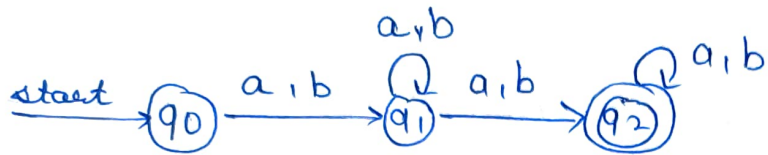


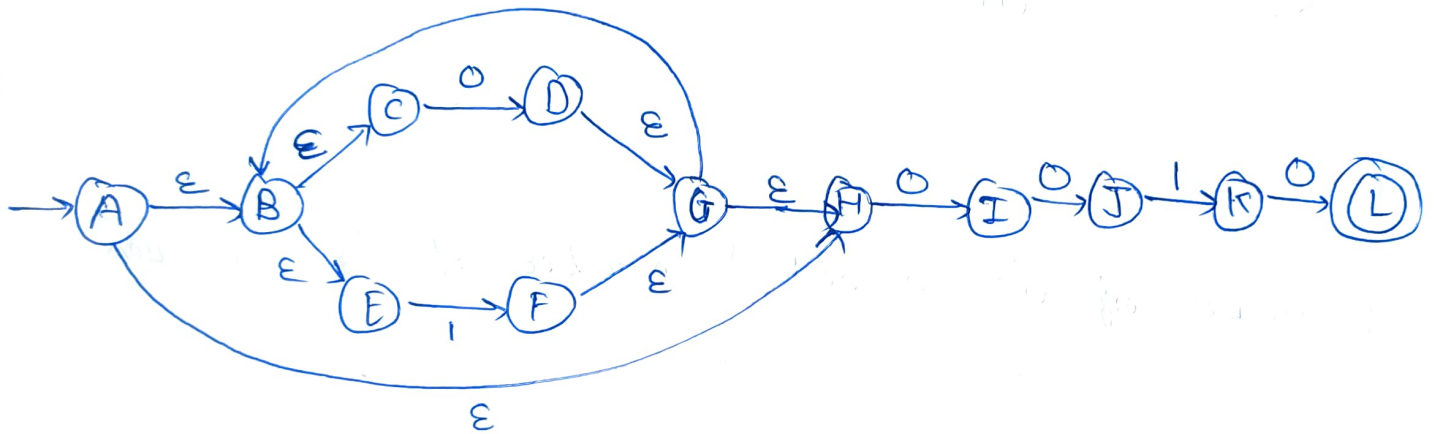
Q. Construct minimum state DFA for reg regular exp $(a|b)^* a(a|b)$.

→ $L = \{aa, ab, aab, aaa, bbab, \dots\}$



Q. Construct NFA for reg exp $(0|1)^* 0010$

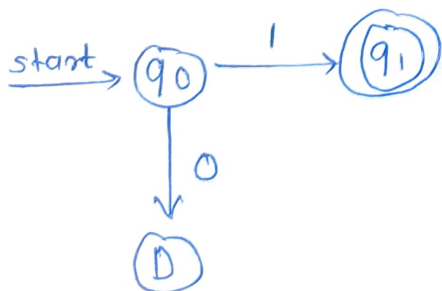
→



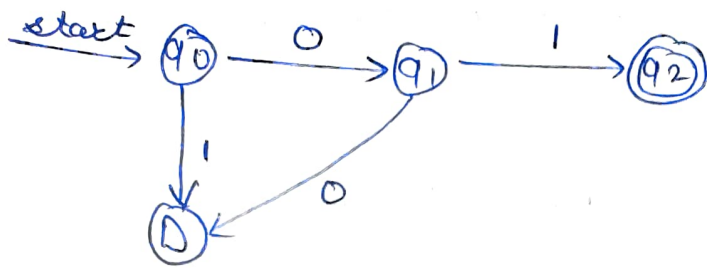
Q. Construct DFA for accepting the following language over an alphabet $\{0,1\}$.

1] accept only 1 as string.

$L = \{1\}$



→ accept string as 01.



3] number of 1's is even & number of 0's is even.

