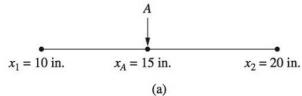
MCE 466 – Homework Assignment #7

Text problems 10.2 (Fig. a only), 10.11 (Fig. a only), 10.15a (Gauss quadrature only), and 4) 2-D Gauss quadrature problem

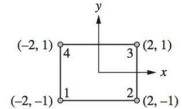
1)

For the two-noded one-dimensional isoparametric element shown in Figure P10–2 (a) and (b), with shape functions given by Eq. (10.1.5), determine (a) intrinsic coordinate s at point A and (b) shape functions N_1 and N_2 at point A. If the displacements at nodes one and two are respectively, $u_1 = 0.005$ in. and $u_2 = -0.005$ in., determine (c) the value of the displacement at point A and (d) the strain in the element.



2)

Determine the Jacobian matrix [J] and its determinant for the elements shown in Figure P10–11. Show that the determinant of [J] for rectangular and parallelogram shaped elements is equal to A/4, where A is the physical area of the element and 4 actually represents the area of the rectangle of sides 2×2 when b = 1 and h = 1 in Figure 6–20.



3)

10.15 Use Gaussian quadature with two and three Gauss points and Table 10–2 to evaluate the following integrals:

(a) $\int_{-\infty}^{1} \cos^{s} ds$

(a)
$$\int_{-1}^{1} \cos \frac{s}{2} ds$$

4) 2-D Gauss quadrature problem: Use 1x1, 2x2 and 3x3 Gauss quadrature to approximate the following integral:

$$\int_{-1}^{1} \int_{-1-1}^{1} \cos s \cos t \, ds \, dt$$