


Command Window

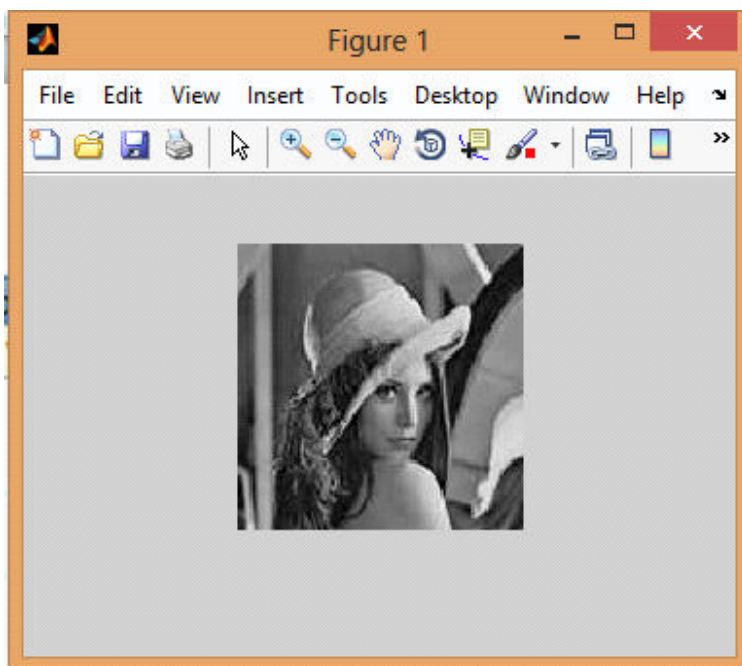
 New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

