# Diversification in the Managed Futures Universe

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## ${\bf Contents}$

Abstract	2
Introduction and Motivation	3
Portfolio Return & Its Variability	3
Portfolio Return	3
Portfolio Return Variability	4
Portfolio Return Confidence Intervals:	4
Too Many Moving Parts	5
Data	6
Raw Data Extraction, Transformation, and Loading (ETL)	6
Data Exploration	15
Data Cleaning	20
Modeling	24
Theory	24
Principal Component Analysis (PCA)	25
Portfolio Factor Sensitivities and Coherent Scenario Analysis	26
Application	28
Data Preprocessing	29
Statistical Factor Analysis	30
Conclusions	35
References	36
Appendix A: GitHub Repository	37
Apprendix B: Fundamental Laws of Investing	38
Importance of Capital Preservation	38

## Abstract

In this paper, we focus on the application of a statistical factor model to a subset of the universe of managed futures investment programs. Our objective is to model the relationships between the returns of a select set of these investment programs and to produce a simple sensitivity providing a map of the return variability of a portfolio to changes in the diversity of the portfolio components as represented by the *importance* of a few factors. The paper is composed of four main sections encompassing the entire data science workflow.

- Section 1: Introduction and Motivation
- Section 2: Data
  - Raw Data Extraction, Transformation, and Loading (ETL)
  - Data Exploration
  - Data Cleaning
- Section 3: Modeling
  - Theory
  - Application
- Section 4: Conclusions

#### Introduction and Motivation

In portfolio allocation applications the objective is to maximize investors' future wealth by determining how to allocate capital among a set of available investments in such a way as to maximize *compound* growth subject to a set of constraints. Maximizing wealth requires that we take advantage of the powerful positive effects of compounding. When we reinvest, the magnitude of investment returns and the variability of those returns make *equal* contributions to compounded total return. Reducing the variability of returns thus has as much impact on total return as the magnitude of returns. The variability of portfolio return is a function of the co-variability of investment component returns. If the component returns tend to move together, the magnitude of fluctuations in the monthly value of the portfolio is higher than if the components move in different directions. A portfolio comprised of components with diversified returns will achieve higher compound growth than a portfolio with less diversified components (holding average component returns constant). In the simplest terms, portfolio allocation is primarily about selecting sets of investments with *future* positive average returns and low co-variability.

As the size of a portfolio increases, the number of inter-relationships between components explodes. It becomes increasingly difficult to understand the drivers of portfolio return as the number of components rises because the number of independent parameters in a covariance matrix grows with the square of the number of investments. Grouping investments that tend to move together and focusing on trying to find groups that are independent is one common way to reduce the dimension of the portfolio allocation problem. This can be accomplished through the use of statistical factor models.

### Portfolio Return & Its Variability

In this section, we introduce definitions for portfolio return and variability that will be used throughout the paper.

#### Portfolio Return

Portfolio return  $r_{P,m}$  is a function of the weights and the returns of portfolio investment components. We define the portfolio return for I component investments for the month m given the monthly returns  $r_{i,m}$  and portfolio weights  $w_{i,m}$  for each component investment i as:

$$r_{P,m} = \sum_{i=1}^{I} (r_{i,m} w_{i,m})$$

Letting  $W_m$  be a vector of portfolio component weights for month m, T denote the transpose operator, and  $R_m$  be a vector of the month m component returns, we can use matrix notation to define the portfolio return as follows:

$$r_{P,m} = W^T R$$

The holdig period return (HPR) for the portfolio is one plus the portfolio return for the month m:

$$HPR_{P,m} = 1 + \sum_{i=1}^{I} (r_{i,m}w_{i,m}) = 1 + r_{P,m}$$

The holding period return is the factor by which we mulitply the starting value of the portfolio to get the ending value of a portfolio, given the monthly returns and weights of each component investment.

Similarly, we define the terminal wealth relative (TWR) as the factor by which we multiply the starting value of the portfolio to get the ending value of the portfolio given the return streams and weights for a sequence of months between one to M:

$$TWR_{P,M} = \prod_{1=m}^{M} \left( 1 + \left( \sum_{i=1}^{I} (r_{i,m} w_{i,m}) \right) \right) = \prod_{1=m}^{M} HPR_{P,m}$$

We define the portfolio compounded return for the interval from months one to M as the portfolio terminal wealth relative minus one:

$$r_{P,M} = \left(\prod_{1=m}^{M} \left(1 + \left(\sum_{i=1}^{I} \left(r_{i,m} w_{i,m}\right)\right)\right)\right) - 1 = \left(\prod_{1=m}^{M} \left(1 + r_{P,m}\right)\right) - 1 = \left(\prod_{1=m}^{M} HPR_{P,m}\right) - 1 = TWR_{P,M} - 1$$

#### Portfolio Return Variability

Assuming that component returns are normally distributed, and thus that portfolio returns are multivariate normally distributed, we can define the standard deviation of the portfolio returns using matrix notation as:

$$\sigma_{P,M} = \sqrt{Var\left(W_m^T R_m\right)} = \sqrt{W_m^T \Sigma W_m}$$

Where  $W_m$  is a vector of portfolio component weights for month m, T denotes the transpose operator,  $R_m$  is a vector of the month m component returns, and  $\Sigma$  is the return covariance matrix.

```
portfolioVolatility <- function (W,COV){
  portfolioStandardDeviation = sqrt( t(W)%*%COV%*%W )
}</pre>
```

#### Portfolio Return Confidence Intervals:

Using our definition of portfolio return variability we can define the expected negative fluctuation (i.e., loss) at a given confidence interval as:

$$VaR = -\alpha_{CL}\sigma_{P,M}$$

Where

 $\alpha_{CL}$  is the critical value at the confidence level CL

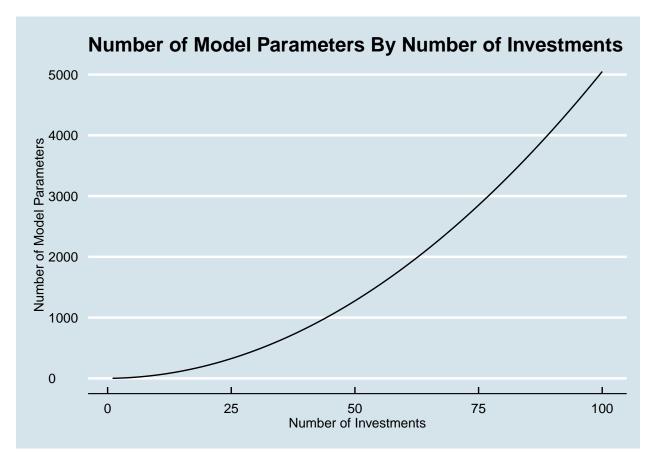
 $\sigma_{P,M}$  is the standard deviation of the portfolio returns over the time interval  $m=1,\ldots,M$ 

This simple parameteric model can be extended in a myriad of ways to account for the established stylized facts pertaining to the statistical characteristics of investment returns. In particular, our factor-based model can be combined with any choice for the marginal distribution of component returns, copulas can be used to include more extreme returns in the joint distribution of returns, and returns can be standardized with forecasts of the time-varying moments about the distribution. In this paper, we use on the simplest possible model for the expected return distribution so that we may focus specifically on the factor model.

## Too Many Moving Parts

The number of independent parameters P in a covariance matrix grows with the number of investments I according to the following function:

$$P = \frac{I\left(I+1\right)}{2}$$



The number of independent parameters to be estimated in the covariance matrix grows with the square of the number of investments, while the number of data points available to estimate a covariance matrix grows only linearly with the number of investments. In other words, the larger the portfolio, the more historical data we typically need to estimate the covariance matrix reliably. This is particularly problematic when our interest is in the temporal evolution of the relationships between investments in the portfolio.

In this paper, we extract the manager, program, and monthly return data for the subset of the managed futures investment universe tracked on the Altergris website. We conduct some limited exploratory data analysis and clean the data to be used in our modeling. We create a statistical factor model using principal component analysis (PCA), then use our statistical factor model to group and interpret the relationships between available programs in the managed futures investment universe. Finally, we compute sensitivities linking the portfolio volatility of a hypothetical set of managed futures investments to changes in the importance of different factors. The sensitivities provide a powerful analytical framework to be used to understand portfolio return variation in terms of a few independent factors.

