# Assignment 4

#### **Drew Murray**

2022-12-19

```
wine = read.csv("C:/Users/dgmur/Downloads/wineFl2022.csv")
str(wine)
```

```
## 'data.frame':
                   350 obs. of 13 variables:
   $ fixed acidity
                         : num 5.9 7 6.9 9.9 6.7 7.6 8 6.5 6.8 12.2 ...
##
                         : num 0.32 0.23 0.24 0.49 0.16 0.78 0.18 0.22 0.28 0.45 ...
  $ volatile acidity
  $ citric acid
                         : num 0.2 0.42 0.49 0.23 0.28 0 0.37 0.27 0.37 0.49 ...
   $ residual sugar
                         : num 14.4 1.1 1.3 2.4 2.5 1.7 0.9 1.6 7 1.4 ...
##
##
  $ chlorides
                         : num 0.05 0.062 0.032 0.087 0.046 0.076 0.049 0.039 0.057 0.075 ...
   $ free sulfur dioxide : num 29 35 35 19 40 33 36 36 35 3 ...
##
   $ total sulfur dioxide: num 144 100 148 115 153 45 109 116 208 6 ...
##
   $ density
                         : num 0.997 0.993 0.993 0.995 0.992 ...
##
   $ pH
                         : num 3.24 3.04 3.45 2.77 3.38 3.31 2.89 3.38 3.57 3.13 ...
   $ sulphates
                               0.41 0.4 0.57 0.44 0.51 0.62 0.44 0.57 0.55 0.63 ...
##
   $ alcohol
                         : num 10.3 9.2 10.7 9.4 11.4 10.7 12.7 11 10.2 10.4 ...
   $ quality
                         : int 6576766755 ...
##
##
   $ type
                         : int 0000011001...
```

```
wine$type=as.factor(wine$type)
wine$quality=as.numeric(wine$quality)
winec = wine[1:11]
View(winec)
#1
#a
cor(winec)
```

```
##
                        fixed acidity volatile acidity citric acid residual sugar
## fixed acidity
                           1.00000000
                                           0.225020854 0.38344924
                                                                      -0.09864763
## volatile acidity
                           0.22502085
                                           1.000000000 -0.32286866
                                                                      -0.17139713
## citric acid
                           0.38344924
                                          -0.322868655
                                                       1.00000000
                                                                       0.16225541
## residual sugar
                                                                       1.00000000
                          -0.09864763
                                          -0.171397128 0.16225541
## chlorides
                           0.32756202
                                           0.341374902 0.08681857
                                                                      -0.12546264
## free_sulfur_dioxide
                          -0.28237859
                                          -0.287109795
                                                        0.04245716
                                                                       0.43035646
## total sulfur dioxide
                          -0.36919701
                                          -0.358818093 0.10598165
                                                                       0.47333598
## density
                           0.53262405
                                                                       0.54020970
                                           0.244588159 0.19580930
## pH
                          -0.23369013
                                           0.228314657 -0.27738639
                                                                      -0.22678197
## sulphates
                           0.30713463
                                           0.186344437 0.10589346
                                                                      -0.19561141
                                           0.004018921 -0.09567631
## alcohol
                          -0.20003736
                                                                      -0.34337904
##
                          chlorides free sulfur dioxide total sulfur dioxide
## fixed acidity
                         0.32756202
                                           -0.282378587
                                                                   -0.3691970
## volatile acidity
                                           -0.287109795
                                                                  -0.3588181
                         0.34137490
## citric acid
                         0.08681857
                                            0.042457162
                                                                   0.1059817
## residual sugar
                        -0.12546264
                                            0.430356464
                                                                   0.4733360
## chlorides
                         1.00000000
                                           -0.248831028
                                                                   -0.3270541
                        -0.24883103
## free sulfur dioxide
                                            1.000000000
                                                                   0.7626948
## total_sulfur_dioxide -0.32705409
                                            0.762694847
                                                                   1.0000000
## density
                         0.37847916
                                            0.005382083
                                                                   -0.0229437
## pH
                         0.01866647
                                           -0.128416387
                                                                  -0.1705793
## sulphates
                         0.39260836
                                           -0.147085345
                                                                  -0.2853768
## alcohol
                        -0.27335277
                                           -0.101607695
                                                                   -0.1933318
##
                             density
                                               рН
                                                     sulphates
                                                                    alcohol
## fixed acidity
                         0.532624054 -0.233690126
                                                   0.307134630 -0.200037357
## volatile acidity
                         0.244588159
                                      0.228314657
                                                   0.186344437
                                                                0.004018921
## citric acid
                         0.195809304 -0.277386386
                                                   0.105893456 -0.095676312
## residual sugar
                         0.540209698 -0.226781965 -0.195611413 -0.343379037
## chlorides
                         0.378479157
                                      ## free sulfur dioxide
                         0.005382083 -0.128416387 -0.147085345 -0.101607695
## total sulfur dioxide -0.022943702 -0.170579290 -0.285376799 -0.193331790
## density
                         1.000000000 -0.005440951 0.228176692 -0.717527825
## pH
                        -0.005440951
                                     1.000000000 0.169653803
                                                                0.129038264
## sulphates
                         0.228176692
                                     0.169653803
                                                   1.000000000
                                                                0.008272161
## alcohol
                        -0.717527825
                                      0.129038264
                                                   0.008272161
                                                                1.000000000
```

cov(winec)

```
##
                        fixed_acidity volatile_acidity
                                                         citric acid
## fixed acidity
                          1.890202538
                                          0.0509847073 7.466255e-02
## volatile acidity
                          0.050984707
                                          0.0271597634 -7.535804e-03
## citric acid
                          0.074662546
                                         -0.0075358043 2.005772e-02
## residual sugar
                         -0.642850594
                                         -0.1338861850 1.089204e-01
## chlorides
                          0.014041393
                                          0.0017541110 3.833680e-04
## free_sulfur_dioxide
                         -7.137701187
                                         -0.8699282440 1.105514e-01
## total sulfur dioxide -29.064296357
                                         -3.3859831355 8.594466e-01
## density
                                          0.0001219106 8.387203e-05
                          0.002214716
## pH
                         -0.047560426
                                          0.0055699075 -5.815366e-03
## sulphates
                          0.061132820
                                          0.0044460147 2.171208e-03
## alcohol
                         -0.326777023
                                          0.0007869709 -1.610020e-02
##
                                           chlorides free sulfur dioxide
                        residual sugar
## fixed acidity
                          -0.642850594
                                        1.404139e-02
                                                           -7.137701e+00
## volatile acidity
                                        1.754111e-03
                                                            -8.699282e-01
                          -0.133886185
## citric acid
                                                            1.105514e-01
                           0.108920385 3.833680e-04
## residual sugar
                          22.466657798 -1.854156e-02
                                                            3.750334e+01
## chlorides
                          -0.018541555 9.721314e-04
                                                            -1.426394e-01
## free sulfur dioxide
                                                            3.380219e+02
                          37.503344249 -1.426394e-01
## total sulfur dioxide 128.465413426 -5.838880e-01
                                                            8.029171e+02
## density
                           0.007744167 3.569008e-05
                                                            2.992719e-04
## pH
                          -0.159121531 8.615407e-05
                                                           -3.494975e-01
## sulphates
                          -0.134231641 1.772203e-03
                                                           -3.915014e-01
## alcohol
                          -1.933878769 -1.012680e-02
                                                            -2.219654e+00
##
                        total_sulfur_dioxide
                                                   density
                                                                       рН
## fixed acidity
                               -2.906430e+01 2.214716e-03 -4.756043e-02
## volatile acidity
                               -3.385983e+00 1.219106e-04 5.569907e-03
## citric acid
                                8.594466e-01 8.387203e-05 -5.815366e-03
                                1.284654e+02 7.744167e-03 -1.591215e-01
## residual sugar
## chlorides
                               -5.838880e-01 3.569008e-05 8.615407e-05
## free_sulfur_dioxide
                                8.029171e+02 2.992719e-04 -3.494975e-01
## total sulfur dioxide
                                3.278649e+03 -3.973325e-03 -1.445856e+00
## density
                               -3.973325e-03 9.147159e-06 -2.435954e-06
## pH
                               -1.445856e+00 -2.435954e-06 2.191303e-02
## sulphates
                               -2.365689e+00 9.990929e-05 3.635853e-03
## alcohol
                               -1.315337e+01 -2.578506e-03 2.269635e-02
##
                            sulphates
                                            alcohol
## fixed acidity
                         6.113282e-02 -3.267770e-01
## volatile acidity
                         4.446015e-03 7.869709e-04
## citric acid
                         2.171208e-03 -1.610020e-02
## residual sugar
                        -1.342316e-01 -1.933879e+00
## chlorides
                         1.772203e-03 -1.012680e-02
## free sulfur dioxide -3.915014e-01 -2.219654e+00
## total sulfur dioxide -2.365689e+00 -1.315337e+01
## density
                         9.990929e-05 -2.578506e-03
## pH
                         3.635853e-03 2.269635e-02
## sulphates
                         2.095960e-02 1.422973e-03
## alcohol
                         1.422973e-03 1.411798e+00
```

```
#b
#I chose correlation because the variables are on a different scale
winec.pca = prcomp(winec, scale. = T)
winec.pca
```

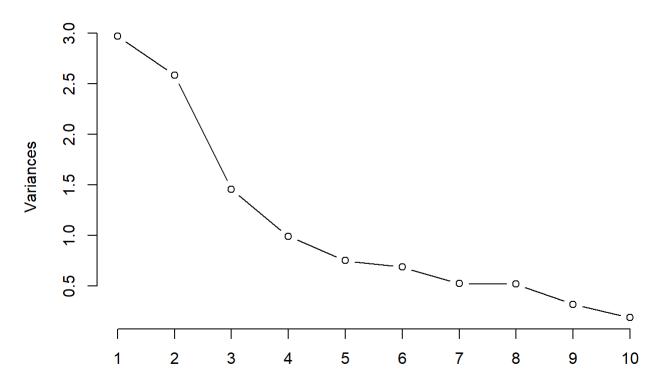
```
## Standard deviations (1, .., p=11):
   [1] 1.7232494 1.6076239 1.2068558 0.9946672 0.8652731 0.8279042 0.7221999
   [8] 0.7184746 0.5619289 0.4299401 0.1660712
##
##
## Rotation (n \times k) = (11 \times 11):
                              PC1
                                         PC2
                                                    PC3
                                                               PC4
##
## fixed acidity
                       0.348489546 -0.29235631 0.32295067 -0.09387512
## volatile acidity
                       ## citric_acid
                      -0.009760994 -0.28502639 0.57385827 0.24915131
## residual sugar
                      -0.267480445 -0.40830325 -0.18326601 -0.09808649
## chlorides
                       0.369862176 -0.19645234 -0.08349223 0.17270436
## free sulfur dioxide -0.418729255 -0.17289180 -0.14492089 0.36002435
## total sulfur dioxide -0.472907822 -0.18332739 -0.11478151 0.21541693
## density
                       0.185040901 -0.53684289 -0.23345742 -0.05441968
## pH
                       ## sulphates
                       0.318732272 -0.07236050 0.02559981 0.70297463
## alcohol
                      -0.028613894   0.47069391   0.23940149   0.16991977
##
                             PC5
                                        PC6
                                                   PC7
                                                               PC8
## fixed acidity
                       0.04334508 -0.35893889 0.08376151 -0.42807410
## volatile_acidity
                       0.39351946 -0.44374763 0.34170306
                                                        0.03221217
## citric acid
                      -0.26312144 -0.08990380 0.48010365 0.20787468
## residual sugar
                      -0.12195280 -0.30847793 -0.25710155
                                                        0.59045465
## chlorides
                       0.35390879 0.51829635 0.30728852 0.42378092
## free_sulfur_dioxide
                       0.35796425 -0.13909626 0.15758820 -0.22149241
## total sulfur dioxide 0.19238345 0.01155103 0.23717318 -0.17675022
## density
                      -0.20539242 -0.15702906 -0.08509948 -0.01480819
## pH
                      -0.61576992 -0.08600367 0.32724636 -0.05467107
## sulphates
                       0.14303805 -0.07636788 -0.53667765 -0.04357396
## alcohol
                       0.16412954 -0.49498534 0.04190356 0.39858458
##
                             PC9
                                       PC10
                                                   PC11
## fixed_acidity
                       0.40906345 0.27322565 0.342065272
## volatile acidity
                      -0.43991846 -0.12679298 0.078278568
## citric acid
                      -0.35278986 -0.22642878 -0.022744994
## residual sugar
                       0.07573828 0.05299393 0.430373805
## chlorides
                       0.31160684 0.14293522 0.048809367
## free sulfur dioxide
                       0.36690764 -0.53679357 -0.002643888
## total_sulfur_dioxide -0.24778764 0.70221161 -0.063510466
## density
                       ## pH
                       0.17856128 0.07100579 0.174135418
## sulphates
                      -0.27646554 0.02552777 0.071039626
## alcohol
```

```
#c
summary(winec.pca)
```

```
## Importance of components:
##
                            PC1
                                   PC2
                                          PC3
                                                  PC4
                                                           PC5
                                                                   PC6
                                                                           PC7
## Standard deviation
                          1.723 1.6076 1.2069 0.99467 0.86527 0.82790 0.72220
## Proportion of Variance 0.270 0.2349 0.1324 0.08994 0.06806 0.06231 0.04742
## Cumulative Proportion 0.270 0.5049 0.6373 0.72726 0.79533 0.85764 0.90505
##
                              PC8
                                      PC9
                                            PC10
                                                    PC11
## Standard deviation
                          0.71847 0.56193 0.4299 0.16607
## Proportion of Variance 0.04693 0.02871 0.0168 0.00251
## Cumulative Proportion 0.95198 0.98069 0.9975 1.00000
```

```
screeplot(winec.pca, type = "lines")
```





