Assignment 6: GLMs (Linear Regressios, ANOVA, & t-tests)

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OVERVIEW

This exercise accompanies the lessons in Environmental Data Analytics on generalized linear models.

Directions

- 1. Change "Student Name" on line 3 (above) with your name.
- 2. Work through the steps, **creating code and output** that fulfill each instruction.
- 3. Be sure to **answer the questions** in this assignment document.
- 4. When you have completed the assignment, Knit the text and code into a single PDF file.
- 5. After Knitting, submit the completed exercise (PDF file) to the dropbox in Sakai. Add your last name into the file name (e.g., "Fay_A06_GLMs.Rmd") prior to submission.

The completed exercise is due on Monday, February 28 at 7:00 pm.

Set up your session

2.1.1

v readr

- 1. Set up your session. Check your working directory. Load the tidyverse, agricolae and other needed packages. Import the *raw* NTL-LTER raw data file for chemistry/physics (NTL-LTER_Lake_ChemistryPhysics_Raw.csv). Set date columns to date objects.
- 2. Build a ggplot theme and set it as your default theme.

```
getwd()
## [1] "C:/Users/dgp20/Documents/ENV 872/Environmental_Data_Analytics_2022/Assignments"
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
      filter, lag
##
## The following objects are masked from 'package:base':
##
      intersect, setdiff, setequal, union
##
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5
                     v purrr
                               0.3.4
## v tibble 3.1.6
                     v stringr 1.4.0
## v tidvr
           1.1.4
                     v forcats 0.5.1
```

Simple regression

Our first research question is: Does mean lake temperature recorded during July change with depth across all lakes?

- 3. State the null and alternative hypotheses for this question: > Answer: H0: There is NOT a statistically significant difference with depth in lake temperature recurded during July in all lakes. Ha: There is a statistically significant difference with depth in lake temperature recurded during July in all lakes.
- 4. Wrangle your NTL-LTER dataset with a pipe function so that the records meet the following criteria:
- Only dates in July.
- Only the columns: lakename, year4, daynum, depth, temperature C
- Only complete cases (i.e., remove NAs)
- 5. Visualize the relationship among the two continuous variables with a scatter plot of temperature by depth. Add a smoothed line showing the linear model, and limit temperature values from 0 to 35 °C. Make this plot look pretty and easy to read.

```
#NOTE- I included results='hide' for this chunk because my knitted PDF was displaying
#every value in my filtered dataset for #4, and I wasn;t sure how to turn it off.
#I don't believe it affected any other aspects here.

#4
chemphys.processed <-
chemphys%>%
filter(daynum >= 181|daynum <= 212)
select(chemphys, lakename, year4, daynum, depth, temperature_C) %>%
filter(lakename != "", year4 != "", daynum != "", depth != "" | temperature_C != "")

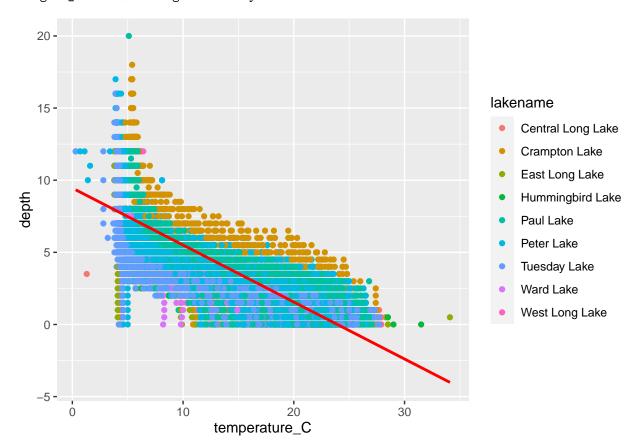
#5
chemphys.processed.scatter <-
chemphys.processed%>%
filter(temperature_C <= 35)

#Setting a new piped dataset to further filter the data for the scatterplot-
#there may be more elegant ways to do this</pre>
```

```
tempdepth.plot <- ggplot(chemphys.processed.scatter, aes(x = temperature_C, y = depth, color = lakename
    geom_point() +
    geom_smooth(method= 'lm', color = 'red')

#Added color by lakename to make graph a bit more aesthetically pleasing and readable.
print(tempdepth.plot)</pre>
```

`geom_smooth()` using formula 'y ~ x'



#Hopefully as pretty as the graph can be with so many values.

6. Interpret the figure. What does it suggest with regards to the response of temperature to depth? Do the distribution of points suggest about anything about the linearity of this trend?

