

INTERVUOS
DE COXFINNZA

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INFERENCIA ESTADÍSTICA

Estimación

Puntual

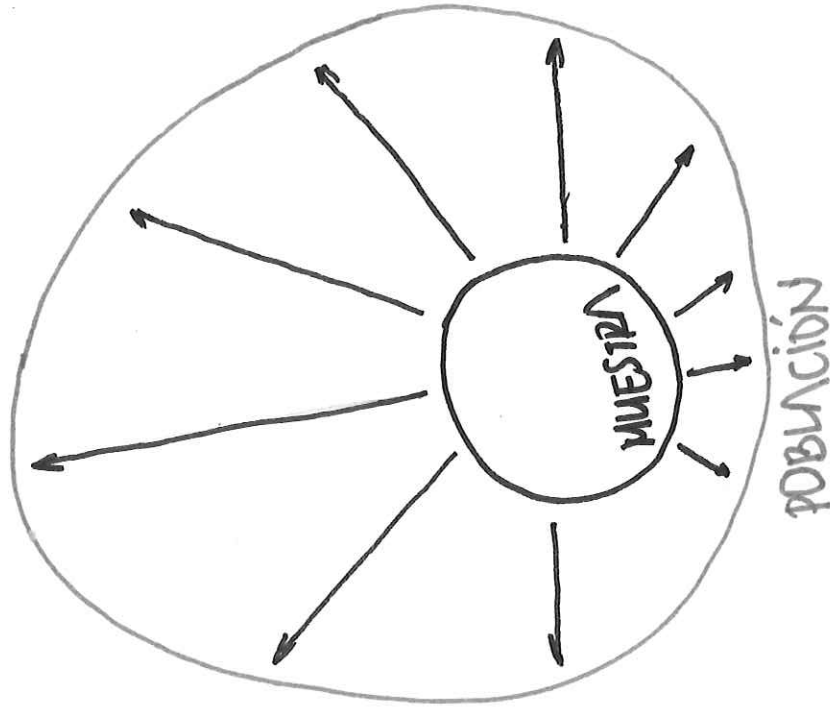
Por intervalos
de confianza

$$\hat{\theta}$$

Pruebas de Hipótesis

$$H_0: \theta = \theta_0$$

$$H_a: \theta \neq \theta_0$$



CUANDO NO SE CONOCE EL VALOR DE UN
PARÁMETRO, SE UTILIZA LA ESTIMACIÓN
PARA ENCONTRAR UN VALOR APROXIMADO A
PARTIR DE LOS VALORES DE UNA MUESTRA

CUANDO SE QUIERE VALIDAR UNA AFIRMACIÓN
SOBRE UN PARÁMETRO DE UNA POBLACIÓN

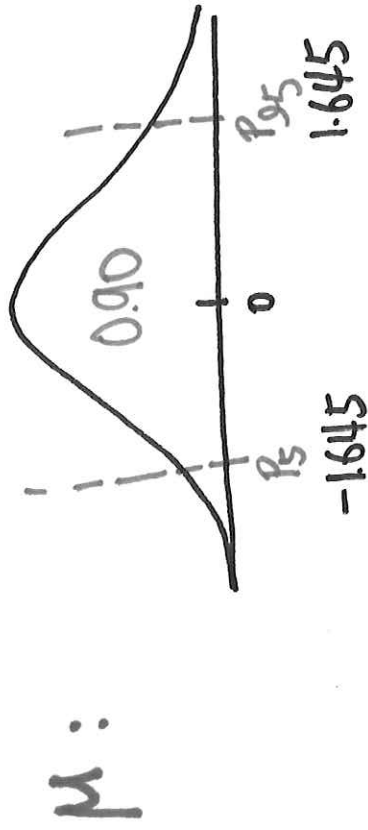
INFERENCIA ESTADÍSTICA

ESTIMACIÓN

ESTIMACIÓN POR INTERVALOS
DE CONFIANZA

(LIC ; LSC)