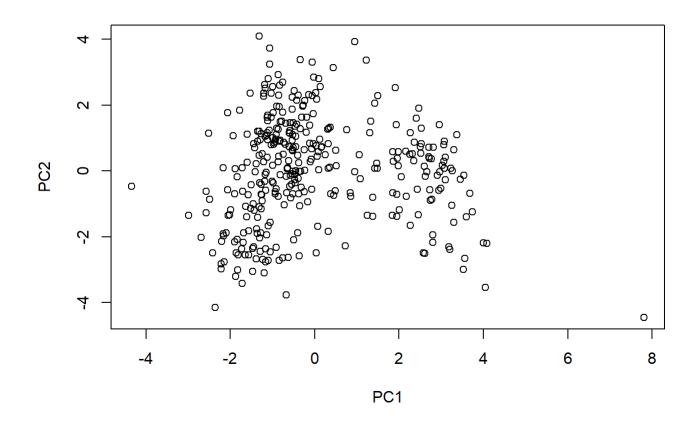
```
#10 PCs

#d

c=cor(winec, winec.pca$x)
round(c,2)
```

```
PC1
                               PC2
                                                       PC6
                                                                         PC9
##
                                     PC3
                                           PC4
                                                 PC5
                                                             PC7
                                                                   PC8
## fixed acidity
                        0.60 -0.47 0.39 -0.09 0.04 -0.30
                                                            0.06 -0.31
                                                                        0.23
## volatile_acidity
                        0.59 0.05 -0.49 -0.18 0.34 -0.37
                                                            0.25
                                                                  0.02 -0.25
## citric_acid
                       -0.02 -0.46 0.69 0.25 -0.23 -0.07
                                                            0.35
                                                                  0.15 - 0.20
## residual_sugar
                       -0.46 -0.66 -0.22 -0.10 -0.11 -0.26 -0.19
                                                                  0.42 0.04
## chlorides
                        0.64 -0.32 -0.10 0.17 0.31 0.43
                                                            0.22
                                                                  0.30
                                                                        0.18
## free sulfur dioxide -0.72 -0.28 -0.17 0.36
                                                0.31 -0.12
                                                            0.11 -0.16
## total_sulfur_dioxide -0.81 -0.29 -0.14 0.21 0.17 0.01
                                                            0.17 -0.13 -0.14
## density
                        0.32 -0.86 -0.28 -0.05 -0.18 -0.13 -0.06 -0.01 0.06
## pH
                         0.22 0.35 -0.56 0.39 -0.53 -0.07
                                                            0.24 - 0.04
## sulphates
                        0.55 -0.12  0.03  0.70  0.12 -0.06 -0.39 -0.03 -0.16
## alcohol
                       -0.05
                              0.76
                                    0.29 0.17 0.14 -0.41 0.03 0.29 0.17
##
                        PC10
                              PC11
## fixed acidity
                        0.12
                              0.06
## volatile acidity
                       -0.05
                              0.01
## citric_acid
                        -0.10
                              0.00
## residual sugar
                        0.02
                              0.07
## chlorides
                         0.06 0.01
## free_sulfur_dioxide -0.23 0.00
## total_sulfur_dioxide 0.30 -0.01
                         0.01 -0.12
## density
## pH
                         0.03 0.03
## sulphates
                        0.01 0.01
## alcohol
                         0.09 -0.06
```

#PC1: Sulfur Dioxide #PC2: Density of Alcohol by amount of sugar #PC3: PH level of acidity #PC4: PH level of sulfur containing bases #PC5: Ph level of volatile acidity and choloride #PC6: Chlorides residual sugar and acidity based on alcohol percantage #PC7: PH level of volatile, citric acid and sulphate #PC8: fixed acidity and residual sugar based on percentage of alcohol #PCA9: acidity, chlorides and sulfur dioxide #PCA10: Sulfur dioxide #e #No, the proportion of variance is too low, and too close to PC2. PC1 has a 27% proportion of va riance, while PC has 23.4% #F plot(winec.pca\$x[,1:2])

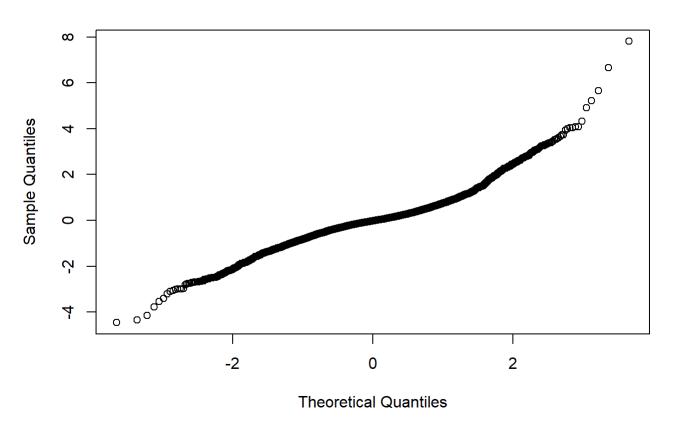


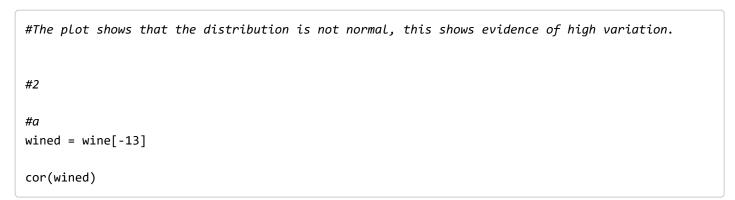
#There are no distingiuishing groups, however, there is an outlier that is skewed to the higher end of PC1

#bonus

qqnorm(winec.pca\$x)

# **Normal Q-Q Plot**





```
##
                        fixed acidity volatile acidity citric acid residual sugar
## fixed acidity
                                            0.225020854 0.38344924
                           1.00000000
                                                                        -0.09864763
## volatile acidity
                           0.22502085
                                            1.000000000 -0.32286866
                                                                        -0.17139713
## citric acid
                           0.38344924
                                           -0.322868655
                                                        1.00000000
                                                                        0.16225541
## residual sugar
                           -0.09864763
                                           -0.171397128 0.16225541
                                                                         1.00000000
## chlorides
                           0.32756202
                                            0.341374902 0.08681857
                                                                        -0.12546264
## free_sulfur_dioxide
                          -0.28237859
                                           -0.287109795
                                                         0.04245716
                                                                        0.43035646
## total sulfur dioxide
                          -0.36919701
                                           -0.358818093 0.10598165
                                                                        0.47333598
## density
                                                                        0.54020970
                           0.53262405
                                            0.244588159 0.19580930
## pH
                           -0.23369013
                                            0.228314657 -0.27738639
                                                                        -0.22678197
## sulphates
                           0.30713463
                                            0.186344437 0.10589346
                                                                        -0.19561141
## alcohol
                           -0.20003736
                                            0.004018921 -0.09567631
                                                                        -0.34337904
## quality
                           -0.11163094
                                           -0.234230528 0.02093266
                                                                        -0.01517474
##
                          chlorides free sulfur dioxide total sulfur dioxide
## fixed acidity
                         0.32756202
                                                                   -0.36919701
                                            -0.282378587
## volatile_acidity
                         0.34137490
                                            -0.287109795
                                                                   -0.35881809
## citric acid
                         0.08681857
                                             0.042457162
                                                                   0.10598165
## residual sugar
                        -0.12546264
                                             0.430356464
                                                                   0.47333598
## chlorides
                                                                   -0.32705409
                         1.00000000
                                            -0.248831028
## free sulfur dioxide -0.24883103
                                             1.000000000
                                                                   0.76269485
## total sulfur dioxide -0.32705409
                                             0.762694847
                                                                    1.00000000
## density
                         0.37847916
                                             0.005382083
                                                                   -0.02294370
## pH
                         0.01866647
                                            -0.128416387
                                                                   -0.17057929
## sulphates
                         0.39260836
                                            -0.147085345
                                                                   -0.28537680
## alcohol
                         -0.27335277
                                            -0.101607695
                                                                   -0.19333179
## quality
                         -0.21776159
                                             0.020542135
                                                                   -0.01026426
##
                             density
                                                рΗ
                                                      sulphates
                                                                      alcohol
## fixed acidity
                         0.532624054 -0.233690126
                                                    0.307134630 -0.200037357
                         0.244588159
## volatile acidity
                                       0.228314657
                                                    0.186344437
                                                                 0.004018921
## citric acid
                         0.195809304 -0.277386386 0.105893456 -0.095676312
## residual sugar
                         0.540209698 -0.226781965 -0.195611413 -0.343379037
## chlorides
                         0.378479157
                                       0.018666467
                                                    0.392608361 -0.273352774
## free_sulfur_dioxide
                         0.005382083 -0.128416387 -0.147085345 -0.101607695
## total sulfur dioxide -0.022943702 -0.170579290 -0.285376799 -0.193331790
## density
                         1.000000000 -0.005440951 0.228176692 -0.717527825
## pH
                         -0.005440951
                                      1.000000000 0.169653803
                                                                 0.129038264
## sulphates
                         0.228176692 0.169653803 1.000000000
                                                                 0.008272161
## alcohol
                        -0.717527825
                                      0.129038264 0.008272161
                                                                 1.000000000
## quality
                         -0.278927117
                                       0.019394617 0.124581349
                                                                 0.396693357
##
                             quality
## fixed acidity
                        -0.11163094
## volatile acidity
                        -0.23423053
## citric acid
                         0.02093266
## residual sugar
                        -0.01517474
## chlorides
                        -0.21776159
## free sulfur dioxide
                         0.02054213
## total sulfur dioxide -0.01026426
## density
                         -0.27892712
## pH
                         0.01939462
## sulphates
                         0.12458135
```

