

1] Context free grammar.

A context free grammar is a 4 tuple

$$G = (V, T, P, S) \text{ where}$$

$V$  is finite set of variables / non-terminal.

$T$  is finite set of terminals (tokens)

$P$  is finite set of prod' of the form

$$A \rightarrow \alpha$$

where  $A \in V$  &  $\alpha \in (VUT)^*$

$S \in V$  is a start symbol.

Ex -

$$E \rightarrow EAE \mid (E) \mid -E \mid id$$

$$A \rightarrow + \mid - \mid * \mid / \mid .$$

here  $E$  &  $A$  are variables / non-terminals.  
 $id, +, -, *, /, *$  are terminals.

2] Syntax analysis:-

In syntax analysis phase the source program is analyzed to check whether it conforms to the source language's syntax & to determine its phrase structure.

This phase is often separated into two-phases:-

- ① lexical analysis - which produces stream of tokens.
- ② parser - which determines the phrase structure of the program based on context free grammar for the language.

## 3] Parsing :-

Parsing is the activity of checking whether a string of symbols is in the language of some grammar, where this string is usually the stream of tokens produced by the lexical analyzer. If the string is in the grammar, we want a parse tree & if it is not, we hope for some kind of error message explaining why not.

There are two main kinds of parsers in use, named for the way they build parse trees:

- ① top-down : A top-down parser attempts to construct a tree from the root, applying productions forward to expand non-terminals into strings of symbols.
- ② bottom-up : A bottom-up parser builds the tree starting with the leaves, using productions in reverse to identify strings of symbols that can be grouped together.

In both cases the construction of derivation is directed by scanning the input sequence from left to right, one symbol at a time.

## 4] Parse tree -

A parse tree is the graphical representation of the structure of a sentence according to its grammar.

The parse tree may be viewed as a representation for a derivation that filters out the choice regarding the order of replacement.

Set the production P be -

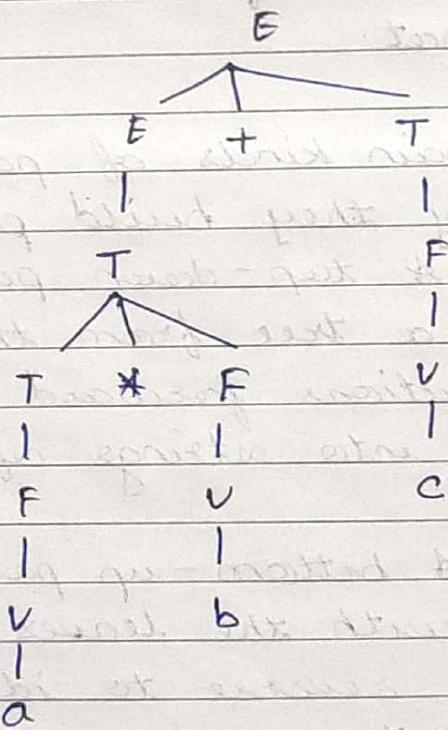
$$E \rightarrow T \mid ET + T$$

$$T \rightarrow F \mid T * F$$

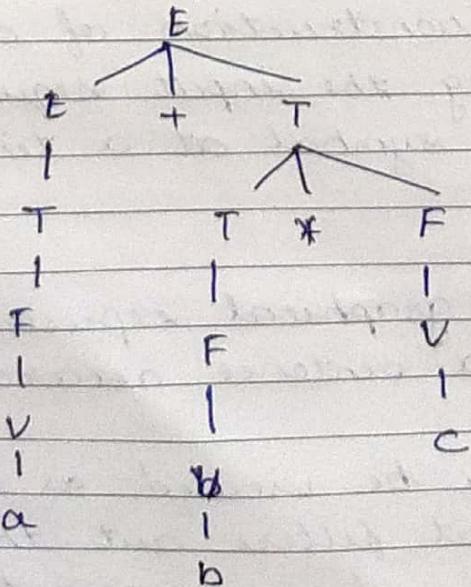
$$F \rightarrow V \mid (E)$$

$$V \rightarrow a \mid b \mid c \mid d$$

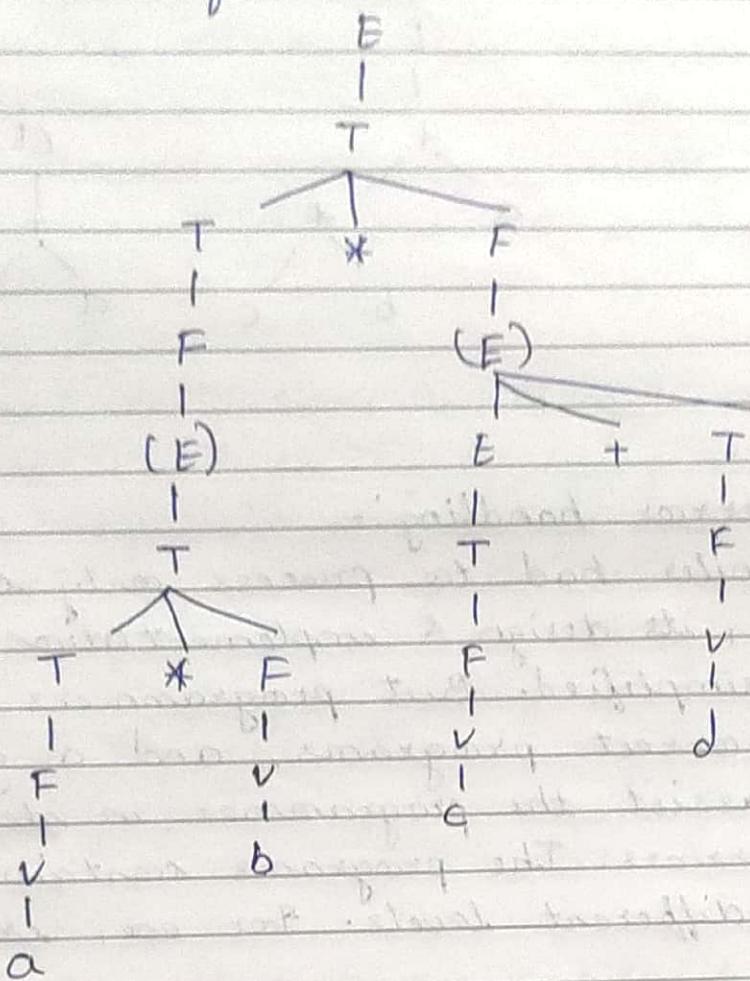
Parse tree for  $a^* b + c$



Parse tree for  $a+b^*c$



Parse tree for  $(a * b) * (c + d)$

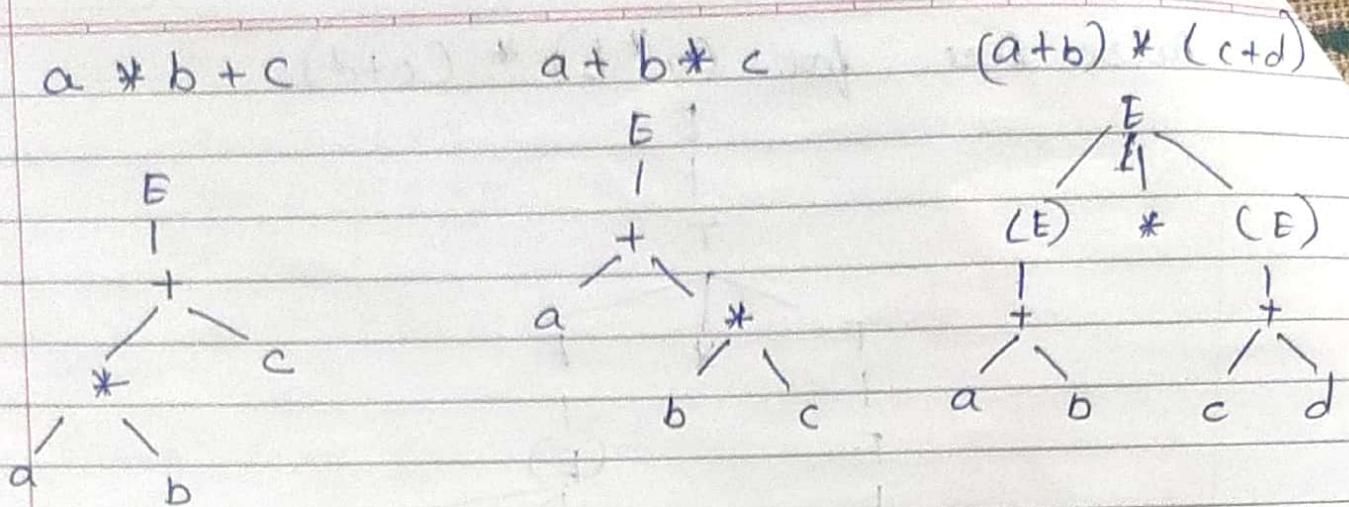


### 5] Syntax tree -

Parse tree can be presented in a simplified form with only the relevant structure info by:-

- leaving out chains of derivation (whose sole purpose is to give operators difference precedence)
- labeling the nodes with the operators in question rather than a non-terminal.