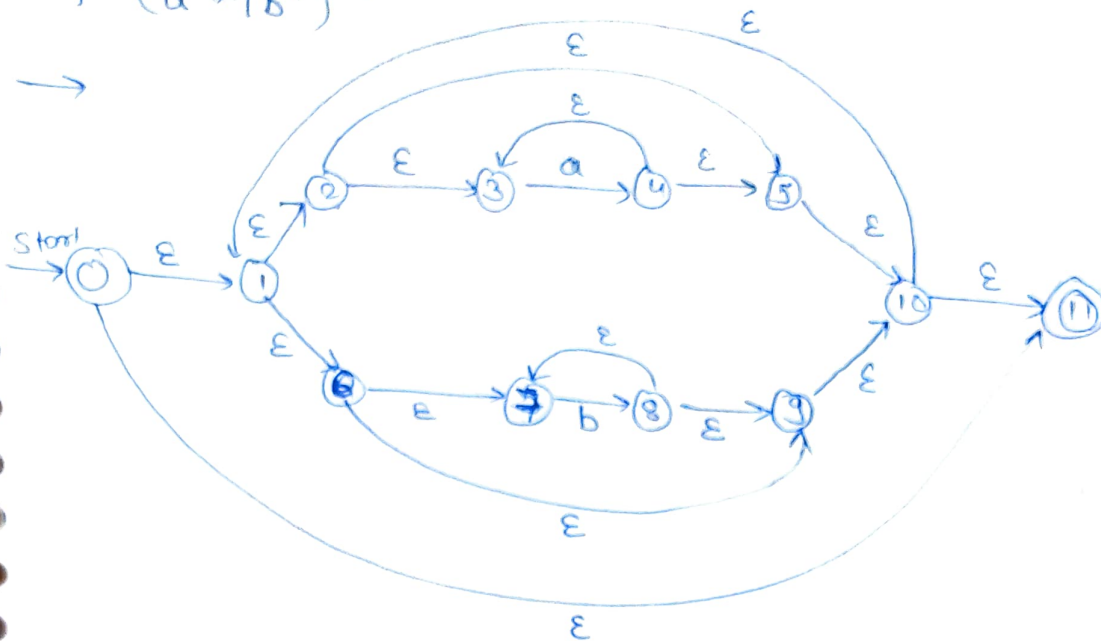
→ $L = \{ 1100, 0011, 00001111, 11110000, \dots \}$



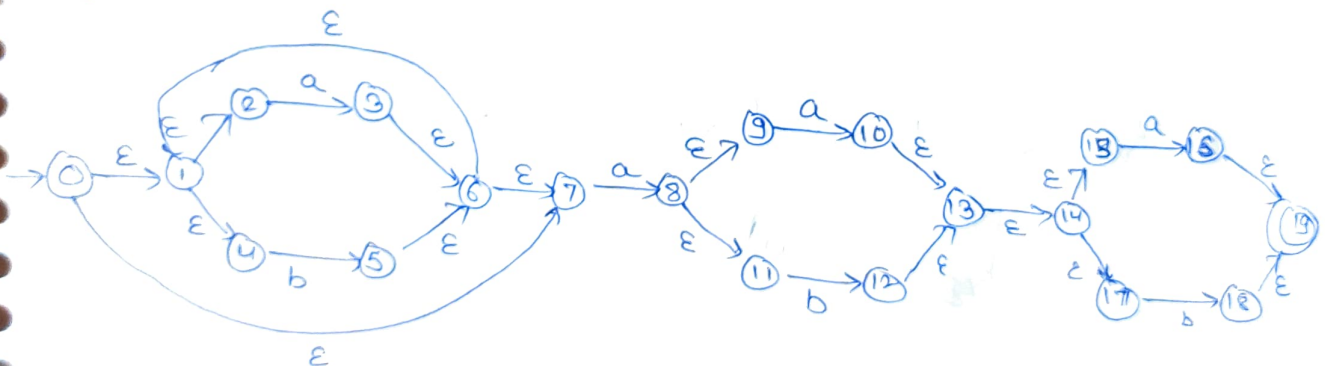
4] number of 0's is odd & number of 1's is even.