Answer: This suggests that temperature tends to decrease with depth across all lakes. Distribution suggests a much higher temperature range at low-depth areas. The distribution does not seem to be completely linear, but rather more proportional, with an almost exponential-looking decrease in temp at deeper depths. Regardless, this does suggest some relationship between temperature and depth, at a glance, which supports Ha.

7. Perform a linear regression to test the relationship and display the results

```
#7
linregtest <- lm(data = chemphys.processed.scatter, temperature_C ~ depth)
#Setting up a variable to run linear regression
summary(linregtest)</pre>
```

```
##
## Call:
  lm(formula = temperature C ~ depth, data = chemphys.processed.scatter)
##
##
  Residuals:
                                     3Q
##
        Min
                  1Q
                       Median
                                             Max
                      -0.1219
##
   -15.7864 -3.1363
                                 3.1815
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
   (Intercept) 19.986395
                           0.037166
                                       537.8
                                               <2e-16 ***
               -1.707162
                           0.006366
                                      -268.2
                                               <2e-16 ***
##
  depth
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 3.961 on 34754 degrees of freedom
## Multiple R-squared: 0.6742, Adjusted R-squared: 0.6742
## F-statistic: 7.192e+04 on 1 and 34754 DF, p-value: < 2.2e-16
#Printing linear regression variables.
```

8. Interpret your model results in words. Include how much of the variability in temperature is explained by changes in depth, the degrees of freedom on which this finding is based, and the statistical significance of the result. Also mention how much temperature is predicted to change for every 1m change in depth.

Answer: The numbers here suggest that, with an average temp of around 19 degrees C, a 1-unit change in depth produces a roughly 1.71-unit decrease in temperature, with 34754 degrees of freedom. Our R-squared value of 0.6742 tells us that 67.42% of temp variation is explained by depth. In terms of statistical significance, given the small p-value and large F-statistic, it is safe to reject the null hypothesis here. We can conclude a statistically significant link between temperature and depth based on this data.

Multiple regression

Let's tackle a similar question from a different approach. Here, we want to explore what might the best set of predictors for lake temperature in July across the monitoring period at the North Temperate Lakes LTER.

- 9. Run an AIC to determine what set of explanatory variables (year4, daynum, depth) is best suited to predict temperature.
- 10. Run a multiple regression on the recommended set of variables.

```
#setting this ahead of #10.
multregtest <- lm(data = chemphys.processed, temperature_C ~ year4 + daynum + depth)
step(multregtest)
## Start: AIC=92515.66
## temperature_C ~ year4 + daynum + depth
##
##
                                     AIC
            Df Sum of Sq
                             RSS
## <none>
                           497693
                                   92516
## - year4
                                   92525
             1
                     167
                          497861
## - daynum 1
                   47378
                          545071
                                   95674
```

```
## - depth
                 1130140 1627834 133700
##
## Call:
## lm(formula = temperature_C ~ year4 + daynum + depth, data = chemphys.processed)
##
## Coefficients:
## (Intercept)
                      year4
                                   daynum
                                                 depth
     -2.268081
                   0.007734
                                 0.034990
                                             -1.708651
#Since removing depth seems to drive up the AIC by the largest amount, it would seem that depth is best
multregtest <- lm(data = chemphys.processed, temperature_C ~ year4 + daynum + depth)
summary(multregtest)
##
## Call:
## lm(formula = temperature_C ~ year4 + daynum + depth, data = chemphys.processed)
##
## Residuals:
##
                                     3Q
        Min
                  1Q
                       Median
                                             Max
##
  -19.7228
            -2.8606
                      -0.1706
                                 2.9267
                                         17.8338
##
## Coefficients:
##
                 Estimate Std. Error
                                      t value Pr(>|t|)
## (Intercept) -2.2680808
                           4.5365880
                                        -0.500 0.617111
                                         3.419 0.000629 ***
## year4
                0.0077342
                           0.0022622
## daynum
                0.0349904
                           0.0006083
                                        57.517
                                               < 2e-16 ***
## depth
               -1.7086514
                           0.0060824 -280.915
                                               < 2e-16 ***
##
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.784 on 34752 degrees of freedom
     (3858 observations deleted due to missingness)
## Multiple R-squared: 0.7026, Adjusted R-squared:
## F-statistic: 2.737e+04 on 3 and 34752 DF, p-value: < 2.2e-16
```

11. What is the final set of explanatory variables that the AIC method suggests we use to predict temperature in our multiple regression? How much of the observed variance does this model explain? Is this an improvement over the model using only depth as the explanatory variable?