The simplified parse tree is sometimes called structural tree or syntax tree.



### 6] Syntax error handling:-

If a compiler had to process only correct programs, its design & implementation would be greatly simplified. But programmers frequently write incorrect programs, and a good compiler should assist the programmer in identifying & locating errors. The programs contain errors at many different levels. For ex, errors can be:

- 1) lexical - such as misspelling an identifier, keyword or operator.
- 2) syntactic - such as an arithmetic expression with unbalanced parenthesis.
- 3) semantic - such as an operator applied to an incompatible operand.
- 4) logical - such as an infinitely recursive call.

~~at++'b~~ Much of error detection & recovery in a compiler is centered around the syntax analysis phase. The goals of error handler in a parser are:

- 1) It should report the presence of errors clearly & accurately.

- 2) It should recover from each error quickly enough to be able to detect subsequent errors.
- 3) It should not significantly slow down the processing of correct programs.

7)

### Ambiguity -

Several derivations will generate the same sentence, perhaps by applying the same production in a different order. This alone is fine, but a problem arises if the same sentence has two distinct parse trees. A grammar is ambiguous if there is any sentence with more than one parse tree.

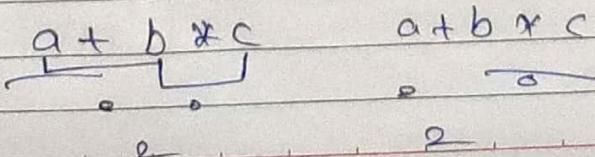
Any parser for an ambiguous grammar has to choose somehow which tree to return.

There are a number of 'sc' to this; the parser could pick one arbitrarily or we can provide some hints about which to choose.

Best of all is to rewrite the grammar so that it is not ambiguous.

There is no general method for removing ambiguity. Ambiguity is acceptable in spoken languages. Ambiguous programming languages are useless unless the ambiguity can be resolved.

Any sentence with more than two variables, such as (arg, arg, arg) will have multiple parse trees.



### 8] Left recursion -

If there is any non-terminal A, such that there is a derivation  $A \rightarrow A\alpha$  for some string  $\alpha$  then, grammar is left recursive.

Algorithm for eliminating left recursion -

1. group all the A prod' together -

$$A \rightarrow A\alpha_1 | A\alpha_2 | \dots | B_1 | B_2 | \dots$$

where,

A is the left recursive non-terminal

$\alpha$  is any string of terminals

$B$  is any string of terminals & non-terminals that does not begin with A.

2. Replace the above A prod' by -

$$A \rightarrow B_1 A' | B_2 A' | \dots$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \dots$$

where  $A'$  is a new non terminal.

Top-down parsers cannot handle left recursive grammar.

If our esp grammar is left recursive -

- This can lead to non-termination in a top-down parser.
- for a top-down parser, any recursion must be right recursion.
- we would like to convert left recursion to right recursion.

3] Eliminate left recursion.

$$S \rightarrow ABC$$

$$A \rightarrow Aa \mid Ad \mid b$$

$$B \rightarrow Bb \mid e$$

$$C \rightarrow Cc \mid g$$

$$\begin{array}{c} S \rightarrow b \\ | \\ ABC \end{array}$$

$$\rightarrow S \rightarrow ABC$$

$$A \rightarrow bA'$$

$$A' \rightarrow aA' \mid \epsilon \mid dA'$$

$$B \rightarrow eB'$$

$$B' \rightarrow bB' \mid e$$

$$C \rightarrow gC'$$

$$C' \rightarrow cC' \mid \epsilon$$

$$A \rightarrow Aa \mid b$$

$$A \rightarrow bA'$$

$$A' \rightarrow aA' \mid \epsilon$$

$$A \rightarrow Ad \mid b$$

$$A \rightarrow bA'$$

$$A' \rightarrow dA' \mid \epsilon$$

10] Eliminate left recursion.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$A \rightarrow Aa \mid b$$

$$A \rightarrow bA'$$

$$A' \rightarrow aA' \mid \epsilon$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \epsilon$$

11] Eliminate left recursion.

$$E \rightarrow E + T \mid E - T \mid T$$

$$T \rightarrow T * F \mid T / F \mid F$$

$$E \rightarrow ET \mid T$$

$$E \rightarrow TE'$$

$$E \rightarrow TE'$$

$$T' \rightarrow +TE' \mid -TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid /FT' \mid \epsilon$$

12] Eliminate left recursion.

$$S \rightarrow Aa1b$$

$$A \rightarrow Ac1Sd1\epsilon$$

→ transforming -

$$S \rightarrow Aa1b$$

$$A \rightarrow Ac1Aad1\epsilon1bd$$

↓

$$S \rightarrow Aa1b$$

$$A \rightarrow A'1bdA'$$

$$A' \rightarrow cA'1\epsilon1adA' \cancel{1bdA'}$$

$$A \rightarrow Ac1\epsilon bd$$

$$A \rightarrow \overset{bd}{\epsilon} A'$$

$$A' \rightarrow cA'1\epsilon$$

$$A \rightarrow Aad1\epsilon$$

$$A \rightarrow \epsilon A'$$

$$A' \rightarrow adA'1\epsilon$$

$$A \rightarrow bd$$

13] Eliminate left recursion.

$$S \rightarrow Aa1b$$

$$A \rightarrow Sc1d$$

→ transforming →

$$S \rightarrow Aa1b$$

$$A \rightarrow Aac1d1bc$$

↓

$$S \rightarrow Aa1b$$

$$A \rightarrow dA'1bcA'$$

$$A' \rightarrow acA'1\epsilon$$

~~$$S \rightarrow Aa1b$$~~

$$A \rightarrow Aac1d$$

~~$$S \rightarrow Sca1b$$~~

$$A \rightarrow dA'$$

~~$$S \rightarrow Aaca1$$~~

$$A' \rightarrow acA'1\epsilon$$

~~$$A \rightarrow Aac1bc$$~~

~~$$A \rightarrow bcA'$$~~

~~$$A' \rightarrow acA'1\epsilon$$~~

14] Left factoring -

Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive parsing.

When it is not clear which of two alternative productions to use to expand a non-terminal  $A$ , we may be able to rewrite the productions to defer the decisions until we have some

enough of the input to make the right choice.

Algorithm:-

For all  $A \in$  non-terminal, find the largest prefix  $\alpha$  that occurs in two or more right-hand sides of  $A$ .

If  $\alpha \neq \epsilon$  then replace all of the "prod"

$$A \rightarrow \alpha \beta_1 | \alpha \beta_2 | \dots | \gamma$$

$$A \rightarrow \alpha A' | \gamma$$

$$A' \rightarrow \beta_1 | \beta_2 | \dots | \epsilon$$

where  $A'$  is a new element of non-terminal.

$$\text{Ex} - v \rightarrow \alpha \beta_1 | \alpha \beta_2 | \dots | \delta$$

$$\rightarrow v \rightarrow \alpha v' | \delta$$

$$v' \rightarrow \beta_1 | \gamma$$

15] Eliminate left factoring.

$$S \rightarrow v := \text{int}$$

$$v \rightarrow \text{alpha} [ \text{"int"} ] | \text{alpha}.$$

→

$$S \rightarrow v := \text{int}$$

$$v \rightarrow \text{alpha} v'$$

$$v' \rightarrow [ \text{"int"} ] | \epsilon$$

16] Eliminate left factoring.

$$S \rightarrow iEtS | iEtSeS | \alpha$$

$$E \rightarrow C$$

$$\rightarrow S \rightarrow iEtS S' | \alpha$$

$$S' \rightarrow e | es$$

$$E \rightarrow C$$

### 17] Top down parsing -

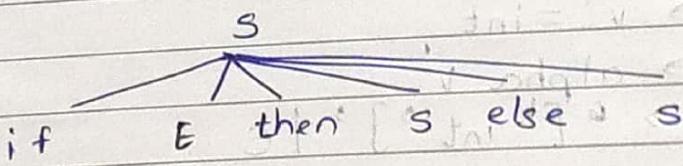
Top down parsing is the construction of a parse tree by starting at start symbol & guessing each derivation until we reach a string that matches input. That is, construct tree from root to leaves.