## Data

In this section we provide detailed information about the acquisition of the data for this paper. A brief overview of the available data is provided below. It is important to note that much of the data collected was ultimately not cleaned and used in our modeling. Data in the database has not been normalized as this application is not transaction-oriented and storage has been set up for a one-time analysis.

Although return data quality appears high, the quality of data pertaining to manager and program information is much lower. This data set will likely be cleaned and used for future research projects. The entire system for collecting and storing the data is included below.

### Raw Data Extraction, Transformation, and Loading (ETL)

We exact the raw manager, program, and monthly return data to pipe-delimited flat files using some custom R functions made considerably simpler through the use of the 'rvest' and 'lubridate' packages.

for each managed futures program on the Altergis website we extract the following types of information:

- CTA Name

```
extractCtaName<-function (programHtmlSession){
    # extract the CTA name
    ctaName <- programHtmlSession %>% html() %>%
        html_nodes("#spnHeadingPP1") %>% html_text()
    # remove foreign language characters
    ctaName
}
```

– Program Name

```
extractProgramName<-function (programHtmlSession){
    # extract the program name
    programName <- programHtmlSession %>% html() %>%
        html_nodes("#spnHeadingPP2") %>% html_text()
    # remove foreign language characters
    programName
}
```

- Monthly Returns

```
extractMonthlyReturns<-function (programHtmlSession,programId){
    # extract CTA Name
    ctaName<-extractCtaName(programHtmlSession)
    # extract the program name
    programName<-extractProgramName(programHtmlSession)
    # extract the monthly returns
    a<-html_table(html_nodes(programHtmlSession, "table")[[1]],fill=TRUE)
    # extract the years
    YYYY<-as.numeric(a$X1[3:(length(a$X1)-1)])
    # find the number of years
    nYears<-length(YYYY)
    # create the empty end of month date matrix
    dates<-matrix(data=NA,nrow=nYears,ncol=12)</pre>
```

```
# find the last day of each month
for (yyyyIndex in seq_along(YYYY)){
  yyyy<-YYYY[yyyyIndex]</pre>
  # find the last day for the current year
  eomDates<-ceiling_date(ISOdate(yyyy,1,1,0,0,0,tz='EST') +</pre>
                             months(1:12))-days(1)
  # store the end of month dates
  dates[yyyyIndex,1:12]<-format(eomDates, '%Y-%m-%d')</pre>
}
# flatten the end of month matrix
eomDates<-matrix(dates,nrow=nYears*12,1)</pre>
# extract the returns
jan<-as.numeric(a$X2[!is.na(sub('Jan',NA,a$X2))])</pre>
feb<-as.numeric(a$X3[!is.na(sub('Feb',NA,a$X3))])</pre>
mar<-as.numeric(a$X4[!is.na(sub('Mar',NA,a$X4))])</pre>
apr<-as.numeric(a$X5[!is.na(sub('Apr',NA,a$X5))])
may<-as.numeric(a$X6[!is.na(sub('May',NA,a$X6))])</pre>
jun<-as.numeric(a$X7[!is.na(sub('Jun',NA,a$X7))])</pre>
jul<-as.numeric(a$X8[!is.na(sub('Jul',NA,a$X8))])</pre>
aug<-as.numeric(a$X9[!is.na(sub('Aug',NA,a$X9))])</pre>
sep<-as.numeric(a$X10[!is.na(sub('Sep',NA,a$X10))])</pre>
oct<-as.numeric(a$X11[!is.na(sub('Oct',NA,a$X11))])</pre>
nov<-as.numeric(a$X12[!is.na(sub('Nov',NA,a$X12))])</pre>
dec<-as.numeric(a$X13[!is.na(sub('Dec',NA,a$X13))])</pre>
# create the monthly return data frame
monthlyReturns<-cbind(ctaName,programName,yyyy,jan,feb,mar,
  apr, may, jun, jul, aug, sep, oct, nov, dec)
# create the monthly return matrix by year
monthlyReturnsMatrix<-as.matrix(cbind(jan,feb,mar,apr,
  may,jun,jul,aug,sep,oct,nov,dec))
# find the dimension of the monthly returns matrix
dimension<-dim(monthlyReturnsMatrix)</pre>
# flatten the monthly return matrix
monthlyReturnsData<-matrix(monthlyReturnsMatrix,dimension[1]*dimension[2],1)
# create the data frame
data<-data.frame(dates=eomDates,monthlyReturns=monthlyReturnsData,</pre>
  stringsAsFactors=FALSE)
# get the sort index
sortIndex<-sort(data[,1],index.return=TRUE)</pre>
# order the data
data<-data[sortIndex$ix,]
# add the CTA Name
data['ctaName']<-ctaName</pre>
# add the program name
data['programName']<-programName</pre>
# add the program ID
data['programId']<-programId</pre>
# find the NAs
naIndex<-is.na(data[,2])</pre>
# return the data
data[!naIndex,]
```

<sup>–</sup> Manager Address

```
extractAddress<-function (programHtmlSession,ctaName,programName){</pre>
  # extract the address
  address<-html_table(html_nodes(programHtmlSession,
    "table") [[10]], fill=TRUE)
  # extract the address
  addressHeader<-t(address[1])
  # remove the colons
  addressHeader<-sub(':','',addressHeader[2:7])
  addressData<-t(address[2])
  # remove new line characters
  addressData<-sub('\n','-',addressData[2:7])
  # create address data frame
  address<-data.frame(cbind(addressHeader,addressData))</pre>
  colnames(address)<-c('column', 'value')</pre>
  address['columnType']<-'address'
  address
}
```

- Investment Methodology

- Instruments Traded

- Sectors of Instruments Traded

- Geographical Focus of Instruments Traded

```
extractGeographicalFocus<-function (programHtmlSession){
    # extract the geographical focus
    geographicalFocus<-html_table(html_nodes(programHtmlSession,
        "table")[[16]])
    # extract the geographical focus
    colnames(geographicalFocus)<-c('column','value')
    geographicalFocus['columnType']<-'geographicalFocus'
    geographicalFocus
}</pre>
```

- Holding Periods (Short/Medium/Long)

```
extractHoldingPeriod<-function (programHtmlSession){
    # extract the holding period
    holdingPeriod<-html_table(html_nodes(programHtmlSession,
        "table")[[17]])
    colnames(holdingPeriod)<-c('column','value')
    holdingPeriod['columnType']<-'holdingPeriod'
    holdingPeriod
}</pre>
```