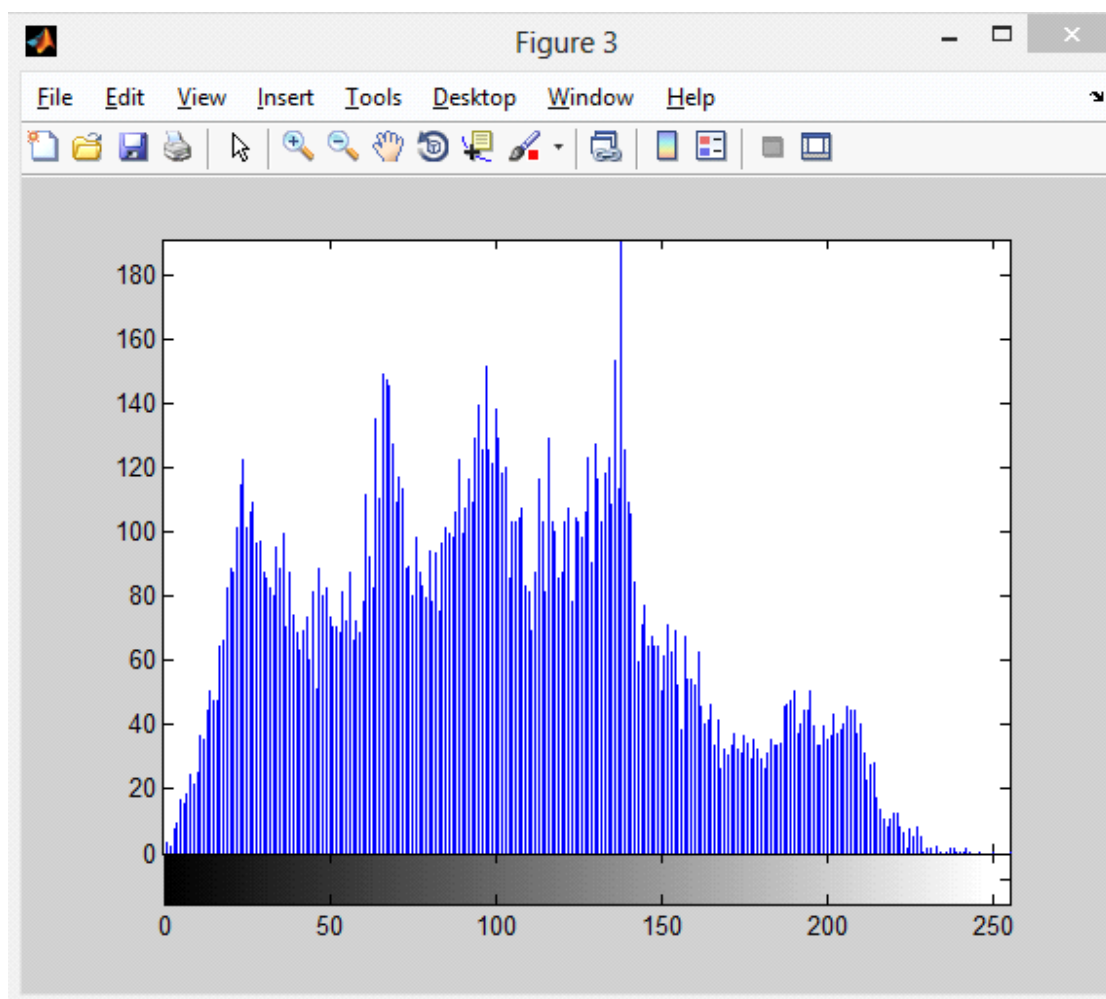
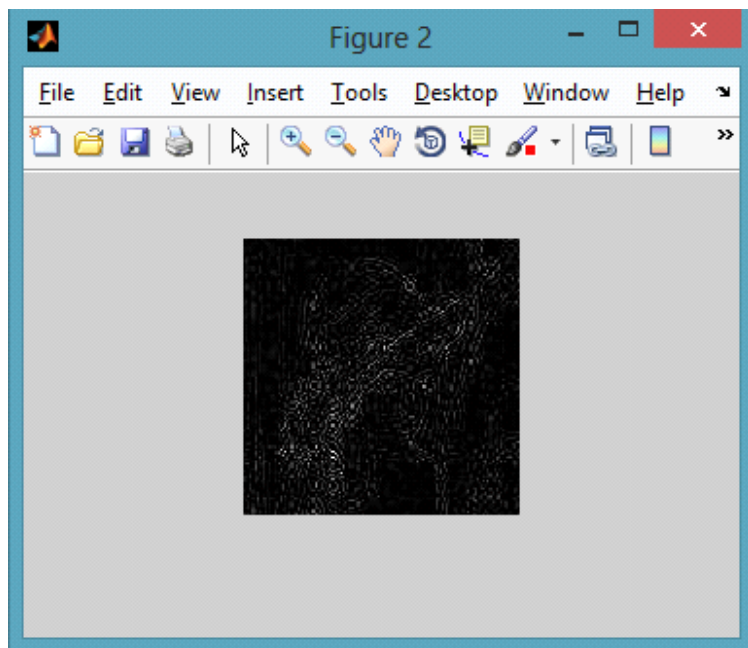
MSE: 14.67

