Contents

1	Overview	2
2	Serial	3
3	Static Decomposition	4
4	Master-Worker Scheme	5
5	Cyclic Decomposition	8
A	Appendix	10
	A.1 Serial	
	A.2 Static Decomposition	12
	A.3 Master Worker Scheme	
	A.4 Cyclic Decomposition	26

1 Overview

The codebase mandelbrot, which can be found at https://github.com/dgsaf/mandelbrot, consists of the original code provided by Associate Professor Nigel Marks, with the following additions:

- src/mandelbrot_static.f90:
- src/mandelbrot_master_worker.f90:
- src/mandelbrot_cyclic.f90:
- mandelbrot.slurm:
- mandelbrot-static.slurm:
- mandelbrot-master_worker.slurm:
- mandelbrot-cyclic.slurm:
- mandelbrot-jobs.sh:
- output/:
- bin/:
- pictures/:

2 Serial

The Mandelbrot serial code, src/mandelbrot.f90, can be found in subsection A.1. Only minor formatting adjustments have been made.

For the case of a 8000×8000 grid, the Mandelbrot serial code required $148.00\,\mathrm{s}$ to terminate.

3 Static Decomposition

The Mandelbrot MPI static decomposition code, src/mandelbrot_static.f90, can be found in subsection A.2.

For the case of a 8000×8000 grid, the Mandelbrot MPI static decomposition code required 61.605 s to terminate, when run with 10 processes. This is to say that it runs approximately 2.4 times faster than the serial code.

However, it should be noted that while this is a significant improvement, the load-balance for this scheme is far from ideal. The load-balance for the 10 processes is shown in Figure 1. It can be seen that more than half the processes spend nearly all their time idle, while a handful of other processes spend nearly all their time working. This indicates a very uneven load-balance, and that further improvements could be made if the over-worked processes were able to share their work with the under-worked processes.

It is within reason to expect load-balance problems for Mandelbrot calculations, given that each point in the grid will require an indeterminate amount of time to calculate. Furthermore, large contiguous portions of the grid may quickly terminate while other regions require far more work hence, one process may have a very easy region of the grid, while another may have a much more complex region and thus require far more time. This is to say that this problem is not ideally suited to a static decomposition.

Load-Balance for Static Decomposition

Figure 1: The load-balance for the Mandelbrot MPI static decomposition scheme, with 10 processes, where N=8000, maxiter = 1000. For each process, the percentage of time spent working is shown in blue, the percentage of time spent waiting in red, and the percentage of time spent communicating is shown in brown (however, this time is negligible and so is barely visible).

4 Master-Worker Scheme

The Mandelbrot MPI master-worker scheme code, src/mandelbrot_master_worker.f90, can be found in subsection A.3.

For the case of a 8000×8000 grid, and with chunksize = 100000, the Mandelbrot MPI master-worker scheme code required $18.548\,\mathrm{s}$ to terminate, when run with 10 processes. This is to say that it runs approximately 3.3 times faster than the MPI static decomposition code, and 8.0 times faster than the serial code. Furthermore, the load-balance is much more even across the worker processes with very little time being spent idling, by any process. The load-balance for the 9 worker processes is shown in Figure 2. The master process is not included in the analysis of the load-balancing, since it doesn't actually do any computational work, instead it simply orchestrates the work done by the worker processes. All the worker processes spend more than 99% of their time working, which is essentially ideal.

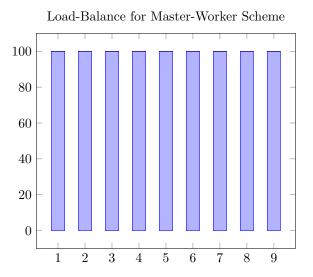


Figure 2: The load-balance for the Mandelbrot MPI master-worker scheme, with 10 processes, where N=8000, maxiter = 1000, and chunksize = 100000. For each worker process, the percentage of time spent working is shown in blue, the percentage of time spent waiting in red, and the percentage of time spent communicating is shown in brown; however, the time spent waiting and communicating is negligible and so both are barely visible.

The time taken for the Mandelbrot MPI master-worker scheme to terminate, for a 8000×8000 grid (that is, 64×10^6 data points), for varying chunk sizes is shown in Figure 3, when run with 10 processes (1 master process and 9 worker processes). It can be seen that the elapsed time is effectively maximised across a range of chunksizes which are neither too small nor too large compared to the total number of data points, with elapsed times in the range of $18 \, \mathrm{s}$ to $20 \, \mathrm{s}$.

However, for small chunk sizes, the elapsed time increases sharply (note that the code failed to execute, for a chunksize of 1, in under 10 minutes). This is to be expected as the amount of coordinating and MPI communication overhead per chunk is constant, while the total number of chunks to work on is increasing. The total time can be estimated as the product of the average time

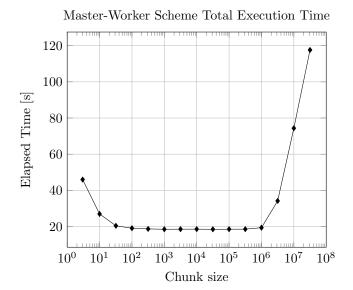


Figure 3: The total execution time for the Mandelbrot MPI master-worker scheme, with 10 processes, where N=8000, maxiter = 1000, for a range of chunk sizes, chunksize = $10^{k/2}$ for $k=1,\ldots,15$. The MPI master-worker scheme, for a chunk size of 1, failed to terminate within 10 minutes and so was disregarded.

per chunk and the number of chunks, whence it is clear that as the chunk size decreasingly tends to 1, the average time per chunk will tend to a constant, and so the total time will increase The load-balance for the 9 worker processes, for a chunksize of 10, is shown in Figure 4.

Furthermore, for large chunk sizes, the elapsed time also increases sharply, which is to be expected. As the chunk sizes become larger, the likelihood of a worker process being given a chunk which requires more time to calculate than an average chunk increases. Coupled with the fact that since there are fewer chunks to distribute among the worker processes, the likelihood for some workers to be idling while other workers finish up difficult chunks increases. Hence, the load-balance becomes less ideal and so the efficiency of the master-worker scheme decreases. At extremely large chunk sizes, some processes may not even be assigned any chunks to work on, which is obviously inefficient when it comes to load-balancing. The load-balance for the 9 worker processes, for a chunksize of 10000000, is shown in Figure 5.

Load-Balance for Master-Worker Scheme

Figure 4: The load-balance for the Mandelbrot MPI master-worker scheme, with 10 processes, where N=8000, maxiter = 1000, and chunksize = 10. For each worker process, the percentage of time spent working is shown in blue, the percentage of time spent waiting in red, and the percentage of time spent communicating is shown in brown; however, the time spent waiting is negligible and so is barely visible.