- Investment Terms and Information

We extract manager, program, and month return data for a single CTA program with a function that calls functions for each sub-type.

```
# extract program data
extractProgramInfo<-function (programHtmlSession,programId){
    # create the program session
    # extract the CTA name
    ctaName<-extractCtaName(programHtmlSession)
    # extract the program name
    programName<-extractProgramName(programHtmlSession)
    # extract the address data into a data frame
    address<-extractAddress(programHtmlSession)
    # extract the investment methodology data into a data frame
    investmentMethodology<-extractInvestmentMethodology(programHtmlSession)
    # extract the instruments data into a data frame
    instruments<-extractInstruments(programHtmlSession)
# extract the sector data into a data frame
    sectors<-extractSectors(programHtmlSession)</pre>
```

```
# extract the geographical focus data into a data frame
  geographicalFocus<-extractGeographicalFocus(programHtmlSession)</pre>
  # extract the holding period data into a data frame
  holdingPeriod<-extractHoldingPeriod(programHtmlSession)
  # extract the investment terms and info data into a data frame
  investmentTermsAndInfo<-extractInvestmentTermsAndInfo(programHtmlSession)
  # bind all of the data frames together
  programInfo<-data.frame(rbind(address,</pre>
    investmentMethodology, instruments, sectors, geographicalFocus,
    holdingPeriod, investmentTermsAndInfo), stringsAsFactors=FALSE)
  # add the program CTA name
  programInfo['ctaName']<-ctaName</pre>
  # add the program name
  programInfo['programName']<-programName</pre>
  # add the program ID
 programInfo['programId']<-programId</pre>
  # return the data
 programInfo
cleanProgramInfo<-function (programInfo){</pre>
  # clean program info
  # remove the \r \n newlines
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if (is.character(x)|is.factor(x)) gsub("\r","",x) else x),
    stringsAsFactors=FALSE)
  # remove the % signs
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub("%","",x) else x),
    stringsAsFactors=FALSE)
  # remove the commas
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub(",","",x) else x),
    stringsAsFactors=FALSE)
  # remove the colons
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub("[:]","",x) else x),
    stringsAsFactors=FALSE)
  # remove the $ sign
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub("[$]","",x) else x),
    stringsAsFactors=FALSE)
  # remove the /
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub("/","",x) else x),
    stringsAsFactors=FALSE)
  # remove the foreign characters
  programInfo <- as.data.frame(lapply(programInfo,</pre>
    function(x) if(is.character(x)|is.factor(x)) gsub("o","o",x) else x),
    stringsAsFactors=FALSE)
  # remove the foreign characters
  programInfo <- as.data.frame(lapply(programInfo,</pre>
```

```
function(x) if(is.character(x)|is.factor(x)) gsub("Ä","A",x) else x),
    stringsAsFactors=FALSE)
# remove the foreign characters
programInfo <- as.data.frame(lapply(programInfo,
    function(x) if(is.character(x)|is.factor(x)) gsub("Ö","O",x) else x),
    stringsAsFactors=FALSE)
programInfo
}</pre>
```

We write the monthly return flat file with one function.

```
# extract and write CTA monthly returns
extractAndWriteMonthlyReturns<-function (outputFileHandle1,
  programHtmlSession,programId){
  # extract the monthly returns
  monthlyReturns<-extractMonthlyReturns(programHtmlSession,programId)
  # write the monthly returns output file
  if (dim(monthlyReturns)[2]==5){
    write.table(monthlyReturns,file=outputFileHandle1,
        row.names=FALSE,col.names=FALSE,sep='|',
        quote = FALSE)
}
</pre>
```

We write the manager and program information with another function.

Finally, one single function is used to extract all of the data sub-types and write the data into two flat files to be loaded into the project database.

```
# define the function to extract the Altegris data
extractAltegrisData<-function (outputDirectory){
    # set the URL string
    urlString<-'http://managedfutures.com/program_profiles.aspx'
    # parse the URL
htmlSession <- html(urlString)
# open the output connection
outputFileHandle1<-file(paste0(outputDirectory,'ctaMonthlyReturns'), "w")
# open the output connection</pre>
```

```
outputFileHandle2<-file(paste0(outputDirectory,'programInfo'), "w")</pre>
  # set the URL
  baseURL='http://managedfutures.com/'
  # find the program URLs
  programURLs <- htmlSession %>% html() %>% html_nodes("a") %>%
    html attr("href")
  # extract the program URLs
  programURLs <- htmlSession %>% html() %>% html_nodes("div a") %>%
    html attr("href")
  # extract the program IDs
  programIDs <- htmlSession %>% html() %>% html_nodes("a") %>%
   html_attr("rel")
  # find the index
  naIndex<-(is.na(programIDs)==FALSE)</pre>
  # extract the program URLs
  programURLs<-programURLs[naIndex]</pre>
  # extract the program IDs
  programIDs<-programIDs [naIndex]</pre>
  # iterate over the programs
  for (programIndex in seq_along(programURLs)){
    # extract program ID
    programId<-programIDs[programIndex]</pre>
    # extract program URL
    programURL<-programURLs[programIndex]</pre>
    # create the full program URL
    programPerformanceURL<-pasteO(baseURL,programURL)</pre>
    # create the program session
    programHtmlSession <- html(programPerformanceURL)</pre>
    # try to get hte monthly returns
    try(extractAndWriteMonthlyReturns(outputFileHandle1,
      programHtmlSession,programId),silent=TRUE)
    # try to get the program info
    try(extractAndWriteProgramInfo(outputFileHandle2,
      programHtmlSession,programId),silent=TRUE)
  }
  # close the connection
  close(outputFileHandle1)
  # close the connection
  close(outputFileHandle2)
}
```

We create a database in MySQL to store the raw, unnormalized data.

```
# define the function to create the altegris database
createAltegrisDatabase <- function(dbHandle){
    # create the 'altegris' database

# create the query
query<-pasteO("CREATE DATABASE ",dbName)
    # execute the query
dbGetQuery(dbHandle,query)
}</pre>
```

```
# define the function to drop the altegris database
dropAltegrisDatabase <- function(dbHandle){
    # drop the 'altegris' database

# create the query
query<-paste0("DROP DATABASE ",dbName)
# execute the query
dbGetQuery(dbHandle,query)
}</pre>
```

We create two database tables, one to store the manager and program data, and the other to store the monthly return data.

```
# define the function to create the CTA program info table
createCtaProgramInfoTable <- function (dbHandle){</pre>
  # create the SQL statement to create the table
  query<-paste0("CREATE TABLE cta program info(",
                "dbUpdateTimestamp TIMESTAMP, ",
                "column_name VARCHAR(250) NOT NULL, ",
                "column_value VARCHAR(250) NOT NULL, ",
                "column_type VARCHAR(50) NOT NULL, ",
                "cta_name VARCHAR(100) NOT NULL, ",
                "program_name VARCHAR(120) NOT NULL, ",
                "program_id INT NOT NULL, ",
                "PRIMARY KEY(program_id,column_name));")
  # create the table
  dbGetQuery(dbHandle,query)
}
# define the function to create the CTA monthly return table
createCtaMonthlyReturnTable <- function (dbHandle){</pre>
  # create the SQL statement to create the table
  query<-paste0("CREATE TABLE cta monthly returns(",
                "dbUpdateTimestamp TIMESTAMP, ",
                "eom_date DATE NOT NULL, ",
                "monthly_return DECIMAL(20,10) NOT NULL, ",
                "cta_name VARCHAR(100) NOT NULL, ",
                "program_name VARCHAR(120) NOT NULL, ",
                "program_id INT NOT NULL, ",
                "PRIMARY KEY(program_id,eom_date));")
  # create the table
  dbGetQuery(dbHandle,query)
}
```

The vast majority of the data collected - particularly that associated with the manager and program information - remains in a 'messy' format and will likely be cleaned for a future research project.

We call the functions to scrape the Altergis website, create the database, create the database tables, and load the tables.

```
# data extraction, database/table creation, and database loading
outputDirectory<-'C:/Users/DerekG/Documents/github/managed_futures/'</pre>
extractFromWeb<-FALSE
createDatabase<-FALSE
createDatabaseTables<-FALSE
loadDatabaseTables<-FALSE
# extract the CTA manager, program and monthly return data
if (extractFromWeb){
  # extract the Altegris data
  extractAltegrisData(outputDirectory)
}
# connect to MySQL
dbHandle<-dbConnect(dbDriver,
                    host=dbHost,port=dbPort,user=dbUser,
                    password=dbPassword)
if (createDatabase){
  # drop the 'altegris' database
  try(dropAltegrisDatabase(dbHandle), silent=TRUE)
  # create the 'altegris' database
  try(createAltegrisDatabase(dbHandle),silent=TRUE)
  # disconnect from the database
  dbDisconnect(dbHandle)
```

```
# connect to the 'altegris' database
dbHandle<-dbConnect(dbDriver,dbname = dbName,</pre>
                    host=dbHost,port=dbPort,user=dbUser,
                    password=dbPassword)
if (createDatabaseTables){
  # create the database tables
  # --monthly returns table
  try(createCtaMonthlyReturnTable(dbHandle),silent=TRUE)
  # --program info table
  try(createCtaProgramInfoTable(dbHandle),silent=TRUE)
if (loadDatabaseTables){
  # load the data to the database
  # --monthly returns table
 loadCtaProgramInfoTable(dbHandle,outputDirectory,'programInfo')
  # --program info table
  loadCtaMonthlyReturnTable(dbHandle,outputDirectory,'ctaMonthlyReturns')
```

In the above code, the connection parameters are hidden, but a reader wishing to reproduce the paper must install MySQL and provide the connection parameters (i.e., dbHost, dbPort, dbUser, and dbPassword). The other connection parameters remain the same.