The advantage of top-down parsing is that a parser can directly be written as a program. Table-driven top-down parsers are of minor practical relevance. Since bottom-up parsers are more powerful than top-down parsers, bottom-up parsing is practically relevant.

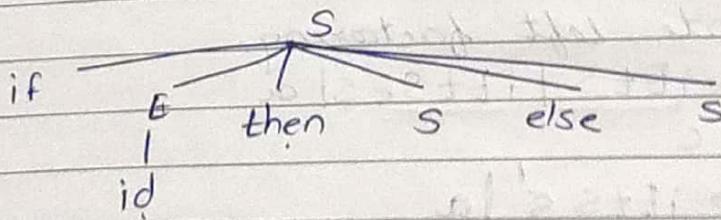
For ex -  $S \rightarrow \text{if } E \text{ then } S \text{ else } S$  | while  $E \rightarrow \text{true} \mid \text{false} \mid \underline{id}$ .

string - If id then while true do print else print.

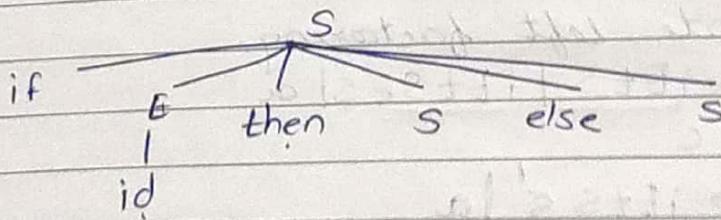
1.



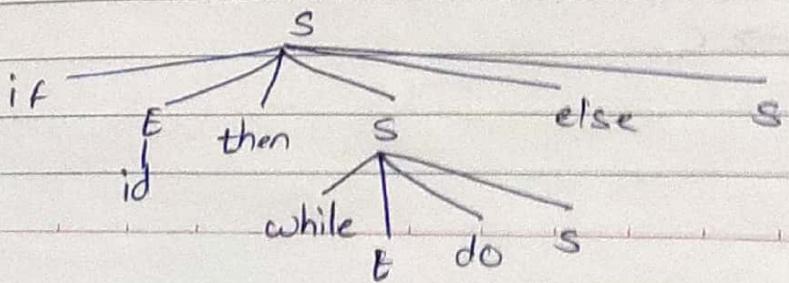
2.



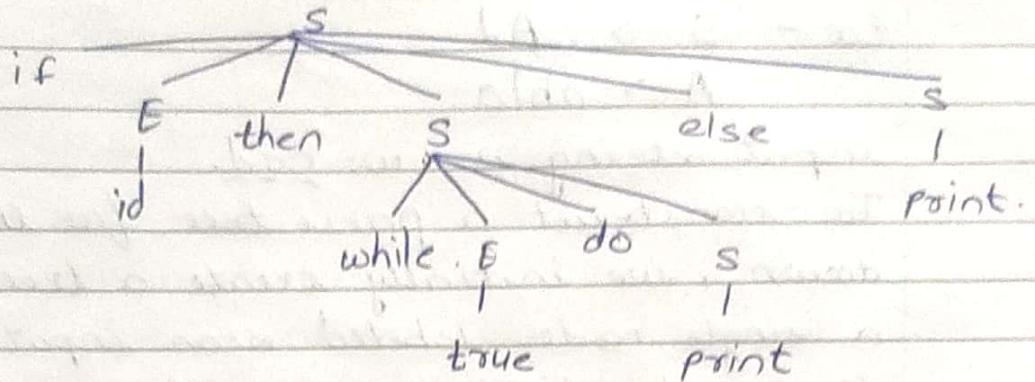
3.



4.



5.



### 18] Recursive descent - parsing -

Top - down parsing can be viewed as an attempt to find a left most derivation for an input string. Equivalently, it can be viewed as an attempt to construct a parse tree for the input starting from root & creating the nodes of the parse tree in preorder.

The special case of recursive-descent parsing, called predictive parsing, where no backtracking is required. The general form of top-down parsing, called recursive descent, that may involve backtracking, that is, making repeated scans of input.

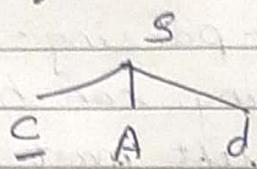
Recursive descent or predictive parsing works only on grammars where the first terminal symbol of each sub expression provides enough information to choose which prod' to use.

Recursive descent parser is a top down parser involving backtracking. It makes repeated scans of input. Backtracking parsers are not seen frequently, as backtracking is very needed to parse programming language constructs.

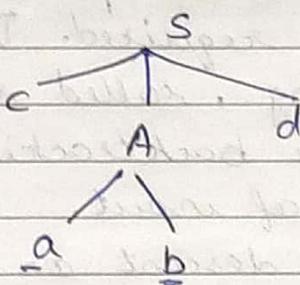
Ex -  $S \rightarrow cAd$   
 $A \rightarrow abla$ .

input string is  $w = \underline{c}ad$ .

To construct a parse tree for this string top-down, we initially create a tree consisting of a single node labeled  $s$  on input pointer point to  $c$ , the first symbol of  $w$ , we then use the first prod' for  $S$  to expand tree & obtain tree →

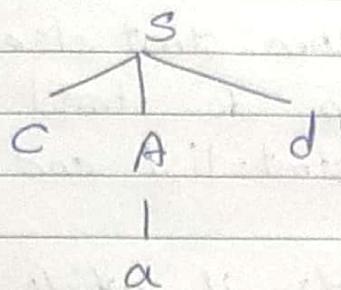


Now, we advance the input pointer to  $a$ , the second symbol of  $w$  and consider the next leaf, labeled  $A$ . We can then expand  $A$  using the first alternative for  $A$  to obtain the tree.



We now have a match for the second input symbol so we advance the input pointer to  $d$ , the third input symbol & compare  $d$  against next leaf, labeled  $b$ . Since  $b$  does not match  $d$ , we report failure & go back to  $A$  to see where there is any alternative for  $A$  that we have not tried but might produce a match.

In going back to  $A$ , we must reset the input pointer to position 2, we now try second alternative for  $A$  to obtain tree :-



The leaf matches second symbol of w & the leaf d matches the third symbol.

The left recursive grammar can cause a recursive-descent parser, even one with backtracking, to go into an infinite loop. That is when we try to expand A, we may eventually find ourselves again trying to expand A without having consumed any input.

### 19] Predictive parsing - LL(1)

Predictive parsing is top-down parsing without backtracking or look-a-head. For many languages, make perfect guesses (avoid backtracking) by using 1-symbol look-a-head, i.e., if  
 $A \rightarrow \alpha_1 \alpha_2 \dots \alpha_n$ .

choose correct  $\alpha_i$  by looking at first symbol it derives. If  $\epsilon$  is an alternative, choose it last.

This approach is also called as predictive parsing. There must be atmost one prod' in order to avoid backtracking. If there is no such prod' then no parse tree exists & an error is returned. The grammar must not be left-recessive.

Predictive parsing works well on those fragments of programming languages in which keywords occur frequently.

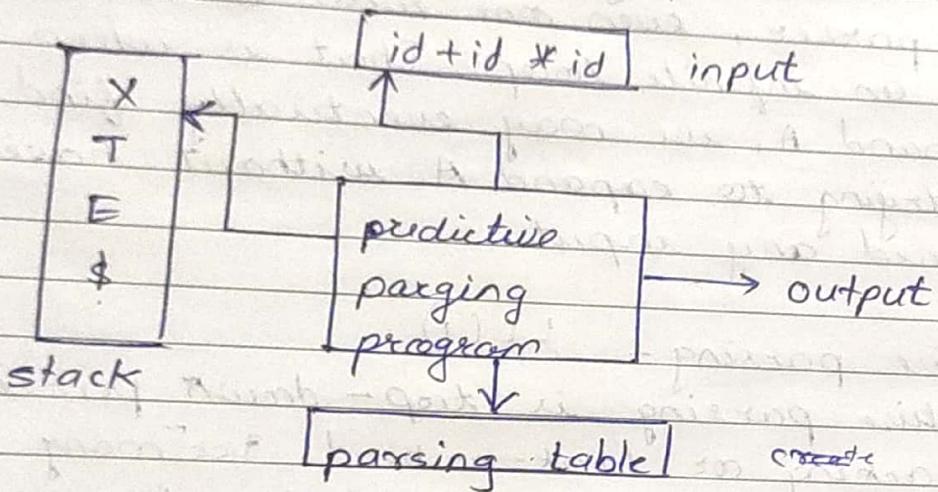
Ex -

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$\text{stmt} \rightarrow \text{if exp then stmt else stmt}$   
 $\text{while exp do stmt}$   
 $\text{begin stmt-list end.}$

then the keywords if, while & begin tell which alternative is the only one that could possibly succeed if we are to find a statement.