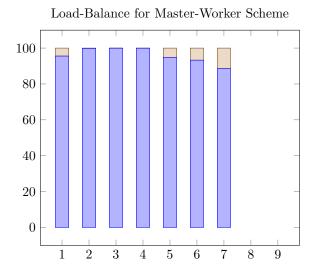


Figure 5: The load-balance for the Mandelbrot MPI master-worker scheme, with 10 processes, where N=8000, maxiter = 1000, and chunksize = 10000000. For each worker process, the percentage of time spent working is shown in blue, the percentage of time spent waiting in red, and the percentage of time spent communicating is shown in brown; however, the time spent waiting is negligible and so is barely visible. Note also that processes 8 and 9 are not present, this is due to them not being assigned any chunks at all, and thus terminated immediately.

5 Cyclic Decomposition

The Mandelbrot MPI cyclic decomposition code, src/mandelbrot_cyclic.f90, can be found in subsection A.4.

For the case of a 8000×8000 grid, the Mandelbrot MPI cyclic decomposition code required 17.393 s to terminate, when run with 10 processes. This is to say that it runs approximately 3.5 times faster than the MPI static decomposition code, and 8.5 times faster than the serial code. This is noticably faster than the MPI static decomposition code, while requiring only minor modifications, in contrast with the significant additional complexity of the MPI master-worker scheme code.

Furthermore, the load-balance is significantly more ideal than for the MPI static decomposition code. The load-balance for the 10 processes is shown in Figure 6. All the processes spend more than 95% of their time working, which is near ideal.

100 - 80 - 60 - 40 - 20 - 0 1 2 3 4 5 6 7 8 9

Load-Balance for Cyclic Decomposition

Figure 6: The load-balance for the Mandelbrot MPI cyclic decomposition scheme, with 10 processes, where N=8000, maxiter = 1000. For each worker process, the percentage of time spent working is shown in blue, the percentage of time spent waiting in red, and the percentage of time spent communicating is shown in brown. It can be seen that the only process with non-negligible communication time is the root thread. This is due to the time spent re-ordering the cyclic data gathered at the root thread into the original sequential order being included in the time spent communicating for the root process. This was chosen since while cyclic decomposition may have benefits, untangling the returned data is a significant consideration.

The improvement of the cyclic decomposition over the static decomposition can be explained by the nature of the Mandelbrot calculation. Large contiguous regions of the grid may be trivially calculated, while other regions may require far more iterations to calculate. The difficulty of a given grid point, on average for certain regions, may be similar to the difficulty of neighbouring grid points. Hence, when a static decomposition is done, one process may be assigned a trivial region while another is assigned a complex region.

However, under a cyclic decomposition, each process is assigned a number of not-necessarily neighbouring grid points - preventing the accumulation of trivial points in proximity by a single

process. Therefore, the average difficulty of each subset is likely to be much more uniform than under a static decomposition, and thus the time spent working by each process is also likely to be more uniform - leading to a more uniform load-balance. This is to say that the Mandelbrot calculation is more suited to a cyclic decomposition than a static decomposition.

A Appendix

A.1 Serial

```
1 program mandelbrot
3
     complex :: z, kappa
     integer :: green, blue, i, j, k, loop
6
     integer :: N, maxiter
    real , allocatable :: x(:)
9
     ! Timing variables.
10
    !! times
                    An array storing time markers used to determine the following
    1.1
                     timing variables.
11
12
    !! time_total Time taken overall.
13
     double precision :: times(1:2)
14
     double precision :: time_total
15
16
     ! Read command line arguments.
17
     call read_input(N, maxiter)
18
19
    allocate(x(0:N*N-1))
20
21
    call cpu_time(times(1))
22
23
     ! mandelbrot calculation
24
     do loop = 0, N*N-1
25
       ! i varies from 0 to N-1
26
       i = int(loop/N)
27
28
       ! j varies from 0 to N-1
       j = mod(loop, N)
30
       kappa = cmplx((4.0*(i-N/2)/N), (4.0*(j-N/2)/N))
31
32
       z = kappa
33
       do while (abs(z) <= 2 .and. k < maxiter)</pre>
35
        k = k+1
36
        z = z*z + kappa
37
       end do
38
39
      x(loop) = log(real(k))/log(real(maxiter))
40
41
42
     call cpu_time(times(2))
43
44
     ! Timing analysis.
45
     time_total = times(2) - times(1)
46
47
     write (*, *) &
48
         "timing for serial code:", NEW_LINE('a'), &
         " total: ", time_total
49
50
51
     ! writing data to file
     write(*, *) "Writing mandelbrot.ppm"
52
```

```
54
      open(7, file="mandelbrot.ppm", status="unknown")
 55
 56
      write(7, 100) "P3", N, N, 255
 57
      do loop = 0, N*N-1
 58
 59
        if (x(loop) < 0.5) then
         green = 2.0*x(loop)*255
 60
 61
          write(7, 110) 255-green, green, 0
 62
        else
 63
         blue = 2.0*x(loop)*255 - 255
 64
          write(7, 110) 0, 255-blue, blue
 65
        end if
 66
      end do
 67
 68 100 format(A2, /, I4, I5, /, I3)
 69 110 format(I3, /, I3, /, I3)
 70
 71
      close(7)
 72
 73
      ! Deallocate
 74
      deallocate(x)
 75
 76
    contains
 77
 78
      ! Read in the value of N, maxiter from command line arguments
 79
      subroutine read_input (N, maxiter)
        integer , intent(out) :: N, maxiter
integer :: num_args
 80
 81
 82
        character(len=20) :: arg
 83
 84
        num_args = command_argument_count()
 85
 86
        if (num_args < 2) then</pre>
         write (*, *) "Usage: <N> <maxiter>"
 87
 88
        end if
 89
 90
        if (num_args >= 1) then
 91
          call get_command_argument(1, arg)
 92
          read (arg, *) N
 93
        else
          write (*, *) "<N> not specified. Using default value, N = 2000."
 94
 95
          N = 2000
 96
        end if
 97
 98
        if (num_args >= 2) then
99
          call get_command_argument(2, arg)
100
          read (arg, *) maxiter
101
        else
102
          write (*, *) &
103
               "<maxiter> not specified. Using default value, maxiter = 1000."
104
          maxiter = 1000
105
        end if
106
107
      end subroutine read_input
108
109
    end program mandelbrot
```