Furthermore, the output directory (outputDirectory) parameter must be set and the 'extract-FromWeb', 'createDatabase', 'createDatabaseTables', 'loadDatabaseTables' flags must be set to TRUE.

### **Data Exploration**

In this section we explore a small sub-set of the collected data.

First we connect to the altergris MySQL database.

```
# connect to the 'altegris' database
dbHandle<-dbConnect(dbDriver,dbname = dbName,
   host=dbHost,port=dbPort,user=dbUser,
   password=dbPassword)</pre>
```

We extract the set of managed futures programs classified as 'Systematic'.

```
# extract the systematic programs
query<-paste0("SELECT * FROM altegris.cta_program_info ",
    "WHERE column_type = 'investmentMethodology' AND ",
    "column_name = 'Systematic' ",
    "ORDER BY cta_name,program_name,column_type;")
# fetch the systematic programs
ctaSystematic<-dbGetQuery(dbHandle,query)</pre>
```

There are three types of responses by managers. Some managers report in a binary way (i.e., either they are or are not 'Systematic'), while other managers report the approximate proportion of their operations that

are 'Systematic'. To make the data consistent, 'No' responses are converted to 0% and 'Yes' responses are converted to 100%.

```
# assume that 'No' indicates no systematic element
ctaSystematic[ctaSystematic[,3] == 'No',3] <-0</pre>
# assume that 'Yes' indicates 100% systematic element
ctaSystematic[ctaSystematic[,3]=='Yes',3]<-100
# create a histogram
percentSystematic<-as.numeric(ctaSystematic[,3])</pre>
# define x
x < -seq(from=1, to=100, by=1)
# count the number of programs with x% systematic
systematicFrequency<-tabulate(percentSystematic)</pre>
# set a threshold under which a program is not considered to be systematic
systematicThreshold<-90</pre>
# find the programs with a systematic component above the threshold
systematicIndex<-percentSystematic>=systematicThreshold
# find the frequency %
systematicFrequencyPercent<-round((systematicFrequency/length(systematicIndex))*100,1)</pre>
# extract the programs above the threshold
programId<-ctaSystematic[systematicIndex,6]</pre>
# create the table data frame
distributionAboveThreshold<-data.frame(x,
  systematicFrequencyPercent,
  cumsum(systematicFrequencyPercent))
```

We can see that 63.6% of the programs are 100% systematic, while 82.6% claim that the proportion of their operation that is systematic is above 90%.

```
# create the table
# re-label the columns
colnames(distributionAboveThreshold)<-c('% systematic',
    '% of CTAs','Cumulative % of CTAs')
knitr::kable(t(distributionAboveThreshold[systematicThreshold:100,1:2]),
    caption='Distribution of Programs with Significant Systematic Components')</pre>
```

Table 1: Distribution of Programs with Significant Systematic Components

	90	91	92	93	94	95	96	97	98	99	100
% systematic	90.0	91	92	93	94	95.0	96	97.0	98.0	99.0	100.0
% of CTAs	4.9	0	0	0	0	7.6	0	1.6	1.6	3.3	63.6

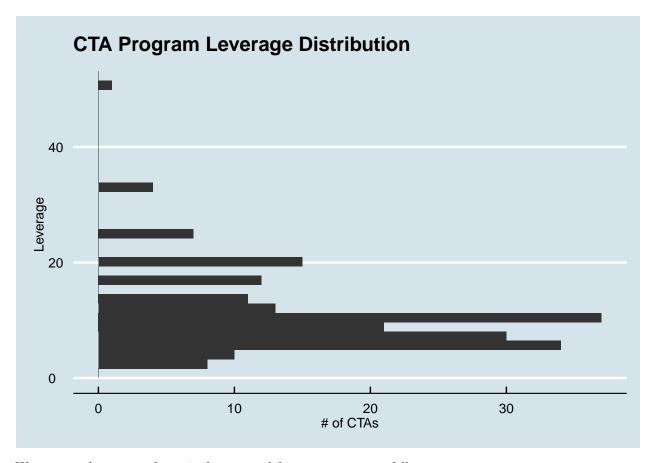
As can be seen in the above table, the vast majority of firms that report a systematic component to their strategies claim that their programs are 90%, 95%, or 100% systematic.

Each managed futures program uses a different level of leverage. The level of allowed leverage is often a constraint set by investors. The inverse of the collected quantity, 'margin-to-equity', is the program leverage. We extract the 'margin-to-equity' as follows:

```
# extract the margin to equity data
query<-paste0("SELECT * FROM altegris.cta_program_info ",
    "WHERE column_type = 'investmentTermsAndInfo' AND ",
    "column_name='Margin Equity Ratio' ",
    "ORDER BY cta_name,program_name,column_type;")
# fetch the margin to equity
ctaMarginToEquity<-dbGetQuery(dbHandle,query)</pre>
```

We convert the 'margin-to-equity' to leverage as follows:

```
# convert the margin-to-equity to numeric
marginToEquity<-(as.numeric(ctaMarginToEquity[,3]))</pre>
# convert the 'margin-to-equity' to leverage
leverage<-round(1/(marginToEquity/100),1)</pre>
# find the min leverage
minLeverage<-min(leverage,na.rm=TRUE)</pre>
# find the max leverage
maxLeverage<-max(leverage,na.rm=TRUE)</pre>
# create x
xLeverage<-seq(from=1,to=maxLeverage,by=1)</pre>
# find the frequency of different leverages
leverageFrequency<-tabulate(leverage)</pre>
# great the graph
leverageDf<-data.frame(leverage)</pre>
ggplot(leverageDf, aes(leverage)) + geom bar() + coord flip()+
  ggtitle('CTA Program Leverage Distribution')+xlab('Leverage')+ylab('# of CTAs')+theme_economist()+
  scale colour economist()
```



We extract the returns for a single managed futures program as follows:

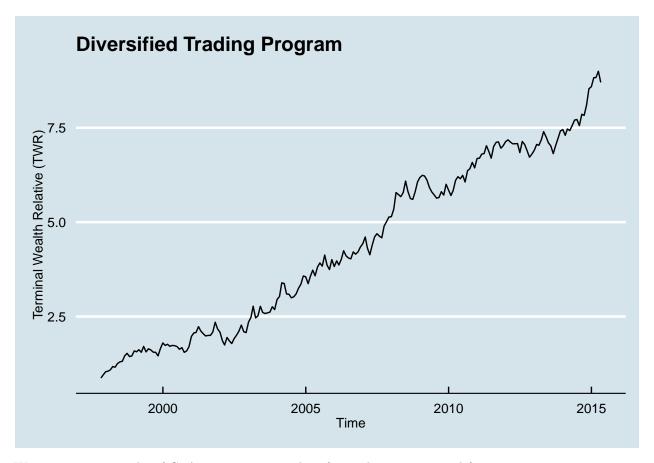
We find all programs that existed prior to 2005-01-01.

```
minDate<-"2005-01-01"
query<-paste0("SELECT DISTINCT cta_name,program_name,program_id,MIN(eom_date) AS minDate ",
    "FROM altegris.cta_monthly_returns WHERE eom_date<'",
    minDate,"' GROUP BY program_id ORDER BY cta_name;")
ctaList<-dbGetQuery(dbHandle,query)
programIds<-ctaList['program_id']
ctaNames<-ctaList['program_id']
ctaPrograms<-ctaList['program_name']
# remove some of the detail from the program name to make names shorter
ctaPrograms[,1]<-gsub('*QEP*','',ctaPrograms[,1])
ctaPrograms[,1]<-gsub('*FRN*','',ctaPrograms[,1])</pre>
```

```
ctaPrograms[,1]<-gsub('*PROP*','',ctaPrograms[,1])
ctaPrograms[,1]<-gsub('*Program*','',ctaPrograms[,1])</pre>
```