The model of predictive parser is as follows:-



A predictive parser has:-  
 stack,  
 input,  
 parsing table,  
 output.

The input buffer consists the string to be parsed, followed by \$, a symbol used as a right end marker to indicate the end of the input string.

The stack consists of a sequence of grammar symbols with \$ on the bottom, indicating the bottom of stack. Initially the stack consists

of the start symbol of grammar on top of \$.

Recursive descent & LL parsers are often called predictive parsers, because they operate by predicting the next step in a derivation.

20)

Computing first  $\rightarrow$

If  $x$  is a grammar symbol, then  $\text{first}(x) =$

- If  $x$  is terminal symbol, then  $\text{first}(x) = \{x\}$ .

- If  $x \rightarrow \epsilon$ , then  $\text{first}(x) = \{\epsilon\}$

- If  $x$  is non-terminal (variable) &  $x \rightarrow a\alpha$ , then  $\text{first}(x) = \{a\}$ .

- 

# If  $x \rightarrow Y_1, Y_2, Y_3$  then  $\text{first}(x)$  will be

① If  $Y$  is terminal then

$\text{first}(x) = \text{first}(Y_1, Y_2, Y_3) = \{Y\}$ .

② If  $Y_1$  is non-terminal (variable) & if  $Y_1$  does not derive to an empty string, i.e., if  $\text{first}(Y_1)$  does not contain  $\epsilon$  then,  
 $\text{first}(x) = \text{first}(Y_1, Y_2, Y_3) = \text{first}(Y_1)$

③ If  $\text{first}(Y_1)$  contains  $\epsilon$  then  
 $\text{first}(x) = \text{first}(Y_1, Y_2, Y_3) = \text{first}(Y_1) - \{\epsilon\} \cup \text{first}(Y_2, Y_3)$ .

similarly  $\text{first}(Y_2, Y_3) = \{Y_2\}$ , if  $Y_2$  is terminal otherwise if  $Y_2$  is non-terminal then

$\text{first}(Y_2, Y_3) = \text{first}(Y_2)$  if  $Y_2$   $\text{first}(Y_2)$  does not contain  $\epsilon$ .

If first ( $\gamma_2$ ) contains  $\epsilon$  then

$$\text{first}(\gamma_2, \gamma_3) = \text{first}(\gamma_2) - \{\epsilon\} \cup \text{first}(\gamma_3).$$

2] Find first of following -

$$① S \rightarrow abc \mid def \mid ghi$$

$$\text{ans} = \text{first}(S) = a, d, g.$$

$$S \rightarrow abc$$

$$(S \rightarrow def)$$

$$S \rightarrow ghi$$

$$② S \rightarrow ABC \mid ghi \mid jkl$$

$$A \rightarrow ab \mid c$$

$$B \rightarrow b$$

$$D \rightarrow d$$

$$\text{ans} = \text{first}(D) = d$$

$$\text{first}(B) = b$$

$$\text{first}(A) = a, b, c$$

$$\text{first}(S) = \text{first}(ABC) \cup \text{first}(ghi) \cup \text{first}(jkl)$$

$$= \text{first}(A) \cup \text{first}(ghi) \cup \text{first}(jkl)$$

$$= a, b, c, g, j.$$

$$③ E \rightarrow TE'$$

$$E' \rightarrow *TE' \mid \epsilon$$

$$T \rightarrow FT$$

$$T' \rightarrow \epsilon \mid +FT'$$

$$F \rightarrow id \mid EE$$

Terminal = a, b, \$

Non terminal = A  
variable

$$\text{ans} = \text{first}(F) = id, F$$

$$\text{first}(T') = \epsilon, +$$

$$\text{first}(T) = \text{first}(F) = id, *F$$

$$\text{first}(E') = *, \epsilon$$

$$\text{first}(E) = \text{first}(T) = id, E$$

$$④ \quad S \rightarrow ABC$$

$$A \rightarrow a b l \epsilon$$

$$B \rightarrow c d l \epsilon$$

$$C \rightarrow e f l \epsilon$$

a, b, ε

ABC

bBC

bBC

bBC

bBC

bBC

$$\text{ans} = \text{first}(c) = e, f, \epsilon$$

$$\text{first}(B) = c, d, \epsilon$$

$$\text{first}(A) = a, b, \epsilon$$

$$\text{first}(S) = \text{first}(ABC)$$

$$= \text{first}(A) - \{\epsilon\} \cup \text{first}(B) - \{\epsilon\}$$

$$= a, b, \epsilon \cup \text{first}(c)$$

$$= a, b, c, d, e, f, \epsilon$$

22)

computing follow →

If  $S$  is the start symbol,  $\text{Follow}(S) = \{\$\}$

If prod is of form  $A \rightarrow \alpha B \beta$ ,  $\beta \neq \epsilon$ .

• if  $\text{first}(\beta)$  does not contain  $\epsilon$  then,  
 $\text{follow}(B) = \{\text{first}(\beta)\}$

• if  $\text{first}(\beta)$  contains  $\epsilon$  then

$$\text{follow}(B) = \text{first}(\beta) - \{\epsilon\} \cup \text{follow}(A).$$

$$A \xrightarrow{\alpha} B \beta$$

Q3) Construct first & follow for grammar

$$A \rightarrow BC \mid EFGH \mid H$$

$$B \rightarrow b$$

$$C \rightarrow c \mid \epsilon$$

$$DE \rightarrow c \mid E$$

$$F \rightarrow CE$$

$$G \rightarrow g$$

$$H \rightarrow h \mid \epsilon$$



\* First set.

$$\text{first}(H) = \{h, \epsilon\}$$

$$\text{first}(G) = \{g\}$$

$$\begin{aligned}\text{first}(F) &= \text{first}(c) \cup \text{first}(E) \\ &= \{c, e, \epsilon\}\end{aligned}$$

$$\text{first}(E) = \{e, \epsilon\}$$

$$\text{first}(C) = \{c, \epsilon\}$$

$$\text{first}(B) = \{b\}$$

$$\begin{aligned}\text{first}(A) &= \text{first}(BC) \cup \text{first}(EFGH) \cup \text{first}(H) \\ &= \text{first}(B) \cup \text{first}(E) \cup \text{first}(H) \\ &= \{b, e, \epsilon, h\} \\ &= \text{first}(B) \cup \text{first}(E) - \{\epsilon\} \cup \text{first}(FGH) \\ &\quad \cup \text{first}(H)\end{aligned}$$

$$= \{b\} \cup \{e\} \cup \text{first}(F) - \{\epsilon\} \cup \text{first}(GH)$$

$$\cup \{h\} - \{\epsilon\} \cup \{h, \epsilon\}$$

$$= \{b\} \cup \{c\} \cup \{c, e\} \cup \{g\} \cup \{h\}, \epsilon$$

$$= \{b, e, c, g, h, \epsilon\}$$

\* follow set.

$$\text{follow}(A) = \{\$\}$$

$$\begin{aligned}\text{follow}(B) &= \text{first}(B) = \{c, S\} \cup \text{follow}(A) \\ &= \{c, \$\}\end{aligned}$$

$$\begin{aligned}\text{follow}(C) &= \text{first}(E) - \{S\} \cup \text{follow}(F) \cup \text{follow}(A) \\ &= \{e, \$, g\}\end{aligned}$$

$$\begin{aligned}\text{follow}(E) &= \text{first}(F) - \{S\} \cup \text{first}(G) \\ &= \{c, e, g\}\end{aligned}$$

$$\begin{aligned}\text{follow}(F) &= \text{first}(G) \\ &= \{g\}\end{aligned}$$

$$\begin{aligned}\text{follow}(G) &= \text{first}(H) - \{S\} \cup \text{follow}(A) \\ &= \{h, \$\}\end{aligned}$$

$$\begin{aligned}\text{follow}(H) &= \text{follow}(A) \\ &= \{\$\}\end{aligned}$$

Q. 24. Construct a predictive parsing table for the given grammar ~~(a)~~ check whether the given grammar is LL(1) or not.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid \text{id.}$$

→

Steps:-

1. Eliminate left recursion
2. left factoring.
3. first & follow functions
4. predictive parsing table
5. parse the input string.