## alcohol 0.39669336 ## quality 1.00000000

cov(wined)

```
##
                        fixed_acidity volatile_acidity
                                                         citric acid
## fixed acidity
                          1.890202538
                                          0.0509847073 7.466255e-02
## volatile acidity
                          0.050984707
                                          0.0271597634 -7.535804e-03
## citric acid
                          0.074662546
                                         -0.0075358043 2.005772e-02
## residual sugar
                         -0.642850594
                                         -0.1338861850 1.089204e-01
## chlorides
                          0.014041393
                                          0.0017541110 3.833680e-04
## free_sulfur_dioxide
                         -7.137701187
                                         -0.8699282440 1.105514e-01
## total sulfur dioxide -29.064296357
                                         -3.3859831355 8.594466e-01
## density
                          0.002214716
                                          0.0001219106 8.387203e-05
## pH
                         -0.047560426
                                          0.0055699075 -5.815366e-03
## sulphates
                          0.061132820
                                          0.0044460147 2.171208e-03
## alcohol
                         -0.326777023
                                          0.0007869709 -1.610020e-02
## quality
                         -0.132358576
                                         -0.0332904625 2.556693e-03
                        residual_sugar
##
                                           chlorides free sulfur dioxide
## fixed acidity
                          -0.642850594 1.404139e-02
                                                           -7.137701e+00
## volatile_acidity
                          -0.133886185
                                       1.754111e-03
                                                           -8.699282e-01
## citric acid
                           0.108920385 3.833680e-04
                                                            1.105514e-01
## residual sugar
                          22.466657798 -1.854156e-02
                                                            3.750334e+01
## chlorides
                                                           -1.426394e-01
                          -0.018541555 9.721314e-04
## free sulfur dioxide
                          37.503344249 -1.426394e-01
                                                            3.380219e+02
## total sulfur dioxide 128.465413426 -5.838880e-01
                                                            8.029171e+02
## density
                           0.007744167 3.569008e-05
                                                            2.992719e-04
## pH
                          -0.159121531 8.615407e-05
                                                           -3.494975e-01
## sulphates
                          -0.134231641 1.772203e-03
                                                           -3.915014e-01
## alcohol
                          -1.933878769 -1.012680e-02
                                                           -2.219654e+00
## quality
                          -0.062030291 -5.855407e-03
                                                            3.257102e-01
##
                        total sulfur dioxide
                                                   density
                                                                      рΗ
## fixed acidity
                               -2.906430e+01 2.214716e-03 -4.756043e-02
## volatile acidity
                               -3.385983e+00 1.219106e-04 5.569907e-03
## citric acid
                                8.594466e-01 8.387203e-05 -5.815366e-03
## residual sugar
                                1.284654e+02 7.744167e-03 -1.591215e-01
## chlorides
                               -5.838880e-01 3.569008e-05 8.615407e-05
## free_sulfur_dioxide
                                8.029171e+02 2.992719e-04 -3.494975e-01
## total sulfur dioxide
                                3.278649e+03 -3.973325e-03 -1.445856e+00
## density
                               -3.973325e-03 9.147159e-06 -2.435954e-06
## pH
                               -1.445856e+00 -2.435954e-06 2.191303e-02
## sulphates
                               -2.365689e+00 9.990929e-05 3.635853e-03
## alcohol
                               -1.315337e+01 -2.578506e-03 2.269635e-02
## quality
                               -5.068604e-01 -7.275238e-04 2.475972e-03
##
                            sulphates
                                            alcohol
                                                          quality
## fixed acidity
                         6.113282e-02 -3.267770e-01 -0.1323585755
## volatile acidity
                         4.446015e-03 7.869709e-04 -0.0332904625
## citric acid
                         2.171208e-03 -1.610020e-02 0.0025566926
## residual sugar
                        -1.342316e-01 -1.933879e+00 -0.0620302906
## chlorides
                         1.772203e-03 -1.012680e-02 -0.0058554073
## free_sulfur_dioxide -3.915014e-01 -2.219654e+00 0.3257101924
## total sulfur dioxide -2.365689e+00 -1.315337e+01 -0.5068604175
## density
                         9.990929e-05 -2.578506e-03 -0.0007275238
## pH
                         3.635853e-03 2.269635e-02 0.0024759722
## sulphates
                         2.095960e-02 1.422973e-03 0.0155545641
```

```
## alcohol 1.422973e-03 1.411798e+00 0.4064943375
## quality 1.555456e-02 4.064943e-01 0.7437494883
```

```
#b I chose correlation maxtrix because the variables are not one the same scale.
wine.pca = prcomp(wined,scale. = T)
wine.pca
```

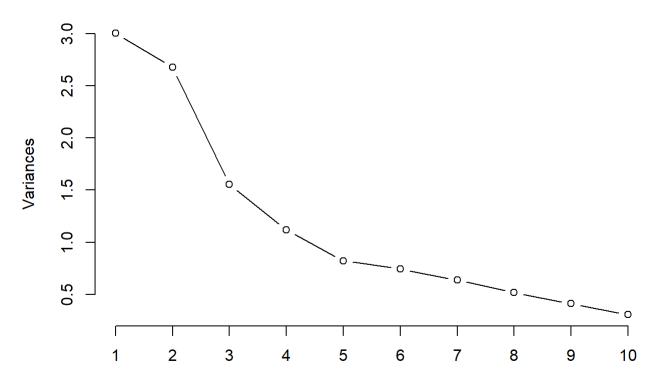
```
## Standard deviations (1, .., p=12):
   [1] 1.7324119 1.6357004 1.2467205 1.0580945 0.9067586 0.8621958 0.7981909
##
##
   [8] 0.7194678 0.6417402 0.5537722 0.4277998 0.1658754
##
## Rotation (n \times k) = (12 \times 12):
##
                                                   PC3
                                                               PC4
                             PC1
                                        PC2
## fixed acidity
                       0.37384753 -0.20920790 0.34944193
                                                        0.101481689
## volatile acidity
                       ## citric acid
                       0.01550334 -0.24883481 0.57469924
                                                       0.007293069
## residual sugar
                      -0.21073912 -0.43076891 -0.08045098 -0.163775376
## chlorides
                       0.39301292 -0.13510339 -0.03755022 -0.114788780
## free sulfur dioxide -0.38691015 -0.23592001 -0.09789778 -0.287638032
## total sulfur dioxide -0.43615175 -0.25936172 -0.09887064 -0.145936568
## density
                       0.25687987 -0.49174628 -0.11498773 -0.167868006
## pH
                       0.10042460 0.22184714 -0.39264147 -0.448034762
## sulphates
                       0.30735851 0.01054705 0.17042324 -0.613979534
## alcohol
                      -0.10540151   0.47361058   0.21246419   -0.082411454
## quality
                      -0.14068511
                                 0.21960665
                                            0.36299199 -0.482597698
##
                             PC5
                                        PC6
                                                   PC7
                                                              PC8
## fixed acidity
                       0.13882760 -0.12231102 0.37554679 -0.32337939
## volatile acidity
                       0.17854081 -0.49137727
                                            0.39081629
                                                       0.20269632
## citric_acid
                      -0.21716706   0.30102439   0.34520552   0.42157398
## residual sugar
                       0.45985782 -0.04057706 -0.03621810
                                                       0.36955879
## chlorides
                      -0.38370342 -0.19562045 -0.44540196
                                                       0.52910531
## free sulfur dioxide -0.29102109 -0.32440834 0.22851724 -0.10881479
## total sulfur dioxide -0.25210986 -0.13491619 0.13311385 -0.02804903
## density
                       ## pH
                      -0.02773031 0.61105097 0.31137342 0.12066866
## sulphates
                      -0.27804516 -0.13216386 -0.04388815 -0.32078443
## alcohol
                       0.05413015 -0.26854548 0.36266713
                                                       0.35593643
## quality
                       0.47615444 -0.11424921 -0.29101433
                                                       0.01265819
##
                             PC9
                                      PC10
                                                 PC11
                                                             PC12
## fixed acidity
                       ## volatile acidity
                       0.11151836 -0.4705296 -0.15021984 -0.075668433
## citric acid
                       0.02304073 -0.3421192 -0.23390324 0.023508793
## residual sugar
                      -0.41382212   0.1504179   0.07075169   -0.432262885
## chlorides
                       0.26011021 0.2458745 0.13589718 -0.047862076
## free sulfur dioxide
                       ## total sulfur dioxide 0.20364509 -0.3097345 0.68535808 0.063560810
## density
                       0.01043673 0.1040176 0.02101411 0.730305663
## pH
                       ## sulphates
                      -0.51367297 -0.1692788 0.04347695 -0.073442865
## alcohol
                      -0.24893466 0.3759888
                                            0.24899992 0.337711305
## quality
                       0.45675359 -0.1735244 -0.06215342 0.009685102
```

```
#c
summary(wine.pca)
```

```
## Importance of components:
##
                             PC1
                                    PC2
                                           PC3
                                                  PC4
                                                           PC5
                                                                   PC6
                                                                           PC7
## Standard deviation
                          1.7324 1.6357 1.2467 1.0581 0.90676 0.86220 0.79819
## Proportion of Variance 0.2501 0.2230 0.1295 0.0933 0.06852 0.06195 0.05309
## Cumulative Proportion 0.2501 0.4731 0.6026 0.6959 0.76440 0.82635 0.87945
##
                              PC8
                                      PC9
                                             PC10
                                                     PC11
                                                              PC12
## Standard deviation
                          0.71947 0.64174 0.55377 0.42780 0.16588
## Proportion of Variance 0.04314 0.03432 0.02556 0.01525 0.00229
## Cumulative Proportion 0.92258 0.95690 0.98246 0.99771 1.00000
```

screeplot(wine.pca, type="lines")

# wine.pca

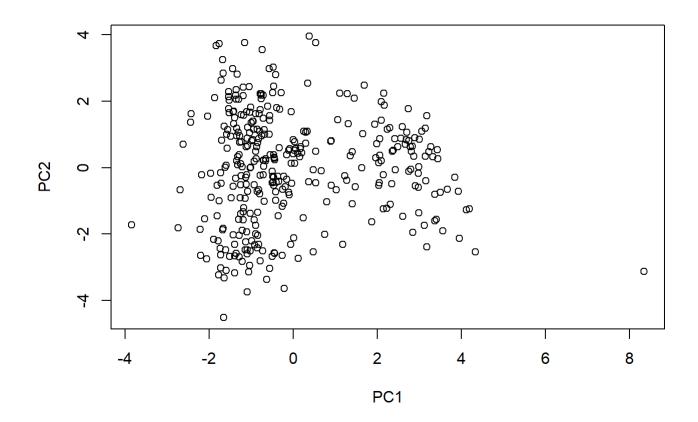


#d
#10 PCs, however, I could get away with 9 PCs in comparison to question 1 due to PC9 in PC2 has
a lower variance explained

#e
d=cor(wined, wine.pca\$x)
round(d,2)

```
PC1
                              PC2
                                          PC4
                                                     PC6
                                                                       PC9
##
                                    PC3
                                                PC5
                                                           PC7
                                                                 PC8
                        0.65 -0.34 0.44 0.11 0.13 -0.11
## fixed acidity
                                                          0.30 -0.23
                                                                      0.19
## volatile_acidity
                        0.60 0.10 -0.48 -0.01 0.16 -0.42
                                                          0.31
                                                                0.15
                                                                      0.07
## citric_acid
                        0.03 -0.41 0.72 0.01 -0.20 0.26
                                                          0.28
                                                                0.30
                                                                      0.01
                       -0.37 -0.70 -0.10 -0.17 0.42 -0.03 -0.03
## residual_sugar
                                                                0.27 -0.27
## chlorides
                        0.68 -0.22 -0.05 -0.12 -0.35 -0.17 -0.36
                                                                0.38
## free_sulfur_dioxide -0.67 -0.39 -0.12 -0.30 -0.26 -0.28
                                                          0.18 -0.08
## total sulfur dioxide -0.76 -0.42 -0.12 -0.15 -0.23 -0.12
                                                          0.11 -0.02
                                                                      0.13
## density
                        0.45 -0.80 -0.14 -0.18 0.27 0.10
                                                          0.04 -0.04
                                                                      0.01
## pH
                        0.17
                             0.36 -0.49 -0.47 -0.03
                                                    0.53
                                                          0.25
## sulphates
                        0.53
                             ## alcohol
                       -0.18
                             0.77 0.26 -0.09 0.05 -0.23
                                                          0.29
                                                                0.26 -0.16
## quality
                       -0.24
                             0.36 0.45 -0.51 0.43 -0.10 -0.23
                                                                0.01 0.29
##
                        PC10
                             PC11 PC12
## fixed acidity
                        0.19 0.12 -0.06
## volatile_acidity
                       -0.26 -0.06 -0.01
## citric_acid
                       -0.19 -0.10 0.00
## residual_sugar
                        0.08 0.03 -0.07
## chlorides
                        0.14 0.06 -0.01
## free_sulfur_dioxide
                        0.20 -0.23 0.00
## total sulfur dioxide -0.17
                             0.29 0.01
## density
                        0.06
                             0.01 0.12
## pH
                        0.08
                             0.03 -0.03
## sulphates
                       -0.09
                             0.02 -0.01
## alcohol
                        0.21 0.11 0.06
## quality
                       -0.10 -0.03 0.00
```

```
#PC1: Wine type based of acidity, chlorides and sulfur dioxide
#PC2: Amount of density based on percentage of alcohol and residual sugar
#PC3: Acidity based on PH level and quality
#PC4: Amount of sulphates based on quality and PH level
#PC5: Quality based on Residual sugar and chlorides
#PC6: Average Ph level based on percentage of volatile acidity and free sulfur dioxide
#PC7: PH level of acidity
#PC8: Total Amount of residual sugars, chlorides and citric acid based on percentage of alcohol
#PC9: Quality based Sulphates and residual sugar
#PC10: Amount of Volatile Acidity based on quality of alchohol
#Yes, my interretations do differ, categorical variable dominated the PCs
#F
summary(wine.pca)
## Importance of components:
                                                  PC4
                                                                  PC6
##
                             PC1
                                    PC2
                                           PC3
                                                          PC5
                                                                          PC7
                          1.7324 1.6357 1.2467 1.0581 0.90676 0.86220 0.79819
## Standard deviation
## Proportion of Variance 0.2501 0.2230 0.1295 0.0933 0.06852 0.06195 0.05309
## Cumulative Proportion 0.2501 0.4731 0.6026 0.6959 0.76440 0.82635 0.87945
##
                              PC8
                                      PC9
                                             PC10
                                                     PC11
                                                             PC12
## Standard deviation
                          0.71947 0.64174 0.55377 0.42780 0.16588
## Proportion of Variance 0.04314 0.03432 0.02556 0.01525 0.00229
## Cumulative Proportion 0.92258 0.95690 0.98246 0.99771 1.00000
#No, the proportion of variance is too close in proportion of variance to PC2
#G
plot(wine.pca$x[,1:2])
```



