

Experiment No.: 9

Title: Write python program to demonstrate statistical testing.

Objectives:

1. To learn how to apply statistical testing.

Theory:

Hypothesis testing:

Hypothesis testing is a statistical method that is used in making statistical decisions using experimental data. Hypothesis Testing is basically an assumption that we make about the population parameter.

Ex : you say avg student in class is 40 or a boy is taller than girls.

all those example we assume need some statistic way to prove those. we need some mathematical conclusion whatever we are assuming is true.

Hypothesis testing is an essential procedure in statistics. A **hypothesis test** evaluates two mutually exclusive statements about a population to determine which statement is best supported by the sample data.

parameter of hypothesis testing:

Null hypothesis :- In inferential statistics, the null hypothesis is a general statement or default position that there is no relationship between two measured phenomena, or no association among groups

In other words it is a basic assumption or made based on domain or problem knowledge.

Example : a company production is = 50 unit/per day etc.

Alternative hypothesis :-

The alternative hypothesis is the hypothesis used in **hypothesis** testing that is contrary to the null hypothesis. It is usually taken to be that the observations are the result of a real effect (with some amount of chance variation superposed)

Example : a company production is !=50 unit/per day etc

Level of significance: Refers to the degree of significance in which we accept or reject the null-hypothesis. 100% accuracy is not possible for accepting or rejecting a hypothesis, so we therefore select a level of significance that is usually 5%.

This is normally denoted with α (maths symbol) and generally it is 0.05 or 5%, which means your output should be 95% confident to give similar kind of result in each sample.

Type I error: When we reject the null hypothesis, although that hypothesis was true. Type I error is denoted by α . In hypothesis testing, the normal curve that shows the critical region is called the alpha region

Type II errors: When we accept the null hypothesis but it is false. Type II errors are denoted by β . In Hypothesis testing, the normal curve that shows the acceptance region is called the beta region.

One tailed test :- A test of a statistical hypothesis, where the region of rejection is on only one side of the sampling distribution, is called a **one-tailed test**.

Example :- a college has ≥ 4000 student or data science $\leq 80\%$ org adopted.

Two-tailed test :- A **two-tailed test** is a statistical test in which the critical area of a distribution is **two-sided** and tests whether a sample is greater than or less than a certain range of values. If the sample being tested falls into either of the critical areas, the alternative hypothesis is accepted instead of the null hypothesis

P-value :- The **P value**, or calculated probability, is the probability of finding the observed, or more extreme, results when the null hypothesis (H_0) of a study question is true — the **definition** of ‘extreme’ depends on how the hypothesis is being tested.

If your P value is less than the chosen significance level then you reject the null hypothesis i.e. accept that your sample gives reasonable evidence to support the alternative hypothesis. It does NOT imply a “meaningful” or “important” difference; that is for you to decide when considering the real-world relevance of your result.

Example : you have a coin and you don't know whether that is fair or tricky so let's decide **null** and **alternate hypothesis**

H₀ : a coin is a fair coin.

H1 : a coin is a tricky coin. and **alpha** = **5% or 0.05**

Now let's toss the coin and calculate **p- value** (probability value).

Toss a coin 1st time and result is **tail**- P-value = 50% (as head and tail have equal probability)

Toss a coin 2nd time and result is **tail**, now **p-value** = $50/2 = 25\%$

and similarly we Toss 6 consecutive time and got result as P-value = **1.5%** but we set our significance level as 95% means 5% error rate we allow and here we see we are beyond that level i.e. our null- hypothesis does not hold good so we need to reject and propose that this coin is a tricky coin which is actually.

Degree of freedom :- Now imagine you're not into hats. You're into data analysis. You have a data set with 10 values. If you're not estimating anything, each value can take on any number, right? Each value is completely free to vary. But suppose you want to test the population mean with a sample of 10 values, using a 1-sample t test. You now have a constraint — the estimation of the mean. What is that constraint, exactly? By definition of the mean, the following relationship must hold: The sum of all values in the data must equal $n \times \text{mean}$, where n is the number of values in the data set.

So if a data set has 10 values, the sum of the 10 values *must* equal the mean \times 10. If the mean of the 10 values is 3.5 (you could pick any number), this constraint requires that the sum of the 10 values must equal $10 \times 3.5 = 35$.

With that constraint, the first value in the data set is free to vary. Whatever value it is, it's still possible for the sum of all 10 numbers to have a value of 35. The second value is also free to vary, because whatever value you choose, it still allows for the possibility that the sum of all the values is 35

T- Test :- A t-test is a type of inferential statistic which is used to determine if there is a significant difference between the means of two groups which may be related in certain features. It is mostly used when the data sets, like the set of data recorded as outcome from flipping a coin a 100 times, would follow a normal distribution and may have

unknown variances. T test is used as a hypothesis testing tool, which allows testing of an assumption applicable to a population.

T-test has 2 types : 1. one sampled t-test 2. two-sampled t-test.

One sample t-test : The One Sample t Test determines whether the sample mean is statistically different from a known or hypothesised population mean. The One Sample t Test is a parametric test.

Example :- you have 10 ages and you are checking whether avg age is 30 or not

```
from scipy.stats import ttest_1samp
import numpy as np
ages = np.genfromtxt("ages.csv")
print(ages)
ages_mean = np.mean(ages)
print(ages_mean)
tset, pval = ttest_1samp(ages, 30)
print("p-values",pval)
if pval < 0.05: # alpha value is 0.05 or 5%
    print(" we are rejecting null hypothesis")
else:
    print("we are accepting null hypothesis")
```

Two sampled T-test :-The Independent **Samples t Test** or 2-sample t-test compares the means of two independent groups in order to determine whether there is statistical evidence that the associated population means are significantly different. The Independent **Samples t Test** is a parametric **test**. This **test** is also known as: Independent **t Test**.

Example : is there any association between week1 and week2

```
from scipy.stats import ttest_ind
import numpy as np
week1 = np.genfromtxt("week1.csv", delimiter=",")
week2 = np.genfromtxt("week2.csv", delimiter=",")
print(week1)
print("week2 data :-\n")
print(week2)
week1_mean = np.mean(week1)
week2_mean = np.mean(week2)
print("week1 mean value:",week1_mean)
print("week2 mean value:",week2_mean)
week1_std = np.std(week1)
week2_std = np.std(week2)
```

```
print("week1 std value:",week1_std)
print("week2 std value:",week2_std)ttest,pval = ttest_ind(week1,week2)
print("p-value",pval)
if pval <0.05:
    print("we reject null hypothesis")
else:
    print("we accept null hypothesis")
```

Paired sampled t-test :- The paired sample t-test is also called dependent sample t-test. It's an uni variate test that tests for a significant difference between 2 related variables. An example of this is if you where to collect the blood pressure for an individual before and after some treatment, condition, or time point.

H0 :- means difference between two sample is 0

H1:- mean difference between two sample is not 0