Answer: While depth is the best predictor, the AIC model seems to suggest that year, day, and depth are all useful in predicting temp, as removal of any of these three drives the AIC up. Removing nothing gets us the best AIC (92515.66), though just barely. Based on this model's r squared value, this model explains about 70.26% of the observed variance. This is better than our depth-only model, which explains about 67.42% of observed variance.

Analysis of Variance

12. Now we want to see whether the different lakes have, on average, different temperatures in the month of July. Run an ANOVA test to complete this analysis. (No need to test assumptions of normality or similar variances.) Create two sets of models: one expressed as an ANOVA models and another expressed as a linear model (as done in our lessons).

```
#First, wrangling data for ANOVA model:
laketemps <- chemphys.processed %>%
  group_by(lakename, sampledate) %>%
  summarise(temperature_C = sum(temperature_C))
## `summarise()` has grouped output by 'lakename'. You can override using the `.groups` argument.
summary(laketemps)
##
             lakename
                           sampledate
                                              temperature_C
## Peter Lake
                 :530
                                :0000-05-24
                                              Min.
                                                    : 71.5
                        Min.
## Paul Lake
                                              1st Qu.:118.3
                  :524
                        1st Qu.:0011-07-13
## Tuesday Lake :311
                        Median :0087-08-04
                                              Median :154.8
## West Long Lake:193
                        Mean
                               :0059-11-24
                                              Mean
                                                     :167.2
## East Long Lake:180
                        3rd Qu.:0093-09-05
                                              3rd Qu.:216.0
## Crampton Lake: 51
                        Max.
                               :0099-08-31
                                              Max.
                                                     :313.1
                                              NA's
## (Other)
                  :113
                                                     :1828
laketemps.anova <- aov(data = laketemps, temperature_C ~ lakename)</pre>
summary(laketemps.anova)
##
              Df Sum Sq Mean Sq F value Pr(>F)
## lakename
               6 55205
                            9201
                                  3.075 0.0102 *
## Residuals
              67 200504
                            2993
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 1828 observations deleted due to missingness
#Linear regression model:
laketemps.lm <- lm(data = laketemps, temperature_C ~ lakename)</pre>
summary(laketemps.lm)
##
## Call:
## lm(formula = temperature_C ~ lakename, data = laketemps)
## Residuals:
        Min
                 1Q
                       Median
                                    3Q
                               41.939 101.950
                        4.256
## -104.883 -39.121
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                          38.68 5.459 7.54e-07 ***
                              211.15
## lakenameEast Long Lake
                              -96.92
                                          49.94 -1.941
                                                          0.0565 .
## lakenameHummingbird Lake
                                          49.94 -1.258
                              -62.82
                                                          0.2128
## lakenamePaul Lake
                              -50.15
                                          41.03 -1.222
                                                         0.2259
## lakenamePeter Lake
                             -16.27
                                          39.95 -0.407
                                                         0.6852
## lakenameTuesday Lake
                             -73.06
                                          40.77 -1.792
                                                          0.0777 .
## lakenameWest Long Lake
                              -82.70
                                          54.70 -1.512
                                                         0.1353
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 54.7 on 67 degrees of freedom
## (1828 observations deleted due to missingness)
## Multiple R-squared: 0.2159, Adjusted R-squared: 0.1457
## F-statistic: 3.075 on 6 and 67 DF, p-value: 0.01018
```

Warning: Removed 141 rows containing missing values (geom_smooth).

13. Is there a significant difference in mean temperature among the lakes? Report your findings.

Answer: The ANOVA model has a small p-value (<0.05), suggesting that there is significant difference in mean temperature between lakes. The linear regression model shows a large F-statistic and a small p-statistic, suggesting that the null hypothesis can be rejected, and that there is in fact a significant variation in mean temperature across lakes. Both tests have very similar p-values, both implying a rejection of the null hypothesis. We can therefore say that there is a significant difference.