Step 1 :- Eliminating left recursion.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' | \epsilon$$

$$F \rightarrow (E) | id$$

Step 2 :- Left factoring.

No left factoring.

Step 3 :- first & follow functions.

$$\text{first}(E) = \text{first}(T) = \text{first}(F) = \{c, id\}$$

$$\text{first}(E') = \{+, \epsilon\}$$

$$\text{first}(T) = \{c, id\}$$

$$\text{first}(T') = \{* , \epsilon\}$$

$$\text{first}(F) = \{c, id\}$$

$$\text{follow}(E) = \{\$, )\}$$

$$\text{follow}(T) = \{+, \$, )\}$$

$$\text{follow}(E') = \{\$\}\}$$

$$\text{follow}(T') = \{+, \$, ), *\}$$

$$\text{follow}(F) = \{* , +, \$, )\}$$

Step 4 :- predictive parsing table.

If  $A \rightarrow \alpha$  consider row of A & column of  $\text{first}(\alpha)$ .

1)  $M[A, a] = A \rightarrow \alpha$ , a is in  $\text{first}(\alpha)$

2)  $M[A, b] = A \rightarrow \alpha$ , if  $\epsilon$  is in  $\text{first}(\alpha)$ , b is in  $\text{follow}(A)$ .

where M is table.

$E$		$E \rightarrow TE'$	$E \rightarrow TE'$
$E'$	$E' \rightarrow +TE'$	$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
$T$		$T \rightarrow FT'$	$T \rightarrow FT'$
$T'$	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$	$T' \rightarrow \epsilon$
$F$		$F \rightarrow (E)$	$F \rightarrow id$

As there are no multiple entries in table,  
hence the given grammar is LL(1).

Step 5:-

Moves made by predictive parser on the  
input  $id * id + id$ .

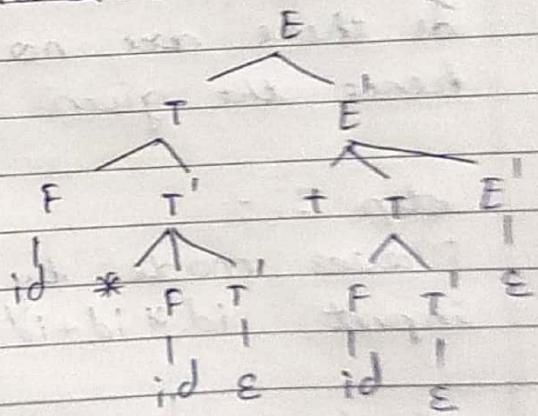
stack	input	output
$\$ E$	$id * id + id \$$	$E \rightarrow TE'$
$\$ E' T$	$id * id + id \$$	$T \rightarrow FT'$
$\$ E' T' F$	$id * id + id \$$	$F \rightarrow id$
$\$ E' T' id$	$id * id + id \$$	
$\$ E' T'$	$* id + id \$$	$T' \rightarrow *FT'$
$\$ E' T' F *$	$* id + id \$$	
$\$ E' T' F$	$id + id \$$	$F \rightarrow id$
$\$ E' T' id$	$id + id \$$	
$\$ E' T'$	$+ id \$$	$T' \rightarrow \epsilon$
$\$ E' \epsilon$	$+ id \$$	$E' \rightarrow +TE'$
$\$ E' T +$	$+ id \$$	
$\$ E' T$	$id \$$	$T \rightarrow FT'$

$\$ET'F$  $\$ET'id$  $\$E'T'$  $\$E'$  $\$$  $id \$$  $id \$$  $\$$  $\$$  $\$$  $F \rightarrow id$  $T' \rightarrow \epsilon$  $E' \rightarrow \epsilon$ 

We can notice  $\$$  in input & stack, i.e., both are empty.

$\therefore$  Predictive parser accept the given input string.

$\therefore$  output is  $\rightarrow$  (optional) Parse tree = optional

 $E \rightarrow TE'$  $T \rightarrow FT'$  $F \rightarrow id$  $T' \rightarrow *FT'$  $F \rightarrow id$  $T' \rightarrow \epsilon$  $E' \rightarrow +TE'$  $T \rightarrow FT'$  $F \rightarrow id$  $T' \rightarrow \epsilon$  $E' \rightarrow \epsilon$ 

25] LL(1) grammar -

The first L stands for "left-to-right scan of input"; The second L stands for "left-most derivation". The '1' stands for 1 taken of look-ahead.

No LL(1) grammar can be ambiguous or left recursive.

If there were no multiple entries in the recursive descent parser table, the given grammar is LL(1).

If the grammar G is ambiguous, left recursive then the recursive descent table will have at least one multiple defined entry.

LL(1) = top-down, predictive parsing.

The weakness of LL(1) parsing is that, it must predict which prod^n to use.

26] Construct a predictive parsing table for the given grammar. @

check whether the grammar is LL(1) or not.

$$S \rightarrow iEtSS' | \alpha$$

$$S' \rightarrow eS | \varepsilon$$

$$E \rightarrow b$$

→ step 1 :- Eliminating left recursion.  
no left recursion.

step 2 :- left factoring  
no left factoring.

step 3 :- computing first & follow.

$$\text{first}(E) = b$$

$$\text{first}(S) = \{ i, a \}$$

$$\text{first}(S') = \{ e, \epsilon \}$$

$$\text{follow}(S) = \{ \$, e \}$$

$$\text{follow}(S') = \{ \$, e \}$$

$$\text{follow}(E) = \{ + \}$$

step 4 :- predictive parsing table.

	b	i	a	e	t	e	\$
S		$S \rightarrow iEtS$	$S \rightarrow a$				
$S'$					$S' \rightarrow eS$		
E	$E \rightarrow b$						

As the table contains multiple defined entry,  
the grammar is not LL(1).

27]

Construct the first & follow & predictive parse table for the grammar.

$$S \rightarrow A C \$$$

$$C \rightarrow c | \epsilon$$

$$A \rightarrow a B C d | B Q | \epsilon$$

$$B \rightarrow b B | d$$

$$Q \rightarrow q.$$

 $\rightarrow$ 

first :-

$$\text{first}(Q) = \{q\}$$

$$\text{first}(B) = \{b, d\}$$

$$\text{first}(A) = \{a, b, d, \epsilon\}$$

$$\text{first}(\epsilon) = \{\epsilon\}$$

$$\text{first}(S) = \{a, b, d, \epsilon\}$$

$$\text{follow}(S) = \{\#\}$$

$$\text{follow}(A) = \{c, \$\}$$

$$\text{follow}(C) = \{\$, d\}$$

$$\text{follow}(B) = \{c, d, q, b\}$$

$$\text{follow}(Q) = \{c, \$\}$$

	a	b	c	d	q	$\epsilon$	\$	#
S	$S \rightarrow A C \$$	$S \rightarrow A C \$$	$S \rightarrow A C \$$	$S \rightarrow A C \$$		$S \rightarrow A C \$$		
B		$B \rightarrow b B$		$B \rightarrow d$				
C			$C \rightarrow c$			$C \rightarrow \epsilon$		
A	$A \rightarrow a B C d$	$A \rightarrow B Q$		$A \rightarrow B Q$		$A \rightarrow \epsilon$		
Q					$Q \rightarrow q$			

Moves made by predictive parser on the input abdc dc \$ is :-

stack	input	output
# S	abdc dc \$ #	$S \rightarrow A C \$$
# \$ C A	abdc dc \$ #	$A \rightarrow a B C d$
# \$ C A d C B a	abdc dc \$ #	
# \$ C A d C B	bdc dc \$ #	$B \rightarrow b B$
# \$ C A d C B b	bdc dc \$ #	
# \$ C A d C B	dc dc \$ #	$B \rightarrow d$
# \$ C A d C . d	dc dc \$ #	
# \$ C A d C €	dc dc \$ #	$C \rightarrow c$
# \$ C A d C	c dc \$ #	
# \$ C A d	d c \$ #	
# \$ C B	c \$ #	$C \rightarrow c$
# \$ C	c \$ #	
# \$	\$ #	
#	#	accepted.

