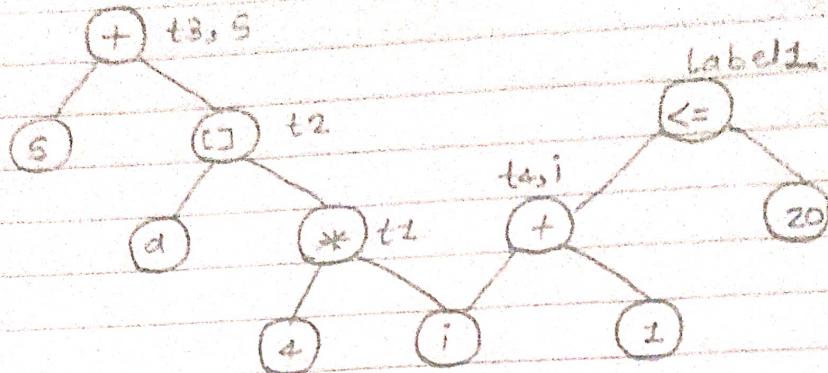


DAG =



Q.12] Generate DAG representation of following code & list out the application of DAG.

```
I = 1;  
while (I <= 10)  
DO  
Sum! = a[i]
```

→

Applications =>

1) DAG (directed acyclic graph) is a useful data structure for implementing transformations on basic blocks.

2) DAG is used in -

i) Determining the common subexpression.

ii) Determining which names are used inside the block & computed outside the block.

- iii) Determining which statements of the block could have their computed value outside the block.
- iv) Simplifying the list of quadruples by eliminating the common subexpression.

Q.9) Explain register allocation and assignment with the suitable example?



- Efficient utilization of limited set of registers is important to generate good code.
- Registers are assigned by -

1) Register allocation

2) Register assignment

- Register allocation is to select the set of variables that will reside in registers at a point in the code.

- Register assignment is to pick the specific register that a variable will reside in.

- This approach has the advantage that it simplifies the design of a compiler.

- Disadvantage is that, applied too strictly, it uses registers inefficiently.

- There are various strategies used in register allocation and assignment that are -

1) Global Register Allocation

2) Usage Counts

3) Register Assignment for outer loops

4) Register Allocation by Graph coloring.

Example =

$$t := a * b$$

$$t := t + a$$

$$t := t / d$$

$$\Downarrow \{ R_1 = t \}$$

$$MOV a, R_1$$

$$MUL b, R_1$$

$$ADD a, R_1$$

$$DIV d, R_1$$

$$MOV R_1, t$$

$$t := a * b$$

$$t := t + a$$

$$t := t / d$$

$$\Downarrow \{ R_0 = a, R_1 = t \}$$

$$MOV a, R_0$$

$$MOV R_0, R_1$$

$$MUL b, R_1$$

$$ADD R_0, R_1$$

$$DIV d, R_1$$

$$MOV R_1, t$$

Q.10] Explain node listing and labeling algorithm with example.



Node Listing Algorithm ⇒

While unlisted interior nodes remain do begin

select an unlisted node n , all of whose parents have been listed;

list n ;

while the leftmost child m of n has no unlisted parents and is not a leaf do begin

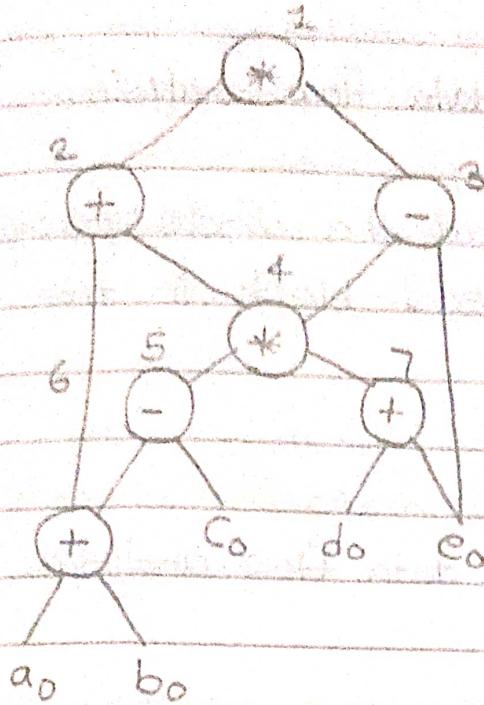
list m ;

$n := m$;

end

end

Exp :-



$t_7 := d + e$
 $t_6 := a + b$
 $t_5 := t_6 - c$
 $t_4 := t_5 - t_7$
 $t_3 := t_4 - e$
 $t_2 := t_6 + t_4$
 $t_1 := t_2 * t_3$

The labeling algorithm =>

if n is a leaf then

if n is the leftmost child of its parent then

$\text{label}(n) := 1$

else

$\text{label}(n) := 0$

else begin

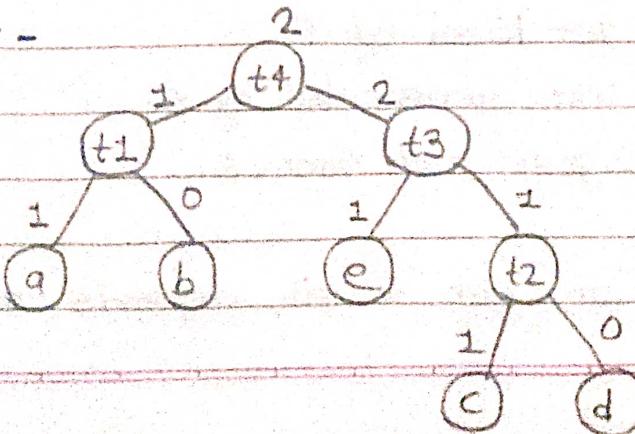
let n_1, n_2, \dots, n_k be the children of n ordered by

label so that $\text{label}(n_1) > \text{label}(n_2) > \dots > \text{label}(n_k)$;

$\text{label}(n) := \max_{1 \leq i \leq k} (\text{label}(n_i) + i - 1)$

end

Exp:-



Q. 3) Explain global data flow analysis using data flow equations.

OR

Q. 14] Discuss in detail about global data flow analysis.



- Collect information about the whole program & distribute the information to each block in the flow graph.