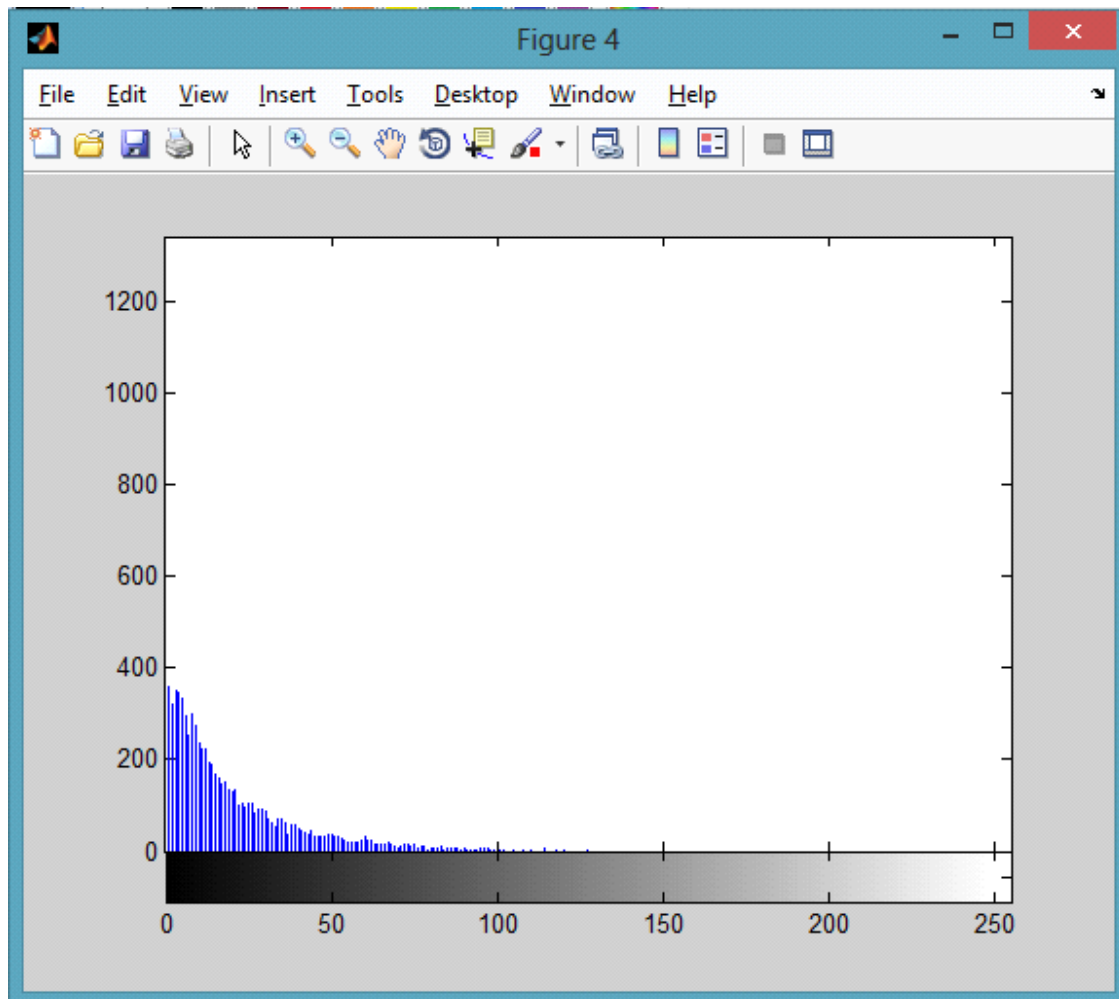
PSNR: 36.4999973 dB

MSE: 14.67

 PSNR: 36.4999973 dB>>







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%% LOSSLESS COMPRESSION-DECOMPRESSION USING DISCRETE COSINE TRANSFORM
TECHNIQUE.
function []=dct1(filename,n,m)
% "filename" is the string of characters including Image name and its
% extension.
% "n" denotes the number of bits per pixel.
% "m" denotes the number of most significant bits (MSB) of DCT
Coefficients.

% Matrix Initializations.
N=8; % Block size for which DCT is Computed.
M=8;
n=8;
m=8;
I=imread('8.tif'); % Reading the input image file and storing
intensity values in 2-D matrix I.
I_dim=size(I); % Finding the dimensions of the image file.
I_Trnsfrm.block=zeros(N,M); % Initialising the DCT Coefficients Structure
Matrix "I_Trnsfrm" with the required dimensions.

Norm_Mat=[16 11 10 16 24 40 51 61 % Normalization matrix (8 X 8) used
to Normalize the DCT Matrix.
12 12 14 19 26 58 60 55
14 13 16 24 40 57 69 56
14 17 22 29 51 87 80 62

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18 22 37 56 68 109 103 77
24 35 55 64 81 104 113 92
49 64 78 87 103 121 120 101
72 92 95 98 112 100 103 99];

save('LenaInitial.txt','I');

%% PART-1: COMPRESSION TECHNIQUE.