A.2 Static Decomposition

```
1 !> mandelbrot_static
3 !
     Adaption of mandelbrot program to use MPI with a static decomposition of the
4
5
6
     For a NxN grid (represented in a 1D array; that is, \{0, ..., N*N - 1\}),
     with n_proc processes.
8
9
     The default chunksize, the size of the data subset to be assigned to each
10 !
     process, is defined to be the smallest integer such that
     > chunksize * n_proc >= N*N.
11 !
     This is so that even in the case where n_proc doesn't divide N*N, every
13 !
     data point is guaranteed to be covered by a process.
14
15
     Each process, p, is assigned a section of the data
16
     \{loop_min(p), ..., loop_max(p)\}\ such that
|17|! > loop_min(0) = 0
|18|! > loop_max(p) = loop_min(p+1) - 1, for p = 0, ..., n_proc - 1
19
     > loop_max(n_proc-1) = N*N - 1.
20 !
     To ensure this, we select
21 !
     > loop_min(p) = max(0, chunksize * p)
     > loop_max(p) = min(N*N-1, chunksize * (p + 1) - 1)
22 !
23 !
     We then define a process indexed chunksize array,
     > chunksize_proc(p) = loop_max(p) - loop_min(p) + 1
     whence, if n_proc divides N*N, we will have chunksize_proc(p) = chunksize.
26 program mandelbrot_static
27
28
    use mpi
29
30
     complex :: z, kappa
31
    integer :: green, blue, i, j, k, loop
32
33
     integer :: N, maxiter
34
     real , allocatable :: x(:)
35
     ! MPI variables.
37
    ! proc_id
                       ID of current MPI process.
38
    ! n_proc
                        Number of MPI processes.
39
                        Stores error code for MPI calls.
40
                        The default chunksize; the maximum possible number of loop
       chunksize
41
                        iterations assigned to each process. Defined to be the
42
                        smallest integer such that
43
                        that chunksize * n_proc >= N*N.
44
       loop_min
                        An array of the lower loop-iteration bound for each
45
                        process.
46
                        An array of the upper loop-iteration bound for each
       loop_max
47
                        process.
       chunksize_proc An array storing the size of the data subset for each
48
49
                        process. If n_proc divides N*N, then each element will
                        simply be equal to chunksize.
50
51
       x_proc
                        A work array, local to each process, which will yield the
52
                        mandelbrot data for the data subset assigned to this
53
                        process. Will have size chunksize_proc(proc_id).
                        A counter variable for looping over processes.
54
    integer :: proc_id, n_proc, err
     integer :: chunksize
```

```
57
     integer , allocatable :: loop_min(:), loop_max(:), chunksize_proc(:)
 58
      real , allocatable :: x_proc(:)
 59
      integer :: proc
 60
      ! Timing variables.
 61
 62
     ! times
                     An array storing time markers used to determine the following
 63
                     timing variables.
     1
 64
         time_setup Time taken for this process to setup MPI variables for
 65
                     partitioning data.
 66
                     Time taken for this process to perform mandelbrot calculations
        time_comp
 67
                     for its given data subset.
                    Time this process spends waiting while other processes finish
 68
     1
        time wait
 69
                     performing their calculations.
 70
                    Time taken for this process to communicate its data subset
        time_comm
 71
                     to the root process.
 72
     ! time_total Time taken overall.
 73
      double precision :: times(1:5)
 74
      double precision :: time_setup, time_comp, time_wait, time_comm, time_total
 75
 76
      ! Read command line arguments.
 77
      call read_input(N, maxiter)
 78
 79
      allocate (x(0:N*N-1))
 80
 81
      ! MPI initialisation.
 82
      call MPI_INIT(err)
 83
 84
      times(1) = MPI_WTIME()
 85
 86
      call MPI_COMM_RANK(MPI_COMM_WORLD, proc_id, err)
 87
      call MPI_COMM_SIZE(MPI_COMM_WORLD, n_proc, err)
 88
 29
      ! Determine (default) chunk size.
 90
      chunksize = ceiling(real(N*N) / real(n_proc))
 91
 92
      ! Determine loop bounds and chunk size for each process.
 93
      allocate(loop_min(0:n_proc-1))
 94
      allocate(loop_max(0:n_proc-1))
 95
     allocate(chunksize_proc(0:n_proc-1))
 96
 97
      do proc = 0, n_proc - 1
98
        loop_min(proc) = max(0, chunksize * proc)
99
        loop_max(proc) = min(N*N-1, chunksize * (proc + 1) - 1)
100
       chunksize_proc(proc) = loop_max(proc) - loop_min(proc) + 1
101
102
103
      ! Allocate work array for given process.
104
      allocate(x_proc(0:chunksize_proc(proc_id)-1))
105
106
      times(2) = MPI_WTIME()
107
108
      ! Mandelbrot calculation.
109
      ! Modified to loop only over a certain subset of indexes (due to utilising
110
      ! static decomposition).
111
      do loop = loop_min(proc_id), loop_max(proc_id)
112
       ! i varies from 0 to N-1
113
        i = int(loop/N)
114
```

```
115
        ! j varies from 0 to N-1
116
        j = mod(loop, N)
117
        kappa = cmplx((4.0*(i-N/2)/N), (4.0*(j-N/2)/N))
118
119
       k = 1
120
        z = kappa
121
       do while (abs(z) <= 2 .and. k < maxiter)</pre>
122
         k = k+1
         z = z*z + kappa
123
124
        end do
125
126
        ! x_proc is indexed to ensure all x_proc(0:chunksize_proc(proc_id)-1) are