INTERVALOS DE CONFIANZA



$$P(-1.645 < Z < 1.645) = 0.90$$

$$P(Z_{\alpha/2} < Z < Z_{\alpha/2}) = 1 - \alpha$$

$$P(-1.645 < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < 1.645) = 0.90$$

$$P(-1.645 \frac{\sigma}{\sqrt{n}} < \bar{X} - \mu < 1.645 \frac{\sigma}{\sqrt{n}}) = 0.90$$

$$P(-1.645 \frac{\sigma}{\sqrt{n}} - \bar{X} < -\mu < 1.645 \frac{\sigma}{\sqrt{n}} - \bar{X}) = 0.90$$

$$P(\bar{X} - 1.645 \frac{\sigma}{\sqrt{n}} < \mu < \bar{X} + 1.645 \frac{\sigma}{\sqrt{n}}) = 0.90$$

$$IC_{\mu: 1-\alpha} \quad \bar{X} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

INTERVALOS DE CONFIANZA

SUPUESTO

μ $\bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$

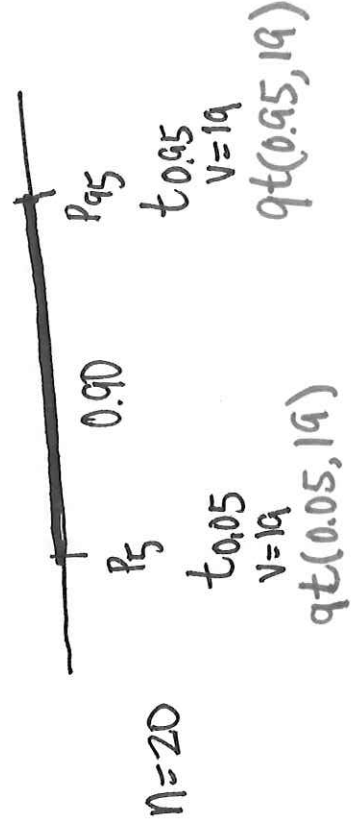
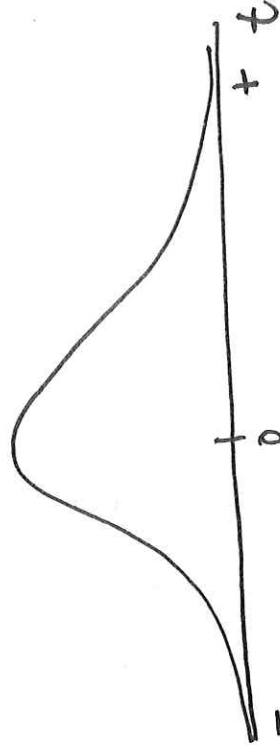
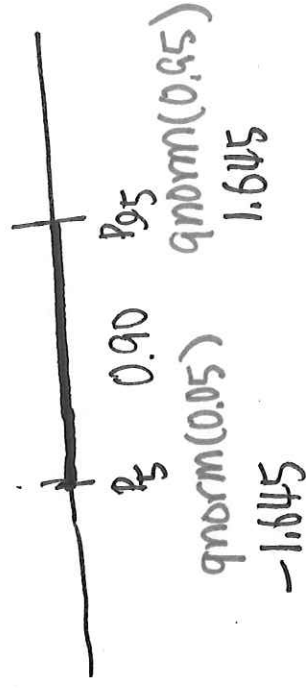
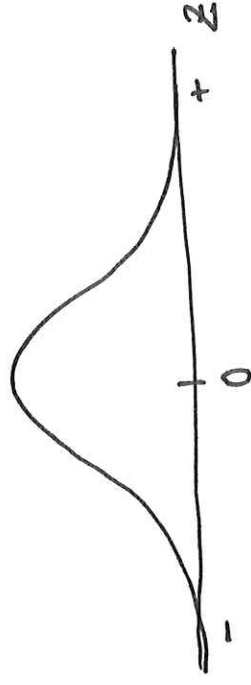
- $X \sim N(\mu, \sigma^2)$
- σ^2 CONOCIDA

$\bar{x} \pm t_{\alpha/2} \frac{s}{\sqrt{n}}$

- $X \sim \text{NORMAL}$
- σ^2 DESCONOCIDA

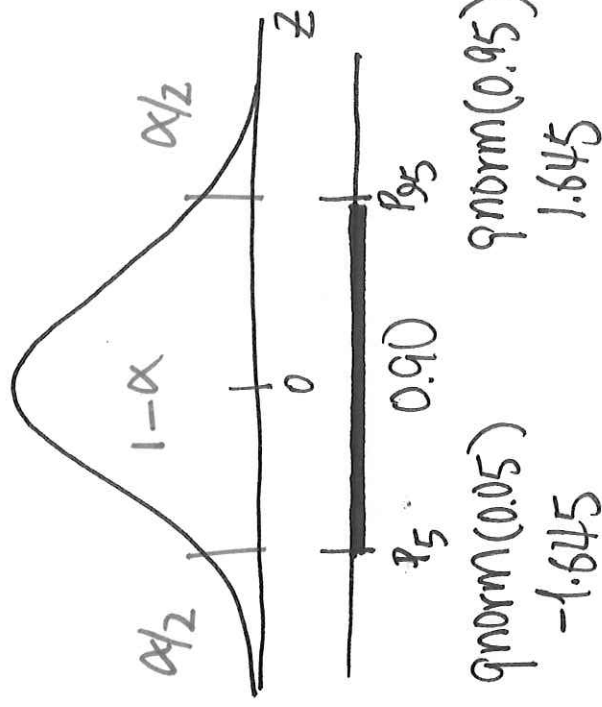
$\bar{x} \pm z_{\alpha/2} \frac{s}{\sqrt{n}}$

- $X \sim \text{DESCONOCIDA}$
- $n \gg \text{TCL} \rightarrow \bar{X} \sim \text{NORMAL}$



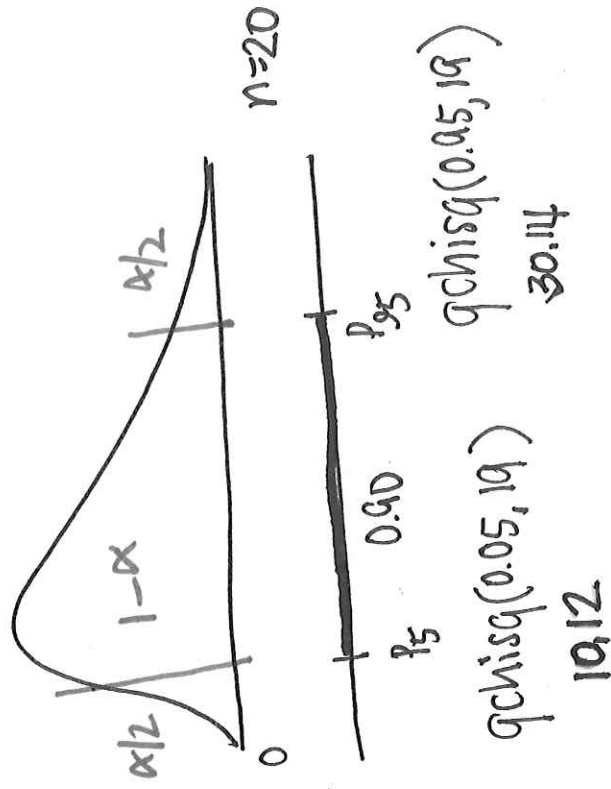
$$P \quad \hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

SUPUESTO
 $n >>$



$$\sigma^2 \left(\frac{(n-1)S^2}{\chi^2_{\alpha/2}} ; \frac{(n-1)S^2}{\chi^2_{1-\alpha}} \right)$$

$\chi^2_{1-\alpha/2}$
 $v=n-1$

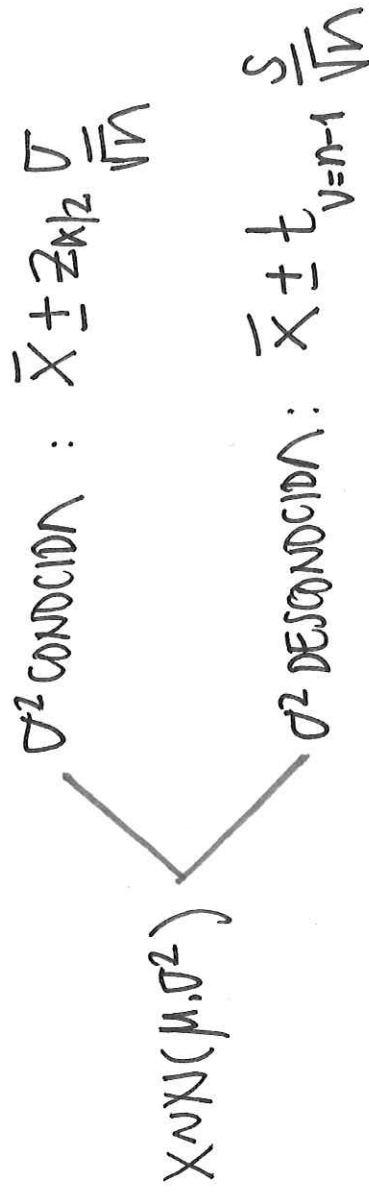


IC μ .