Q. Construct NFA for following regular exp (using Thompson's rule).

1) $(a^* | b^*)^*$



2) $(a|b)^* a(a|b)(a|b)$

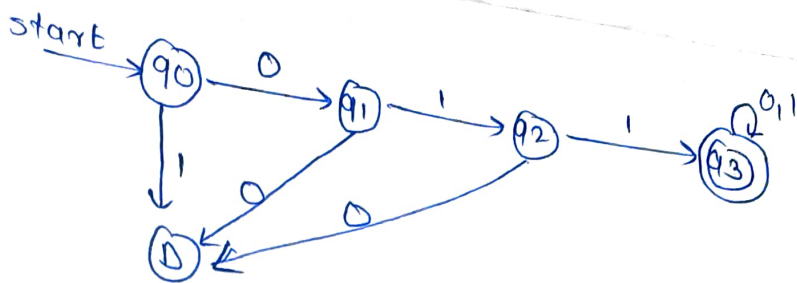


Q. Construct DFA for following.

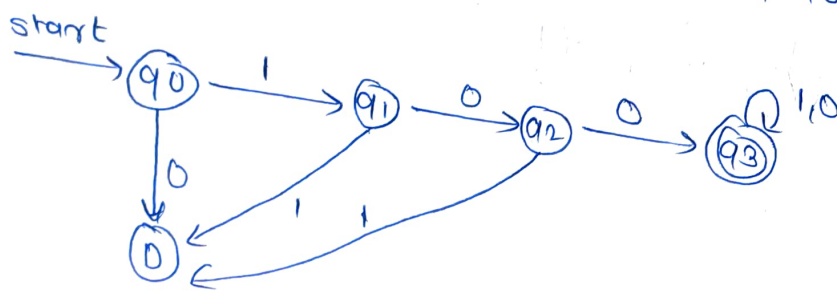
1] all strings starting with 011.

→ $L = \{011, 0110, 0111, 01101, 01110, \dots\}$

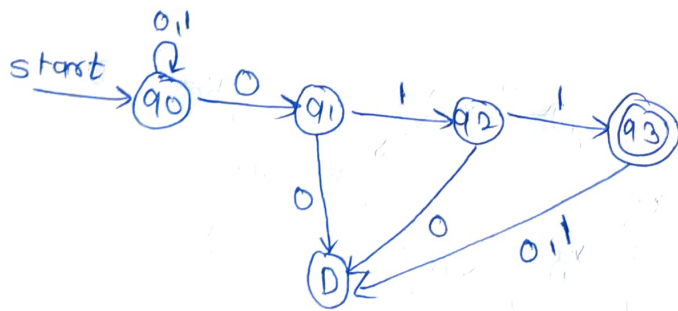
diagram to represent



2] all strings starting with 100,
 $\rightarrow L = \{100, 1000, 1001, 10001, 10010, \dots\}$

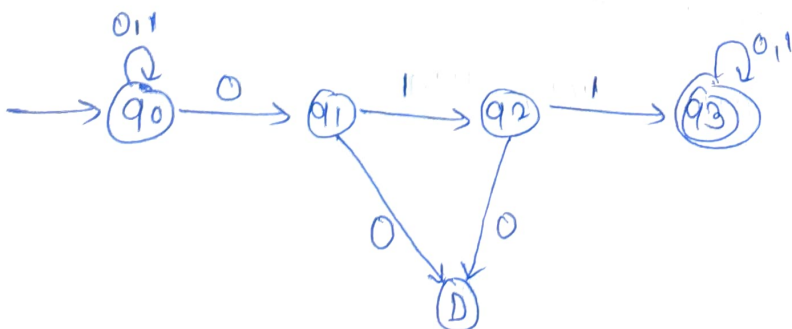


3] all strings ending with 011
 $\rightarrow L = \{0011, 011, 01011, 10011, 00011, 11011, \dots\}$