28

Bottom up parsing -

Bottom up parser builds a derivation by working from the input sentence back towards the start symbol S.

Right most derivation in reverse order is done in bottom up parsing.

In terms of parse tree, this is working from leaves to root.

$$\text{ex} - \begin{aligned} E &\rightarrow E+E \\ E &\rightarrow E * E \\ E &\rightarrow (E) \\ E &\rightarrow id \end{aligned}$$

input :  $id_1 + id_2 * id_3$

$\Rightarrow$  Right most derivation.

$$\begin{aligned} E &\rightarrow E+E \\ &\rightarrow E+E * E \\ &\rightarrow E+E * id_3 \\ &\rightarrow E+id_2 * id_3 \\ &\rightarrow id_1 + id_2 * id_3 \end{aligned}$$

bottom-up approach: go from left to right.  
 $id_1 + id_2 * id_3$

$$\begin{array}{ll} E + id_2 * id_3 & E \rightarrow id \\ E + E * id_3 & E \rightarrow id \\ E + E * E & E \rightarrow id \\ E + E & E \rightarrow E * E \\ E & E \rightarrow E + E \end{array}$$

start symbol.

Hence, acceptable.

29]

### Topdown vs bottom up parsing -

Top down parsing  
construct tree from root to leaves.

Produces left-most derivation.

Recursive descent, LL parsers.

Bottom up parsing.  
construct tree from leaves to root.

Produces reverse right-most derivation.

shift reduce, LR,  
LALR.

30]

### handles -

Always making progress by replacing a substring with LHS of a matching prod will not lead to the goal/start symbol.

A handle of a string is a substring that matches the right side of production and where red<sup>n</sup> to non-red terminal on the left side of prod<sup>n</sup> represents one step along the reverse of a right most derivation.

If the grammar is unambiguous, every right sentential form has exactly one handle.

31)

### Handle pruning -

Keep removing handles, replacing them with corresponding LHS of prod<sup>n</sup>, until we reach start symbol of grammar.

Ex -  $S \rightarrow aABe$   
 $A \rightarrow Abc1h$   
 $B \rightarrow d$

input string : abbcde

handles during parsing of abbcde

Right-contextual form	handle	reducing prod'
Here 'b' is the handle at it matches with right side of prod'	b	$A \rightarrow b$
abb <del>cde</del>	Abc	$A \rightarrow Abc$
a <del>Abcde</del>	d	$B \Rightarrow d$
a <del>Ad<del>e</del></del>	aABe	$S \rightarrow aABe$
<del>aABe</del>	s	

If handle matches with right side of prod', replace it with left side of prod'

32) Shift-reduce parsing -  
 shift-reduce parsing uses a stack to hold grammar symbols & input buffer to hold string to be parsed, because handles always appear at the top of the stack, i.e., there's no need to look deeper into the state.

A shift-reduce parser has four actions -  
 ① shift - next word is shifted onto stack until a handle is formed.

② reduce - right end of handle is at top of stack, locate left end of handle within the stack. Pop handle off

stack & push appropriate LHS.

- ⑨ accept - stop parsing on successful completion of parse & report success.
- ⑩ error - call an error reporting / recovery routine.

33] Shift reduce parsing conflict -

- ① shift-reduce -

Both a shift action & a reduce action are possible in the same state.

- ② reduce-reduce -

Two or more distinct reduce actions are possible in the same state.

34] ③ shift-reduce parsing :-

- shift-reduce parsing is a process of reducing a string to the start symbol of grammar.
- It uses stack to hold grammar & an input to hold the string.
- A shift-reduce parser performs two actions:
  - ① shift
  - ② reduce
- At shift action, the current symbol in the input string is pushed to a stack.

- At each reduction, the symbol will be replaced by the non-terminals.

### - Example ①

grammar

$$S \rightarrow S + S$$

$$S \rightarrow S - S$$

$$S \rightarrow (S)$$

$$S \rightarrow a$$

input string  
 $a_1 - (a_2 + a_3)$

ans =

stack

\$

\$a1

\$a1 \$

\$S-

\$S-(

\$S-(a2

\$S-(s

\$S-(s+

\$S-(s+a3

\$S-(s+s

\$S-(s+s)

\$S-(s)

\$S-S

\$S

input string

$a_1 - (a_2 + a_3) \$$

$-(a_2 + a_3) \$$

$-(a_2 + a_3) \$$

$(a_2 + a_3) \$$

$a_2 + a_3) \$$

$+a_3) \$$

$+a_3) \$$

$a_3) \$$

) \$

) \$

\$

\$

\$

\$

\$

action

shift  $a_1$

reduce by  $S \rightarrow a$

shift -

shift (

shift  $a_2$

reduce by  $S \rightarrow a$

shift  $\epsilon +$

shift  $a_3$

reduce by  $S \rightarrow a$

shift )

reduce by  $S \rightarrow S + S$

reduce by  $S \rightarrow (S)$

reduce by  $S \rightarrow S - S$

accept

LL(1)

LR(0)

LR(1)

## - Example ②

grammar

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow id$$

input string

 $id_1 + id_2 * id_3$ 

stack	input	action
\$	$id_1 + id_2 * id_3 \$$	shift $id_1$
\$ $id_1$	$+ id_2 * id_3 \$$	reduce by $E \rightarrow id$
\$ $E$	$+ id_2 * id_3 \$$	shift $+$
\$ $E +$	$id_2 * id_3 \$$	shift $* id_2$
\$ $E + id_2$	$* id_3 \$$	reduce by $E \rightarrow id$
\$ $E + E$	$* id_3 \$$	reduce by $E \rightarrow E + E$
\$ $E + E *$	$id_3 \$$	shift $*$
\$ $E + E * id_3$	$\$$	reduce by $E \rightarrow id$
\$ $E + E * E$	$\$$	shift $+$
\$ $E$	$* id_3 \$$	shift $*)$
\$ $E *$	$id_3 \$$	shift $id_3$
\$ $E * id_2$	$\$$	reduce by $E \rightarrow id$
\$ $E * E$	$\$$	reduce by $E \rightarrow E * E$
\$ $E$	$\$$	accept

## - Example ③

grammar

$$E \rightarrow 2E2$$

$$E \rightarrow 3E3$$

$$E \rightarrow 4$$

input string

~~24~~ 32423

start

\$

\$S

\$32

\$324

\$32E

\$32E2

\$5E

\$3E3

\$E

input

3 9 2 4 2 3 \$ .

2 4 0 2 \$ .

4 2 3 \$ .

2 3 \$ .

2 3 \$ .

3 \$ .

3 \$ .

3 \$ .

3 \$ .

3 \$ .

3 \$ .

3 \$ .

Decision

Shift 3

Shift 2

Shift 1

sets reduction E → 311

Shift 2

reduce T → 2E2

Shift 3

reduce E → 3E3

accept

### 35] Operator grammar -

A grammar that is used to define mathematical operators is called an operator grammar or operator precedence grammar.

A grammar is said to be operator precedence grammar if it has 2 properties:-

- (i) no RHS of any "prod" has 'ε'
- (ii) no two non-terminals are adjacent on RHS.

Ex -  $E \rightarrow E+E \mid E * E \cdot \text{lid.}$  ✓

$S \rightarrow S A S \mid a$  X

$A \rightarrow b S b \mid b$

There are 3 operator precedence relations:-

i)  $a > b \rightarrow$  means a has higher precedence than b. (ii)

a takes precedence over b.

2)  $a \leq b \rightarrow$  means a yields precedence to b  $\Leftrightarrow$  a has lower precedence than b.

3)  $a \doteq b \rightarrow$  means a has same precedence as b.

### 36] Operator precedence parser.

- This parser is only used for operator grammar.
- Ambiguous grammar are not allowed in any parser except operator precedence parser.
- operation precedence relation table.

$$E \rightarrow E+E \mid E * E \mid id$$

	id	+	*	\$
id	-	>	>	>
+	<	>	<	>
*	<	>	>	>
\$	<	<	<	-

Two ids will never be compared because they will never be compared side by side.

Id has highest priority.

\$ has least precedence.

+ has left associativity.

\* has left associativity.

input string	precedence set <sup>n</sup> inserted	action.
$id + id * id$	$\$ < id > + < id > * > id$	$E \rightarrow id$
$E + id * id$	$\$ + < id > * > id$	

input string	precedence set <sup>n</sup> inserted	action.
$id + id * id$	$\$ < id > + < id > * < id > \$$	$E \rightarrow id$
$E + id * id$	$\$ + < id > * < id > \$$	$E \rightarrow id$
$E + E * id$	$\$ + * < id > \$$	$E \rightarrow id$
$E + E * E$	$\$ + * \$$	
$E + E * E$	$\$ < + < * > \$$	$E \rightarrow E * E$
$E + E$	$\$ < + > \$$	$E \rightarrow E + E$
$E$	$\$ \$$	accepted.