Data flow information :-

- Information collected by data flow analysis.

Data flow equations :-

- A set of equations solved by DFA to gather data flow information.

- Component of data flow equations :-

Sets containing collected information =

1) in set = info. coming into BB from outside

2) gen set = info collected within BB

3) kill set = info collected within BB, will affect.

4) Out set = info leaving the BB.

- A typical data flow equation :

$$\text{out}[s] = \text{gen}[s] \cup (\text{in}[s] - \text{kill}[s])$$

where,

s : statement

in[s] : info goes into s

kill[s] : info get killed by s

gen[s] : New info. generated by s

out[s] : Info. goes out from s.

- The notation of gen & kill depends on the desired information.

- In some cases, it may be defined in terms of out-equation is solved as analysis traverses in the backward direction.

- Data flow analysis follows control flow graph. Equations are set at the level of basic blocks, or even for a statement.

Q.8] Explain structure preserving transformation techniques with example.



a) Common subexpression elimination \Rightarrow

$$a := b + c \quad a := b + c$$

$$b := a - d \quad \Rightarrow \quad b := a - d$$

$$c := b + c \quad c := b + c$$

$$d := a - d \quad d := b \quad d := b$$

Since the second and fourth expressions compute the same expression, the basic block can be transformed as above.

b) Dead-code elimination \Rightarrow

Suppose x is dead, that is never subsequently used, at the point where the statement $x := y + z$ appears in basic block.

$$i = 0;$$

$$\text{if } (i == 1) \quad \Rightarrow \quad i = 0;$$

$$a = x + 5;$$

c) Renaming temporary variables \Rightarrow

A statement $t := b + c$ can be changed to $u := b + c$ and all uses of this instance of t can be changed to u without changing the value of basic block. Such a block is called a normal-form block.

d) Interchange of statements \Rightarrow

- Suppose a block has the following two adjacent statements.

Suppose,

Statements : $t1 := b + c$

$t2 := x + y$

- We can interchange the two statements without affecting the value of the block if & only if neither x nor y is t and neither b nor c is t .

Q. 13] Explain principles sources of optimization.

\rightarrow

- 1) Common Sub expression elimination
- 2) Copy propagation
- 3) Dead - Code elimination
- 4) Constant folding.

Refer Tut 6, Q. 1]

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Tutorial No. 8

Page No.:
Date: youuu

Q.1] Explain activation tree and control stack with example?



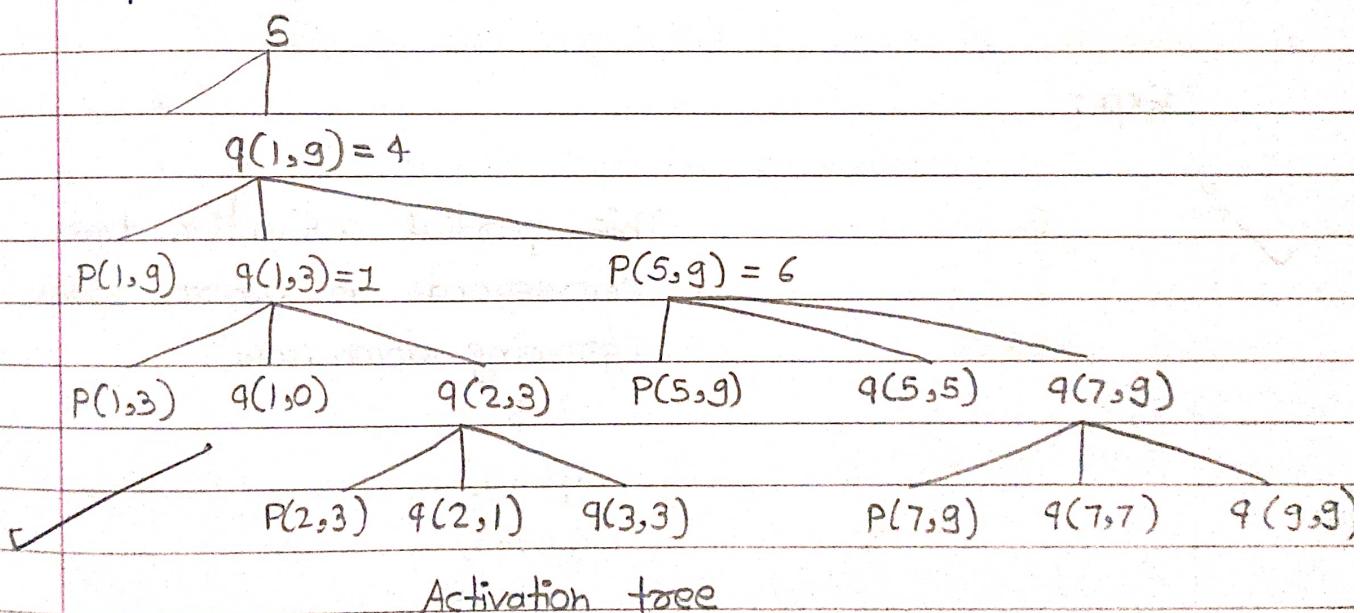
- Every execution of a procedure is called an activation.

- The lifetime of an activation of procedure P is the sequence of steps between the first and last step of P's body, including any procedures called while P is running.

- If the procedure is recursive, several of its activation may be alive at the same time.

- Therefore, each execution of procedure body is referred to as activation of procedure.

Exp:



- Each node represents the activation of a procedure.

- Each root represents activation of a main program.