#There are distinguishable groups, and there is one outlier on the PC1 axis. There is a difference compared to question one because the groups are distinuishable

#### #Bonus

#I would prefer with categorical variables because it more easier to interpret relationships in each PC. An alternative method would be creating subsets for the data based factors of the categ orical variables, and then use PCA for each subset.

#3

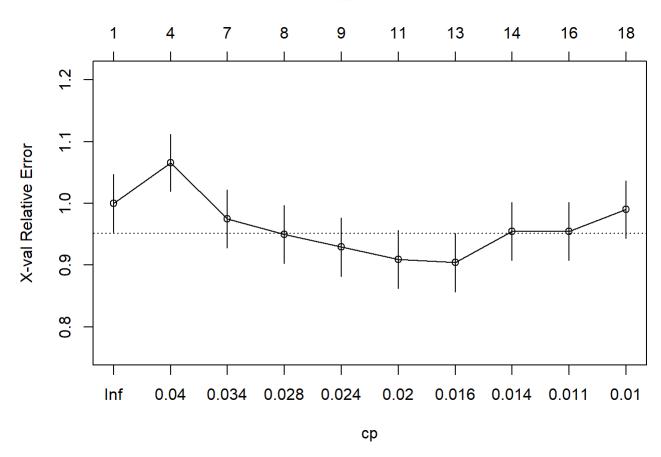
library(rpart)
library(rpart.plot)

#a
wine\$quality=as.factor(wine\$quality)
fit= rpart(quality~., method = "class", data=wine)
printcp(fit)

```
##
## Classification tree:
## rpart(formula = quality ~ ., data = wine, method = "class")
##
## Variables actually used in tree construction:
## [1] alcohol
                            chlorides
                                                 density
## [4] fixed_acidity
                            рΗ
                                                 sulphates
## [7] total_sulfur_dioxide volatile_acidity
##
## Root node error: 198/350 = 0.56571
##
## n= 350
##
##
           CP nsplit rel error xerror
## 1 0.043771
                        1.00000 1.00000 0.046833
## 2 0.037037
                    3
                        0.86869 1.06566 0.046233
## 3 0.030303
                        0.75758 0.97475 0.046993
## 4
     0.025253
                   7
                        0.72727 0.94949 0.047113
## 5 0.022727
                   8
                        0.70202 0.92929 0.047181
## 6 0.017677
                   10
                        0.65657 0.90909 0.047224
## 7 0.015152
                   12
                        0.62121 0.90404 0.047231
## 8 0.012626
                   13
                        0.60606 0.95455 0.047092
## 9 0.010101
                   15
                        0.58081 0.95455 0.047092
## 10 0.010000
                   17
                        0.56061 0.98990 0.046902
```

```
plotcp(fit)
```