We iterate over each program with historical data available prior to 2005-01-01 and extract the return data, adding each CTA program return stream to a group object.

```
# create the xts object to hold the group data
groupData <- xts()</pre>
for (programIndex in 1:dim(programIds)[1]){
  # get the program ID
 programId<-programIds[programIndex,1]</pre>
  # get the CTA name
  ctaName<-ctaList[programIndex,2]</pre>
  # fetch the program returns
  ctaReturn<-fetchMonthlyReturnsForCtaByProgramId(dbHandle,programId)
  dataObject<-xts(ctaReturn[,2],order.by=as.POSIXct(ctaReturn[,1],format='\"Y-\"m-\"d'))
  recentData<-last(dataObject,'10 year')</pre>
  df<-data.frame(date=index(recentData),coredata(recentData))</pre>
  # create the individual graph
  p1 <- ggplot(ctaReturn, aes(x=eomDate, y=cumprod(1+monthlyReturn))) + geom_line() +
    ggtitle(ctaName)+xlab('Time')+ylab('Terminal Wealth Relative (TWR)')+theme_economist()+
    scale_colour_economist()
  # label the return data with the program ID
  colnames(recentData)<-programId</pre>
  # add the individual progrma data to the group
  groupData <- merge(groupData, recentData)</pre>
groupDataDimension<-dim(groupData)</pre>
print(p1)
```



We extract 112 months of CTA program return data for 76 distinct managed futures programs.

Our data includes most of the managers with the most impressive track records.

Table 2: Sample of 10 of the 76 Programs

	cta_name	program_name	minDate
8	Campbell & Company, LP	Campbell Managed Futures	1983-04-30
1	Abraham Trading Company	Abraham Diversified Program	1990-01-31
9	Chesapeake Capital Corporation	Diversified Program QEP	1990-01-31
22	DUNN Capital Management, Inc.	World Monetary and Agriculture (WMA) Program QEP	1990-01-31
26	EMC Capital Advisors LLC	Classic Program QEP	1990-01-31
34	Hawksbill Capital Management	Global Diversified Program <i>QEP</i>	1990-01-31
43	Mark J. Walsh & Company	Standard Program	1990-01-31
44	Michael J. Frischmeyer, CTA	Michael J. Frischmeyer, CTA CLSD	1990-01-31
45	Millburn Corporation	Diversified Program	1990-01-31
57	Rabar Market Research, Inc.	Diversified Program $QEP$	1990-01-31

## **Data Cleaning**

Data cleaning of the majority of the collected data pertaining to manager and program information was beyond the scope of this project and as a result, none of this data was used in the modeling sector of the paper.

The manager and program information collected is somewhat unstructured and visual inspection of the managed futures website reveals many reporting inconsistencies across managers. Our quick exploratory

analysis confirms that data is reported somewhat inconsistently by CTAs. In particular, there appears to be very little validation of the manager and program information submitted by CTAs. As a result, this part of the collected data set requires a lot of cleaning and standardization before it can be used effectively in our modeling.

In this section we provide a brief example of the types of inconsistencies in the available progam and manager data

We extract the information about the geographical region of each manager as follows:

```
# create the query
query<-paste0("SELECT DISTINCT column_value,COUNT(column_value) ",
    "FROM altegris.cta_program_info WHERE column_type = 'address' ",
    "AND column_name='Country' GROUP BY column_value ORDER BY ",
    "column_value;")
# extract the data
ctaCountry<-dbGetQuery(dbHandle,query)
# create the table
colnames(ctaCountry)<-c('Country','# of Programs')
knitr::kable(ctaCountry,caption='Programs By Country - Raw')</pre>
```

Table 3: Programs By Country - Raw

Country	# of Programs
	4
Austria	2
Bahamas	1
Canada	6
Channel Islands	1
Cyprus	1
Finland	4
France	2
Germany	1
Hong Kong	1
Israel	1
Korea	1
Liechtenstein	1
Macedonia	1
Netherlands	2
Singapore	1
Spain	2
St. Croix USVI	1
Switzerland	6
UK	1
United Kingdom	16
United Kingdon	3
United States	35
US	1
USA	111

Spelling errors and single countries coded with multiple names (i.e., United Kingdom, United Kingdom, or UK for instance) are clear.

We can clean up the data as follows:

```
# replace empty with Unreported
ctaCountry[ctaCountry[,1]=='',1]<-'Unreported'</pre>
# reclassify US Virgin Islands as United States
ctaCountry[,1]<-gsub('St. Croix USVI', 'United States', ctaCountry[,1])</pre>
# we clean up the US entries
ctaCountry[,1]<-gsub('USA','United States',ctaCountry[,1])</pre>
ctaCountry[,1]<-gsub('US','United States',ctaCountry[,1])</pre>
# we clean up the UK entries
ctaCountry[,1]<-gsub('UK','United Kingdom',ctaCountry[,1])</pre>
ctaCountry[,1]<-gsub('United Kingdon','United Kingdom',ctaCountry[,1])</pre>
# create the country factor
countryFactor <- factor(ctaCountry[,1])</pre>
# redo the counts by country
cleanTable<-aggregate(x=ctaCountry[,2],by=list(countryFactor),FUN="sum")</pre>
# compute the percent by region
countryPercent<-round(cleanTable[,2]/sum(cleanTable[,2]),4)</pre>
# add row names
rownames(cleanTable)<-cleanTable[,1]</pre>
# create the table
cleanTable<-cbind(cleanTable,countryPercent*100)</pre>
# remove country column
# label the columns
colnames(cleanTable)<-c('Country','# of Programs','% of Programs')</pre>
# create the sort index
sortIndex<-sort.int(cleanTable[,2],index.return=TRUE,decreasing=TRUE)
# write the clean table
knitr::kable(cleanTable[sortIndex$ix,2:3],caption='Programs By Country - Cleaned')
```

Table 4: Programs By Country - Cleaned

	# of Programs	% of Programs
United States	148	71.84
United Kingdom	20	9.71
Canada	6	2.91
Switzerland	6	2.91
Finland	4	1.94
Unreported	4	1.94
Austria	2	0.97
France	2	0.97
Netherlands	2	0.97
Spain	2	0.97
Bahamas	1	0.49
Channel Islands	1	0.49
Cyprus	1	0.49
Germany	1	0.49
Hong Kong	1	0.49
Israel	1	0.49
Korea	1	0.49
Liechtenstein	1	0.49
Macedonia	1	0.49
Singapore	1	0.49

Now we can see that 71.84% of the reporting managed futures programs are operated out of the United States and 9.71% are operated out of the United Kingdom. The vast majority of programs are operated out of these two regions (81.55%). It is also notable that 1.94% of managers do not provide information about their geographical location.

```
# disconnect from the 'altegris' database
dbDisconnect(dbHandle)
```

## [1] TRUE

## Modeling

In the previous section, we provided an overview of the process used to obtain the monthly returns for all distinct CTA programs available in the Altegris managed futures database. In this section we first provide a brief overview of the theory underlying our simple factor model of managed futures program returns. We then build and use a factor model to create sensitivities that map the proportion of total variance in the investment universe to portfolio variation. This sensitivity allows us to monitor the time-varying proportion of variance explained by the first few statistical factors and instantly convert these measures of market state into portfolio variability.

### Theory

In this section, we provide a brief overview the theoretical underpinnings of the modeling approach employed in our application. In particular, we provide an outline of the eigen-decomposition underlying the statistical factor analysis and outline an approach for determining how many investment components contribute to each statistical factor. We conclude this section by introducing an approach for computing factor sensitivities.

Standardized Returns Standardization rescales a variable while preserving its order.