% Computing the Quantized & Normalized Discrete Cosine Transform.
%  $Y(k,l) = (2/\text{root}(NM)) * c(k) * c(l) * \sum_{i=0:N-1} \sum_{j=0:M-1} y(i,j) \cos(\pi(2i+1)k/(2N)) \cos(\pi(2j+1)l/(2M))$ 
% where  $c(u) = 1/\text{root}(2)$  if  $u=0$ 
%           = 1 if  $u>0$ 

for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M
        for k=1:N
            for l=1:M
                prod=0;
                for i=1:N
                    for j=1:M
                        prod=prod+double(I(N*(a-1)+i,M*(b-1)+j))*cos(pi*(k-1)*(2*i-1)/(2*N))*cos(pi*(l-1)*(2*j-1)/(2*M));
                    end
                end
                if k==1
                    prod=prod*sqrt(1/N);
                else
                    prod=prod*sqrt(2/N);
                end
                if l==1
                    prod=prod*sqrt(1/M);
                else
                    prod=prod*sqrt(2/M);
                end
                I_Trnsfrm(a,b).block(k,l)=prod;
            end
        end
        % Normalizing the DCT Matrix and Quantizing the resulting values.
        I_Trnsfrm(a,b).block=round(I_Trnsfrm(a,b).block./Norm_Mat);
    end
end

% zig-zag coding of the each 8 X 8 Block.
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M
        I_zigzag(a,b).block=zeros(1,0);
        freq_sum=2:(N+M);
        counter=1;
        for i=1:length(freq_sum)
            if i<=((length(freq_sum)+1)/2)
                if rem(i,2)~=0
                    x_indices=counter:freq_sum(i)-counter;
                else
                    x_indices=freq_sum(i)-counter:-1:counter;
                end
                index_len=length(x_indices);
                y_indices=x_indices(index_len:-1:1); % Creating reverse
of the array as "y_indices".
                for p=1:index_len
                    if I_Trnsfrm(a,b).block(x_indices(p),y_indices(p))<0

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        bin_eq=dec2bin(bitxor(2^n-
1,abs(I_Trnsfrm(a,b).block(x_indices(p),y_indices(p))),n);
        else

bin_eq=dec2bin(I_Trnsfrm(a,b).block(x_indices(p),y_indices(p)),n);
        end

I_zigzag(a,b).block=[I_zigzag(a,b).block,bin_eq(1:m)];
        end
    else
        counter=counter+1;
        if rem(i,2)~=0
            x_indices=counter:freq_sum(i)-counter;
        else
            x_indices=freq_sum(i)-counter:-1:counter;
        end
        index_len=length(x_indices);
        y_indices=x_indices(index_len:-1:1); % Creating reverse
of the array as "y_indices".
        for p=1:index_len
            if I_Trnsfrm(a,b).block(x_indices(p),y_indices(p))<0
                bin_eq=dec2bin(bitxor(2^n-
1,abs(I_Trnsfrm(a,b).block(x_indices(p),y_indices(p))),n);
                else

bin_eq=dec2bin(I_Trnsfrm(a,b).block(x_indices(p),y_indices(p)),n);
                end

I_zigzag(a,b).block=[I_zigzag(a,b).block,bin_eq(1:m)];
            end
        end
    end
end

% Clearing unused variables from Memory space
clear I_Trnsfrm prod;
clear x_indices y_indices counter;

% Run-Length Encoding the resulting code.
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M