127
       x_proc(loop-loop_min(proc_id)) = log(real(k))/log(real(maxiter))
128
129
130
131
     times(3) = MPI_WTIME()
132
133
      ! MPI wait for all process to finish.
134
     call MPI_BARRIER(MPI_COMM_WORLD, err)
135
136
      times(4) = MPI_WTIME()
137
138
      ! MPI gather the work array from each process to the root process.
139
      call MPI_GATHERV(x_proc, chunksize_proc(proc_id), MPI_REAL, x, &
140
          chunksize_proc, loop_min, MPI_REAL, 0, MPI_COMM_WORLD, err)
141
142
      times(5) = MPI_WTIME()
143
144
      ! Timing analysis.
145
     time_setup = times(2) - times(1)
146
     time_comp = times(3) - times(2)
     time_wait = times(4) - times(3)
147
     time_comm = times(5) - times(4)
148
149
     time_total = times(5) - times(1)
150
151
     if (proc_id == 0) then
152
       write (*, *) &
153
            "timing for MPI static code:", NEW_LINE('a'), &
154
            " total: ", time_total
155
156
        write (*, *) "time spent working/waiting/communicating:"
157
      end if
158
159
      call MPI_BARRIER(MPI_COMM_WORLD, err)
160
      write (*, '(a, i1, a, f5.2, a, f5.2, a, f5.2, a)') &
161
162
          " ", proc_id, ": ", &
163
          100.0*time_comp/time_total, " % / ", &
164
          100.0*time_wait/time_total, " % / ", &
          100.0*time_comm/time_total, " %"
165
166
167
      ! Write timing data to an output file.
168
      call write_timing_data (N, maxiter, n_proc, proc_id, &
169
          time_setup, time_comp, time_wait, time_comm, time_total)
170
171
      call MPI_BARRIER(MPI_COMM_WORLD, err)
172
```

```
173
      ! Writing data to file (only done by root process).
174
      if (proc_id == 0) then
175
176
        write (*, *) "Writing mandelbrot_static.ppm"
177
178
        open(7, file="mandelbrot_static.ppm", status="unknown")
179
180
        write(7, 100) "P3", N, N, 255
181
182
        do loop = 0, N*N-1
183
          if (x(loop) < 0.5) then
            green = 2.0*x(loop)*255
184
185
             write(7, 110) 255-green, green, 0
186
          else
187
             blue = 2.0*x(loop)*255 - 255
188
             write(7, 110) 0, 255-blue, blue
189
          end if
190
        end do
191
192 100 format(A2, /, I4, I5, /, I3)
193 | 110 | format(I3, /, I3, /, I3)
194
195
        close(7)
196
197
      end if
198
199
      ! Deallocate
200
      deallocate(loop_min)
201
      deallocate(loop_max)
202
      deallocate(chunksize_proc)
203
      deallocate(x_proc)
204
      deallocate(x)
205
206
      ! MPI finalisation.
207
      call MPI_FINALIZE(err)
208
209
    contains
210
211
      ! Read in the value of \ensuremath{\mathtt{N}}\xspace,\ \ensuremath{\mathtt{maxiter}}\xspace from command line arguments
212
      subroutine read_input (N, maxiter)
        integer , intent(out) :: N, maxiter
213
214
        integer :: num_args
        character(len=20) :: arg
215
216
217
        num_args = command_argument_count()
218
219
        if (num_args < 2) then</pre>
         write (*, *) "Usage: <N> <maxiter>"
220
221
        end if
222
223
        if (num_args >= 1) then
224
          call get_command_argument(1, arg)
225
          read (arg, *) N
226
227
          write (*, *) "<N> not specified. Using default value, N = 2000."
228
229
        end if
230
```

```
231
        if (num_args >= 2) then
232
          call get_command_argument(2, arg)
233
          read (arg, *) maxiter
234
        else
235
         write (*, *) &
236
              "<maxiter> not specified. Using default value, maxiter = 1000."
237
         maxiter = 1000
238
        end if
239
240
      end subroutine read_input
241
242
      ! Write the timing data (for the given parameters: N, maxiter, chunksize,
243
      ! n_proc), for a given process.
244
245
     ! The timing data includes the time taken spent: setting up, communicating,
246
     ! performing computations, waiting, and the total time spent.
247
      ! The filename is defined by (N, maxiter, n_proc, proc_id)
248
249
      subroutine write_timing_data (N, maxiter, n_proc, proc_id, &
         time_setup, time_comp, time_wait, time_comm, time_total)
250
251
        integer , intent(in) :: N, maxiter, proc_id
252
        double precision , intent(in) :: time_setup, time_comp, time_wait, &
253
            time_comm, time_total
        character(len=1000) :: timing_file
254
255
        character(len=20) :: str_N, str_maxiter, str_n_proc, str_proc_id
256
        integer :: file_unit
257
258
        ! Construct timing filename to be of the form:
259
        ! "output/timing.static.N=<N>.maxiter=<maxiter>.n_proc=<n_proc>\
260
        ! .proc_id=<proc_id>.dat"
261
        write (str_N, *) N
262
        write (str_maxiter, *) maxiter
        write (str_n_proc, *) n_proc
263
264
        write (str_proc_id, *) proc_id
265
266
        write (timing_file, *) &
267
            "output/timing.static.", &
            "N-", trim(adjustl(str_N)), ".", &
268
269
            "maxiter-", trim(adjustl(str_maxiter)), ".", &
            "n_proc-", trim(adjustl(str_n_proc)), ".", &
270
271
            "proc_id-", trim(adjustl(str_proc_id)), ".dat"
272
273
        ! Append the timing data to the data file
274
        file_unit = 10 + proc_id
275
276
        open (file_unit, file=trim(adjust1(timing_file)), action="write")
277
278
        write (file_unit, *) time_setup, time_comp, time_wait, &
279
           time_comm, time_total
280
281
        close (file_unit)
282
283
     end subroutine write_timing_data
284
285 end program mandelbrot_static
```

