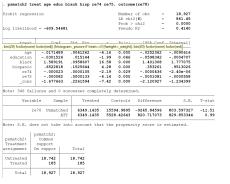
Estimating treatment effect

Once the propensity scores are estimated/finalized, they can be used to estimate the treatment effect. Methods for estimating ATT:

- NN matching: calculate the average difference in Y between treated and (matched) untreated observations. Use weights if multiple matched observations
- Inverse probability weighting: for untreated group construct a weight $w_j = P_j(X)/(1-(P_j(X)))$ and use to calculate a weighted average of Y over the untreated observations. Subtract from the average of Y for the treated observations.
- Interval matching: calculate the average difference in Y within each interval.
- Kernel matching: each treated observation has a "composite" match using the entire set of untreated observations. Each of the latter is weighted by a similarity measure.
- Other: using propensity score to construct a regression sample and/or weight observations in a regression.

Example

psmatch2 treat age educ black hisp re74 re75, outcome(re78)



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Inverse probability weighting (IPW)

Inverse probability weighting "upweights" treated cases with lower likelihood of treatment P(X).

Note: IPW estimators become unstable when there is low overlap (cases with very low probability of treatment). Re: these observations get extremely high weight when using inverse probability.

Stata's teffects ipw

teffects ipw can estimate ATT and ATE using inverse probability weighting. Propensity scores (probability of treatment) are used in the weights. The syntax is very similar to psmatch:

```
teffects ipw (y) (t x, tmodel), options
```

y is the outcome, x are the covariates, and t is the treatment indicator. tmodel is the type of propensity score model you would like to estimate (e.g., logit, probit). In the options can specify ate, atet, or the potential outcome means po.

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Matching vs. regression

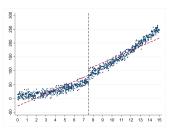
If potential outcomes are independent of treatment conditional on X, why not just estimate a regression controlling for X?

- Matching does not require assumptions about functional form for the outcome model (e.g., a linear relationship between Y and X).
- Regression runs the risk of extrapolating onto a space where there is little common support.
- Matching focuses our attention on balance and the degree of common support.

That said, propensity score matching "shifts the problem to the task of estimating the propensity score." If the model for the propensity score is mis-specified, the propensity score matching estimator will be biased.

Matching vs. regression

By making strong functional form assumptions, one can use regression to estimate treatment effects even when there is little overlap in X between the treated and untreated cases. But getting the functional form wrong can lead to poor inferences. We'll see this later with regression discontinuity:



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Matching vs. regression

See also Murnane & Willett ch. 12 on the differences between matching strategies and regression.