

Tutorial No.7

Context Free Grammar

1. What language is generated by following CFG: (CO1)

- a. $S \rightarrow aSa | bSb | \Lambda$
- b. $S \rightarrow aSa | bSb | a | b$
- c. $S \rightarrow aSb | bSa | \Lambda$
- d. $S \rightarrow aSa | bSb | aAb | bAa$
 $A \rightarrow aAa | bAb | a | b | \Lambda$

2. Find CFG generating following language: (CO4)

- a. $L = \{ XcX^R \mid X \in \{a,b\}^* \}$
- b. $L = \{ a^m b^n \mid m > n \text{ and } n > 0 \}$
- c. The set of odd length string in $\{a,b\}^*$ with middle symbol a.
- d. The set of even length string in $\{a,b\}^*$ with middle two symbols equal.
- e. The set of odd length string in $\{a,b\}^*$ whose first, middle and last symbols same.
- f. $L = \{ a^i b^j c^k \mid j=i \text{ or } j=k \}$
- g. $L = \{ a^i b^j c^k \mid i = j+k \}$
- h. $L = \{ a^i b^j \mid i \leq 2j \}$

3. Show following grammar as ambiguous grammar: (CO4)

- a. $E \rightarrow E+E \mid E^*E \mid a$
- b. $S \rightarrow aAS \mid a$
 $A \rightarrow SbA \mid SS \mid ba$
- c. $S \rightarrow aS \mid \Lambda$
 $S \rightarrow aSbS$

4. Convert Following Grammar to CNF form: (CO4)

- a. $S \rightarrow PQP$
 $P \rightarrow OP \mid \Lambda$
 $Q \rightarrow 1Q \mid \Lambda$
- b. $S \rightarrow AACD$
 $A \rightarrow aAb \mid \Lambda$
 $C \rightarrow aC \mid a$
 $D \rightarrow aDa \mid bDb \mid \Lambda$

5. Write Regular Grammar for: (CO4)

- a. $L = \{ x \mid n_0(x) \text{ and } n_1(x) \text{ are even} \}$
- b. $L = \{ a^n b^m \mid n, m \geq 0 \}$
- c. $r = a^* + b^*$