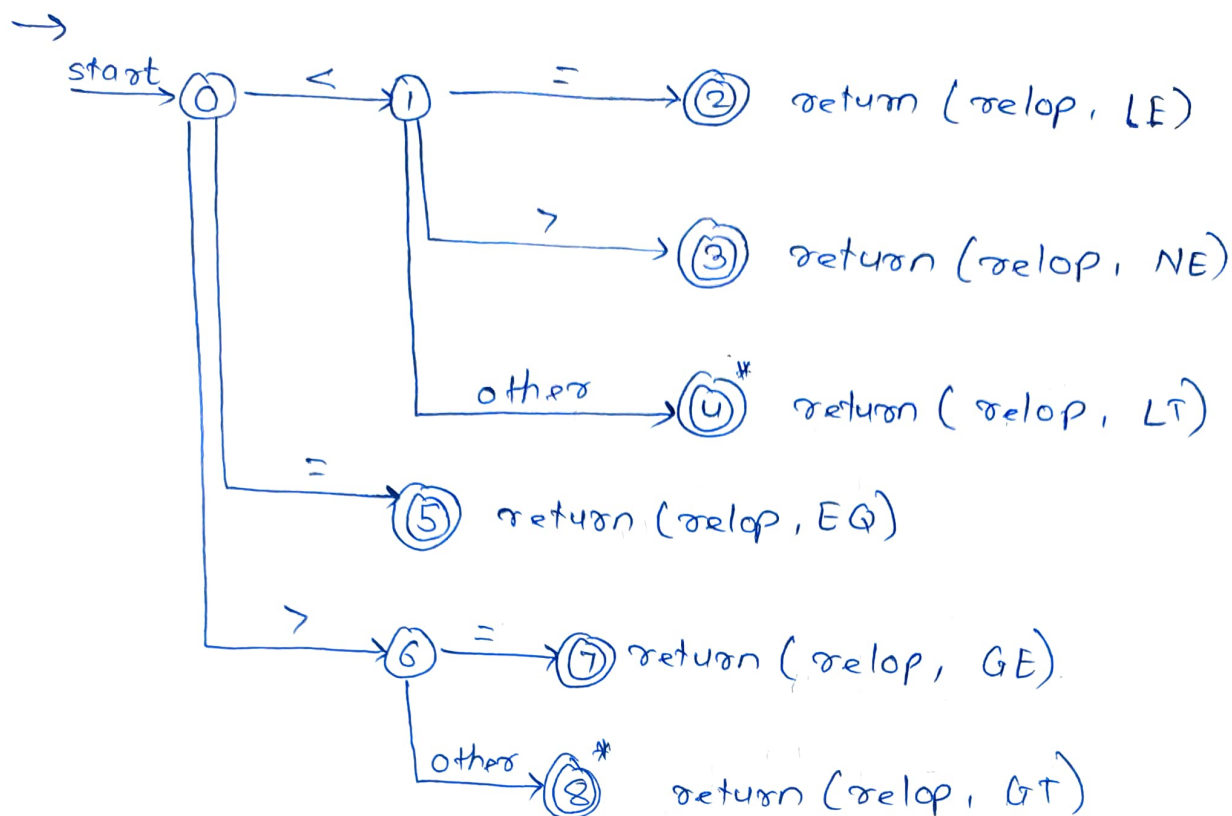


4] all strings with 011 as substring.

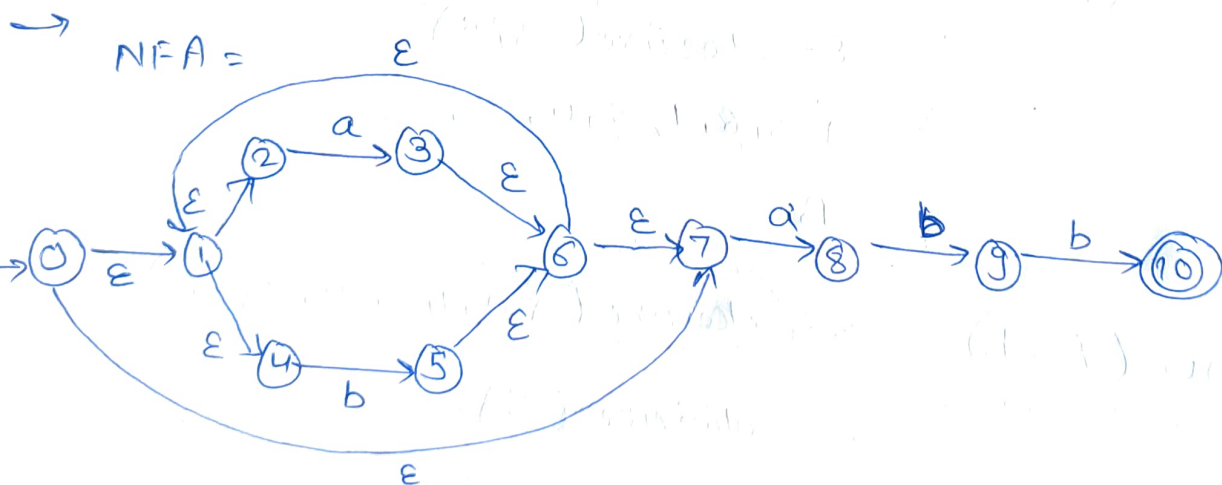
$\rightarrow L = \{011, 0011, 01101, 011011, 1101100, 1101111, 0001111, \dots\}$