We denote the monthly return of the  $i^{th}$  investment for the  $m^{th}$  month as  $r_{i,m}$  and define the standardized return as:

$$\hat{r}_{i,m} = \frac{(r_{i,m} - \bar{r}_{i,M})}{\sigma(r_{i,M})}$$

Where

 $\hat{r}_{i,m}$  is the standardized return of the  $i^{th}$  investment for the  $m^{th}$  month using data over the time interval one to M

 $r_{i,m}$  is the observed return of the  $i^{th}$  investment for the  $m^{th}$  month

 $\bar{r}_{i,M} = \frac{1}{M} \sum_{m=1}^{M} (\hat{r}_m)$  is the mean of the return stream of the  $i^{th}$  investment over the time interval one to M  $\sigma(r_{i,M}) =$ is the standard deviation of the returns for the  $i^{th}$  investment over the time interval one to M

**Correlations** We represent the standardized returns as an  $I \times M$  matrix  $\hat{R}$  with an empirical correlation matrix C defined as:

$$C = \frac{1}{M}\hat{R}\hat{R}^T$$

Where

T denotes the matrix transform

The correlation matrix (C) of returns  $(\hat{R})$  and the covariance matrix  $(\Sigma_{\hat{R}})$  of standardized returns  $(\hat{R})$  are identical.

#### Principal Component Analysis (PCA)

The objective of principal component analysis (PCA) is to find a linear transformation  $\Omega$  that maps a set of observed variables  $\hat{R}$  into a set of uncorrelated variables F. We define the  $I \times M$  statistical factor matrix as

$$F = \Omega \hat{R}$$

Where each row  $f_k$   $(k=1,\ldots,N)$  corresponds to a factor F of  $\hat{R}$  and the transformation matrix  $\Omega$  has elements  $\omega_{k,i}$ . The first row of  $\omega_1$  (which contains the first set of factor coefficients or 'loadings') is chosen such that the first factor  $(f_1)$  is aligned with the direction of maximal variance in the I-dimensional space defined by  $\hat{R}$ . Each subsequent factor  $(f_k)$  accounts for as much of the remaining variance of the standardized returns  $\hat{R}$  as possible, subject to the constraint that the  $\omega_k$  are mutually orthogonal. The vectors  $\omega_k$  are further constrained by requiring that  $\omega_k \omega_k^T = 1$  for all k.

The correlation matrix C is an  $I \times I$  diagonalizable symmetric matrix that can be written in the form

$$C = \frac{1}{M}EDE^{T}$$

Where D is a diagonal matrix of eigenvalues d and E is an orthogonal matrix of the corresponding eigenvectors.

The eigenvectors of the correlation matrix C correspond to the directions of maximal variance such that  $\Omega = E^T$ . Statistical factors / principal components F are found using the diagonalization above.

If the sign of every coefficient in a statistical factor  $f_k$  is reversed, neither the variance of  $f_k$  nor the orthogonality of  $\omega$  with respect to each of the other eigenvectors changes. For this reason, the signs of factors (PCs) are arbitrary. This feature of PCA can be problematic when we are interested in the temporal evolution of factors.

**Proportion of Variance** The covariance matrix  $\Sigma_F$  for the statistical factor matrix F can be written as:

$$\Sigma_F = \frac{1}{M} F F^T = \frac{1}{M} \Omega \hat{R} \hat{R}^T \Omega^T = D$$

Where D is the diagonal matrix of eigenvalues d.

The total variance of the standardized returns  $\hat{R}$  for the I investments is then

$$\sum_{i=1}^{I} \sigma^{2}(\hat{r}_{i}) = tr(\Sigma_{\hat{R}}) = \sum_{i=1}^{I} d_{i} = \sum_{i=1}^{N} \sigma^{2}(f_{i}) = tr(D) = I$$

Where  $\Sigma_{\hat{R}}$  is the covariance matrix for  $\hat{R}$ 

 $\sigma^2(\hat{r}_i) = 1$  is the variance of the vector  $\hat{r}_i$  of standardized returns for investment i.

The proportion of the total variance in  $\hat{R}$  explained by the  $k^{th}$  factor is then

$$\frac{\sigma^{2}(f_{k})}{\sum_{i=1}^{I} \sigma^{2}(\hat{r_{i}})} = \frac{d_{k}}{\sum_{i=1}^{I} d_{k}} = \frac{d_{k}}{I}$$

The proportion of the variance from the  $k^{th}$  factor is equal to the ratio of the  $k^{th}$  largest eigenvalue  $d_k$  to the number of investments I.

**Number of Significant Components** To determine how many statistical factors are needed to describe the correlations between investments, many methods have been proposed. There is no widespread agreement on an optimal approach. In this paper we focus on the first factor where we are able to find a clear economic interpretation.

Significant Statistical Factor Coefficients An increase in the variance associated with a factor can be the result of increases in the correlations among only a few investment programs (which then have large factor coefficients) or an effect in which many investment programs make significant contributions to the factor. Since the two types of changes have very different implications for portfolio management, this distinction is critically important. It becomes much more difficult to reduce risk by diversifying across different investments when correlations between all investments increase. In contrast, increases in correlations within an investment type when correlations between investment types are not increaseing have a less significant impact on diversification.

Inverse Participation Ratio (IPR) The inverse participation ratio  $IPR_k$  of the  $k^{th}$  factor  $\omega_k$  is defined as:

$$IPR_k = \sum_{i=1}^{I} \left(\omega_{k,i}\right)^4$$

The IPR quantifies the reciprocal of the number of elements that make a significant contribution to each eigenvector.

The behavior of the IPR is bounded by two cases:

- [1] An eigenvector with identical contributions  $\omega_{k,i} = \frac{1}{\sqrt{I}}$  from all I investments has  $IPR_k = \frac{1}{I}$
- [2] An eigenvector with a single factor  $\omega_{k,i} = 1$  and remaining factors equal to zero has IPR = 1

The inverse of the IPR - the so-called participation ratio - provides a more intuitive measure of the significance of a given factor as a large PR indicates that many investments contribute to the factor, while a small PR signals that few investments contribute to the factor:

$$PR = \frac{1}{IPR_k}$$

The participation ratio quantifies the number of eigenvector (loading) components that participate in a factor and provides a measure of concentration.

The bigger a PR is, the more participants the statistical factor has, the more uniformly distributed the participation is, and the more correlations are driven by the statistical factor.

Participation ratios facilitate the identification of statistical facotrs that represent macroeconomic scenarios, namely those with with many participants. They also help us identify factors that represent microeconomic scenarios, namely factors with few participants.

### Portfolio Factor Sensitivities and Coherent Scenario Analysis

We can use our factor model to determine the impact of an increase in the proportion of variance described by any given statistical factor on our correlation matrix. By perturbing the eigenvalues up and down and applying the appropriate re-normalizations we create changes in the correlations driven by a common factor.

The following three functions are used to implement the sensitivity analysis in the application section of the paper.