14. Create a graph that depicts temperature by depth, with a separate color for each lake. Add a geom_smooth (method = "lm", se = FALSE) for each lake. Make your points 50 % transparent. Adjust your y axis limits to go from 0 to 35 degrees. Clean up your graph to make it pretty.

```
#14.
#reusing some code from #6- looks like I was thinking ahead in using separate colors for each lake!

laketemps.plot <- ggplot(chemphys.processed, aes(x = temperature_C, y = depth, color = lakename), inher
    geom_point(alpha = 0.5) +
    geom_smooth(method= 'lm', se = FALSE, size = 1.35) +
    ylim(0, 35)

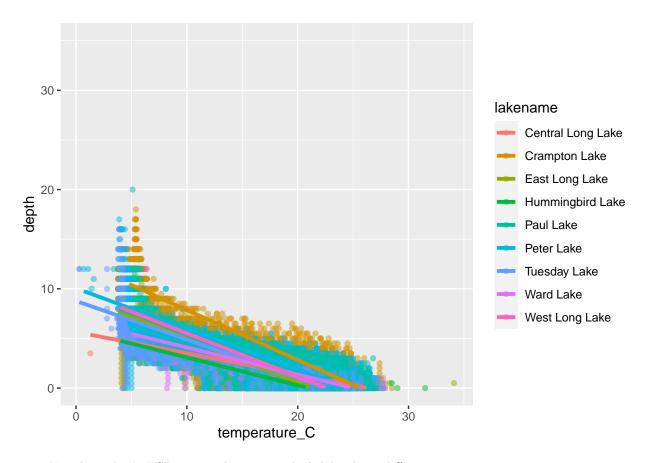
#Changed line sizes, because even with 50% opacity, the sheer number of points was making it difficult

print(laketemps.plot)

## 'geom_smooth()' using formula 'y ~ x'

## Warning: Removed 3858 rows containing non-finite values (stat_smooth).

## Warning: Removed 3858 rows containing missing values (geom_point).</pre>
```



15. Use the Tukey's HSD test to determine which lakes have different means.

#15 TukeyHSD(laketemps.anova)

```
##
     Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
  Fit: aov(formula = temperature_C ~ lakename, data = laketemps)
##
##
## $lakename
##
                                         diff
                                                     lwr
                                                                 upr
                                                                         p adj
## East Long Lake-Crampton Lake
                                   -96.916667 -248.71410
                                                          54.880767 0.4614693
## Hummingbird Lake-Crampton Lake
                                                          88.980767 0.8682843
                                  -62.816667 -214.61410
## Paul Lake-Crampton Lake
                                   -50.150000 -174.86432
                                                          74.564318 0.8830144
## Peter Lake-Crampton Lake
                                   -16.266667 -137.70461 105.171280 0.9996218
## Tuesday Lake-Crampton Lake
                                   -73.055556 -196.99764
                                                          50.886530 0.5582194
## West Long Lake-Crampton Lake
                                   -82.700000 -248.98576 83.585757 0.7368665
## Hummingbird Lake-East Long Lake
                                    34.100000 -101.67175 169.871752 0.9876065
## Paul Lake-East Long Lake
                                               -57.85249 151.385828 0.8212222
                                    46.766667
                                              -20.04103 181.341026 0.2007073
## Peter Lake-East Long Lake
                                    80.650000
## Tuesday Lake-East Long Lake
                                              -79.83628 127.558500 0.9921992
                                    23.861111
## West Long Lake-East Long Lake
                                    14.216667 -137.58077 166.014101 0.9999532
## Paul Lake-Hummingbird Lake
                                    12.666667
                                               -91.95249 117.285828 0.9997894
## Peter Lake-Hummingbird Lake
                                    46.550000 -54.14103 147.241026 0.7971086
## Tuesday Lake-Hummingbird Lake
                                   -10.238889 -113.93628 93.458500 0.9999361
## West Long Lake-Hummingbird Lake -19.883333 -171.68077 131.914101 0.9996677
```

```
## Peter Lake-Paul Lake
                                   33.883333 -17.59368
                                                         85.360348 0.4238795
## Tuesday Lake-Paul Lake
                                   -22.905556 -80.04003
                                                         34.228923 0.8844843
## West Long Lake-Paul Lake
                                                         92.164318 0.9848660
                                   -32.550000 -157.26432
## Tuesday Lake-Peter Lake
                                                         -7.212055 0.0146837
                                   -56.788889 -106.36572
## West Long Lake-Peter Lake
                                   -66.433333 -187.87128 55.004614 0.6425652
## West Long Lake-Tuesday Lake
                                   -9.644444 -133.58653 114.297641 0.9999843
```

16. From the findings above, which lakes have the same mean temperature, statistically speaking, as Peter Lake? Does any lake have a mean temperature that is statistically distinct from all the other lakes?

Answer: Crampton Actually, it seems that none of the lakes have the same mean temp as Peter Lake- the closest seems to be Crampton Lake with a -16.266667 difference- still not quite the same. Most all of the lakes seem to have mean temps that are statistically distinct from each other, based on the diff estimates and their associated p values.

17. If we were just looking at Peter Lake and Paul Lake. What's another test we might explore to see whether they have distinct mean temperatures?

Answer: We could also use a t-test to explore the difference between these two means.