summary(fit)

```
## Call:
## rpart(formula = quality ~ ., data = wine, method = "class")
##
##
##
              CP nsplit rel error
                                                   xstd
                                      xerror
     0.04377104
                      0 1.0000000 1.0000000 0.04683334
## 1
##
  2
      0.03703704
                      3 0.8686869 1.0656566 0.04623272
## 3
      0.03030303
                      6 0.7575758 0.9747475 0.04699258
      0.02525253
                      7 0.7272727 0.9494949 0.04711262
## 4
## 5
      0.02272727
                      8 0.7020202 0.9292929 0.04718063
      0.01767677
                     10 0.6565657 0.9090909 0.04722386
## 6
      0.01515152
                     12 0.6212121 0.9040404 0.04723081
## 7
## 8
     0.01262626
                     13 0.6060606 0.9545455 0.04709173
## 9
     0.01010101
                     15 0.5808081 0.9545455 0.04709173
## 10 0.01000000
                     17 0.5606061 0.9898990 0.04690176
##
## Variable importance
##
                alcohol
                                      density total_sulfur_dioxide
##
                                           13
                     18
                                                                 13
                                    chlorides
##
              sulphates
                                                     fixed_acidity
##
                                                                  8
                     12
       volatile_acidity
                         free_sulfur_dioxide
##
                                                    residual_sugar
##
                      6
                                            4
##
                                           рΗ
                                                       citric_acid
                   type
##
                      4
                                            4
                                                                  2
##
##
   Node number 1: 350 observations,
                                        complexity param=0.04377104
##
     predicted class=6 expected loss=0.5657143 P(node) =1
##
       class counts:
                        14
                              108
                                    152
                                           67
##
      probabilities: 0.040 0.309 0.434 0.191 0.026
##
     left son=2 (218 obs) right son=3 (132 obs)
##
     Primary splits:
##
         alcohol
                              < 10.75
                                         to the left, improve=20.929650, (0 missing)
##
         density
                              < 0.99222
                                        to the right, improve=10.996840, (0 missing)
##
         chlorides
                              < 0.0445
                                         to the right, improve= 7.709710, (0 missing)
##
         free sulfur dioxide < 17.5
                                         to the left, improve= 3.759377, (0 missing)
##
         volatile acidity
                              < 0.455
                                         to the right, improve= 3.660000, (0 missing)
##
     Surrogate splits:
         density
                        < 0.992935 to the right, agree=0.820, adj=0.523, (0 split)
##
##
         chlorides
                        < 0.0365
                                    to the right, agree=0.731, adj=0.288, (0 split)
##
         fixed acidity < 6.05
                                    to the right, agree=0.649, adj=0.068, (0 split)
##
         residual sugar < 1.25
                                    to the right, agree=0.649, adj=0.068, (0 split)
##
         sulphates
                         < 0.335
                                    to the right, agree=0.646, adj=0.061, (0 split)
##
## Node number 2: 218 observations,
                                        complexity param=0.04377104
     predicted class=6
                        expected loss=0.559633 P(node) =0.6228571
##
##
       class counts:
                        11
                               95
                                     96
                                           11
##
      probabilities: 0.050 0.436 0.440 0.050 0.023
##
     left son=4 (209 obs) right son=5 (9 obs)
     Primary splits:
##
         total sulfur dioxide < 220
                                          to the left, improve=4.775559, (0 missing)
##
##
         volatile_acidity
                               < 0.2275
                                          to the right, improve=4.748625, (0 missing)
```

```
##
         density
                               < 0.99369 to the left,
                                                        improve=2.768169, (0 missing)
                                          to the right, improve=2.679951, (0 missing)
##
         рΗ
                               < 3.055
##
         sulphates
                               < 0.375
                                          to the left,
                                                        improve=2.469719, (0 missing)
##
   Node number 3: 132 observations,
                                        complexity param=0.03703704
##
     predicted class=6 expected loss=0.5757576 P(node) =0.3771429
##
##
       class counts:
                          3
                               13
                                     56
                                           56
##
      probabilities: 0.023 0.098 0.424 0.424 0.030
     left son=6 (125 obs) right son=7 (7 obs)
##
##
     Primary splits:
##
         chlorides
                               < 0.023
                                          to the right, improve=3.863152, (0 missing)
##
                                                        improve=3.237374, (0 missing)
         total sulfur dioxide < 80.5
                                          to the left,
         volatile acidity
                                          to the right, improve=3.213442, (0 missing)
##
                               < 0.485
##
         sulphates
                               < 0.375
                                          to the left,
                                                        improve=3.043466, (0 missing)
##
         free_sulfur_dioxide < 15.5</pre>
                                          to the left,
                                                        improve=2.932734, (0 missing)
##
   Node number 4: 209 observations,
                                        complexity param=0.04377104
##
     predicted class=5 expected loss=0.5454545 P(node) =0.5971429
##
                               95
                                     87
       class counts:
                        11
                                           11
##
      probabilities: 0.053 0.455 0.416 0.053 0.024
##
     left son=8 (154 obs) right son=9 (55 obs)
##
     Primary splits:
##
                                          to the right, improve=5.501982, (0 missing)
         volatile_acidity
                               < 0.2275
##
         sulphates
                               < 0.555
                                          to the left,
                                                        improve=3.023857, (0 missing)
                               < 3.295
                                          to the left,
                                                        improve=2.873411, (0 missing)
##
         рН
                                                        improve=2.214736, (0 missing)
##
         total_sulfur_dioxide < 22.5
                                          to the left,
         density
                               < 0.99369 to the left,
                                                        improve=2.144072, (0 missing)
##
##
     Surrogate splits:
                                         to the left, agree=0.770, adj=0.127, (0 split)
##
         residual sugar
                              < 14
##
         alcohol
                              < 8.95
                                         to the right, agree=0.756, adj=0.073, (0 split)
##
         free sulfur dioxide < 75.5
                                         to the left, agree=0.742, adj=0.018, (0 split)
##
         density
                              < 0.999405 to the left, agree=0.742, adj=0.018, (0 split)
##
   Node number 5: 9 observations
##
##
     predicted class=6 expected loss=0 P(node) =0.02571429
##
       class counts:
                          0
                                0
##
      probabilities: 0.000 0.000 1.000 0.000 0.000
##
## Node number 6: 125 observations,
                                        complexity param=0.03703704
     predicted class=6 expected loss=0.552 P(node) =0.3571429
##
##
       class counts:
                          3
                               13
                                     56
                                           49
                                                  4
      probabilities: 0.024 0.104 0.448 0.392 0.032
##
##
     left son=12 (32 obs) right son=13 (93 obs)
##
     Primary splits:
##
         total_sulfur_dioxide < 80.5</pre>
                                          to the left,
                                                        improve=2.975253, (0 missing)
##
         chlorides
                               < 0.0485
                                          to the right, improve=2.779764, (0 missing)
                               < 1.55
                                          to the left,
                                                        improve=2.767268, (0 missing)
##
         residual sugar
##
         volatile acidity
                               < 0.485
                                          to the right, improve=2.697455, (0 missing)
         free_sulfur_dioxide < 14</pre>
                                          to the left, improve=2.552000, (0 missing)
##
##
     Surrogate splits:
##
         type
                              splits as
                                         RL,
                                                        agree=0.928, adj=0.719, (0 split)
##
         chlorides
                              < 0.0585
                                         to the right, agree=0.896, adj=0.594, (0 split)
```

```
##
                                         to the left, agree=0.896, adj=0.594, (0 split)
         free sulfur dioxide < 18.5
##
                              < 0.99372 to the right, agree=0.864, adj=0.469, (0 split)
         density
##
         fixed acidity
                              < 8.05
                                         to the right, agree=0.840, adj=0.375, (0 split)
##
   Node number 7: 7 observations
##
##
     predicted class=7 expected loss=0 P(node) =0.02
##
       class counts:
                          0
                                0
##
      probabilities: 0.000 0.000 0.000 1.000 0.000
##
## Node number 8: 154 observations,
                                        complexity param=0.03030303
##
     predicted class=5 expected loss=0.4675325 P(node) =0.44
##
                         9
       class counts:
                               82
                                     56
                                            5
                                                  2
      probabilities: 0.058 0.532 0.364 0.032 0.013
##
     left son=16 (88 obs) right son=17 (66 obs)
##
##
     Primary splits:
         sulphates
                               < 0.555
##
                                          to the left,
                                                        improve=3.987013, (0 missing)
##
         alcohol
                               < 9.85
                                          to the left,
                                                        improve=3.692264, (0 missing)
##
         total sulfur dioxide < 174
                                          to the right, improve=2.783800, (0 missing)
##
                                          to the right, improve=2.257234, (0 missing)
         fixed_acidity
                               < 6.25
                                          to the right, improve=1.979978, (0 missing)
##
         free sulfur dioxide < 36.5
##
     Surrogate splits:
##
         type
                               splits as
                                          LR,
                                                        agree=0.721, adj=0.348, (0 split)
##
         total_sulfur_dioxide < 92.5</pre>
                                          to the right, agree=0.714, adj=0.333, (0 split)
##
         chlorides
                               < 0.069
                                          to the left,
                                                        agree=0.675, adj=0.242, (0 split)
         fixed acidity
                               < 8.05
                                                        agree=0.662, adj=0.212, (0 split)
##
                                          to the left,
##
         free_sulfur_dioxide < 18.5</pre>
                                          to the right, agree=0.630, adj=0.136, (0 split)
##
   Node number 9: 55 observations,
##
                                       complexity param=0.01262626
     predicted class=6 expected loss=0.4363636 P(node) =0.1571429
##
##
       class counts:
                          2
                               13
                                     31
                                            6
##
      probabilities: 0.036 0.236 0.564 0.109 0.055
     left son=18 (37 obs) right son=19 (18 obs)
##
     Primary splits:
##
##
         рΗ
                                          to the left, improve=3.896970, (0 missing)
                               < 3.275
##
         fixed acidity
                               < 7.05
                                          to the left,
                                                        improve=3.797332, (0 missing)
                               < 0.525
                                          to the right, improve=3.431768, (0 missing)
##
         sulphates
##
         total_sulfur_dioxide < 137.5
                                          to the left, improve=3.131276, (0 missing)
##
         chlorides
                               < 0.039
                                          to the right, improve=2.855303, (0 missing)
     Surrogate splits:
##
                                          to the left, agree=0.782, adj=0.333, (0 split)
##
         sulphates
                               < 0.565
         volatile acidity
                               < 0.1175
                                          to the right, agree=0.709, adj=0.111, (0 split)
##
                                          to the right, agree=0.709, adj=0.111, (0 split)
##
         residual sugar
                               < 1.7
##
         total sulfur dioxide < 167.5
                                          to the left, agree=0.709, adj=0.111, (0 split)
##
         density
                               < 0.99908
                                          to the left,
                                                        agree=0.709, adj=0.111, (0 split)
##
   Node number 12: 32 observations,
                                        complexity param=0.01010101
##
##
     predicted class=6 expected loss=0.4375 P(node) =0.09142857
##
       class counts:
                         1
                                7
                                     18
      probabilities: 0.031 0.219 0.562 0.188 0.000
##
     left son=24 (14 obs) right son=25 (18 obs)
##
##
     Primary splits:
##
         sulphates
                                         to the left, improve=3.393849, (0 missing)
                              < 0.605
```

```
to the left,
##
         free sulfur dioxide < 14
                                                       improve=2.988366, (0 missing)
##
                                                       improve=2.598128, (0 missing)
         density
                              < 0.9938
                                         to the left,
##
         chlorides
                              < 0.0695
                                         to the left,
                                                       improve=2.473214, (0 missing)
         volatile_acidity
##
                                         to the right, improve=1.687500, (0 missing)
                             < 0.325
##
     Surrogate splits:
                                                        agree=0.844, adj=0.643, (0 split)
##
         density
                               < 0.9938
                                          to the left,
##
         chlorides
                               < 0.0565
                                          to the left,
                                                        agree=0.781, adj=0.500, (0 split)
##
                               splits as
                                                        agree=0.781, adj=0.500, (0 split)
         type
                                          LR,
                               < 6.7
                                                        agree=0.750, adj=0.429, (0 split)
##
         fixed acidity
                                          to the left,
##
         total sulfur dioxide < 37.5
                                          to the right, agree=0.719, adj=0.357, (0 split)
##
## Node number 13: 93 observations,
                                        complexity param=0.03703704
     predicted class=7 expected loss=0.5376344 P(node) =0.2657143
##
##
       class counts:
                         2
                                6
                                     38
                                           43
##
      probabilities: 0.022 0.065 0.409 0.462 0.043
     left son=26 (70 obs) right son=27 (23 obs)
##
##
     Primary splits:
##
         sulphates
                               < 0.565
                                          to the left, improve=5.525893, (0 missing)
##
                               < 1.55
                                          to the left,
                                                        improve=3.730862, (0 missing)
         residual_sugar
                               < 0.990985 to the right, improve=2.280156, (0 missing)
##
         density
                                          to the right, improve=2.126679, (0 missing)
##
         total_sulfur_dioxide < 153.5
##
                               < 3.055
                                          to the left,
                                                        improve=1.542593, (0 missing)
##
     Surrogate splits:
##
         citric acid
                              < 0.165
                                         to the right, agree=0.785, adj=0.130, (0 split)
                              < 13.7
                                         to the left, agree=0.785, adj=0.130, (0 split)
##
         alcohol
                                         to the right, agree=0.774, adj=0.087, (0 split)
##
         volatile_acidity
                              < 0.115
         free_sulfur_dioxide < 60.5</pre>
                                         to the left, agree=0.763, adj=0.043, (0 split)
##
##
                                        complexity param=0.01515152
## Node number 16: 88 observations,
##
     predicted class=5 expected loss=0.3636364 P(node) =0.2514286
##
       class counts:
                         6
                                     24
                                            2
                               56
      probabilities: 0.068 0.636 0.273 0.023 0.000
##
     left son=32 (73 obs) right son=33 (15 obs)
##
##
     Primary splits:
##
         fixed acidity
                               < 6.25
                                          to the right, improve=3.040349, (0 missing)
         total_sulfur_dioxide < 156.5</pre>
                                          to the right, improve=2.786830, (0 missing)
##
##
         alcohol
                               < 10.55
                                          to the left, improve=1.503987, (0 missing)
##
         volatile acidity
                               < 0.69
                                          to the right, improve=1.448292, (0 missing)
         residual sugar
                               < 5.65
                                          to the left, improve=1.415388, (0 missing)
##
##
     Surrogate splits:
         density
                        < 0.99234 to the right, agree=0.875, adj=0.267, (0 split)
##
                                    to the left, agree=0.852, adj=0.133, (0 split)
##
         рΗ
                        < 3.395
##
         residual_sugar < 16.15
                                    to the left,
                                                  agree=0.841, adj=0.067, (0 split)
##
## Node number 17: 66 observations,
                                        complexity param=0.02525253
     predicted class=6 expected loss=0.5151515 P(node) =0.1885714
##
       class counts:
##
                         3
                               26
                                     32
                                            3
##
      probabilities: 0.045 0.394 0.485 0.045 0.030
     left son=34 (8 obs) right son=35 (58 obs)
##
##
     Primary splits:
##
                                          to the left, improve=2.452194, (0 missing)
         total_sulfur_dioxide < 22.5
##
         citric acid
                               < 0.425
                                          to the right, improve=2.201154, (0 missing)
```

```
##
         alcohol
                              < 9.85
                                          to the left, improve=1.836398, (0 missing)
##
         sulphates
                              < 0.625
                                          to the right, improve=1.601399, (0 missing)
##
         chlorides
                              < 0.093
                                          to the right, improve=1.566234, (0 missing)
##
     Surrogate splits:
##
         free sulfur dioxide < 4.5
                                         to the left, agree=0.909, adj=0.25, (0 split)
##
## Node number 18: 37 observations,
                                        complexity param=0.01262626
##
     predicted class=6 expected loss=0.5945946 P(node) =0.1057143
##
       class counts:
                         2
                              12
                                     15
                                            5
##
      probabilities: 0.054 0.324 0.405 0.135 0.081
##
     left son=36 (15 obs) right son=37 (22 obs)
##
     Primary splits:
         fixed acidity
##
                              < 6.85
                                          to the left,
                                                        improve=2.872727, (0 missing)
##
         sulphates
                              < 0.415
                                          to the left,
                                                        improve=2.132867, (0 missing)
##
         density
                              < 0.99495
                                         to the right, improve=1.807692, (0 missing)
##
         рΗ
                              < 3.05
                                          to the right, improve=1.767241, (0 missing)
##
         total_sulfur_dioxide < 137.5
                                          to the left, improve=1.417647, (0 missing)
##
     Surrogate splits:
##
         sulphates
                                to the left, agree=0.730, adj=0.333, (0 split)
                     < 0.4
                                              agree=0.703, adj=0.267, (0 split)
         density
                     < 0.992415 to the left,
##
##
         citric acid < 0.245
                                to the left, agree=0.676, adj=0.200, (0 split)
##
         рΗ
                     < 3.16
                                to the right, agree=0.676, adj=0.200, (0 split)
##
         alcohol
                                to the right, agree=0.676, adj=0.200, (0 split)
                     < 10.45
##
   Node number 19: 18 observations
##
##
     predicted class=6 expected loss=0.1111111 P(node) =0.05142857
##
       class counts:
                         0
                                1
                                     16
                                            1
      probabilities: 0.000 0.056 0.889 0.056 0.000
##
##
## Node number 24: 14 observations
##
     predicted class=5 expected loss=0.5 P(node) =0.04
##
       class counts:
                         1
                                7
                                      5
                                            1
      probabilities: 0.071 0.500 0.357 0.071 0.000
##
##
## Node number 25: 18 observations
     predicted class=6 expected loss=0.2777778 P(node) =0.05142857
##
##
       class counts:
                         0
                                0
                                     13
                                            5
##
      probabilities: 0.000 0.000 0.722 0.278 0.000
##
## Node number 26: 70 observations,
                                        complexity param=0.02272727
##
     predicted class=6 expected loss=0.5 P(node) =0.2
##
       class counts:
                         2
                                5
                                     35
                                           25
##
      probabilities: 0.029 0.071 0.500 0.357 0.043
     left son=52 (43 obs) right son=53 (27 obs)
##
     Primary splits:
##
         density
##
                             < 0.990985 to the right, improve=2.926935, (0 missing)
         alcohol
                             < 11.05
                                         to the right, improve=2.385714, (0 missing)
##
##
         chlorides
                             < 0.0345
                                         to the left, improve=2.035047, (0 missing)
                                         to the left, improve=1.768627, (0 missing)
##
         residual_sugar
                             < 1.65
                                         to the right, improve=1.330939, (0 missing)
##
         free sulfur dioxide < 22.5
##
     Surrogate splits:
##
         alcohol
                                         to the left, agree=0.871, adj=0.667, (0 split)
                              < 12.1
```

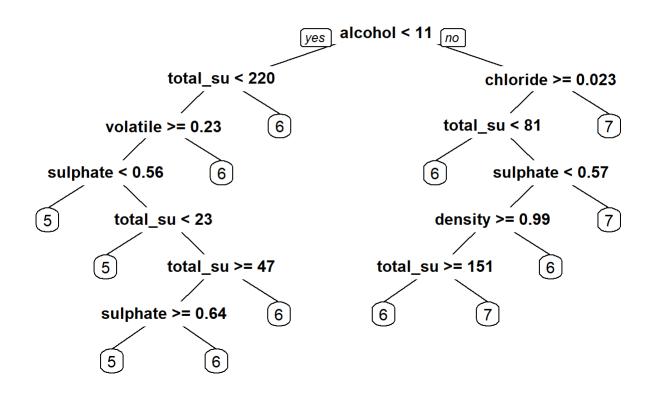
```
to the right, agree=0.771, adj=0.407, (0 split)
##
         residual sugar
                               < 3.6
                                          to the right, agree=0.729, adj=0.296, (0 split)
##
         chlorides
                               < 0.0355
##
         total sulfur dioxide < 112.5
                                          to the right, agree=0.729, adj=0.296, (0 split)
##
                               < 3.03
                                          to the right, agree=0.657, adj=0.111, (0 split)
         рН
##
##
   Node number 27: 23 observations
##
     predicted class=7 expected loss=0.2173913 P(node) =0.06571429
##
       class counts:
                         0
                                1
                                      3
                                           18
                                                  1
##
      probabilities: 0.000 0.043 0.130 0.783 0.043
##
##
   Node number 32: 73 observations
##
     predicted class=5 expected loss=0.3150685 P(node) =0.2085714
       class counts:
                               50
##
                         6
                                     15
                                            2
      probabilities: 0.082 0.685 0.205 0.027 0.000
##
##
## Node number 33: 15 observations
##
     predicted class=6 expected loss=0.4 P(node) =0.04285714
##
       class counts:
                         0
                                6
                                      9
##
      probabilities: 0.000 0.400 0.600 0.000 0.000
##
##
   Node number 34: 8 observations
##
     predicted class=5 expected loss=0.25 P(node) =0.02285714
##
       class counts:
                         0
                                6
                                      1
                                                  1
##
      probabilities: 0.000 0.750 0.125 0.000 0.125
##
## Node number 35: 58 observations,
                                        complexity param=0.01767677
##
     predicted class=6 expected loss=0.4655172 P(node) =0.1657143
##
       class counts:
                         3
                               20
                                     31
      probabilities: 0.052 0.345 0.534 0.052 0.017
##
##
     left son=70 (39 obs) right son=71 (19 obs)
##
     Primary splits:
         total sulfur dioxide < 47
                                          to the right, improve=3.011215, (0 missing)
##
##
         alcohol
                               < 9.85
                                          to the left, improve=2.359824, (0 missing)
                              < 8.5
                                          to the right, improve=1.943591, (0 missing)
##
         free_sulfur_dioxide
##
         citric acid
                               < 0.48
                                          to the right, improve=1.685157, (0 missing)
         sulphates
                               < 0.72
                                          to the right, improve=1.605187, (0 missing)
##
##
     Surrogate splits:
                                         to the right, agree=0.828, adj=0.474, (0 split)
##
         free sulfur dioxide < 11
                                         to the left, agree=0.793, adj=0.368, (0 split)
         chlorides
##
                              < 0.0715
                              < 2.3
                                         to the right, agree=0.776, adj=0.316, (0 split)
##
         residual sugar
         volatile_acidity
                                         to the left, agree=0.759, adj=0.263, (0 split)
##
                              < 0.525
                                                       agree=0.759, adj=0.263, (0 split)
##
         type
                              splits as
                                         LR,
##
   Node number 36: 15 observations
##
##
     predicted class=5 expected loss=0.4 P(node) =0.04285714
##
       class counts:
                         1
                                9
                                      4
                                                  1
      probabilities: 0.067 0.600 0.267 0.000 0.067
##
##
## Node number 37: 22 observations
##
     predicted class=6 expected loss=0.5 P(node) =0.06285714
##
       class counts:
                         1
                                3
                                     11
##
      probabilities: 0.045 0.136 0.500 0.227 0.091
```

```
##
## Node number 52: 43 observations,
                                        complexity param=0.02272727
##
     predicted class=7 expected loss=0.5581395 P(node) =0.1228571
##
       class counts:
                         2
                                5
                                           19
                                     16
##
      probabilities: 0.047 0.116 0.372 0.442 0.023
     left son=104 (16 obs) right son=105 (27 obs)
##
##
     Primary splits:
##
         total sulfur dioxide < 150.5
                                          to the right, improve=2.620155, (0 missing)
##
         fixed acidity
                               < 5.95
                                          to the left, improve=1.924917, (0 missing)
##
         density
                               < 0.99217
                                          to the right, improve=1.820155, (0 missing)
##
         alcohol
                               < 11.05
                                          to the right, improve=1.820155, (0 missing)
##
                               < 3.135
                                          to the right, improve=1.765610, (0 missing)
         рН
     Surrogate splits:
##
##
         fixed acidity
                              < 7.05
                                         to the right, agree=0.721, adj=0.25, (0 split)
##
         volatile_acidity
                              < 0.42
                                         to the right, agree=0.721, adj=0.25, (0 split)
                              < 10.75
                                         to the right, agree=0.721, adj=0.25, (0 split)
##
         residual sugar
##
         chlorides
                              < 0.049
                                         to the right, agree=0.721, adj=0.25, (0 split)
                                         to the right, agree=0.721, adj=0.25, (0 split)
##
         free_sulfur_dioxide < 36.5</pre>
##
   Node number 53: 27 observations,
                                        complexity param=0.01010101
##
     predicted class=6 expected loss=0.2962963 P(node) =0.07714286
##
##
       class counts:
                          0
                                     19
                                            6
##
      probabilities: 0.000 0.000 0.704 0.222 0.074
##
     left son=106 (18 obs) right son=107 (9 obs)
     Primary splits:
##
                               < 12.84667 to the left,
                                                        improve=3.370370, (0 missing)
##
         alcohol
         free sulfur dioxide < 37.5
##
                                          to the left,
                                                        improve=1.919577, (0 missing)
                               < 0.98916
                                          to the right, improve=1.411306, (0 missing)
##
                                          to the right, improve=1.348148, (0 missing)
##
         total sulfur dioxide < 108
##
         residual sugar
                               < 1.45
                                          to the left, improve=1.038258, (0 missing)
##
     Surrogate splits:
                                         to the left, agree=0.815, adj=0.444, (0 split)
##
         volatile acidity
                             < 0.36
                              < 0.98916 to the right, agree=0.815, adj=0.444, (0 split)
##
         density
         fixed acidity
                              < 5.55
                                         to the right, agree=0.778, adj=0.333, (0 split)
##
##
         residual sugar
                              < 2.7
                                         to the left, agree=0.778, adj=0.333, (0 split)
         free_sulfur_dioxide < 37.5</pre>
                                         to the left, agree=0.778, adj=0.333, (0 split)
##
##
   Node number 70: 39 observations,
                                        complexity param=0.01767677
##
     predicted class=5 expected loss=0.5641026 P(node) =0.1114286
##
       class counts:
                         3
##
                               17
                                     16
                                            3
##
      probabilities: 0.077 0.436 0.410 0.077 0.000
     left son=140 (20 obs) right son=141 (19 obs)
##
##
     Primary splits:
                                          to the right, improve=2.653576, (0 missing)
##
         sulphates
                               < 0.635
##
         free_sulfur_dioxide < 24.5</pre>
                                          to the left,
                                                        improve=2.289817, (0 missing)
##
         chlorides
                               < 0.0705
                                          to the right, improve=2.289817, (0 missing)
##
         total sulfur dioxide < 140.5
                                          to the left,
                                                        improve=1.880769, (0 missing)
##
         residual sugar
                               < 5.55
                                          to the left,
                                                        improve=1.788701, (0 missing)
##
     Surrogate splits:
##
         citric acid
                              < 0.33
                                         to the right, agree=0.718, adj=0.421, (0 split)
##
         chlorides
                                         to the right, agree=0.692, adj=0.368, (0 split)
                              < 0.043
##
         рН
                              < 3.355
                                         to the left, agree=0.641, adj=0.263, (0 split)
```

```
##
                        < 7.05
                                        to the right, agree=0.615, adj=0.211, (0 split)
         fixed acidity
##
         free sulfur dioxide < 21
                                        to the left, agree=0.615, adj=0.211, (0 split)
##
## Node number 71: 19 observations
##
     predicted class=6 expected loss=0.2105263 P(node) =0.05428571
##
       class counts:
                         0
                               3
                                    15
##
      probabilities: 0.000 0.158 0.789 0.000 0.053
##
## Node number 104: 16 observations
##
     predicted class=6 expected loss=0.4375 P(node) =0.04571429
##
       class counts:
                         1
                               2
                                     9
                                           3
                                                 1
##
      probabilities: 0.062 0.125 0.562 0.188 0.062
##
## Node number 105: 27 observations
##
     predicted class=7 expected loss=0.4074074 P(node) =0.07714286
##
       class counts:
                         1
                               3
                                     7
                                          16
##
      probabilities: 0.037 0.111 0.259 0.593 0.000
##
## Node number 106: 18 observations
##
     predicted class=6 expected loss=0.1111111 P(node) =0.05142857
##
       class counts:
                         0
                               0
                                    16
                                           1
      probabilities: 0.000 0.000 0.889 0.056 0.056
##
##
## Node number 107: 9 observations
     predicted class=7 expected loss=0.4444444 P(node) =0.02571429
##
##
       class counts:
                         0
                               0
                                     3
                                                 1
      probabilities: 0.000 0.000 0.333 0.556 0.111
##
##
## Node number 140: 20 observations
##
     predicted class=5 expected loss=0.35 P(node) =0.05714286
##
       class counts:
                         1
                              13
                                     6
      probabilities: 0.050 0.650 0.300 0.000 0.000
##
##
## Node number 141: 19 observations
##
     predicted class=6 expected loss=0.4736842 P(node) =0.05428571
##
       class counts:
                         2
                               4
                                    10
                                           3
##
      probabilities: 0.105 0.211 0.526 0.158 0.000
```

```
pfit<- prune(fit, cp=fit$cptable[which.min(fit$cptable[,"xerror"]),"CP"])
#b
prp(pfit,main = "Pruned Classification Tree for Wine Qualities")</pre>
```

### **Pruned Classification Tree for Wine Qualities**



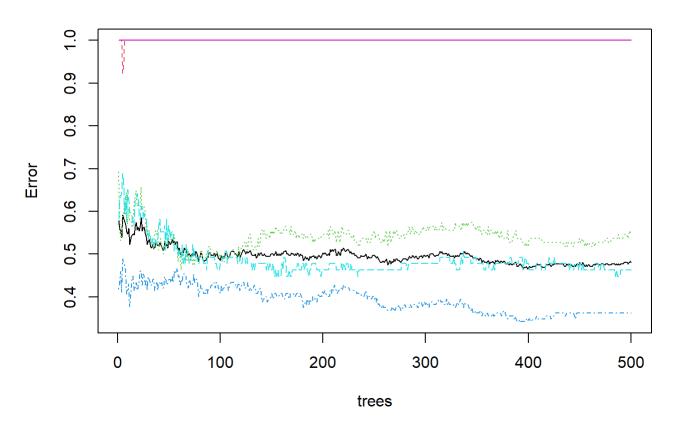
#The predicted the wine quality would be a 6
#c
library(randomForest)

## randomForest 4.7-1.1

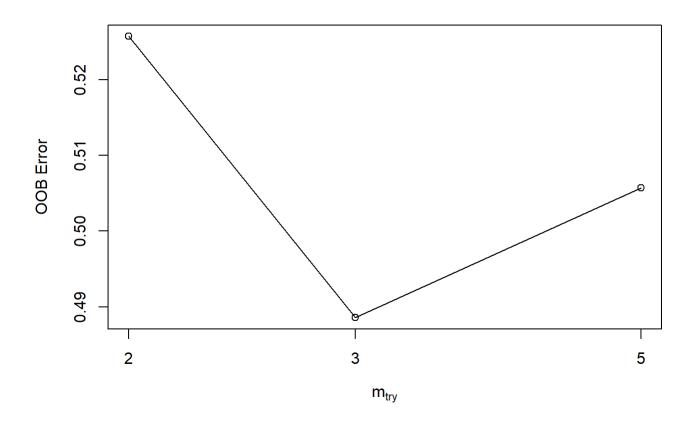
## Type rfNews() to see new features/changes/bug fixes.

set.seed(478)
wine\$quality=as.factor(wine\$quality)
x = randomForest(quality~., data=wine)
plot(x)