Q. Draw a transition diagram to represent relational operators.



Q. Construct NFA from a regular exp $(a|b)^*abb$.
Convert into DFA using subset constⁿ method.



Transition table for NFA is:-

	a	b	ϵ
0	-	-	1,7
1	-	-	2,4
2	3	-	-
3	-	-	6
4	-	5	-
5	-	-	6
6	-	-	7,1
7	8	-	-
8	-	9	-
9	-	10	-
10	-	-	-

$$\textcircled{1} \epsilon\text{-closure}(0) = \{0, 1, 2, 4, 7\} = A$$

$$\begin{aligned} \textcircled{2} \text{move}(A, a) &= \epsilon\text{-closure}(\{0, 1, 2, 4, 7\}, a) \\ &= \epsilon\text{-closure}(3, 8) \\ &= \{3, 6, 1, 2, 4, 8, 7\} \\ &= B \end{aligned}$$

$$\begin{aligned} \textcircled{3} \text{move}(A, b) &= \epsilon\text{-closure}(\{0, 1, 2, 4, 7\}, b) \\ &= \epsilon\text{-closure}(5) \\ &= \{5, 6, 1, 7, 2, 4\} \\ &= C \end{aligned}$$

$$\begin{aligned} \textcircled{4} \text{move}(B, a) &= \epsilon\text{-closure}(\{1, 2, 3, 4, 6, 7, 8\}, a) \\ &= \epsilon\text{-closure}(3, 8) \\ &= B \end{aligned}$$

$$\begin{aligned}
 \textcircled{5} \text{ move}(B, b) &= \varepsilon\text{-closure}(\{1, 2, 3, 4, 8, 7, 8\}, b) \\
 &= \varepsilon\text{-closure}(B, 9) \\
 &= \{5, 6, 1, 7, 2, 4, 9\} \\
 &= D
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{6} \text{ move}(C, a) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7\}, a) \\
 &= \varepsilon\text{-closure}(3, 8) \\
 &= B
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{7} \text{ move}(C, b) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7\}, b) \\
 &= \varepsilon\text{-closure}(3) \\
 &= C
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{8} \text{ move}(D, a) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7, 9\}, a) \\
 &= \varepsilon\text{-closure}(3, 8) \\
 &= B
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{9} \text{ move}(D, b) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7, 9\}, b) \\
 &= \varepsilon\text{-closure}(5, 10) \\
 &= \{5, 6, 7, 1, 2, 4, 10\} \\
 &= E
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{10} \text{ move}(E, a) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7, 10\}, a) \\
 &= \varepsilon\text{-closure}(3, 8) \\
 &= B
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{11} \text{ move}(E, b) &= \varepsilon\text{-closure}(\{1, 2, 4, 5, 6, 7, 10\}, b) \\
 &= \varepsilon\text{-closure}(5) \\
 &= C
 \end{aligned}$$

$A = \{0, 1, 2, 4, 7\} \Rightarrow$ starting state

$B = \{1, 2, 3, 4, 6, 7, 8\}$

$C = \{1, 2, 4, 5, 6, 7\}$

$D = \{1, 2, 4, 5, 6, 7, 9\}$

$E = \{1, 2, 4, 5, 6, 7, 10\} \rightarrow$ accepting state

Transition diagram for DFA is:

state	a	b
$\rightarrow A$	B	C
B	B	D
C	B	C
D	B	E
E	B	C

DFA =