SURUESTO₁

SURUESTO₂

IC



: TCL $\bar{X} \pm z_{\alpha/2} \frac{s}{\sqrt{n}}$

$n >>$

$X \sim ?$

$n <$

: MÉTODO NO PARAMÉTRICO
(REMUESTRO)

DIFERENCIA DE MEDIAS

$\mu_1 - \mu_2$ • GRUPOS PAREADOS O EMPAREJADOS

$$\bar{d} \pm t_{\alpha/2} \frac{S_d}{\sqrt{n}}$$

$$X_1 \sim N(\mu_1, \sigma_1^2)$$

$$X_2 \sim N(\mu_2, \sigma_2^2)$$

X_1	X_2	$d = X_1 - X_2$
X_{11}	X_{21}	d_1
X_{12}	X_{22}	d_2
\vdots	\vdots	\vdots
X_{1n}	X_{2n}	d_n

$$\bar{d} = \frac{\sum d_i}{n}$$

S_d

- GRUPOS INDEPENDIENTES
- SUPUESTOS: NUNCA $\sigma_1^2 = \sigma_2^2$

$$\bullet \sigma_1^2 \neq \sigma_2^2$$

$$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

v^*

$$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

$$v = n_1 + n_2 - 2$$

$$\text{donde } S_p^2 = \frac{(n_1 - 1) s_1^2 + (n_2 - 1) s_2^2}{n_1 + n_2 - 2}$$

$$\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$v^* = \left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right)^2$$

$$\frac{\frac{(s_1^2/n_1)^2 + (s_2^2/n_2)^2}{n_1 - 1}}{n_2 - 1}$$

NOTA:

$$(-, -)$$

$$\mu_1 < \mu_2$$

$$(-, +)$$

$$\mu_1 = \mu_2$$

$$(+, +)$$

$$\mu_1 > \mu_2$$

COMPARACIÓN DE PROPORCIONES

$p_1 - p_2$

$$(\hat{p}_1 - \hat{p}_2) \pm Z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$$

NOTA:

$(-, -): p_1 < p_2$

$(-, +): p_1 = p_2$

$(+, +): p_1 > p_2$

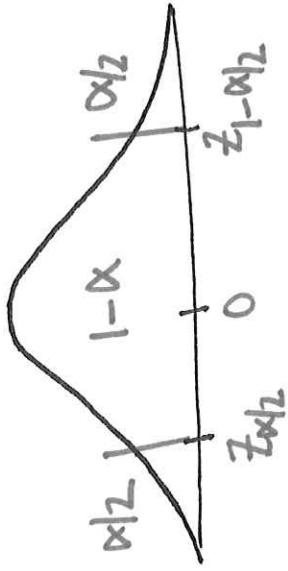
RAZÓN DE VARIANZAS

$$\frac{s_1^2}{s_2^2} \left(\frac{s_1^2/n_1-1}{s_2^2/n_2-1} f_{1-\alpha/2, v_1, v_2} \right) ; \left(\frac{s_1^2/n_1-1}{s_2^2/n_2-1} f_{1-\alpha/2, v_1, v_2} \right)$$

;

TAMANO DE MUESTRA

- ESTIMACION DE μ



$$P(z_{\alpha/2} \leq z \leq z_{1-\alpha/2}) = 1-\alpha$$

$$P(\bar{X} - z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{X} + z_{\alpha/2} \frac{\sigma}{\sqrt{n}}) = 1-\alpha$$

$$\mu = \bar{X} + z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

DESPEJAMOS n

$$n = \frac{z_{\alpha/2}^2 \cdot \sigma^2}{e^2}$$

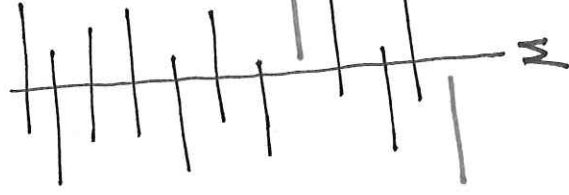
$$e = |\mu - \bar{X}| < e$$

CONFIANZA (1)