Disadvantages of operator precedence parsing:-

- ① hard to handle tokens like minus sign, which has two different precedences.
- ② only a small class of grammars can be parsed.
- ③ usage is limited.

## 37) LR - Parsing -

The 'L' is for left-to-right scanning of the input & 'R' is for constructing a right most derivation in reverse.

1. LR parsers can be constructed to recognize virtually all programming language constructs for which context free grammars can be written.
2. The LR parsing method is the most general non-backtracking shift-reduce parsing method known.
3. The class of grammars that can be parsed using LR methods is a proper subset of the class of grammars that can be parsed with predictive parsers.
4. An LR parser can detect a syntactic error as soon as it is possible to do so on a left-to-right scan of the input.

## 38) LR parsers -

LR( $k$ ) parsers are most general non-backtracking shift-reduce parsers. Two cases of interest are  $k=0$  &  $k=1$ .

LR(1) is of practical relevance.

$k$  stands for no. of input symbols of look-ahead that are used in making parsing decisions.

When ( $k$ ) is omitted, ' $k$ ' is assumed to be 1.

LR(1) parsers are table-driven, shift-reduce parsers that use a limited right context (1 token) to handle recognition.

LR(1) parsers recognize languages that have an LR(1) grammar. A grammar is LR(1), if given a right-most derivation,

grammar rule combined with a dot indicates a position in its RHS.

Ex -  $A \rightarrow XYZ$  generates 4 LR(1) items.

$A \rightarrow .XYZ$  indicates that the parser is looking for a string that can be derived from XYZ.

$A \rightarrow XY.z$  indicates that the parser has seen a string derived from XY & is looking for one derivable from z.

$A \rightarrow X.Yz$  indicates that the parser has seen a string derived from X & is looking for one derivable from Yz.

$A \rightarrow XYZ.$  indicates that the parser has seen a string derived from XYZ.

LR(0) items play a key role in SLR(1) table construction algorithm.

LR(1) items play a key role in the LR(1) & LALR(1) table construction algorithm.

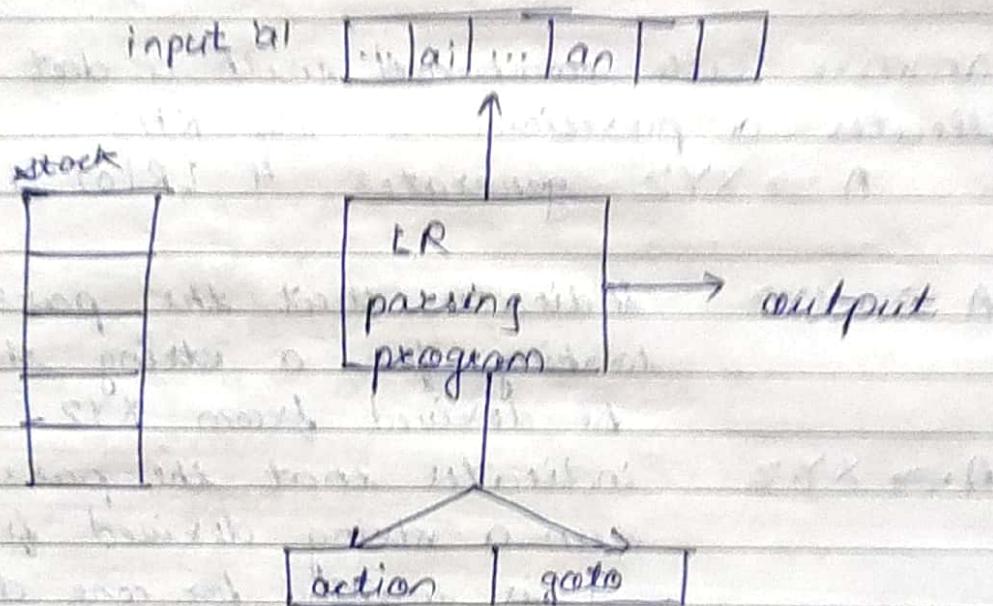
LR parsers have more info available than

LL parser when choosing a prod'!

LR knows everything derived from RHS plus k lookahead symbols.

LL just knows k lookahead symbols into what derived from RHS.

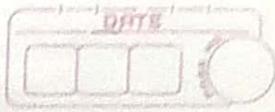
### 39] LR parsing algorithm :-



It consists of an input, an output, a stack, a driver program and a parsing table that has two parts:- action & goto.

The LR parser program determines  $s_m$ , the current state on the top of the stack &  $a_i$ , the current input symbol. It then consists action  $[s_m, a_i]$ , which can have one of four values:-

1. shift  $s$ , where  $s$  is state.
2. reduce by a grammar prod'  $A \rightarrow \beta$
3. accept
4. error.



The function 'goes to' takes a state & grammar symbol as arguments & produces a state. The 'goes' function of parsing table constructed from a grammar  $G$  using the SLR, canonical LR or LALR method.

u0) LR(0) parsing -

$$S \rightarrow AA$$

$$A \rightarrow aA \mid b$$

→ step 1:- Augmented grammar.

$$S' \rightarrow S$$

$$S \rightarrow AA$$

$$A \rightarrow aA \mid b$$

d.abc

da.bcd

Step 1:-

$$S \rightarrow AA \quad -①$$

$$A \rightarrow aA \quad -②$$

$$A \rightarrow b \quad -③$$

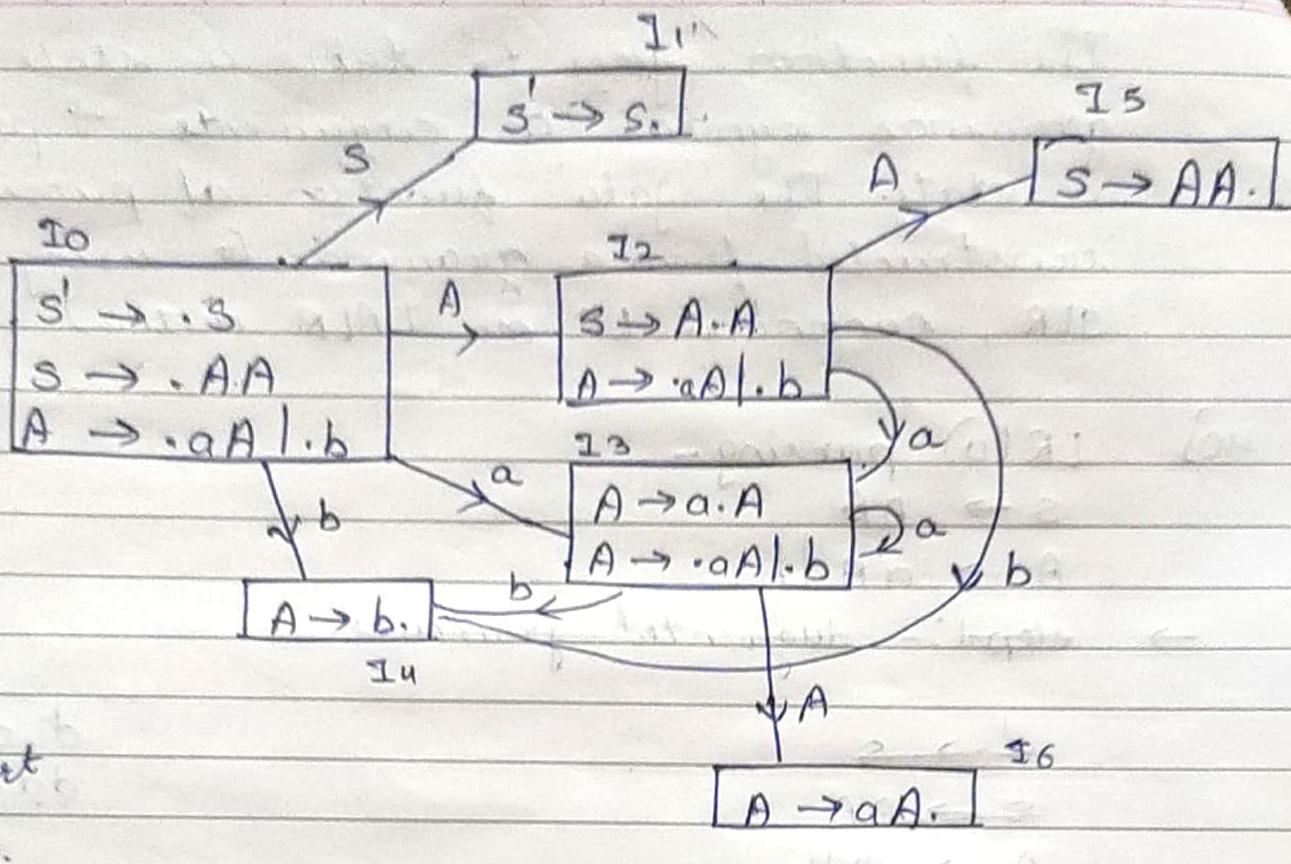
Step 2:- Augmented grammar

$$S' \rightarrow S$$

$$S \rightarrow \cdot AA$$

$$A \rightarrow \cdot aA \mid b$$

Step 3:- applying closure.



action part  
contains  
terminals.  
goto  
part  
contains  
variables.

step 4:- LR(0) parsing table.