        % Computing the Count values for the corresponding symbols and
        % saving them in "I_run" structure.
        count=0;
        run=zeros(1,0);
        sym=I_zigzag(a,b).block(1);
        j=1;
        block_len=length(I_zigzag(a,b).block);
        for i=1:block_len
            if I_zigzag(a,b).block(i)==sym
                count=count+1;
            else
                run.count(j)=count;
                run.sym(j)=sym;
                j=j+1;
                sym=I_zigzag(a,b).block(i);
                count=1;
            end
            if i==block_len
                run.count(j)=count;

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        run.sym(j)=sym;
    end
end

    % Computing the codelength needed for the count values.
    dim=length(run.count); % calculates number of symbols being
encoded.
    maxvalue=max(run.count); % finds the maximum count value in the
count array of run structure.
    codelength=log2(maxvalue)+1;
    codelength=floor(codelength);

    % Encoding the count values along with their symbols.
    I_runcode(a,b).code=zeros(1,0);
    for i=1:dim

I_runcode(a,b).code=[I_runcode(a,b).code,dec2bin(run.count(i),codelength),r
un.sym(i)];
    end
end
end
% Saving the Compressed Code to Disk.
save ('LenaCompressed.txt','I_runcode');

% Clearing unused variables from Memory Space.
clear I_zigzag run;

%% PART-2: DECOMPRESSION TECHNIQUE.

% Run-Length Decoding of the compressed image.
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M
        enc_str=I_runcode(a,b).code;

        % Computing the length of the encoded string.
        enc_len=length(enc_str);

        % Since Max. Count is unknown at the receiver, Number of bits used
for each
        % count value is unknown and hence cannot be decoded directly.
Number of bits
        % used for each count can be found out by trial and error method
for all
        % the possible lengths => factors of encoded string length.

        % Computing the non-trivial factors of the "enc_len" (length of
encoded
        % string) i.e., factors other than 1 & itself.
        factors_mat=zeros(1,0);
        if enc_len<=(n+1)
            realfact=enc_len;
        else
            for i=2:enc_len-2 % "enc_len-1" is always not a divisor
of "enc_len".
                if(mod(enc_len,i)==0)
                    factors_mat=[factors_mat,i];
                end
            end

            % Trial and Error Method to Find the Exact count value.
            for i=1:length(factors_mat)

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        flagcntr=0;
        temp_dim=enc_len/factors_mat(i);
        for j=1:temp_dim
            if strcmp(enc_str(1+(j-
1)*factors_mat(i):j*factors_mat(i)),dec2bin(0,factors_mat(i)))==0
                if j==1
                    flagcntr=flagcntr+1;
                else
                    if enc_str((j-
1)*factors_mat(i))~=enc_str(j*factors_mat(i))
                        flagcntr=flagcntr+1;
                    else
                        break;
                    end
                end
            else
                break;
            end
        end
        if flagcntr==temp_dim
            realfact=factors_mat(i);
            break;
        end
    end
end

% Clearing unused variables from Memory space
clear factors_mat flagcntr j

% Finding out the count values of corresponding symbols in the
encoded
% string and then decoding it accordingly.
dec_str=zeros(1,0);
temp_dim=enc_len/realfact;
for i=1:temp_dim
    count_str=enc_str(1+(i-1)*realfact:(i*realfact)-1);
    countval=bin2dec(count_str);
    for j=1:countval
        dec_str=[dec_str,enc_str(i*realfact)];
    end
end
I_runcode(a,b).code=dec_str;
end
end

% Clearing unused variables from Memory space
clear enc_str dec_str temp_dim realfact enc_len
clear countval count_str

% Reconstructing the 8 X 8 blocks in Zig-Zag fashion.
I_rec_Trnsfm.block=zeros(N,M);
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M
        bpp=length(I_runcode(a,b).code)/(N*M); % "bpp" is the bits-per-
pixel in reconstruction of image.
        bpp_diff=n-bpp;
        freq_sum=2:(N+M);
        counter=1;
        c_indx=1;
        for i=1:length(freq_sum)
            if i<=((length(freq_sum)+1)/2)
                if rem(i,2)~=0