$$n = \frac{z_{\alpha/2}^2 \sigma^2}{Q^2}$$

ERROR DE (3)
MUESTREO

(1) CONFIANZA (2) VARIANZA



- PRUEBA PILOTO
- ESTUDIO PREVIO
- EXPERTO

$$\sigma^2 \frac{\text{Máx} - \text{mín}}{4}$$

(2) ERROR DE MUESTREO

(1) y (2) A CARGO DEL INVESTIGADOR

TAMANO DE MUESTRA

• ESTIMACION DE P

$$n = \frac{z_{\alpha/2}^2 \cdot pq}{e^2} \cdot \text{CONFIANZA (1)}$$

ERRORE DE (3) MUESTREO

(1) CONFIANZA	$z_{\alpha/2}$	ERRORE DE MUESTREO
90%	1.645	$ p - \hat{p} < e$
95%	1.96	
99%	2.576	

VARIANZA

- PRUEBA PILOTO,
- VARIANZA MAXIMA
- EXPERTO

p	q	pq
0.1	0.9	0.09
0.2	0.8	0.16
0.3	0.7	0.21
0.4	0.6	0.24
0.5	0.5	0.25
0.6	0.4	0.24
0.7	0.3	0.21
0.8	0.2	0.16
0.9	0.1	0.09

VARIANZA MAX → 0.5 0.5 0.25
 VARIANZA MAX → 0.6 0.4 0.24

TAMANO DE MUESTRA

μ .

P.

CONFIANZA (1)

CONFIANZA (1)

σ^2 — VARIANZA (2)

σ^2 — VARIANZA (2)

• PRUEBA PILOTO

• PRUEBA PILOTO
• VARIANZA MAX

$$n = \frac{Z_{\alpha/2}^2 \sigma^2}{Q^2}$$

ERROR DE MUESTREO (3)

ERROR DE MUESTREO (3)

(1) y (3)



A CARGO DEL
INVESTIGADOR

$$n = \frac{n_0 N}{n_0 + N - 1}$$

SE DEBE CORREGIR
EL TAMAÑO DE
MUESTRA POR
POBLACION FINITA

$$\text{SI } \frac{n}{N} > 0,05$$

INTERVALOS DE CONFIANZA NO PARAMÉTRICOS

CUANDO $n < 30$

$X \sim ?$ (NO NORMAL)

MÉTODO 1: $(p_{\alpha/2}; p_{1-\alpha/2})$

MÉTODO NO PARAMÉTRICO

MÉTODO 2:
 $(2\bar{X} - p_{1-\alpha/2}; 2\bar{X} - p_{\alpha/2})$

• MUESTRA: x_1, x_2, \dots, x_n

• REMUESTREO

MUESTREO ALTERNATIVO CON REPETICIÓN

• SE RECONSTRUYE POBLACIÓN SIMULANDO
UNA GRAN CANTIDAD DE VALORES
DEL ESTIMADOR

• SE CALCULAN LOS PERCENTILES

NAVIDI
(2006)

INTERVALOS DE CONFIANZA

$$IC_{\mu}: \bar{X} \pm z_{\alpha/2} \frac{S}{\sqrt{n}} \quad (1)$$

$$\bar{X} \pm t_{\alpha/2} \frac{S}{\sqrt{n}} \quad (2)$$

$$\bar{X} \pm z_{\alpha/2} \frac{S}{\sqrt{n}} \quad (3)$$

$$IC_p: \hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \quad (4)$$

$$IC_{p_1-p_2}:$$

$$(\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} \quad (9)$$

$$IC_{\sigma^2}: \left(\frac{(n-1)S^2}{\chi_{1-\alpha/2}}; \frac{(n-1)S^2}{\chi_{\alpha/2}} \right) \quad (5)$$

$$IC_{\sigma_1^2/\sigma_2^2}: \left(\frac{S_1^2}{S_2^2} \cdot \frac{1}{f_{1-\alpha/2}}; \frac{S_1^2}{S_2^2} \cdot \frac{1}{f_{\alpha/2}} \right) \quad (10)$$

$$IC_{\mu_1-\mu_2}: \bar{d} \pm t_{\alpha/2} \frac{S_d}{\sqrt{n}} \quad (6)$$

$$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} \frac{S_p}{\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \quad (7)$$

$$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} \frac{S_p}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}} \quad (8)$$