X



```
## mtry = 3 00B error = 48.86%
## Searching left ...
## mtry = 5 00B error = 50.57%
## -0.03508772 1
## Searching right ...
## mtry = 2 00B error = 52.57%
## -0.07602339 1
```



```
x1 = randomForest(quality~., ntree=300,mtry=3,nodesize=2, data=wine)
print(x1)
```

```
##
## Call:
   ##
              Type of random forest: classification
##
##
                  Number of trees: 300
## No. of variables tried at each split: 3
##
##
        OOB estimate of error rate: 50%
## Confusion matrix:
   4 5 6 7 8 class.error
##
               1.0000000
## 4 0 7 7 0 0
## 5 0 51 51 6 0
               0.5277778
## 6 0 42 91 19 0
               0.4013158
## 7 0 4 30 33 0
               0.5074627
## 8 0 4 4 1 0
               1.0000000
```

```
x2 = randomForest(quality~., ntree=300,mtry=2,nodesize=2,data=wine)
print(x2)
```

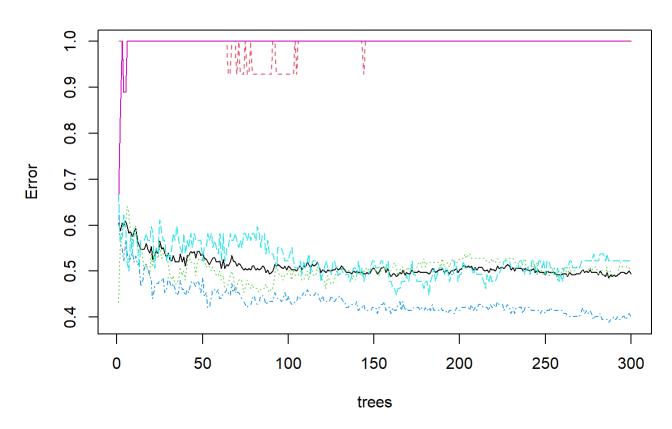
```
##
## Call:
   randomForest(formula = quality ~ ., data = wine, ntree = 300,
                                                                     mtry = 2, nodesize = 2)
##
                 Type of random forest: classification
                       Number of trees: 300
##
## No. of variables tried at each split: 2
##
##
          OOB estimate of error rate: 50.29%
## Confusion matrix:
##
     4 5 6 7 8 class.error
## 4 0 7 6 1 0
                   1.0000000
## 5 0 49 55 4 0
                   0.5462963
## 6 0 38 93 21 0
                   0.3881579
## 7 0 4 31 32 0
                   0.5223881
## 8 0 4 3 2 0
                   1.0000000
```

```
x3 = randomForest(quality~., ntree=300,mtry=5,data=wine)
print(x3)
```

```
##
## Call:
   randomForest(formula = quality ~ ., data = wine, ntree = 300,
##
                                                                      mtry = 5
##
                  Type of random forest: classification
##
                        Number of trees: 300
## No. of variables tried at each split: 5
##
           OOB estimate of error rate: 49.43%
##
## Confusion matrix:
       5 6 7 8 class.error
##
## 4 0 7 7 0 0
                   1.0000000
## 5 0 54 48 6 0
                   0.5000000
## 6 0 36 91 25 0
                   0.4013158
## 7 0 3 32 32 0
                   0.5223881
## 8 0 4 4 1 0
                   1.0000000
```

```
plot(x3)
```

**x3** 



```
## 1
## 5
## Levels: 4 5 6 7 8
```

```
#E
printcp(pfit)
```

```
##
## Classification tree:
## rpart(formula = quality ~ ., data = wine, method = "class")
##
## Variables actually used in tree construction:
## [1] alcohol
                            chlorides
                                                 density
## [4] sulphates
                            total_sulfur_dioxide volatile_acidity
##
## Root node error: 198/350 = 0.56571
##
## n= 350
##
##
           CP nsplit rel error xerror
                                           xstd
## 1 0.043771
                   0
                       1.00000 1.00000 0.046833
## 2 0.037037
                       0.86869 1.06566 0.046233
## 3 0.030303
                   6
                       0.75758 0.97475 0.046993
## 4 0.025253
                   7 0.72727 0.94949 0.047113
## 5 0.022727
                   8
                       0.70202 0.92929 0.047181
## 6 0.017677
                  10
                       0.65657 0.90909 0.047224
## 7 0.015152
                  12
                       0.62121 0.90404 0.047231
```

```
print(x3)
```

```
##
## Call:
   randomForest(formula = quality ~ ., data = wine, ntree = 300,
                                                                      mtry = 5
                 Type of random forest: classification
##
##
                       Number of trees: 300
## No. of variables tried at each split: 5
##
          OOB estimate of error rate: 49.43%
##
## Confusion matrix:
    4 5 6 7 8 class.error
## 4 0 7 7 0 0
                   1.0000000
## 5 0 54 48 6 0
                   0.5000000
## 6 0 36 91 25 0
                   0.4013158
## 7 0 3 32 32 0
                   0.5223881
## 8 0 4 4 1 0
                   1.0000000
```

```
#The classification tree predicted 6 while the random forest predicted 5. The error rate for
# the CT was about 56.5% while, RF was about 48%

bikes = read.csv("C:/Users/dgmur/Downloads/SeoulBikes_Fl2022.csv")

dim(bikes)
```

```
## [1] 730 16
```

```
730 obs. of 13 variables:
## 'data.frame':
## $ RentedBikeCount: int 930 219 85 937 812 802 754 780 222 35 ...
  $ Temperature
                  : num -7.6 -4.2 3.2 -0.8 -8.1 -4.2 -0.2 -7 -5.4 -0.2 ...
##
   $ Humidity
                  : int 37 79 92 69 36 78 96 59 56 90 ...
  $ WindSpeed
                  : num 1.1 2.1 1.8 3.5 1.6 0 0.8 0.8 0.7 1.2 ...
##
  $ Visibility
                  : int 2000 1436 244 954 2000 1518 173 1559 1940 378 ...
##
                       -19.8 -7.3 2 -5.7 -20.5 -7.4 -0.7 -13.6 -12.8 -1.6 ...
##
   $ DewPointTemp
                  : num
  ##
  $ Rainfall
                  : num 0000000000...
##
  $ Snowfall
##
                  : num
                       0 0 0 0 0 0.2 0.8 0 0 4.1 ...
                        "Winter" "Winter" "Winter" ...
##
  $ Seasons
                  : chr
                        "No Holiday" "No Holiday" "No Holiday" ...
##
   $ Holiday
                  : chr
                        "Yes" "Yes" "Yes" "Yes" ...
##
   $ Functioning.Day: chr
                        "Morning" "Morning" "Morning" ...
   $ Time
                  : chr
##
```

```
bikes$Seasons= as.factor(bikes$Seasons)

bikes$Holiday= as.factor(bikes$Holiday)

bikes$Functioning.Day=as.factor(bikes$Functioning.Day)

bikes$Time=as.factor(bikes$Time)

#a

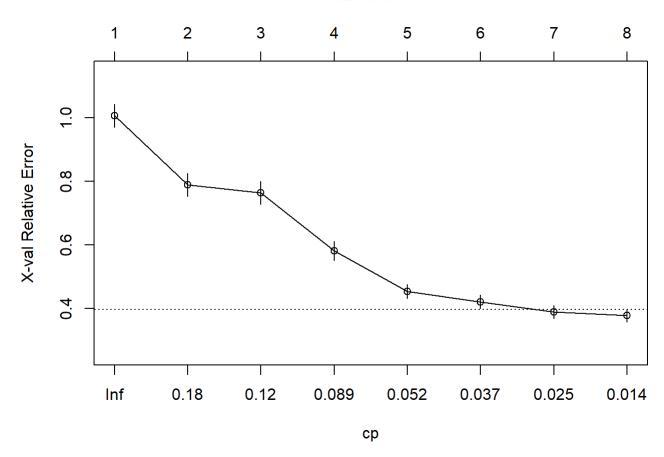
fit2= rpart(RentedBikeCount~., method = "anova", data=bikes)

printcp(fit2)
```

```
##
## Regression tree:
## rpart(formula = RentedBikeCount ~ ., data = bikes, method = "anova")
##
## Variables actually used in tree construction:
## [1] Functioning.Day Humidity
                                                       SolarRadiation
                                       Seasons
## [5] Temperature
##
## Root node error: 640097003/730 = 876845
##
## n= 730
##
##
           CP nsplit rel error xerror
                                           xstd
## 1 0.269598
                       1.00000 1.00621 0.036343
## 2 0.116823
                   1
                       0.73040 0.78870 0.036018
## 3 0.114820
                   2
                      0.61358 0.76427 0.036189
## 4 0.068987
                   3
                     0.49876 0.58097 0.030018
## 5 0.039809
                   4
                       0.42977 0.45350 0.022044
## 6 0.034160
                   5
                       0.38996 0.42065 0.020941
## 7 0.018238
                       0.35580 0.38881 0.020175
                   6
## 8 0.010000
                   7
                       0.33756 0.37699 0.019396
```

```
plotcp(fit2)
```





summary(fit2)