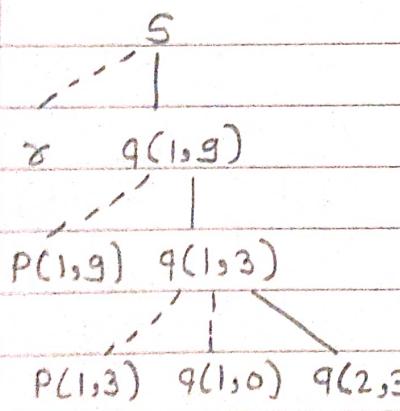
- Any node from A to B, if and only if control flows from A to B.

- If node A is parent node, if and only if control flows from A to B.
- If A is left child node of B, if lifetime of A occurs before lifetime of B.

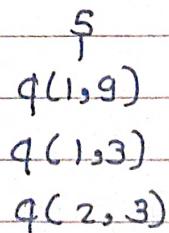
Control Stacks =

- We can use a stack to keep track of currently-active activations.
- We push a record onto the stack when a procedure is called and pop that record off the stack when the procedure returns.
- At any point in time, the control stack represents a path from the root of activation tree to one of the nodes.

Exp:



This partial activation tree corresponds to control stack (growing downward)



Q.2) Explain stack allocation with example?



- Stack keep track of procedure activations
- Manage runtime allocation with a stack storage
- Local data are allocated on the stack.

- Stack allocation is a procedure in which stack is used to organize the storage.
- The stack used in stack allocation is known as control stack.
- In this type of allocation, creation of data objects is performed dynamically.
- In stack allocation, activation records are created for the allocation of memory.
- These activation records are pushed onto the stack using last in first out (LIFO) method.
- Locals are stored in activation records at run time and memory addressing is done by using pointers and registers.
- In this the allocation / deallocation is automatic.
- It is less expensive & space for allocation is limited.
- It cannot support recursion.

Q.3] Explain what is activation record? Explain the contents of activation record?

→ - Any information needed for a single activation of a procedure is stored in ACTIVATION RECORD, sometimes called the STACK FRAME.

- A pointer to the current activation record is maintained in a register.

Actual Parameters
Returned value
Control link
Access link
Saved machine status
Local data
Temporaries

1) Temporaries =
evaluation of expression

2) Local data =
field for local data

3) Saved machine status =
Information about the machine state before the procedure call.

- Return address (value of program counter)
- Register contents

4) Access link =
access nonlocal data

5) Control links =

Points to the activation record of the caller.

6) Returned values =

Space for the value to be returned.

7) Actual parameters =

Space for actual parameters.

Q.4] Explain dynamic storage allocation strategies?



Dynamic storage allocation strategies =>

- 1) Stack allocation
- 2) Heap allocation

1) Stack allocation =

- The stack allocation is a runtime storage management technique. The activation records are pushed and popped as activations begin and end respectively.

- Storage for the locals in each call of the procedure is contained in the activation record for that call.

- Thus, locals are bound to fresh storage in each activation, because a new activation record is pushed onto stack when the call is made.

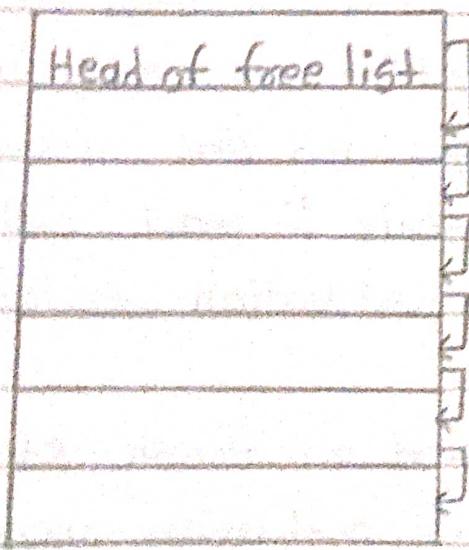
- It can be determined the size of the variables at a run time & hence local variables can have different storage locations & different values during various activations.

2) Heap Storage Allocation =

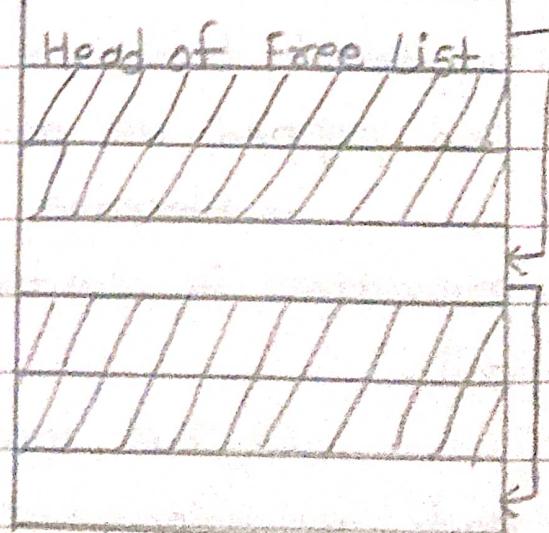
- It enables the allocation of memory in a Non-nested design. Storage can be allocated & freed arbitrarily from an area known as heap.
- Heap allocation is helpful for executing data whose size varies as the program is running.
- Heap is maintained as a list of free space called free space list.

Activation Record of C
— — of B
— — of A

fig. Stack Allocation



Initial Free Space list



Free Space After Execution

fig. Heap Storage Allocation

Q.5]

Explain following parameter passing methods:

a) Call by Value =

- The actual parameters are evaluated & their σ -values are passed to called procedure.
- The formal parameters do not changes the value of actual parameter.
operation on
- The arguments are evaluated at the time of call and the value parameters are copied and either behave as -
 - a) behave as constant values during executing of procedure.
 - b) are viewed as initialized local variables.

Exp:

callByValue (int y)
{

y = y + 1;

print (y);

}

main ()

{

int x = 42;

print (x);

callByValue (x);

print (x);

}

Output :

x = 42

y = 43

x = 42

\leftarrow x's value does not changes when y's value is changed.

b) Call by value result =

- The arguments are evaluated at call time and the value parameters are copied and used as local variables.

