

$$v_1 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad v_2 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad v_3 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad v_4 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad v_5 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}.$$

Problem 4

Determine if the vectors are linearly independent:

- a) $\{v_1, v_2\}$ b) $\{v_1, v_2, v_3\}$ c) $\{v_1, v_2, v_5\}$ d) $\{v_2, v_3, v_4\}$ e) $\{v_1, v_2, v_3, v_4\}$

Problem 5

Compute the dimension of V , and find a base \mathcal{B} of V :

- a) $V = \text{span}(v_1, v_2)$ b) $V = \text{span}(v_1, v_2, v_3)$ c) $V = \text{span}(v_1, v_2, v_5)$
 d) $V = \text{span}(v_2, v_3, v_4)$ e) $V = \text{span}(v_1, v_2, v_3, v_4)$

Problem 6

Find all eigenvalues of A , and a base for the eigenspace E_λ for each eigenvalue λ :

- a) $A = \begin{bmatrix} 3 & 7 \\ 7 & 3 \end{bmatrix}$ b) $A = \begin{bmatrix} 1 & 1 \\ -1 & 3 \end{bmatrix}$ c) $A = \begin{bmatrix} 2 & -4 \\ 3 & -1 \end{bmatrix}$ d) $A = \begin{bmatrix} 4 & 0 & 1 \\ 0 & 5 & 0 \\ 1 & 0 & 4 \end{bmatrix}$
 e) $A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 \end{bmatrix}$ f) $A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 2 & 1 \\ 0 & 0 & 2 \end{bmatrix}$