A.3 Master Worker Scheme

```
1 !> mandelbrot_master_worker
3 !
     Adaption of Mandelbrot program to use MPI with master_worker parallelism.
4
5
     For a NxN grid (represented in a 1D array; that is, {0, .., N*N - 1}),
6
     with n_proc processes, and a specified chunksize.
8
     The data is broken up into contiguous subsets, with size chunksize, indexed
     by an integer. Each subset defined by
9
10
     > {loop_min(task), ..., loop_max(task)} for task = 1, ..., n_task.
11
     The master process will distribute integers to the worker processes,
12 !
13
     representing which task they are to be working on. The master process will
14
     retain a ledger of which task each worker process is working on. If a worker
15
     process is not working on any task, this will be recorded in the ledger as
16
     task_ledger(proc) = no_task := 0.
     Initially, all worker processes are assigned a task to work on. The master
17 !
18 !
     thread will then wait for the workers to return the Mandelbrot data, and if
19
     there are more tasks left to work on, distribute them to the idle workers.
20
     When there are no more tasks left to work on, the master process will then
21 !
     switch to collecting unfinished tasks, and telling the workers that return
22 !
     them that there is no more to do. When all outstanding tasks have been
23
     collected, the master thread finishes the master-worker scheme.
24
25 !
     The worker processes will first receive a logical flag from the master thread
     indicating if there is any work to do. If there is, they will then receive an
27 !
     integer indicating which task (that is, which subset of the data) they will
28 !
     work on. After they have performed the Mandelbrot calculation for that subset
29
     of data, they will send the Mandelbrot data back to the master thread and
30 !
     wait for its response. When the master thread accepts the workers data, it
31 ! will tell the worker if there is more work to do, and if there is, send it
|32|! another task to perform. When there are no more tasks to work on, the worker
33
     will finish.
34
  program mandelbrot_master_worker
35
36
    use mpi
37
38
    complex :: z, kappa
39
    integer :: green, blue, i, j, k, loop
40
41
    integer :: N, maxiter
42
    real , allocatable :: x(:)
43
44
    ! MPI variables.
45
        master id
46
                        ID of current MPI process.
        proc_id
47
        n_proc
                        Number of MPI processes.
48
                         Stores error code for MPI calls.
        err
49
                        MPI tag variable.
50
                        MPI request variable.
        request
51
                        MPI status variable. Used by the master process to
52
                        determine the proc_id of worker processes returning tasks.
53
                        The number of loop iterations assigned to a process for
        chunksize
54
                         one task.
55
        n tasks
                        The number of tasks.
56
                        An array of the lower loop-iteration bounds for each
        loop_min
```

```
57
                          task.
 58
                          An array of the upper loop-iteration bounds for each
          loop_max
 59
 60
                          A work array, local to each process, which will yield the
          x_task
 61
                          mandelbrot data for the data subset assigned to this
 62
                          worker process. The master thread will use this to copy
 63
                          across the mandelbrot data returned by the worker
 64
                          processes.
 65
                          A counter variable for looping over tasks.
          task
 66
          proc
                          A counter variable for looping over processes.
 67
          proc_recv
                          The proc_id of the worker process returning a task to the
 68
                          master process.
 69
          task_recv
                          The task completed by the worker process returning a task
 70
                          to the master process.
 71
          task_ledger
                          A record (kept by the master process) of which task each
 72
                          process is currently working on. If the worker process,
 73
                          proc, isn't working on any task, then
 74
                          task_ledger(proc) = no_task.
 75
          no task
                          An integer representing an idle task; that is, no task.
 76
 77
          all_tasks_distributed
                                 A flag indicating whether or not all the tasks
 78
                          have been distributed amongst the worker process. Once the
 79
                          master thread has determined that all tasks have been
 80
                          distributed, it will send the worker threads this flag as
 81
                          they come to return tasks.
 82
     integer , parameter :: master_id = 0
 83
      integer :: proc_id, n_proc, err, tag, request
84
     integer :: status(MPI_STATUS_SIZE)
 85
     integer :: chunksize, n_tasks
 86
     integer , allocatable :: loop_min(:), loop_max(:)
 87
     real , allocatable :: x_task(:)
 88
     integer :: proc, task
 29
     integer :: proc_recv, task_recv
     logical :: all_tasks_distributed
 90
 91
     integer , allocatable :: task_ledger(:)
 92
     integer , parameter :: no_task = 0
 93
 94
      ! Timing variables.
 95
                      An array storing time markers used to determine the following
          times
 96
                      timing variables.
 97
          time_setup Time taken for this process to setup MPI variables for
98
                      partitioning data.
99
                      Time taken for a worker process to perform mandelbrot
          time_comp
100
                      calculations for its given data subset. For the master thread,
101
                      this is used to track the time it takes to copy returned data
102
                      into the final data set.
103
          time_wait
                      For a worker process, this measures the time spent waiting for
104
                      the master process to receive this workers completed task.
105
                      For the master process, this is not a suitable variable,
106
                      since time spent waiting is hard to differentiate from time
107
                      spent communicating.
108