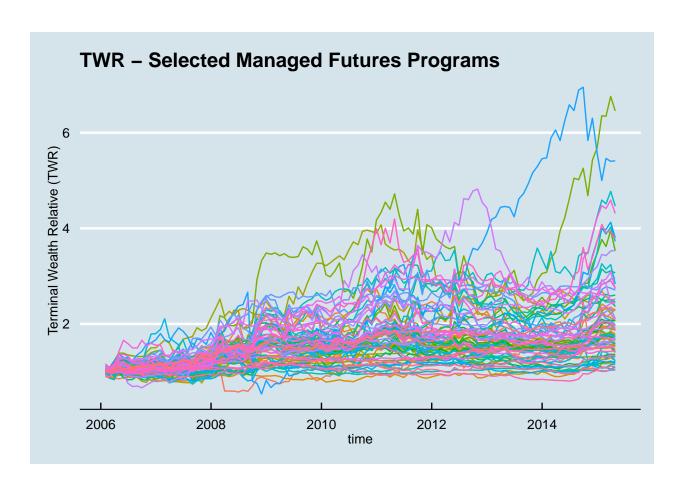
```
perturbCorrelation<-function (shockFactor,factorIndex,eigenvalues,eigenvectors){</pre>
  # create the hash to store the results
  scenario<-hash()</pre>
  scenarioEigenvalues <- eigenvalues
  scenarioEigenvalues[factorIndex] <- eigenvalues[factorIndex] * shockFactor</pre>
  C1 <- eigenvectors %*% diag(scenarioEigenvalues) %*% t(eigenvectors)
  # extract the variance
  V <- diag(1/sqrt(C1))</pre>
  # normalize the correlation matrix
  C2 <- diag(V) %*% C1 %*% diag(V)
  # eigen decomposition
  scenarioDecomposition=eigen(C2)
  # extract the stressed eigenvalues
  eigenvaluesF=scenarioDecomposition$values
  # extract the stressed eigenvector
  eigenvectorF=scenarioDecomposition$vectors
  # number of factors
  numberOfFactors<-sum(eigenvaluesF)</pre>
  # compute the proportion of variance
  scenarioProportionOfVariance<-eigenvaluesF/numberOfFactors
  # store the correlation matrix
  scenario['correlation']<-C2</pre>
  # store the proportion of variance
  scenario['proportionOfVariance']<-scenarioProportionOfVariance</pre>
  # return the scenario
  scenario
perturbFactorCorrelation <- function (factorIndex,eigenvalues,eigenvectors){</pre>
  # create the hash
  scenarios<-hash()</pre>
  # create shock scenarios
  shockFactors<-seq(from=0.2,to=5,by=0.2)
  # iterate over shock factors
  for (shockIndex in seq_along(shockFactors)){
    # extract the shock
    shockFactor<-shockFactors[shockIndex]</pre>
    # increase the importance of the factorIndex factor
    scenario<-perturbCorrelation(shockFactor,factorIndex,eigenvalues,eigenvectors)</pre>
    # store the correlation
    scenarios[paste0('scenario_',shockIndex)]<-scenario</pre>
  }
  # return scenarios
  scenarios
factorBasedCorrelationSensitivity<-function (numberOfFactors,C){</pre>
  # find the number of rows and columns
  dimension <-dim(C)
  # create the storage matrix
  sensitivity<-matrix(0,numberOfFactors,dimension[2])</pre>
```

# compute the eigendecomposition

```
decomposition=eigen(C)
# extract eigenvalues
eigenvalues=decomposition$values
# extract eigenvectors
eigenvectors=decomposition$vectors
# find the proportion of variance
proportionOfVariance=eigenvalues/length(eigenvalues)
# find the explained variance
explainedVariance=cumsum(proportionOfVariance)
# create hash
scenariosByFactor<-hash()</pre>
# iterate over each factor
for (factorIndex in 1:numberOfFactors){
  # perturb the factor
  scenarios<-perturbFactorCorrelation(factorIndex,eigenvalues,eigenvectors)</pre>
  scenariosByFactor[paste0('factor_',factorIndex)]<-scenarios</pre>
  scenarioIndices<-sort(as.numeric(gsub('scenario_','',</pre>
    names(scenariosByFactor[paste0('factor_',factorIndex)]))))
scenariosByFactor
```

## Application

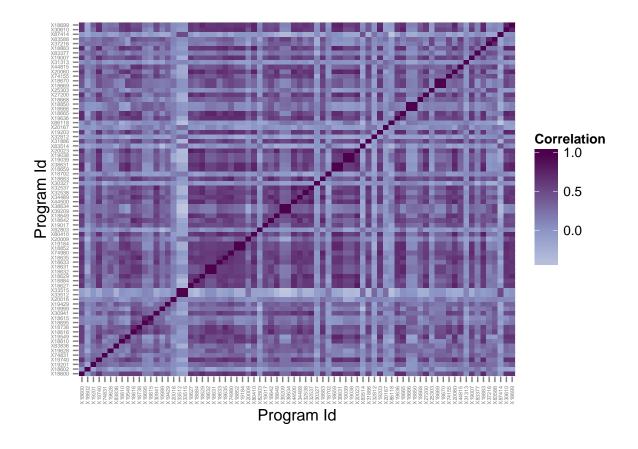
In this section we apply the theory outlined in the above section. In particular, we build a simple factor model of managed futures program returns and use it to create sensitivities that map the proportion of total variance in the investment universe to portfolio variation. This sensitivity allows us to monitor the time-varying proportion of variance explained by the first few statistical factors and instantly convert these measures of market state into portfolio variability. This is particularly useful during times of crisis when the importance of the first few factors increase significantly.



## Data Preprocessing

Prior to any modeling, we standardize the managed futures program returns.

We compute then create a heatmap of the correlation.



#### Statistical Factor Analysis

We now decompose the correlation matrix into statistical factors.

The top 5 factors explain a very significant proportion of the total variance.

Table 5: Top 5 Factors

Factors	Proportion of Variance	Cumulative Proportion of Variance
Factor 1	36.8	36.8
Factor 2	8.8	45.7
Factor 3	6.5	52.1
Factor 4	4.0	56.1
Factor 5	3.6	59.8
Factor 6	3.0	62.8
Factor 7	2.5	65.3
Factor 8	2.2	67.6
Factor 9	2.2	69.8
Factor 10	2.0	71.8

The first statistical factor accounts for 37% of the variation of the systems. Indeed the first factor is the most significant by far. The second factor accounts for another 9% of the variation, and the third component accounts for 6% more. Indeed, the first three factors together account for 52% of the variation. The first 10 factors account for 37% proportion of the variation in the system. By focusing on just three factors we can

understand a very significant proportion of the total variation in the managed futures universe under study.

When we sort the factor loadings by the first factor we can see that the all but two (relative value) funds contribute to the first factor, with the long- and medium- term trend-following funds making the strongest contributions and the volatility selling, short-term and relative value programs having small or negative loadings.

The ten smallest factor loadings are:

Table 6: Smallest Factor 1 Loadings

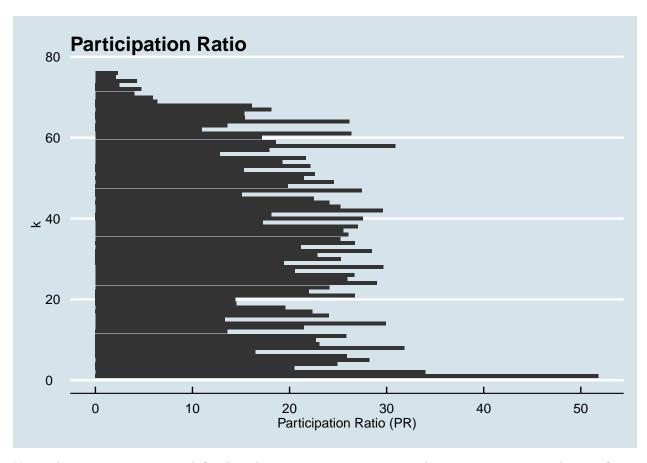
	Manager Name	Program Name	Factor 1
19	Doherty Advisors, LLC	Relative Value Volatility 2X	-0.0434
18	Doherty Advisors, LLC	Relative Value Volatility 1X	-0.0410
74	Warrington Asset Management Corp.	Strategic Fund	-0.0228
52	Paskewitz Asset Management, LLC	Contrarian 3X Stock Index	-0.0209
50	Omni Trading, LLC	S&P 500 Option Overwriting	-0.0039
54	Quantitative Investment Management, LLC	Global	0.0023
42	Kinkopf Capital Management, LLC	Kinkopf S&P	0.0034
68	Systematic Alpha Management LLC	Systematic Alpha Futures	0.0044
2	AgTech Trading Company	Ag Trading	0.0052
32	Goldman Management, Inc.	Goldman Management Stock Index Futures	0.0079

The ten largest factor loadings are:

Table 7: Largest Factor 1 Loadings

	Manager Name	Program Name	Factor 1
75	Welton Investment Partners LLC	Global Directional Portfolio	0.1514
41	Kelly Angle Inc.	Genesis	0.1516
66	SMN Investment Services GmbH	Diversified Futures	0.1522
27	Estlander & Partners Ltd.	Alpha Trend	0.1522
22	DUNN Capital Management, Inc.	World Monetary and Agriculture (WMA)	0.1525
1	Abraham Trading Company	Abraham Diversified	0.1530
49	Mulvaney Capital Management Ltd	Global Diversified	0.1550
38	ISAM - International Standard Asset Management	Systematic	0.1563
56	Quest Partners LLC	AlphaQuest Original (AQO)	0.1586
26	EMC Capital Advisors LLC	Classic	0.1603