State	action			goto		
	a	b	\$	A	A	S
0	$S_3$	$S_4$		2		1
1			accept			
2	$S_3$	$S_4$		5		
3	$S_3$	$S_4$		6		
4	$\tau_3$	$\tau_3$	$\tau_3$			
5	$\tau_1$	$\tau_1$	$\tau_1$			
6	$\tau_2$	$\tau_2$	$\tau_2$			

$s \rightarrow \alpha A$

q1) SLR(0) parsing.

$$S \rightarrow AA$$

$$A \rightarrow aAlb$$

step 1:-

$$S \rightarrow AA \quad -①$$

$$A \rightarrow aA \quad -②$$

$$A \rightarrow b \quad -③$$

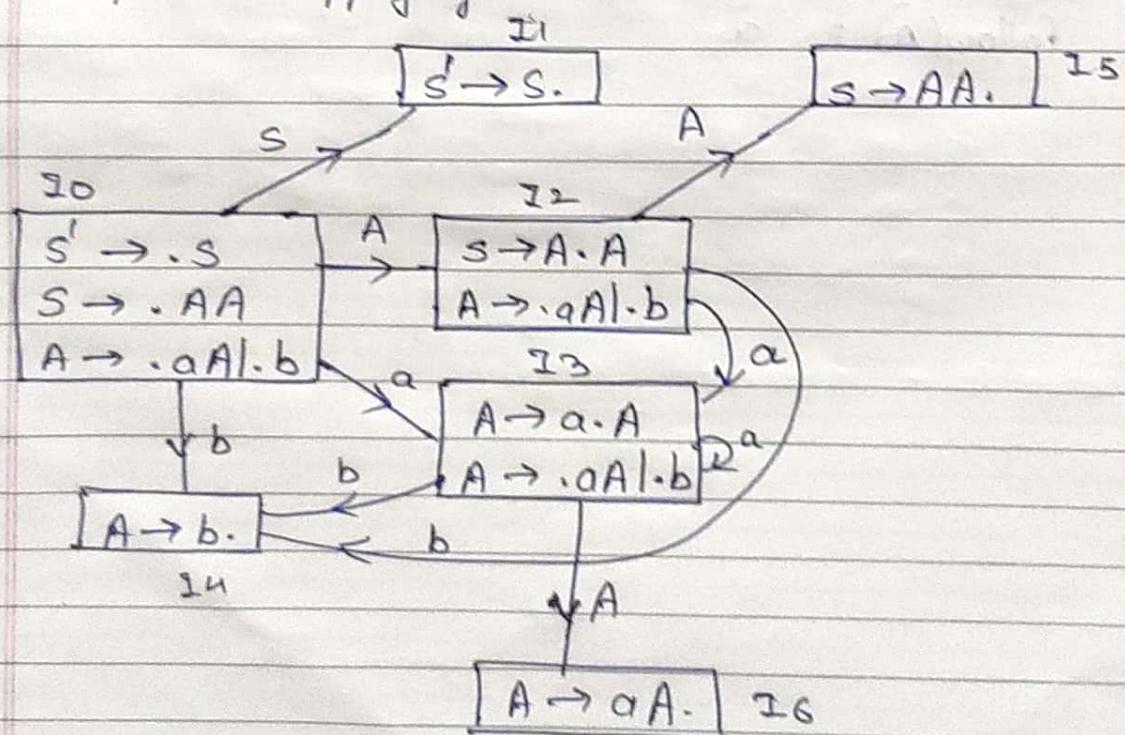
step 2:- augmented grammar.

$$S' \rightarrow S$$

$$S \rightarrow .AA$$

$$A \rightarrow .aAl.b$$

step 3:- applying closure



step 4 - SLR(1) parsing table.

goto is same as LR(0)

shift actions are same as LR(0)

reduce actions are different than LR(0).

don't write reduce action for whole row. Write only in follow's columns.

	action				goto	
	a	b	$\epsilon \$$		A	S
0	$s_3$	$s_4$			2	1
1			accept			
2	$s_3$	$s_4$			5	
3	$s_3$	$s_4$			6	
4	$s_4$					
5			$T_5$			
6	$r_6$					

$$\text{follow}(S) = \$$$

$$\text{follow}(A) = a$$

42]

CLR parsing table.

CLR &amp; LR(0) use LR(0) canonical items

 $S \rightarrow aAd \mid aBd \mid aBe \mid bAe$  $S \rightarrow aAd \mid bBd \mid aBe \mid bAe$  $A \rightarrow c \quad b, d \leftarrow A$  $B \rightarrow c \quad a, b \leftarrow B$ Step 1:-  $\begin{array}{l} S \rightarrow aAd \mid bBd \mid aBe \mid bAe \\ \hline \end{array}$  $S \rightarrow aAd \quad -① \quad b, d \leftarrow A$  $S \rightarrow bBd \quad -② \quad a, b \leftarrow B$  $S \rightarrow aBe \quad -③ \quad -A$  $S \rightarrow bAe \quad -④$  $A \rightarrow c \quad -⑤$  $B \rightarrow c \quad -⑥$ 

Step 2:- Augmented grammar is given

 $S \rightarrow \cdot S, \$$  \$ is lookahead $S \rightarrow \cdot aAd, \$$  $S \rightarrow \cdot bBd, \$$  $S \rightarrow \cdot aBe, \$$  $S \rightarrow \cdot bAe, \$$ 

Step 3:- closure apply.

I1	*	$S \rightarrow aA.d, \$$
$S' \rightarrow S, \$$		
$S \rightarrow .S, \$$	A	$S \rightarrow aB.e, \$$
$S \rightarrow .aAd, \$$		$S \rightarrow aB.e, \$$
$S \rightarrow .bBd, \$$	B	$S \rightarrow aB.e, \$$
$S \rightarrow .aBe, \$$	C	$A \rightarrow c., d$
$S \rightarrow .BAe, \$$	D	$B \rightarrow c., e$
	E	$A \rightarrow c., d$
	F	$B \rightarrow c., e$
	G	$S \rightarrow b.Bd, \$$
	H	$S \rightarrow b.Bd, \$$
	I	$S \rightarrow b.Ae, \$$
	J	$B \rightarrow c., d$
	K	$B \rightarrow c., d$
	L	$A \rightarrow c., e$
	M	$B \rightarrow c., d$
	N	$A \rightarrow c., e$
	O	$S \rightarrow BAe, \$$
	P	$S \rightarrow BAe, \$$
	Q	$B \rightarrow c., d$
	R	$A \rightarrow c., e$

step 4:- CLR parsing table.

gotos are same as LR(0)

shift moves are same as LR(0).

reduce moves should not be written in whole row. Reduce moves should be written only in lookahead column.

3, Ad.  $\leftarrow$  2

High priority = 0 goto

	action					\$	goto			\$	
	a	b	c	d	e	\$	A	B	S		
0	$s_2$	$s_3$				accept				1	
1						accept					
2			$s_6$			.	4	5			
3			$s_9$				8	7			
4				$s_{10}$							
5					$s_{11}$						
6				$\gamma_5$	$\gamma_6$						
7					$s_{12}$						
8						$s_{13}$					
9				$\gamma_6$	$\gamma_5$						
10						$\gamma_5$	$\gamma_1$				
11							$\gamma_3$				
12							$\gamma_2$				
13							$\gamma_4$				