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% Shannon-Fano Encoding for Grayscale Images
clc;
clear all;
close all;

% Load and prepare image
img_data = imread("Lin-Dan.jpg");

% Convert to grayscale if needed
if size(img_data, 3) == 3
    img_data = rgb2gray(img_data);
end

% Display original image
figure;
imshow(img_data);

% Calculate histogram and probability distribution
intensity_freq = imhist(img_data);
prob_dist = intensity_freq / sum(intensity_freq);

% Extract non-zero intensity levels
active_pixels = find(prob_dist > 0) - 1;
prob_dist = prob_dist(prob_dist > 0);

% Sort by probability (descending order)
[sorted_prob, sort_indices] = sort(prob_dist, 'descend');
sorted_pixels = active_pixels(sort_indices);

% Initialize code storage
binary_codes = strings(1, length(sorted_pixels));

% Generate Shannon-Fano codes
binary_codes = encode_shannon_fano(sorted_pixels, sorted_prob, binary_codes,
1, length(sorted_prob));

% Display results
disp("Top 20 Shannon-Fano Codes for Image Symbols:");
disp("GrayLevel    Probability    Code");
disp("-----");

for k = 1:min(20, length(sorted_pixels))
    fprintf("%3d        %.6f        %s\n", ...
        sorted_pixels(k), sorted_prob(k), binary_codes(k));
end

% Calculate average code length
avg_length = 0;
for k = 1:length(sorted_prob)
    avg_length = avg_length + sorted_prob(k) * strlen(binary_codes(k));
end
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% Calculate entropy
entropy_val = 0;
for k = 1:length(sorted_prob)
    entropy_val = entropy_val - sorted_prob(k) * log2(sorted_prob(k));
end

% Display statistics
disp("-----");
fprintf("Entropy (H) = %.4f bits/pixel\n", entropy_val);
fprintf("Average Code Length (L_avg) = %.4f bits/pixel\n", avg_length);
fprintf("Coding Efficiency = %.2f %%\n", (entropy_val / avg_length) * 100);

% Shannon-Fano recursive encoding function
function code_array = encode_shannon_fano(pixel_vals, probs, code_array,
left, right)
    % Base case: single element
    if left >= right
        return;
    end

    % Calculate total probability for current range
    total_weight = sum(probs(left:right));

    % Find optimal split point
    cumulative = 0;
    partition_point = left;

    for j = left:right
        cumulative = cumulative + probs(j);
        if cumulative >= total_weight / 2
            partition_point = j;
            break;
        end
    end

    % Assign '0' to upper partition
    for j = left:partition_point
        code_array(j) = code_array(j) + "0";
    end

    % Assign '1' to lower partition
    for j = partition_point + 1:right
        code_array(j) = code_array(j) + "1";
    end

    % Recursively encode both partitions
    code_array = encode_shannon_fano(pixel_vals, probs, code_array, left,
partition_point);
    code_array = encode_shannon_fano(pixel_vals, probs, code_array,
partition_point + 1, right);
end

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Top 20 Shannon-Fano Codes for Image Symbols:

GrayLevel	Probability	Code
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1	0.210962	000
0	0.095074	001
3	0.042223	01000
2	0.042117	01001
4	0.028201	0101
15	0.021884	011000
5	0.017167	011001
16	0.016694	01101
6	0.013240	011100
14	0.012426	011101
7	0.012316	01111
13	0.011535	1000000
17	0.011094	1000001
20	0.010703	100001
8	0.010239	1000100
19	0.010146	1000101
18	0.009715	100011
9	0.008736	10010000
10	0.007622	10010001
11	0.007085	1001001

Entropy (H) = 6.0289 bits/pixel
Average Code Length (L_avg) = 6.1540 bits/pixel
Coding Efficiency = 97.97 %



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