- The final values of these variables are copied back to the location of the arguments when the procedure exits.

Exp :

callByValueResult (int y, int z)

{

y = y+1; z = z+1;

print (y);

print (z);

}

main ()

{

int x = 42;

print (x);

callByValueResult (x, x);

print (x);

}

Output :

x = 42

y = 43

z = 43

x = 43 ↙

Note that x's value is different from both using call-by-value and call-by-Reference.

c) Call by name =

- The procedure body is substituted for call in caller with actual parameters substituted for formals.
- The actual parameters can be surrounded by parenthesis to preserve their integrity.
- The local name of called procedure and names of calling procedure are distinct.

Exp :

```
callByName (int closure y)
{
```

```
    point(y);
```

```
    point(y);
```

```
}
```

```
main()
```

```
{
```

```
    int x = 42;
```

```
    point(x);
```

```
    callByName ( [[x = x+1]] );
```

```
    point(x);
```

```
}
```

Output :

x = 42

y = 43

y = 44

x = 44

↑

x's value changes
when y is evaluated

d) Call by reference =

- The arguments must have allocated memory locations.

- The compiler passes the address of the variable, and the parameter becomes an alias for the argument.

- Local accesses to the parameter are turned into indirect accesses.

Exp :

```
callByRef (int &y)
```

```
{  
    y = y + 1;  
    print(y);  
}
```

```
main ()  
{
```

```
    int x = 42;  
    print(x);  
    callByRef (x);  
    print(x);  
}
```

Output :

x = 42

y = 43

x = 43

↑ x's value changes when
y's value is changed.

Refer:

Tutorial No. 5

SDT & TAC

Unit No. 5

Q.1] $x = a + a * (b - c) + (b - c) * d$

Write the grammar and SDD to evaluate the below expression & construct syntax tree.

$$x := 2 + 2 * (5 - 3) + (7 - 6) * 4$$



$$S \rightarrow id : E \quad \{ \text{gen } (\text{id.name}) = E.\text{place} \}$$

$$E \rightarrow E + T \quad \{ E.\text{val} = E.\text{val} + T.\text{val} \}$$

$$E \rightarrow E - T \quad \{ E.\text{val} = E.\text{val} - T.\text{val} \}$$

$$E \rightarrow T \quad \{ E.\text{val} = T.\text{val} \}$$

$$T \rightarrow T * F \quad \{ T.\text{val} = T.\text{val} * F.\text{val} \}$$

$$T \rightarrow F \quad \{ T.\text{val} = F.\text{val} \}$$

$$F \rightarrow \text{num} \quad \{ F.\text{val} = \text{num.lval} \}$$

$$S = x = -8$$

$$\begin{array}{c} | \\ id : E.\text{val} = -8 \end{array}$$

$$\begin{array}{ccc} | & & | \\ x & & E.\text{val} = 15 - T.\text{val} = 24 \end{array}$$

$$\begin{array}{ccccc} | & & | & & | \\ E.\text{val} = 9 & + & T.\text{val} = 3 & T.\text{val} = 6 & * F.\text{val} = 4 \end{array}$$

$$\begin{array}{ccccccc} | & & & & & & | \\ E.\text{val} = 2 - T.\text{val} = 3 F.\text{val} = 3 F.\text{val} = 6 & & & & & & \text{num.lval} = 4 \end{array}$$

$$\begin{array}{ccccc} | & & & & | \\ E.\text{val} = + T.\text{val} = 10 F.\text{val} = 3 \text{ num.lval} = 3 & & & & \text{num.lval} = 6 \end{array}$$

$$\begin{array}{ccccc} | & & & & | \\ T.\text{val} = 2 * F.\text{val} = 5 & & & & \text{num.lval} = 3 \end{array}$$

$$\begin{array}{ccccc} | & & & & | \\ E.\text{val} = F.\text{val} = \text{num.lval} = 5 & & & & \end{array}$$

$$\begin{array}{ccccc} | & & & & | \\ 2 & & 2 & & \text{num.lval} = 2 \end{array}$$

$$\begin{array}{ccccc} | & & & & | \\ \text{num.lval} = 2 & & & & \end{array}$$

Q.2] Generate the 3 address code for following:

a) main()

{

int i=1;

int a[10];

while (i<=10)

 a[i]=0;

}



1) i=1

2) t1 = 10 * i

3) t2 = a[t1]

4) if i<=10 then goto 6>

5) goto 3>

6) t3=0

7) a[i] = t3

8)

b) begin

 add=0;

 i=1;

 j=1;

 do

 begin

 add = add + a[i] * a[j];

 i = i+1;

 j = j+1;

 end

 while (i<=20 and j<=20)

end

- 1) add = 0
 2) i = 1
 3) j = 1
 4) t1 = 4 * i
 5) t2 = 4 * j
 6) t3 = a[t1]
 7) t4 = a[t2]
 8) t5 = t3 * t4
 9) t6 = add + t5
 10) add = t6
 11) t7 = i + 1
 12) i = t7
 13) t8 = j + 1
 14) j = t8
 15) if i ≤ 20 goto 17)
 16) goto 19)
 17) if j ≤ 20
 18) goto 19)
 19)

Q.3] What is Backpatching? Write grammar & SDD for following expression $a \< b$ and $c \< d \text{ or } e \< f$.



- The code for boolean expression inserts symbolic labels for jumps.
- If therefore needs a separate pass to get them to appropriate addresses.
- So, we use a technique named backpatching To avoid this -
 - Backpatching is a process to face the unknown labels.

- In this we use 3 fn as follows :

1) makelist(i) =

By using this fn we can create a new list.

2) Merge (P1, P2) =

Concatenating two lists pointed by P1 & P2.

3) Backpatch (p, i) =

Insert i as target label for each of the instruction on list pointed by p.

Backpatching for a < b and b < d or e < f =>

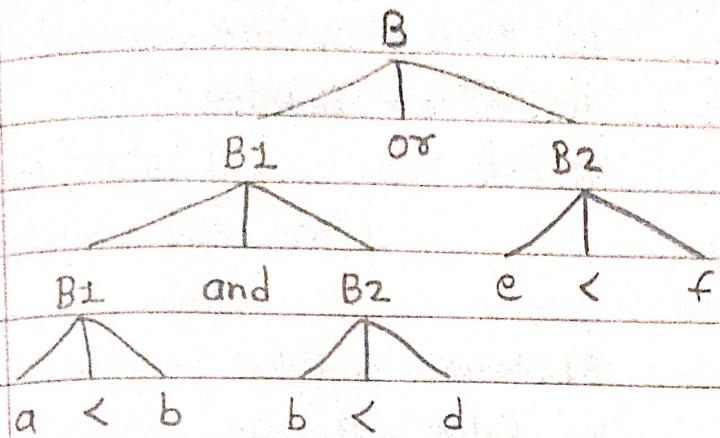
1) $B \rightarrow B_1 \parallel MB_2$ { Backpatch (B1.falselist, M.instr);
 B.truealist = Merge (B1.truealist,
 B2.truealist);
 B.falselist = B2.falselist; }

2) $B \rightarrow B_1 \& MB_2$ { Backpatch (B1.truealist, M.instr);
 B.truealist = B2.truealist;
 B.falselist = Merge (B1.falselist,
 B2.falselist); }

3) $B \rightarrow \text{True}$ { B.truealist = makelist (next instr);
 emit ("goto_"); }

4) $B \rightarrow \text{False}$ { B.falselist = makelist (next instr);
 emit ("goto_"); }

a < b and b < d or e < f



100 : if a < b then goto 102

101 : goto 104

102 : if b < d then goto 106

103 : goto 104

104 : if e < f then goto 106

105 : goto 107

106 : True

107 : False

Q.4] Write grammar and SDD for following boolean expression.

B → B1 || B2

B → B1 && B2

B → ! B1

B → B1 ~elop B2

→

1) B → B1 || B2

B.true = B.true

B1.false = newlabel()

B2.true = B.true

B2.false = B.false

B.code = B1.code ||

label(B1.false) || B2.code

2) $B \rightarrow B_1 \ \&\& \ B_2$

$B_1.\text{true} = \text{newlabel}(C)$
 $B_1.\text{false} = B.\text{false}$
 $B_2.\text{true} = B.\text{true}$
 $B_2.\text{false} = B.\text{false}$
 $B.\text{code} = B_1.\text{code} \parallel \text{label}(B_1.\text{true})$
 $\parallel B_2.\text{code}$

3) $B \rightarrow !B_1$

$B_1.\text{true} = B.\text{false}$
 $B_1.\text{false} = B.\text{true}$
 $B.\text{code} = B_1.\text{code}$

4) $B \rightarrow E_1 \ \&\& \ E_2$

$B.\text{code} = E_1.\text{code} \parallel E_2.\text{code} \parallel$
 $\text{gen}(\text{'if'} \ E_1.\text{addr} \ \&\& \ .\text{op} \ E_2.\text{addr}$
 $\text{'goto'} \ B.\text{true}) \parallel \text{gen}(\text{'goto'}$
 $B.\text{false})$

5) $B \rightarrow \text{True}$

$B.\text{code} = \text{gen}(\text{'goto'} \ B.\text{true})$

6) $B \rightarrow \text{false}$

$B.\text{code} = \text{gen}(\text{'goto'} \ B.\text{false})$

Q.5] Write SDD for flow of control statements like if-then,
if-then-else & while.

→

a) if =>

$S \rightarrow \text{if } (B) \ S_1$

		$B.\text{code}$	$\rightarrow B.\text{true}$	$B.\text{true} = \text{newlabel}(C)$
			$\rightarrow B.\text{false}$	$B.\text{false} = S_1.\text{next} = S.\text{next}$
$B.\text{true}: \quad$		$S_1.\text{code}$		$S.\text{code} = B.\text{code} \parallel \text{label}(B.\text{true}) \parallel S_1.\text{code}$
$B.\text{false}: \quad$		$S.\text{next}$		\dots

b) if - else =>

$s \rightarrow \text{if } (B) s_1 \text{ else } s_2$

B.code	$\rightarrow B.\text{true}$ $\rightarrow B.\text{false}$	$B.\text{true} = \text{newlabel}()$ $s_1.\text{next} = s.\text{next}$
B.true: s1.code goto s.next		$B.\text{false} = \text{newlabel}()$ $s_2.\text{next} = s.\text{next}$
B.false: s2.code s.next		$s.\text{code} = B.\text{code} \parallel \text{label}(B.\text{true}) \parallel s_1.\text{code} \parallel$ $\text{Label}(B.\text{false}) \parallel s_2.\text{code}$

c) while =>

$s \rightarrow \text{while } (B) s_1$

B.code	$\rightarrow B.\text{true}$ $\rightarrow B.\text{false}$	$\text{begin} = \text{newlabel}()$ $B.\text{true} = \text{newlabel}()$
B.true: s1.code goto begin		$B.\text{false} = s.\text{next}()$ $s_1.\text{next} = \text{begin}$
B.false: s.next ----		$s.\text{code} = \text{label}(\text{begin}) \parallel B.\text{code}$ $\parallel \text{label}(B.\text{true}) \parallel s_1.\text{code}$ $\parallel \text{gen}(\text{'goto' begin})$

Q30M

Tutorial No. 7

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Q.1] Generate TAC for following:

$c = 0$

do
{

if ($a < b$) then

$x++;$

else

$x--;$

$c++;$

} while ($c < 5$)

→

TAC =

1) $c = 0$

2) if ($a < b$) goto (4)

3) goto (7)

4) $T_1 = x + 1$

5) $x = T_1$

6) goto (9)

7) $T_2 = x - 1$

8) $x = T_2$

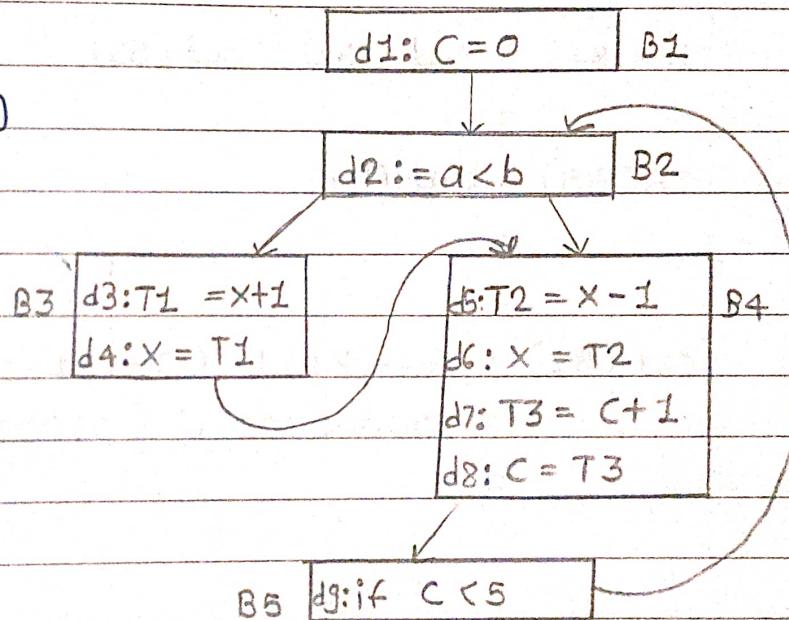
9) $T_3 = c + 1$

10) $c = T_3$

11) if ($c < 5$) goto (2)

12)

CFG =



Data Flow Analysis =

$$\text{gen}(B_1) = \{d_1\} = \{100000000\}$$

$$\text{gen}(B_2) = \{d_2\} = \{010000000\}$$

$$\text{gen}(B_3) = \{d_3, d_4\} = \{001100000\}$$

$$\text{gen}(B_4) = \{d_5, d_6, d_7, d_8\} = \{000011110\}$$

$$\text{gen}(B_5) = \{d_9\} = \{000000001\}$$

$$\text{kill}(B_1) = \{d_7, d_8, d_9\} = \{000000111\}$$

$$\text{kill}(B_2) = \emptyset$$

$$\text{kill}(B_3) = \{d_5, d_6\} = \{000011000\}$$

$$\text{kill}(B_4) = \{d_1, d_3, d_4, d_9\} = \{101100001\}$$

$$\text{kill}(B_5) = \{d_1, d_7, d_8\} = \{100000110\}$$

$$In(B_1) = Gen(B_2)$$

$$= \{d_2\} = \{010000000\}$$

$$In(B_2) = out(B_1)$$

=

$$In(B_3) = out(B_2)$$

=

$$In(B_4) = out(B_2) \cup out(B_3)$$

=

$$In(B_5) = out(B_4)$$

=

$$Out(B_1) = Gen(B_1) \cup (In(B_1) - \text{kill}(B_1))$$

$$010000000 = 100000000 \cup (010000000 - 000000111)$$

$$= 000000111 =$$

* Find LR(0) items & Construct parsing table. (a, α)

1) $S \rightarrow a$ || CLR

$S \rightarrow T$

$S \rightarrow (T)$

$T \rightarrow T \cdot S$

$T \rightarrow S$

→

		I ₁ $S' \rightarrow S \cdot, \$$								
		I ₂ $S \rightarrow a \cdot, \$$								
				I ₃ $S \rightarrow T \cdot, \$$						
I ₀	S		I ₂			I ₅		I ₁₀		
		$S' \rightarrow \cdot S \cdot, \$$		$S \rightarrow \cdot a, \$$		$S \rightarrow (T \cdot), \$$		$S \rightarrow (T \cdot \cdot), \$$		
				$S \rightarrow \cdot T, \$$	I ₃	$T \rightarrow T \cdot, S,)$		$T \rightarrow T \cdot, S,)$		
				$S \rightarrow \cdot (T), \$$	I ₄	$T \rightarrow S \cdot,)$				
				(① $S \rightarrow (\cdot T), \$$						
				② $T \rightarrow \cdot T, S,)$						
				③ $T \rightarrow \cdot S,)$						
				④ $S \rightarrow \cdot a,)$	I ₇	$S \rightarrow a \cdot,)$				
				⑤ $S \rightarrow \cdot T,)$	I ₈					
				⑥ $S \rightarrow \cdot (T),)$		$S \rightarrow T \cdot,)$				
I ₁₂	'		I ₁₁		I ₉					
		$S \rightarrow (T \cdot),)$		$T \rightarrow T \cdot, S,)$	$S \rightarrow (\cdot T),)$	$S \rightarrow (\cdot T \cdot),)$				
						$T \rightarrow \cdot T, S,)$				
						$T \rightarrow \cdot S,)$				
						$S \rightarrow \cdot a,)$				
						$S \rightarrow \cdot T,)$				
						$S \rightarrow \cdot (T),)$				

* Reading table for S.R. *

State	Action				Gate			
	i	d	=	*	S	S	L	R
0	53		55		1	2		4
1				accept				
2		56						
3		54			54			
4					52			
5	53		55			7	8	
6	53		55			7	9	
7		55			55			
8		23			23			
9					21			

follow(S') = { \$ }

follow(s) = { \$ }

follow(L) = { \$, = }

$$\text{follow}(R) = \{\$, =\}$$

ii) $S' \rightarrow S$

|| LR(0) & SLR

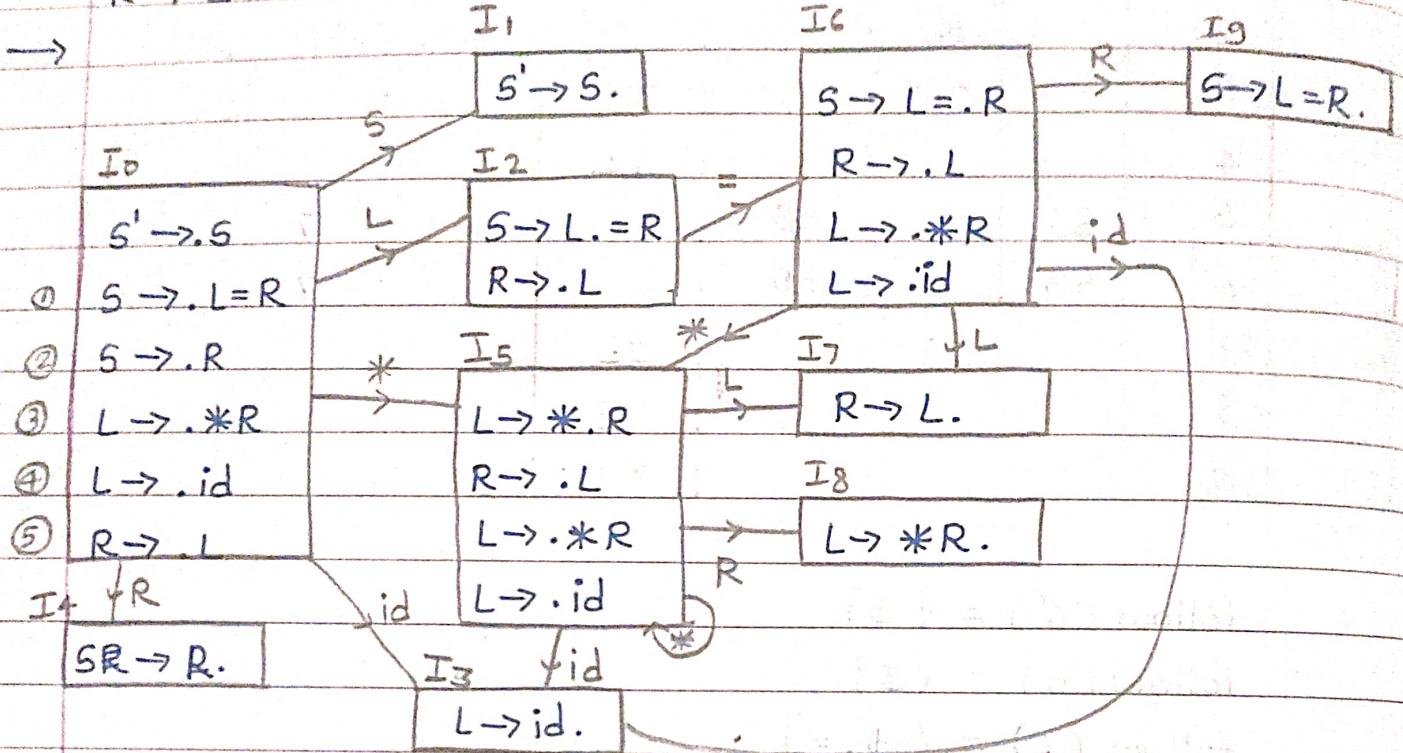
$S \rightarrow L=R$

$S \rightarrow R$

$L \rightarrow *R$

$L \rightarrow id$

$R \rightarrow L$



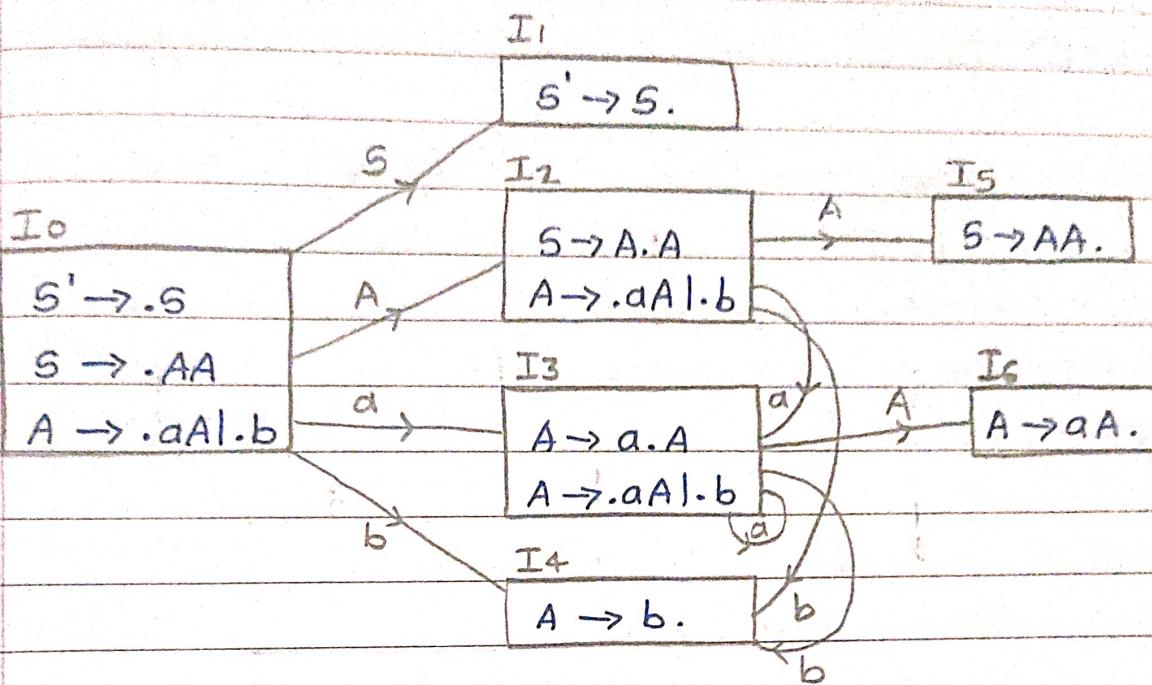
* Parsing table for LR(0) =

	Action					Goto		
	id	=	*	\$	S	L	R	
0	s3		s5		1	2	4	
1				accept				
2		s6						
3	s4	s4	s4	s4				
4	s2	s2	s2	s2				
5	s3		s5		7	8		
6	s3		s5		7	9		
7	s5	s5	s5	s5				
8	s3	s3	s3	s3				
9	s1	s1	s1	s1				

1) LR(0) Parser \Rightarrow

e.g. i) $S \rightarrow AA$
 $A \rightarrow aAlb$

\rightarrow



Parsing table =

State No.	Action			Goto	
	a	b	\$	A	S
0	53	54		2	1
1			accept		
2	53	54		5	
3	53	54		6	
4	53	53	53		
5	51	51	51		
6	52	52	52		

5) $E \rightarrow TE'$

$E' \rightarrow +TE' | \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' | \epsilon$

$F \rightarrow (E) | id$

→

$first(E) = first(T) = first(F) = \{ (, id \}$

$F(E') = \{ +, E \}$

$F(T) = first(F) = \{ (, id \}$

$F(T') = \{ *, \epsilon \}$

$F(F) = \{ (, id \}$

$Follow(E) = \{ \$,) \}$

$F(E') = follow(E) = \{ \$,) \}$

$F(T) = [(first(E') - \epsilon) \cup follow(E) \cup follow(E')] = \{ +, \$,) \}$

$F(T') = follow(T) = \{ +, \$,) \}$

$F(F) = (first(T') - \epsilon \cup follow(T) \cup follow(T')) = \{ *, +, \$,) \}$

6) $S \rightarrow ACB | cbB | Ba$

$A \rightarrow da | BC$

$B \rightarrow g | E$

$C \rightarrow h | E$

→

$first(S) = \{ d, g, h, \epsilon, b, a \}$

$first(A) = first(d) \cup first(B) - \epsilon \cup first(c) = \{ d, g, h, \epsilon \}$

$f(B) = \{ g, \epsilon \}$

$f(c) = \{ h, \epsilon \}$

$Follow(S) = \{ \$ \}$

$f(A) = \{ first(c) - \epsilon \cup first(B) - \epsilon \cup follow(S) \} = \{ h, g, \$ \}$

$f(B) = \{ follow(S) \cup first(a) \cup first(c) - \epsilon \cup follow(A) \} = \{ \$, a, hg \}$

$f(c) = \{ first(B) - \epsilon \cup follow(S) \cup first(b) \cup follow(A) \} =$

$\{ g, b, b, h \}$

First

$$S \rightarrow A$$

$$\text{first}(S) = \text{first}(A) = \{a\}$$

$$A \rightarrow aBA'$$

$$f(A) = \{a\}$$

$$A' \rightarrow dA' | \epsilon$$

$$f(A') = \{d, \epsilon\}$$

$$B \rightarrow b$$

$$f(B) = \{b\}$$

$$C \rightarrow g$$

$$f(C) = \{g\}$$

$$\text{Follow}(S) = \{\$\}$$

$$\text{Follow}(A) = \text{follow}(S) = \{\$\}$$

$$f(A') = \text{follow}(A) = \{\$\}$$

$$f(B) = \text{first}(A') \cup \text{follow}(A) = \{d, \$\}$$

$$f(C) = \text{NA}$$

3)

First

$$S \rightarrow (L) | a$$

$$\{c, a\}$$

$$L \rightarrow SL'$$

$$\{c, a\} - f(S)$$

$$L' \rightarrow , SL' | \epsilon$$

$$\{, , \epsilon\}$$

Follow

$$f(S) = \{\$, , ,)\} - \text{first}(L') - E \cup$$

$$\text{follow}(L) \cup \text{follow}$$

$$\uparrow L'$$

$$f(L') = \text{follow}(L) = \{)\}$$

4) $S \rightarrow AaAb | BbBa$

$$A \rightarrow E$$

$$B \rightarrow E$$

→

$$\text{first}(S) = \{a, b\}$$

$$\text{follow}(S) = \{\$\}$$

$$\text{first}(A) = \{E\}$$

$$\text{follow}(A) = \text{first}(A) \cup \text{first}(b) = \{a, b\}$$

$$\text{first}(B) = \{E\}$$

$$\text{follow}(B) = \{a, b\}$$

* Compute First & follow \Rightarrow

$$1) S \rightarrow aBDh$$

$$B \rightarrow cC$$

$$C \rightarrow bCIE$$

$$D \rightarrow EF$$

$$E \rightarrow gIE$$

$$F \rightarrow fIE$$

\rightarrow

$$\text{First}(S) = \{a\}$$

$$\text{First}(B) = \{c\}$$

$$\text{First}(C) = \{b, E\}$$

$$\text{First}(D) = (\text{First}(E) - \epsilon) \cup \text{First}(F) = \{g, f, E\}$$

$$\text{First}(E) = \{g, E\}$$

$$\text{First}(F) = \{f, E\}$$

$$\text{Follow}(S) = \{\$\}$$

$$\text{Follow}(B) = (\text{first}(D) - \epsilon) \cup \text{first}(h) = \{g, f, h\}$$

$$\text{Follow}(C) = (\text{follow}(B)) = \{g, f, h\}$$

$$\text{Follow}(D) = (\text{first}(h)) = \{h\}$$

$$\text{Follow}(E) = ((\text{first}(F) - \epsilon) \cup \text{follow}(D)) = \{f, h\}$$

$$\text{Follow}(F) = (\text{follow}(D)) = \{h\}$$

2)

$$S \rightarrow A$$

$$A \rightarrow aB \mid Ad$$

$$B \rightarrow b$$

$$C \rightarrow g$$

\rightarrow

Eliminate left recursion,