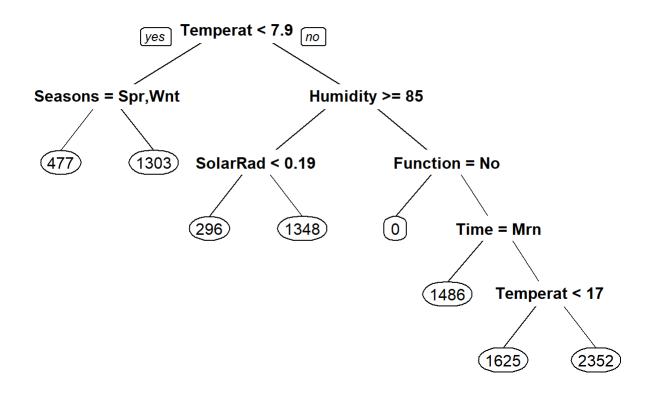
```
## Call:
## rpart(formula = RentedBikeCount ~ ., data = bikes, method = "anova")
##
##
##
             CP nsplit rel error
                                                  xstd
                                     xerror
## 1 0.26959787
                     0 1.0000000 1.0062097 0.03634349
## 2 0.11682322
                     1 0.7304021 0.7887003 0.03601774
## 3 0.11481981
                     2 0.6135789 0.7642709 0.03618950
## 4 0.06898737
                     3 0.4987591 0.5809696 0.03001769
## 5 0.03980925
                     4 0.4297717 0.4534989 0.02204431
## 6 0.03415988
                     5 0.3899625 0.4206475 0.02094054
## 7 0.01823837
                     6 0.3558026 0.3888055 0.02017526
## 8 0.01000000
                     7 0.3375642 0.3769880 0.01939600
##
## Variable importance
##
       Temperature
                                                     SolarRadiation
                            Seasons
                                       DewPointTemp
                                                                            Humidity
##
                22
                                 16
                                                 15
                                                                  12
                                                                                  11
   Functioning.Day
                               Time
                                           Rainfall
                                                            Snowfall
                                                                           WindSpeed
##
##
                                  5
                                                  4
                                                                   3
                                                                                    3
                 8
##
        Visibility
##
                 2
##
   Node number 1: 730 observations,
##
                                        complexity param=0.2695979
     mean=1259.314, MSE=876845.2
##
##
     left son=2 (266 obs) right son=3 (464 obs)
##
     Primary splits:
##
         Temperature
                         < 7.85
                                  to the left,
                                                improve=0.26959790, (0 missing)
##
         Seasons
                        splits as RRRL,
                                                improve=0.25654450, (0 missing)
                                                improve=0.25609000, (0 missing)
##
         SolarRadiation < 0.205
                                 to the left,
##
         DewPointTemp
                        < -2.25
                                 to the left,
                                                improve=0.17980060, (0 missing)
##
         Humidity
                         < 84.5
                                  to the right, improve=0.09142905, (0 missing)
##
     Surrogate splits:
##
         DewPointTemp
                        < 2.75
                                  to the left,
                                                agree=0.892, adj=0.703, (0 split)
##
         Seasons
                        splits as RRRL,
                                                agree=0.882, adj=0.677, (0 split)
                                                agree=0.818, adj=0.500, (0 split)
##
         SolarRadiation < 0.075
                                 to the left,
##
         Snowfall
                         < 0.1
                                  to the right, agree=0.688, adj=0.143, (0 split)
##
         Humidity
                        < 34.5
                                  to the left,
                                                agree=0.653, adj=0.049, (0 split)
##
   Node number 2: 266 observations,
##
                                        complexity param=0.03980925
     mean=617.1617, MSE=239589
##
##
     left son=4 (221 obs) right son=5 (45 obs)
##
     Primary splits:
##
         Seasons
                        splits as RL-L,
                                                improve=0.39983550, (0 missing)
##
         Temperature
                        < 3.25
                                  to the left,
                                                improve=0.14399360, (0 missing)
##
         DewPointTemp
                        < -10.25 to the left,
                                                improve=0.07283931, (0 missing)
         SolarRadiation < 0.115 to the left,
                                                improve=0.07059487, (0 missing)
##
##
         Holiday
                        splits as
                                   LR,
                                                improve=0.05290116, (0 missing)
##
     Surrogate splits:
##
         Temperature
                                   to the left,
                                                 agree=0.842, adj=0.067, (0 split)
                          < 6.75
                                                 agree=0.835, adj=0.022, (0 split)
##
         Functioning.Day splits as
                                    RL,
##
## Node number 3: 464 observations,
                                        complexity param=0.1168232
```

```
mean=1627.444, MSE=870253.3
##
##
     left son=6 (57 obs) right son=7 (407 obs)
##
     Primary splits:
##
         Humidity
                                   to the right, improve=0.1851873, (0 missing)
                         < 84.5
                                   to the right, improve=0.1700205, (0 missing)
##
         Rainfall
                         < 0.15
                                                 improve=0.1587288, (0 missing)
##
         Functioning.Day splits as
##
                         splits as RL,
                                                 improve=0.1203948, (0 missing)
##
         SolarRadiation < 0.155 to the left, improve=0.1168390, (0 missing)
##
     Surrogate splits:
##
         Rainfall
                      < 0.4
                               to the right, agree=0.933, adj=0.456, (0 split)
##
         Visibility
                      < 283.5 to the left, agree=0.897, adj=0.158, (0 split)
##
         DewPointTemp < 25.45 to the right, agree=0.884, adj=0.053, (0 split)
         WindSpeed
                      < 0.1
                               to the left, agree=0.881, adj=0.035, (0 split)
##
##
##
   Node number 4: 221 observations
     mean=477.4977, MSE=91569.86
##
##
##
   Node number 5: 45 observations
##
     mean=1303.067, MSE=400265.6
##
## Node number 6: 57 observations,
                                       complexity param=0.01823837
     mean=554.7193, MSE=395396.7
##
##
     left son=12 (43 obs) right son=13 (14 obs)
##
     Primary splits:
         SolarRadiation < 0.185 to the left, improve=0.51799300, (0 missing)
##
##
         Rainfall
                        < 0.75
                                 to the right, improve=0.30090910, (0 missing)
                        < 90.5
                                 to the right, improve=0.14186150, (0 missing)
         Humidity
##
                                 to the left, improve=0.07291409, (0 missing)
##
         Temperature
                        < 19.3
         DewPointTemp
                        < 18.55 to the left, improve=0.07291409, (0 missing)
##
##
     Surrogate splits:
##
         Temperature < 24.5
                               to the left, agree=0.825, adj=0.286, (0 split)
         DewPointTemp < 23.8</pre>
                               to the left,
                                              agree=0.807, adj=0.214, (0 split)
##
##
   Node number 7: 407 observations,
##
                                        complexity param=0.1148198
##
     mean=1777.678, MSE=753026.4
     left son=14 (22 obs) right son=15 (385 obs)
##
##
     Primary splits:
##
         Functioning.Day splits as LR,
                                                 improve=0.23980490, (0 missing)
                                                 improve=0.14092870, (0 missing)
         Time
                         splits as RL,
##
                         < 20.45 to the left, improve=0.11122760, (0 missing)
##
         Temperature
##
         WindSpeed
                         < 2.25
                                   to the left,
                                                 improve=0.07788779, (0 missing)
                         < 57.5
                                  to the right, improve=0.06370545, (0 missing)
##
         Humidity
##
   Node number 12: 43 observations
##
##
     mean=296.4884, MSE=99407.6
##
   Node number 13: 14 observations
##
##
     mean=1347.857, MSE=470625.8
##
## Node number 14: 22 observations
##
     mean=0, MSE=0
##
```

```
## Node number 15: 385 observations,
                                        complexity param=0.06898737
##
     mean=1879.26, MSE=605158.2
##
     left son=30 (164 obs) right son=31 (221 obs)
##
     Primary splits:
##
         Time
                                             improve=0.18953340, (0 missing)
                     splits as RL,
##
         WindSpeed
                     < 1.35
                              to the left,
                                            improve=0.10008420, (0 missing)
##
         Temperature < 17.05 to the left,
                                            improve=0.08926161, (0 missing)
##
         Humidity
                     < 57.5
                              to the right, improve=0.06494347, (0 missing)
##
         Rainfall
                     < 0.05
                              to the right, improve=0.04771395, (0 missing)
##
     Surrogate splits:
##
         WindSpeed
                     < 1.25
                              to the left, agree=0.769, adj=0.457, (0 split)
         Humidity
##
                     < 57.5
                              to the right, agree=0.735, adj=0.378, (0 split)
##
         Visibility < 1064
                              to the left, agree=0.631, adj=0.134, (0 split)
##
         Temperature < 13.85 to the left, agree=0.590, adj=0.037, (0 split)
##
         Rainfall
                     < 0.05
                              to the right, agree=0.577, adj=0.006, (0 split)
##
## Node number 30: 164 observations
     mean=1486.116, MSE=463720.8
##
##
## Node number 31: 221 observations,
                                        complexity param=0.03415988
     mean=2171.005, MSE=510303.6
##
     left son=62 (55 obs) right son=63 (166 obs)
##
##
     Primary splits:
##
         Temperature
                        < 16.55 to the left,
                                               improve=0.19388370, (0 missing)
         DewPointTemp
                        < 0.4
                                 to the left,
                                                improve=0.09247077, (0 missing)
##
##
         SolarRadiation < 0.685 to the left,
                                                improve=0.08959975, (0 missing)
                        < 72.5
                                 to the right, improve=0.08502754, (0 missing)
##
         Humidity
         Visibility
                        < 642.5 to the left,
                                                improve=0.04144956, (0 missing)
##
##
     Surrogate splits:
##
         SolarRadiation < 0.075 to the left, agree=0.860, adj=0.436, (0 split)
##
         DewPointTemp
                        < 2.85
                                 to the left, agree=0.855, adj=0.418, (0 split)
                        < 505.5 to the left, agree=0.769, adj=0.073, (0 split)
##
         Visibility
##
## Node number 62: 55 observations
     mean=1624.545, MSE=444930.4
##
##
## Node number 63: 166 observations
##
     mean=2352.06, MSE=400242.7
```

```
pfit2<- prune(fit2, cp=fit$cptable[which.min(fit$cptable[,"xerror"]),"CP"])
#b
prp(pfit2,main = "Pruned Classification Tree for Rented Bike Count")</pre>
```

## **Pruned Classification Tree for Rented Bike Count**

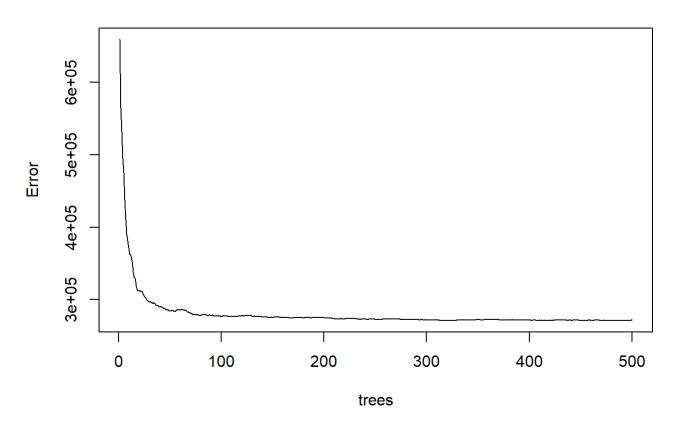


#tree predicted 1486

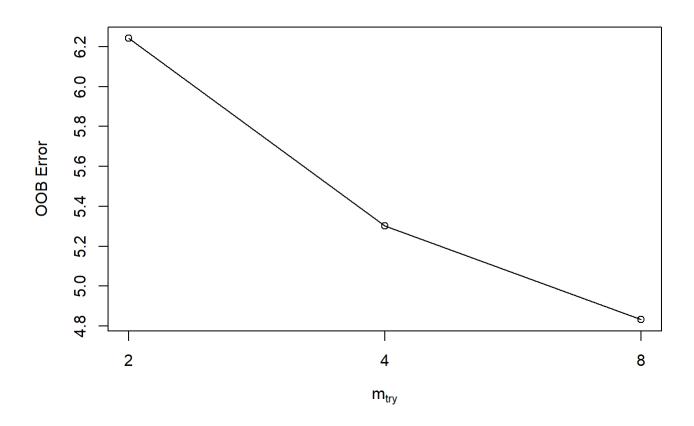
#c
set.seed(55)

z = randomForest(RentedBikeCount~., data=bikes)
plot(z)

Z



```
## mtry = 4 00B error = 5.302175
## Searching left ...
## mtry = 8 00B error = 4.832046
## 0.0886673 1
## Searching right ...
## mtry = 2 00B error = 6.241474
## -0.1771534 1
```



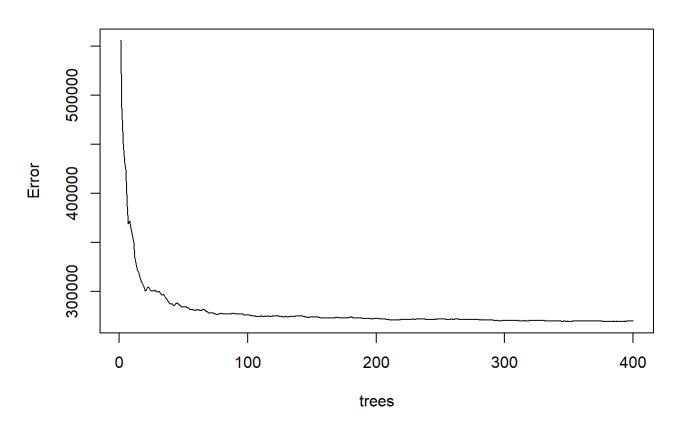
```
z1 = randomForest(RentedBikeCount~., ntree=400,mtry=8,nodesize=2, data=bikes)
print(z1)
```

```
z2 = randomForest(RentedBikeCount~., ntree=400,mtry=8,nodesize=1, data=bikes)
print(z2)
```

```
z3 = randomForest(RentedBikeCount~., ntree=400,mtry=8,nodesize=5, data=bikes)
print(z3)
```

```
#I selected z2
plot(z2)
```

**z2** 



```
#d
zp=predict(z1, x.new, interval="predict", level=0.95)
zp
```

```
## 1
## 1192.925
```

```
#RF predicted 1147.564
#E
printcp(pfit2)
```

```
##
## Regression tree:
## rpart(formula = RentedBikeCount ~ ., data = bikes, method = "anova")
##
## Variables actually used in tree construction:
## [1] Functioning.Day Humidity
                                      Seasons
                                                      SolarRadiation
## [5] Temperature
                      Time
##
## Root node error: 640097003/730 = 876845
##
## n= 730
##
##
           CP nsplit rel error xerror
                                          xstd
## 1 0.269598
                      1.00000 1.00621 0.036343
## 2 0.116823
                  1
                     0.73040 0.78870 0.036018
## 3 0.114820
                  2 0.61358 0.76427 0.036189
## 4 0.068987
                  3 0.49876 0.58097 0.030018
## 5 0.039809
                  4 0.42977 0.45350 0.022044
## 6 0.034160
                  5 0.38996 0.42065 0.020941
## 7 0.018238
                  6 0.35580 0.38881 0.020175
## 8 0.010000
                  7
                      0.33756 0.37699 0.019396
```

```
print(z2)
```

 $\#The\ regression\ tree\ had\ a\ rootnode\ error\ rate\ of\ 100\%\ and\ rf\ had\ a\ 69\%\ variance\ explained$  zp

```
## 1
## 1192.925
```

```
# regression tree predicted 1486 while rf was 1147.564
```