                      For a worker process, this measures the time spent
          time_comm
                      communicating with the master thread. For the master thread,
109
110
                      this measures the all time spent communicating with the
111
                      worker process
          time_total Time taken overall.
112
113
      double precision :: times(1:8)
      double precision :: time_setup, time_comp, time_wait, time_comm, time_total
```

```
115
116
      ! Read command line arguments.
117
      call read_input(N, maxiter, chunksize)
118
119
      allocate (x(0:N*N-1))
120
121
      ! Initialise timing variables
122
      time_setup = 0d0
      time_comp = 0d0
123
124
      time_wait = 0d0
125
      time\_comm = 0d0
126
     time_total = 0d0
127
128
      ! MPI initialisation.
     call MPI_INIT(err)
129
130
131
     times(1) = MPI_WTIME()
132
133
      call MPI_COMM_RANK(MPI_COMM_WORLD, proc_id, err)
134
      call MPI_COMM_SIZE(MPI_COMM_WORLD, n_proc, err)
135
136
      ! Arbitrarily set tag = 0.
137
      tag = 0
138
139
      ! Determine number of tasks needed for given chunksize.
140
     n_tasks = ceiling(real(N*N) / real(chunksize))
141
142
      allocate(loop_min(1:n_tasks))
143
      allocate(loop_max(1:n_tasks))
144
145
      do task = 1, n_tasks
        loop_min(task) = max(0, chunksize * (task - 1))
146
147
        loop_max(task) = min(N*N-1, chunksize * task - 1)
148
149
150
      ! Default value for flag indicating all tasks have been handed out
151
      all_tasks_distributed = .false.
152
153
      ! Allocate work arrays.
154
      allocate(x_task(0:chunksize-1))
155
156
      ! Master-Worker Scheme
      if (proc_id == master_id) then
157
158
        ! Master process.
159
160
        ! Allocate process ledger (records which task a given process is working
161
162
        allocate(task_ledger(1:n_proc-1))
163
        task_ledger(:) = no_task
164
165
        times(2) = MPI_WTIME()
166
        time_setup = times(2) - times(1)
167
168
        ! Initialise task counter.
169
        task = 1
170
171
        ! Distribute initial tasks.
172
        do proc = 1, n_proc - 1
```

```
173
174
          call MPI_ISEND(all_tasks_distributed, 1, MPI_LOGICAL, proc, tag, &
175
              MPI_COMM_WORLD, request, err)
176
177
         if (all_tasks_distributed) then
178
179
            task_ledger(proc) = no_task
180
          else
            call MPI_ISEND(task, 1, MPI_INTEGER, proc, tag, MPI_COMM_WORLD, &
181
182
                request, err)
183
           task_ledger(proc) = task
184
185
           task = task + 1
186
          end if
187
188
          all_tasks_distributed = (task > n_tasks)
189
        end do
190
191
        times(3) = MPI WTIME()
192
        time_comm = time_comm + times(3) - times(2)
193
194
        ! Loop until all tasks distributed.
195
        do while (.not. all_tasks_distributed)
         times(4) = MPI_WTIME()
196
197
198
          ! Receive completed task from worker.
199
          call MPI_RECV(x_task, chunksize, MPI_REAL, MPI_ANY_SOURCE, tag, &
200
              MPI_COMM_WORLD, status, err)
201
202
          proc_recv = status(MPI_SOURCE)
203
          task_recv = task_ledger(proc_recv)
204
205
          times(5) = MPI_WTIME()
206
207
          do loop = loop_min(task_recv), loop_max(task_recv)
208
           x(loop) = x_task(loop - loop_min(task_recv))
209
210
211
          times(6) = MPI_WTIME()
212
213
          ! Tell worker there is more work to do.
214
          call MPI_ISEND(all_tasks_distributed, 1, MPI_LOGICAL, proc_recv, tag, &
215
              MPI_COMM_WORLD, request, err)
216
217
          ! Distribute new task.
218
          call MPI_ISEND(task, 1, MPI_INTEGER, proc_recv, tag, MPI_COMM_WORLD, &
219
              request, err)
220
221
          task_ledger(proc_recv) = task
222
          task = task + 1
223
224
          all_tasks_distributed = (task > n_tasks)
225
226
          times(7) = MPI_WTIME()
227
          time_comp = time_comp + times(6) - times(5)
228
          time\_comm = time\_comm + (times(5) - times(4)) + (times(7) - times(6))
229
230
        end do
```

```
231
232
        ! Collect outstanding tasks.
233
        do while (any(task_ledger /= no_task))
234
         times(4) = MPI_WTIME()
235
236
          ! Receive completed task from worker.
237
          call MPI_RECV(x_task, chunksize, MPI_REAL, MPI_ANY_SOURCE, tag, &
238
              MPI_COMM_WORLD, status, err)
239
240
          proc_recv = status(MPI_SOURCE)
241
          task_recv = task_ledger(proc_recv)
242
243
          times(5) = MPI_WTIME()
244
          do loop = loop_min(task_recv), loop_max(task_recv)
245
246
           x(loop) = x_task(loop - loop_min(task_recv))
247
          end do
248
249
          times(6) = MPI_WTIME()
250
251
          ! Tell worker there is no more work to do.
          call MPI_ISEND(all_tasks_distributed, 1, MPI_LOGICAL, proc_recv, tag, &
252
253
              MPI_COMM_WORLD, request, err)
254
255
          ! No more work to distribute.
256
          task_ledger(proc_recv) = no_task
257
258
          times(7) = MPI_WTIME()
259
260
          time_comp = time_comp + times(6) - times(5)
261
          time_comm = time_comm + (times(5) - times(4)) + (times(7) - times(6))
262
263
264
        deallocate(task_ledger)
265
266
       times(8) = MPI_WTIME()
267
268
        time_total = times(8) - times(1)
269
      else
270
        ! Worker process.
271
272
        times(2) = MPI_WTIME()
273
        time_setup = times(2) - times(1)
274
275
        ! Receive direction if there are/aren't more tasks to perform.
276
        call MPI_RECV(all_tasks_distributed, 1, MPI_LOGICAL, master_id, tag, &
277
            MPI_COMM_WORLD, status, err)
278
279
        ! Work until no more tasks to be distributed.
280
        do while (.not. all_tasks_distributed)
281
         times(3) = MPI_WTIME()
282
283
          ! Collect task to complete.
284
          call MPI_RECV(task, 1, MPI_INTEGER, master_id, tag, MPI_COMM_WORLD, &
285
              status, err)
286
287
          times(4) = MPI_WTIME()
288
```

```
289
          ! Complete task.
          x_{task}(:) = 0.0
290
          call mandelbrot_calculation(N, maxiter, loop_min(task), loop_max(task), &
291
292
              x task)
293
294
          times(5) = MPI_WTIME()
295
296
          ! Return completed task.
          call MPI_SEND(x_task, chunksize, MPI_REAL, master_id, tag, &
297
298
              MPI_COMM_WORLD, err)
299
300
          ! Receive direction if there are/aren't more tasks to perform.
301
          call MPI_RECV(all_tasks_distributed, 1, MPI_LOGICAL, master_id, tag, &
302
              MPI_COMM_WORLD, status, err)