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        x_indices=counter:freq_sum(i)-counter;
    else
        x_indices=freq_sum(i)-counter:-1:counter;
    end
    index_len=length(x_indices);
    y_indices=x_indices(index_len:-1:1); % Creating reverse
of the array as "y_indices".
    for p=1:index_len
        decm_eq=bin2dec([I_runcode(a,b).code(1+m*(c_indx-
1):m*c_indx),dec2bin(0,bpp_diff)]);
        if decm_eq>(2^(n-1))-1
            decm_eq=decm_eq-(2^n-1);
        end

I_rec_Trnsfm(a,b).block(x_indices(p),y_indices(p))=decm_eq;
        c_indx=c_indx+1;
    end
else
    counter=counter+1;
    if rem(i,2)~=0
        x_indices=counter:freq_sum(i)-counter;
    else
        x_indices=freq_sum(i)-counter:-1:counter;
    end
    index_len=length(x_indices);
    y_indices=x_indices(index_len:-1:1); % Creating reverse
of the array as "y_indices".
    for p=1:index_len
        decm_eq=bin2dec([I_runcode(a,b).code(1+m*(c_indx-
1):m*c_indx),dec2bin(0,bpp_diff)]);
        if decm_eq>(2^(n-1))-1
            decm_eq=decm_eq-(2^n-1);
        end

I_rec_Trnsfm(a,b).block(x_indices(p),y_indices(p))=decm_eq;
        c_indx=c_indx+1;
    end
end
end
end
end

% Clearing unused variables from Memory space
clear I_runcode x_indices y_indices
clear c_indx freq_sum

% Denormalizing the Reconstructed Tranform matrix using the same
% Normalization matrix.
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M
        I_rec_Trnsfm(a,b).block=(I_rec_Trnsfm(a,b).block).*Norm_Mat;
    end
end

% Inverse-Discrete Cosine Transform on the reconstructed Matrix.
%  $y(i,j) = (2/\text{root}(NM)) * \sum_{i=0}^{N-1} \sum_{j=0}^{M-1}$ 
Y(k,1)c(k)*c(1)*cos(pi(2i+1)k/(2N))*cos(pi(2j+1)l/(2M))
% where c(u)=1/root(2) if u=0
%           = 1 if u>0
for a=1:I_dim(1)/N
    for b=1:I_dim(2)/M

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        for i=1:N
            for j=1:M
                prod=0;
                for k=1:N
                    for l=1:M
                        if k==1

temp=double(sqrt(1/2)*I_rec_Trnsfm(a,b).block(k,l))*cos(pi*(k-1)*(2*i-
1)/(2*N))*cos(pi*(l-1)*(2*j-1)/(2*M));
                        else

temp=double(I_rec_Trnsfm(a,b).block(k,l))*cos(pi*(k-1)*(2*i-
1)/(2*N))*cos(pi*(l-1)*(2*j-1)/(2*M));
                        end
                        if l==1
                            temp=temp*sqrt(1/2);
                        end
                        prod=prod+temp;
                    end
                end
                prod=prod*(2/sqrt(M*N));
                I_rec((a-1)*N+i,(b-1)*M+j)=prod;
            end
        end
    end

% Clearing unused variables from Memory Space.
clear I_rec_Trnsfm

% Displaying the Reconstructed Image.
diff=im2double(I)*255-I_rec;
diff=diff/max(max(diff));
diff=im2uint8(diff);
I_rec=I_rec/max(max(I_rec));
I_rec=im2uint8(I_rec);
figure,imshow(I_rec,[0,2^n-1]);
figure,imshow(diff,[0 2^n-1])
figure, imhist(I_rec);
figure, imhist(diff);

n=size(I);
M=n(1);
N=n(2);
MSE = sum(sum((I- I_rec).^2))/(M*N);
PSNR = 10*log10(256*256/MSE);
fprintf('\nMSE: %7.2f ', MSE);
fprintf('\nPSNR: %9.7f dB', PSNR);

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