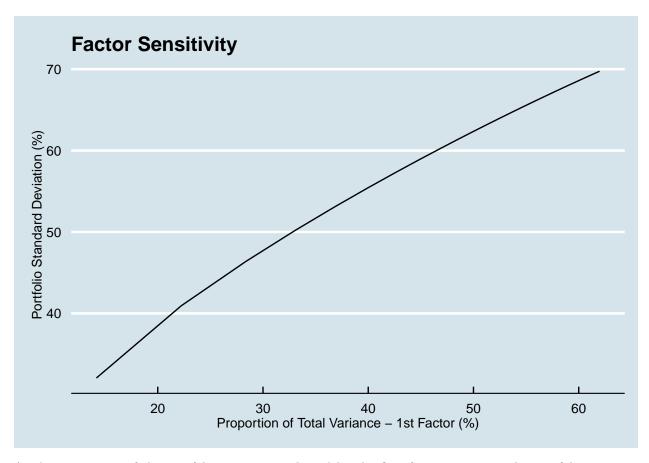
The first factor can be thus thought of as a 'long directional volatility' factor.



Using the participation ratio defined in the previous section, we see that 52 components make significant contributions to the first factor. This is in strong contrast to the other factors where the number of components making significant contributions is between 2 and 34.

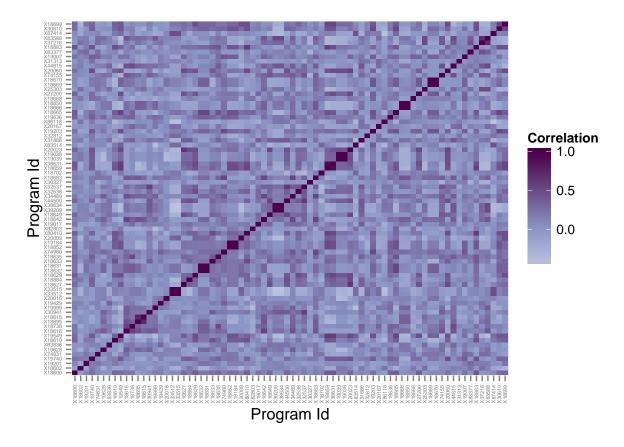
Although more examination of the factors would be required to get an deeper intuitive sense of the *meaning* of the factors, we proceed to illustrating how our simple statistical factor model can be used to create sensitivities.

**Determining the Impact of Factors on Portfolio Variability** We can perturb the importance of the first factor up and down and use our equation for portfolio standard deviation to determine the impact on a portfolio with equal allocations to our 76 managed futures programs.

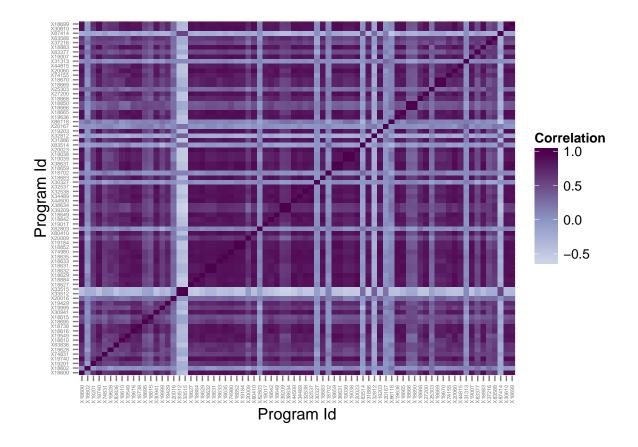


As the proportion of the portfolio variance explained by the first factor increases, the portfolio variance increases. Using this sensitivity measure, we can track the current proportion of variance explained by the first factor and instantly know the impact on the variation of portfolio returns.

We can visualize a scenario where the importance of the first factor falls to extremes:



We can visualize a scenario where the importance of the first factor rises to extremes:



## Conclusions

Our factor analysis revealed a very significant proportion of the total variance of the modeled managed futures universe can be captured by a single statistical factor. This factor corresponds to a very intuitive scenario. The sensitivity analysis developed - given the intuitive interpretation of the first factor - can be used to better understand variation in the managed futures universe and can be used to identify programs that provide better diversification.

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## Appendix A: GitHub Repository

All of the R code used to produce this paper can be found in the following github repository:

https://github.com/dgn2/managed\_futures

The github repository also includes the .Rmd file used to generate the .pdf working paper file and includes code to:

- extract CTA manager, program, and monthly return data from the Altegris managed futures website
- create a MySQL database with tables to store extracted CTA manager, program, and monthly return data
- load CTA manager, program, and monthly return data to the MySQL database
- conduct limited exploratory analysis of the data
- conduct limited cleaning of the data used in subsequent statistical modeling
- estimate statistical factors based on the monthly returns of a select set of CTA programs
- compute sensitivities

## Apprendix B: Fundamental Laws of Investing

## Importance of Capital Preservation

The amount to recover from a loss increases geometrically with the magnitude of the loss.

$$G = \left(\frac{1}{1 - L}\right) - 1$$

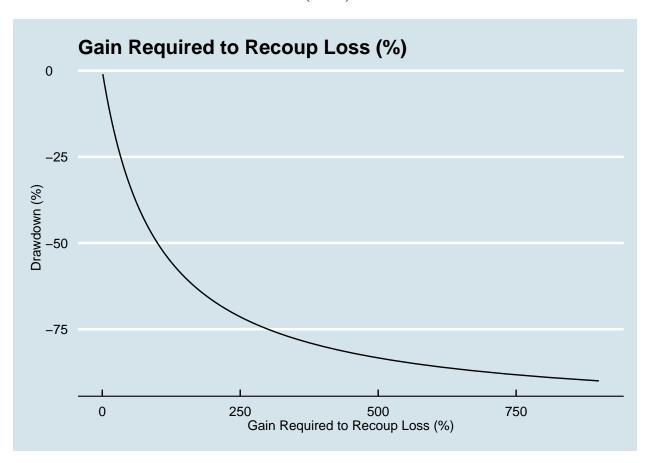


Table 8: Gain Required to Recoup Loss (%)

	Gain Required to Recoup Loss (%)	Drawdown (%)
5	5.26	-5
10	11.11	-10
15	17.65	-15
20	25.00	-20
30	42.86	-30
40	66.67	-40
50	100.00	-50
60	150.00	-60
70	233.33	-70

## **Time to Recover in Years**

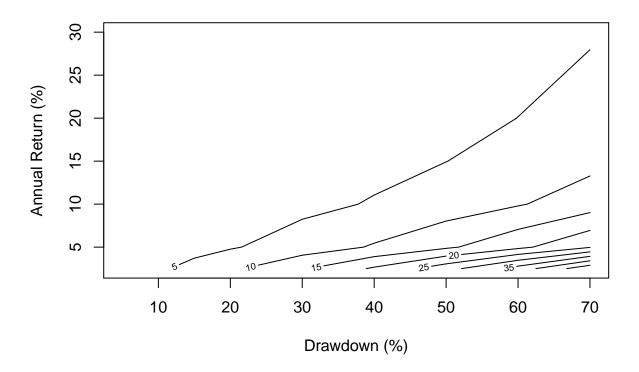


Table 9: Time to Recover From Drawdown (Years)

	2.5	5	10	15	20	30
5	2.08	1.05	0.54	0.37	0.28	0.20
10	4.27	2.16	1.11	0.75	0.58	0.40
15	6.58	3.33	1.71	1.16	0.89	0.62
20	9.04	4.57	2.34	1.60	1.22	0.85
30	14.44	7.31	3.74	2.55	1.96	1.36
40	20.69	10.47	5.36	3.65	2.80	1.95
50	28.07	14.21	7.27	4.96	3.80	2.64
60	37.11	18.78	9.61	6.56	5.03	3.49
70	48.76	24.68	12.63	8.61	6.60	4.59