303
304
          times(6) = MPI_WTIME()
305
306
          time_wait = time_wait + times(4) - times(3)
          time_comp = time_comp + times(5) - times(4)
307
308
          time_comm = time_comm + times(6) - times(5)
309
        end do
310
311
        times(7) = MPI_WTIME()
312
313
        time_total = times(7) - times(1)
314
      end if
315
316
      ! Timing analysis.
317
      if (proc_id == master_id) then
        write (*, *) &
318
319
            "timing for MPI master-worker code, chunksize:", chunksize, &
320
            NEW_LINE('a'), &
            " total: ", time_total
321
322
323
        write (*, *) "time spent working/waiting/communicating:"
324
325
326
      call MPI_BARRIER(MPI_COMM_WORLD, err)
327
328
      if (proc_id /= master_id) then
        write (*, '(a, i1, a, f5.2, a, f5.2, a, f5.2, a)') &
    " ", proc_id, ": ", &
329
330
331
            100.0*time_comp/time_total, " % / ", &
            100.0*time_wait/time_total, " % / ", &
332
            100.0*time_comm/time_total, " \%"
333
334
      end if
335
336
      ! Write timing data to an output file.
337
      call write_timing_data (N, maxiter, chunksize, n_proc, proc_id, &
338
          time_setup, time_comp, time_wait, time_comm, time_total)
339
340
      ! Writing Mandelbrot data to file (only done by master process).
341
      if (proc_id == master_id) then
342
343
        write (*, *) "Writing mandelbrot_master_worker.ppm"
344
345
        open(7, file="mandelbrot_master_worker.ppm", status="unknown")
346
```

```
347
        write(7, 100) "P3", N, N, 255
348
349
        do loop = 0, N*N-1
350
          if (x(loop) < 0.5) then
351
            green = 2.0*x(loop)*255
352
            write(7, 110) 255-green, green, 0
353
          else
354
            blue = 2.0*x(loop)*255 - 255
355
            write(7, 110) 0, 255-blue, blue
356
          end if
357
        end do
358
359 100 format(A2, /, I4, I5, /, I3)
360 110 format(I3, /, I3, /, I3)
361
362
      close(7)
363
364
      end if
365
366
      ! Deallocate
367
      deallocate(loop_min)
368
      deallocate(loop_max)
369
      deallocate(x_task)
370
      deallocate(x)
371
372
      ! MPI finalisation.
373
      call MPI_FINALIZE(err)
374
375 contains
376
377
      ! Mandelbrot calculation.
378
      subroutine mandelbrot_calculation (N, maxiter, lower_bound, upper_bound, x)
        integer , intent(in) :: N, maxiter, lower_bound, upper_bound
379
        real , intent(out) :: x(0:upper_bound - lower_bound)
380
381
        complex :: z, kappa
382
        integer :: loop, k
383
384
        do loop = lower_bound, upper_bound
385
          ! i varies from 0 to N-1
386
          i = int(loop/N)
387
388
          ! j varies from 0 to N-1
389
          j = mod(loop, N)
390
          kappa = cmplx((4.0*(i-N/2)/N), (4.0*(j-N/2)/N))
391
392
          k = 1
393
          z = kappa
394
          do while (abs(z) \le 2 .and. k \le maxiter)
395
           k = k+1
396
            z = z*z + kappa
397
          end do
398
399
          x(loop-lower_bound) = log(real(k))/log(real(maxiter))
400
401
      end subroutine mandelbrot_calculation
402
403
      ! Read in the value of N, maxiter, chunksize from command line arguments.
404
      subroutine read_input (N, maxiter, chunksize)
```

```
405
        integer , intent(out) :: N, maxiter, chunksize
406
        integer :: num_args
407
        character(len=20) :: arg
408
409
        num_args = command_argument_count()
410
411
        if (num_args < 3) then</pre>
412
         write (*, *) "Usage: <N> <maxiter> <chunksize>"
413
        end if
414
415
        if (num_args >= 1) then
416
         call get_command_argument(1, arg)
417
          read (arg, *) N
418
        else
419
         write (*, *) "<N> not specified. Using default value, N = 2000."
420
         N = 2000
421
        end if
422
423
        if (num_args >= 2) then
424
         call get_command_argument(2, arg)
425
          read (arg, *) maxiter
426
        else
427
          write (*, *) &
428
              "<maxiter> not specified. Using default value, maxiter = 1000."
429
         maxiter = 1000
430
        end if
431
432
        if (num_args >= 3) then
433
         call get_command_argument(3, arg)
434
          read (arg, *) chunksize
435
        else
436
          write (*, *) &
437
             "<chunksize > not specified. Using default value, chunksize = 100000."
438
          chunksize = 100000
439
        end if
440
441
      end subroutine read_input
442
443
      ! Write the timing data (for the given parameters: N, maxiter, chunksize,
444
      ! n_proc), for a given process.
445
446
      ! The timing data includes the time taken spent: setting up, communicating,
447
      ! performing computations, waiting, and the total time spent.
448
449
      ! The filename is defined by (N, maxiter, n_proc, proc_id), and the chunksize
450
      ! is included in the data output to allow for comparison of timing with
451
      ! varying chunksize.
452
      subroutine write_timing_data (N, maxiter, chunksize, n_proc, proc_id, &
453
         time_setup, time_comp, time_wait, time_comm, time_total)
454
        integer , intent(in) :: N, maxiter, chunksize, proc_id
455
        double precision , intent(in) :: time_setup, time_comp, time_wait, &
456
            time_comm, time_total
        character(len=1000) :: timing_file
457
458
        character(len=20) :: str_N, str_maxiter, str_n_proc, str_proc_id
459
        integer :: file_unit
460
461
        ! Construct timing filename to be of the form:
462
        ! "output/timing.master_worker.N=<N>.maxiter=<maxiter>.n_proc=<n_proc>\
```

```
463
        ! .proc_id=<proc_id>.dat"
464
        write (str_N, *) N
465
        write (str_maxiter, *) maxiter
466
        write (str_n_proc, *) n_proc
467
        write (str_proc_id, *) proc_id
468
469
        write (timing_file, *) &
            "output/timing.master_worker.", &
470
            "N-", trim(adjustl(str_N)), ".", &
471
            "maxiter-", trim(adjustl(str_maxiter)), ".", &
"n_proc-", trim(adjustl(str_n_proc)), ".", &
472
473
474
            "proc_id-", trim(adjustl(str_proc_id)), ".dat"
475
476
        ! Append the chunksize and timing data to the data file
        file_unit = 10 + proc_id
477
478
479
        open (file_unit, file=trim(adjustl(timing_file)), action="write", &
480
            position="append")
481
482
        write (file_unit, *) chunksize, time_setup, time_comp, time_wait, &
483
            time_comm , time_total
484
485
        close (file_unit)
486
487
      end subroutine write_timing_data
488
489
    end program mandelbrot_master_worker
```

A.4 Cyclic Decomposition

```
1 !> mandelbrot_cyclic
2
3 !
     Adaption of mandelbrot program to use MPI with a cyclic decomposition of the
4
5
6
     For a NxN grid (represented in a 1D array; that is, \{0, ..., N*N - 1\}),
     with n_proc processes.
8
9
     The default chunksize, the size of the data subset to be assigned to each
10
     process, is defined to be the smallest integer such that
     > chunksize * n_proc >= N*N.
11
     This is so that even in the case where n_proc doesn't divide N*N, every
13
     data point is guaranteed to be covered by a process. However, we note that
     the remainder of this program has not been adapted to work in cases where
14
15
     n_{proc} doesn't divide N*N. May lead to segfault errors in such a case.
16
17 !
     Each process, p = 0, ..., n_proc-1, is assigned a section of the data
     {p + (n_proc * k) , k = 0, ..., chunksize-1}, to perform the mandelbrot}
18 !
19
     calculation on.
20
21 !
     The results of each process are then gathered by the root process, and the
22 ! block-sequential arranged data is recovered from the cyclically arranged
23
24
  program mandelbrot_cyclic
25
26
    use mpi
27
28
    complex :: z, kappa
29
    integer :: green, blue, i, j, k, loop
30
31
    integer :: N, maxiter
32
    real , allocatable :: x(:)
33
34
    ! MPI variables.
35
                        ID of current MPI process.
       proc_id
                        Number of MPI processes.
       n_proc
37
                        Stores error code for MPI calls.
       err
38
                        The default chunksize; the maximum possible number of loop
        chunksize
39
                         iterations assigned to each process. Defined to be the
40
                         smallest integer such that
41
                        that chunksize * n_proc >= N*N.
42
                        Note that this program has not been adapted to work for
43
                         cases where n_proc does not divide N*N.
44
                         A work array, local to each process, which will yield the
       x_proc
45
                        mandelbrot data for the data subset assigned to this
46
                        process. Will have size chunksize.
47
       x_cyclic
                        {\tt A} work array, for the root process, which will gather the
                        cyclic data, and from which x(:) can be recovered A counter variable for looping over processes.
48
49
50
                        A counter variable used for clarity when performing cyclic
51
                        loops.
52
    integer :: proc_id, n_proc, err
53
     integer :: chunksize
54
     real , allocatable :: x_proc(:), x_cyclic(:)
     integer :: proc, 1
```

```
57
      ! Timing variables.
 58
        times
                     An array storing time markers used to determine the following
 59
                     timing variables.
 60
         time_setup Time taken for this process to setup MPI variables for
 61
                     partitioning data.
 62
        time_comp
                     Time taken for this process to perform mandelbrot calculations
 63
                     for its given data subset.
 64
         time_wait
                     Time this process spends waiting while other processes finish
                     performing their calculations.
 65
 66
                    Time taken for this process to communicate its data subset
        time_comm
 67
                     to the root process.
 68
      ! time_total Time taken overall.
 69
      double precision :: times(1:5)
 70
      double precision :: time_setup, time_comp, time_wait, time_comm, time_total
 71
 72
      ! Read command line arguments.
 73
      call read_input(N, maxiter)
 74
 75
      allocate(x(0:N*N-1))
 76
 77
      ! MPI initialisation.
 78
      call MPI_INIT(err)
 79
      times(1) = MPI_WTIME()
 80
 81
 82
      call MPI_COMM_RANK(MPI_COMM_WORLD, proc_id, err)
 83
      call MPI_COMM_SIZE(MPI_COMM_WORLD, n_proc, err)
84
 85
      ! Determine (default) chunk size.
86
      chunksize = ceiling(real(N*N) / real(n_proc))
 87
 88
      ! Allocate work array for given process.
 89
      allocate(x_proc(0:chunksize-1))
 90
      allocate(x_cyclic(0:N*N-1))
 91
 92
      times(2) = MPI_WTIME()
 93
 94
      ! Mandelbrot calculation.
 95
      ! Modified to loop only over a certain subset of indexes (due to utilising
 96
      ! cyclic decomposition).
 97
      do 1 = 0, chunksize-1
 98
        loop = (n_proc * 1) + proc_id
99
100
        ! i varies from 0 to N-1
101
        i = int(loop/N)
102
103
        ! j varies from 0 to N-1
104
        j = mod(loop, N)
105
        kappa = cmplx((4.0*(i-N/2)/N), (4.0*(j-N/2)/N))
106
107
        k = 1
108
        z = kappa
109
        do while (abs(z) <= 2 .and. k < maxiter)</pre>
110
         k = k+1
111
         z = z*z + kappa
112
        end do
113
114
        x_proc(1) = log(real(k))/log(real(maxiter))
```

```
115
     end do
116
117
      times(3) = MPI_WTIME()
118
119
      ! MPI wait for all process to finish.
      call MPI_BARRIER(MPI_COMM_WORLD, err)
120
121
122
      times(4) = MPI_WTIME()
123
124
      ! MPI gather the work array from each process to the root process.
125
      call MPI_GATHER(x_proc, chunksize, MPI_REAL, x_cyclic, chunksize, MPI_REAL, &
126
         0, MPI_COMM_WORLD, err)
127
128
      ! Extract the original data from the cyclically distributed data
129
     if (proc_id == 0) then
130
131
       do loop = 0, N*N-1
132
         proc = mod(loop, n_proc)
133
         1 = (loop - proc) / n_proc
134
135
          x(loop) = x_cyclic((chunksize*proc) + 1)
136
        end do
137
138
      end if
139
140
     times(5) = MPI_WTIME()
141
142
      ! Timing analysis.
143
     time_setup = times(2) - times(1)
     time_comp = times(3) - times(2)
144
145
     time_wait = times(4) - times(3)
146
      time\_comm = times(5) - times(4)
147
      time_total = times(5) - times(1)
148
149
     if (proc_id == 0) then
150
       write (*, *) &
151
            "timing for MPI cyclic code:", NEW_LINE('a'), &
            " total: ", time_total
152
153
154
        write (*, *) "time spent working/waiting/communicating:"
155
156
157
      call MPI_BARRIER(MPI_COMM_WORLD, err)
158
159
      write (*, '(a, i1, a, f5.2, a, f5.2, a, f5.2, a)') &
160
            ", proc_id, ": ", &
          100.0*time_comp/time_total, " % / ", &
161
          100.0*time_wait/time_total, " % / ", &
162
          100.0*time_comm/time_total, " %"
163
164
165
      ! Write timing data to an output file.
      call write_timing_data (N, maxiter, n_proc, proc_id, &
166
167
         time_setup, time_comp, time_wait, time_comm, time_total)
168
169
      call MPI_BARRIER(MPI_COMM_WORLD, err)
170
171
      ! Writing data to file (only done by root process).
172
     if (proc_id == 0) then
```

```
173
174
        write (*, *) "Writing mandelbrot_cyclic.ppm"
175
176
        open(7, file="mandelbrot_cyclic.ppm", status="unknown")
177
178
        write(7, 100) "P3", N, N, 255
179
180
        do loop = 0, N*N-1
181
         if (x(loop) < 0.5) then
182
            green = 2.0*x(loop)*255
183
            write(7, 110) 255-green, green, 0
184
          else
185
            blue = 2.0*x(loop)*255 - 255
186
            write(7, 110) 0, 255-blue, blue
187
          end if
188
        end do
189
190 100 format(A2, /, I4, I5, /, I3)
191 | 110 | format(I3, /, I3, /, I3)
192
193
        close(7)
194
195
      end if
196
197
      ! Deallocate
198
      deallocate(x_proc)
199
      deallocate(x_cyclic)
200
      deallocate(x)
201
202
      ! MPI finalisation.
203
     call MPI_FINALIZE(err)
204
205 contains
206
207
      ! Read in the value of N, maxiter from command line arguments
      subroutine read_input (N, maxiter)
208
        integer , intent(out) :: N, maxiter
integer :: num_args
209
210
211
        character(len=20) :: arg
212
213
        num_args = command_argument_count()
214
215
        if (num_args < 2) then</pre>
216
        write (*, *) "Usage: <N> <maxiter>"
217
        end if
218
219
        if (num_args >= 1) then
220
         call get_command_argument(1, arg)
221
          read (arg, *) N
222
223
          write (*, *) "<N> not specified. Using default value, N = 2000."
224
         N = 2000
225
        end if
226
227
        if (num_args >= 2) then
228
          call get_command_argument(2, arg)
229
          read (arg, *) maxiter
230
        else
```

```
231
          write (*, *) &
              "<maxiter> not specified. Using default value, maxiter = 1000."
232
233
          maxiter = 1000
234
        end if
235
236
      end subroutine read_input
237
238
      ! Write the timing data (for the given parameters: N, maxiter, chunksize,
239
      ! n_proc), for a given process.
240
241
      ! The timing data includes the time taken spent: setting up, communicating,
242
      ! performing computations, waiting, and the total time spent.
243
244
      ! The filename is defined by (N, maxiter, n_proc, proc_id)
245
      subroutine write_timing_data (N, maxiter, n_proc, proc_id, &
246
         time_setup, time_comp, time_wait, time_comm, time_total)
247
        integer , intent(in) :: N, maxiter, proc_id
248
        double precision , intent(in) :: time_setup, time_comp, time_wait, &
           time_comm, time_total
249
250
        character(len=1000) :: timing_file
251
        character(len=20) :: str_N, str_maxiter, str_n_proc, str_proc_id
252
        integer :: file_unit
253
254
        ! Construct timing filename to be of the form:
255
        ! "output/timing.cyclic.N=<N>.maxiter=<maxiter>.n_proc=<n_proc>\
256
        ! .proc_id=<proc_id>.dat"
257
        write (str_N, *) N
258
        write (str_maxiter, *) maxiter
259
        write (str_n_proc, *) n_proc
260
        write (str_proc_id, *) proc_id
261
262
        write (timing_file, *) &
            "output/timing.cyclic.", &
263
            "N-", trim(adjustl(str_N)), ".", &
264
265
            "maxiter-", trim(adjustl(str_maxiter)), ".", &
"n_proc-", trim(adjustl(str_n_proc)), ".", &
266
267
            "proc_id-", trim(adjustl(str_proc_id)), ".dat"
268
269
        ! Append the timing data to the data file
270
        file_unit = 10 + proc_id
271
272
        open (file_unit, file=trim(adjustl(timing_file)), action="write")
273
274
        write (file_unit, *) time_setup, time_comp, time_wait, &
275
            time_comm, time_total
276
277
        close (file_unit)
278
279
      end subroutine write_timing_data
280
281
    end program mandelbrot_cyclic
```