# Haskell: Assignment 1

#### Notes:

- For all of the problems below, you *must* write a type signature for any function/value you write in your code.
- You should turn in the **first two problems** on Canvas in a .hs file that has the functions you define for each part.
- You should *print out Problem 3*, write your answer on that sheet, and turn it in on Thursday, October 26 in class.
- You can test your code yourself by loading your .hs file into ghci.

### Problem 1 – Factorial

For each of the following sub-problems, you are going to write a factorial function that meets a specific requirement. The following is relevant to both parts:

- The input to the function is an Int, n
- The output of the function is the mathematical factorial of the input, n!, also an Int
- You do not have to handle negative input values assume the input is 0 or greater.

## a. Guard Expression

Write the factorial function using a *guard expression*. You may want to refer to the fibonacci function fib in the lecture notes.

#### b. Pattern Matching

Write the factorial function using pattern matching (and no guards). You may want to refer to the second fibonacci function fib' from the lecture notes.

## Problem 2 - Maybe

Haskell does not have an untyped empty value like NULL in C++, nil in Ruby, None in Python, null in Java, etc. Instead, Haskell uses data types and polymorphism to reach a similar end. The type used for this is Maybe, which is defined as:

```
data Maybe a = Nothing | Just a
```

Nothing is Haskell's equivalent of NULL. But this type definition looks kind of funny, primarily because of the a.

Recall Haskell's general list type, [a]. The a is a type variable, so one way to read [a] is "a list of elements of any type". The a in Maybe a is also a type variable. So, just as we can have a list of Ints with the type [Int], we can also have a Maybe Int.

Now turning to Maybe's constructors, we have Nothing and Just a.

- Nothing is simply a constructor with no arguments by default, its type binding is Nothing :: Maybe a, but within a particular context it may be Nothing :: Maybe Int, Nothing :: Maybe String, etc.
- The Just a constructor tells us that we can use the Just constructor with an *argument of any type* (hence the type variable a).

Let's look at a few examples using Maybe's constructors.

If we bind Nothing to a symbol n and we don't assign a type, like so:

```
n = Nothing
```

Then the compiler will infer n's type to be Maybe a, since it has no way to narrow down the type variable a any further.

We could also force n to be of a more specific type:

```
n :: Maybe Int
n = Nothing

or
n = Nothing :: Maybe Int
```

The compiler can infer a bit more about a binding that uses Just:

```
j = Just "hi"
```

In this case, Haskell will infer that j's type binding must be j:: Maybe String, since we provided a String argument to the Just data constructor.

To see where Maybe might be useful, consider the function head :: [a] -> a, which returns the first element of a list. What if the input list is empty? head

wouldn't be able to return a value of the expected type. In fact, if you called head [] in ghci, you'd get an error.

Now imagine a function headMaybe with the type binding:

```
headMaybe :: [a] -> Maybe a
```

Example function calls:

```
headMaybe [1, 2, 3]
=> Just 1
headMaybe ['a', 'b', 'c']
=> Just 'a'
headMaybe []
=> Nothing
```

From these examples, we can see that headMaybe returns Just <first\_element> on success, and Nothing on failure.

Define the function headMaybe so that it behaves as described above.

Hint: All you should use on the right-hand side (RHS) of your definition are the constructors for Maybe as well as the head function mentioned above.

## Problem 3 – Reduction

Recall the Peano number data type example from lecture:

```
data Peano = Zero | Succ Peano
    deriving Show
```

In lecture, we wrote a particular definition for a function add that added two Peanos together. Our definition was longer than it needed to be, though. Here's a partial definition for a different form of the add function:

```
add :: Peano -> Peano -> Peano
add Zero p = p
```

- a. Add *one* more case to the add function's definition that completes the definition and will successful add all Peano numbers. Write the line below. *Hint: Think about the two fundamental cases in a recursive function.*
- b. Using your completed definition of add, write out the reduction steps for the expression add two one, where two = Succ (Succ Zero) and one = Succ Zero. Be sure to define your reduction rules before you do the reduction steps (there should be 4 rules in this case).

Rules:

Steps: