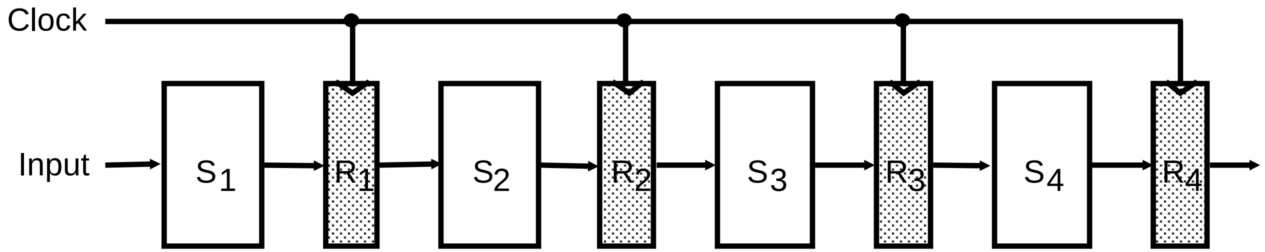
OPERATIONS IN EACH PIPELINE STAGE

Clock Pulse Number	Segment 1		Segment 2		Segment 3
	R1	R2	R3	R4	R5
1	A1	B1			
2	A2	B2	A1 * B1	C1	
3	A3	B3	A2 * B2	C2	A1 * B1 + C1
4	A4	B4	A3 * B3	C3	A2 * B2 + C2
5	A5	B5	A4 * B4	C4	A3 * B3 + C3
6	A6	B6	A5 * B5	C5	A4 * B4 + C4
7	A7	B7	A6 * B6	C6	A5 * B5 + C5
8			A7 * B7	C7	A6 * B6 + C6
9					A7 * B7 + C7

GENERAL PIPELINE

General Structure of a 4-Segment Pipeline



Space-Time Diagram

Segment	1	2	3	4	5	6	7	8	9
1	T1	T2	T3	T4	T5	T6			
2		T1	T2	T3	T4	T5	T6		
3			T1	T2	T3	T4	T5	T6	
4				T1	T2	T3	T4	T5	T6

Clock cycles

PIPELINE SPEEDUP

n: Number of tasks to be performed

Conventional Machine (Non-Pipelined)

t_n: Clock cycle

τ_1: Time required to complete the n tasks

$\tau_1 = n * t_n$

Pipelined Machine (k stages)

t_p: Clock cycle (time to complete each suboperation)

τ_κ: Time required to complete the n tasks

$\tau_\kappa = (k + n - 1) * t_p$

Speedup

S_k: Speedup

$S_k = n*t_n / (k + n - 1)*t_p$

$$\lim_{n \to \infty} S_k = \frac{t_n}{t_p} \quad (= k, \text{ if } t_n = k * t_p)$$

PIPELINE AND MULTIPLE FUNCTION UNITS

Example

- 4-stage pipeline
- subopertion in each stage; t_p = 20nS
- 100 tasks to be executed
- 1 task in non-pipelined system; 20*4 = 80nS

Pipelined System

$$(k + n - 1)*t_p = (4 + 99) * 20 = 2060nS$$

Non-Pipelined System

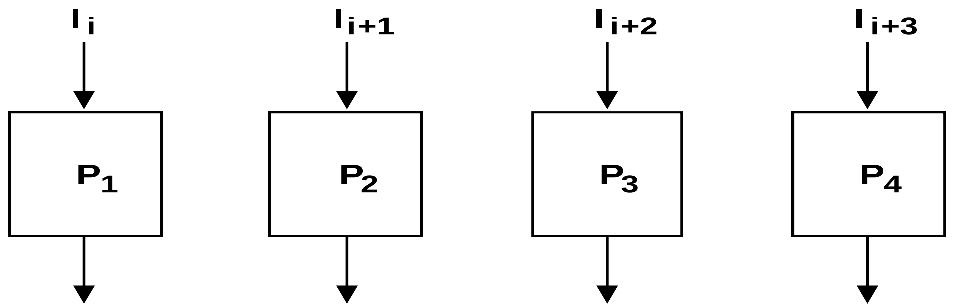
$$n*k*t_p = 100 * 80 = 8000nS$$

Speedup

$$S_k = 8000 / 2060 = 3.88$$

4-Stage Pipeline is basically identical to the system with 4 identical function units

Multiple Functional Units

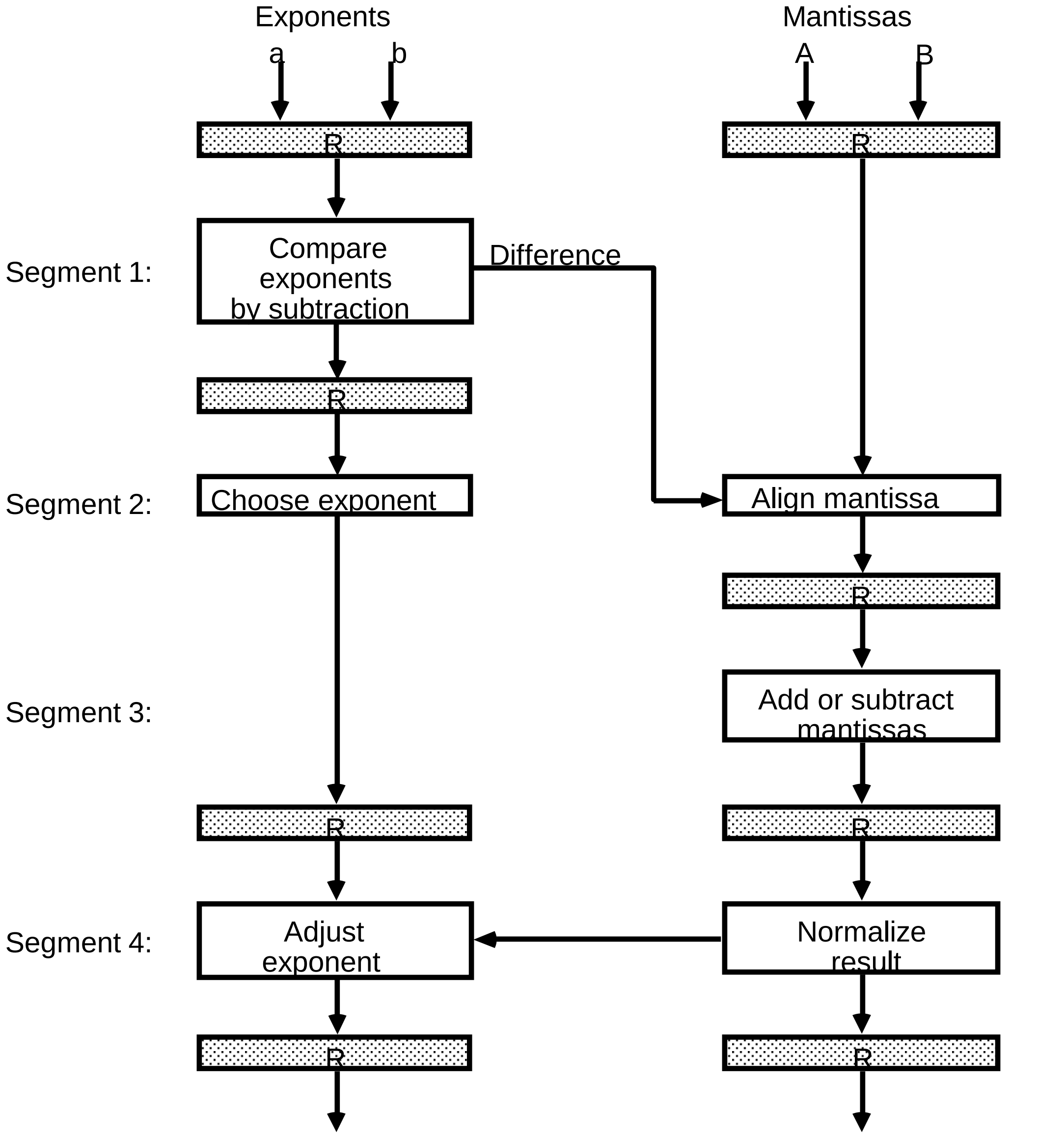


ARITHMETIC PIPELINE

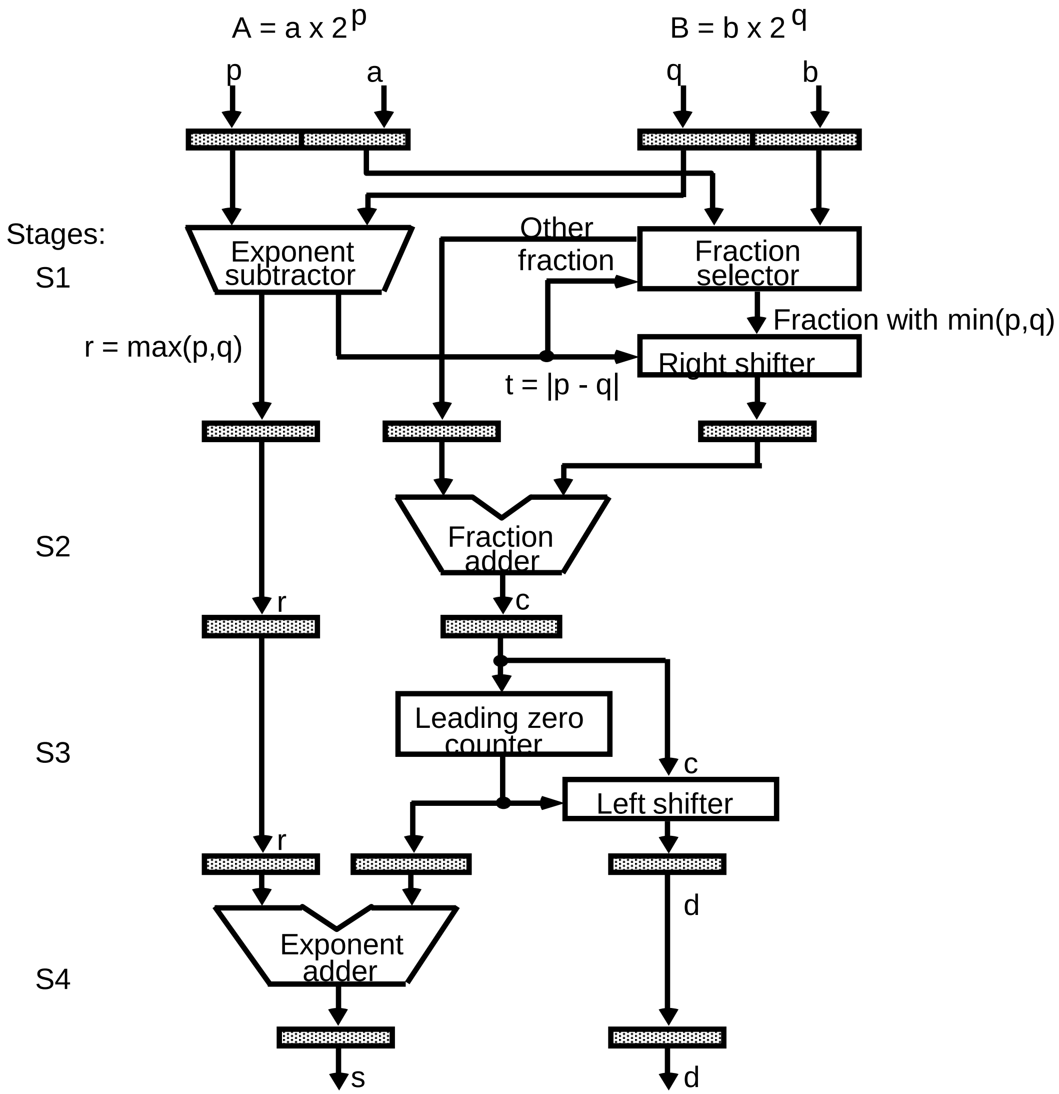
Floating-point adder

$X = A \times 2^a$
$Y = B \times 2^b$

[1] Compare the exponents
[2] Align the mantissa
[3] Add/sub the mantissa
[4] Normalize the result



4-STAGE FLOATING POINT ADDER



$C = A + B = c \times 2^r = d \times 2^s$
$(r = \max(p,q),\ 0.5 \le d < 1)$

INSTRUCTION CYCLE

Six Phases* in an Instruction Cycle

[1] Fetch an instruction from memory
[2] Decode the instruction
[3] Calculate the effective address of the operand
[4] Fetch the operands from memory
[5] Execute the operation
[6] Store the result in the proper place

* Some instructions skip some phases
* Effective address calculation can be done in the part of the decoding phase
* Storage of the operation result into a register is done automatically in the execution phase

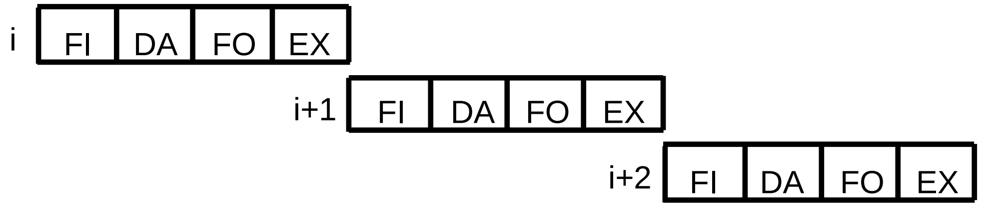
==> 4-Stage Pipeline

[1] FI: Fetch an instruction from memory
[2] DA: Decode the instruction and calculate the effective address of the operand
[3] FO: Fetch the operand
[4] EX: Execute the operation

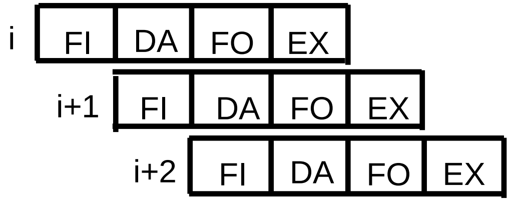
INSTRUCTION PIPELINE

Execution of Three Instructions in a 4-Stage Pipeline

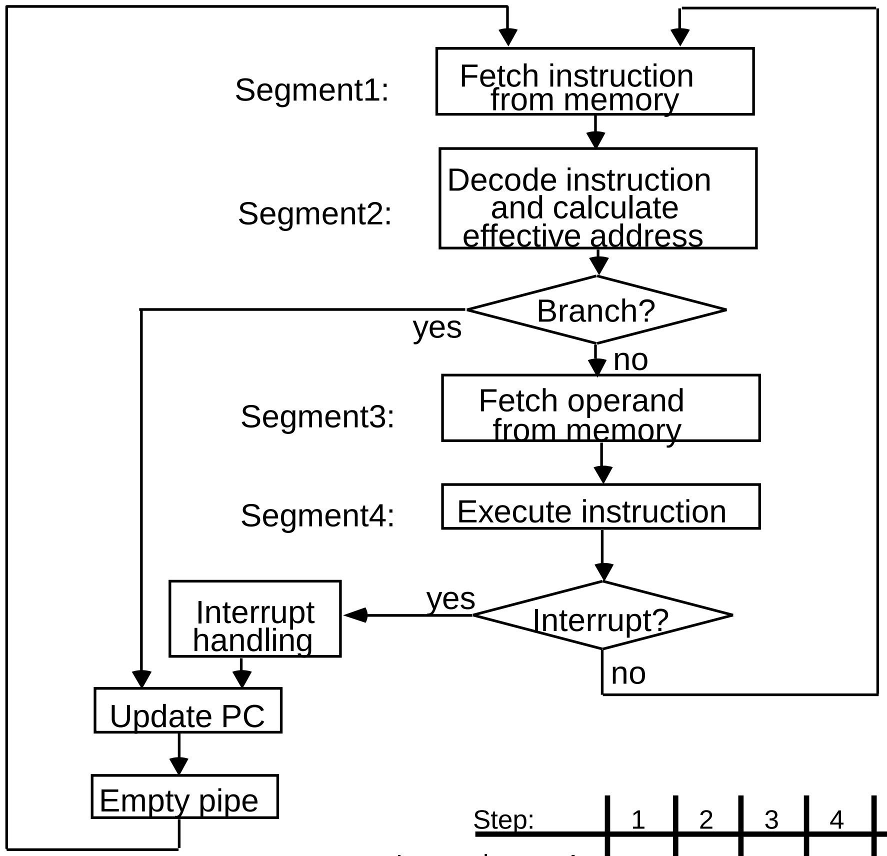
Conventional



Pipelined



INSTRUCTION EXECUTION IN A 4-STAGE PIPELINE



Step:		1	2	3	4	5	6	7	8	9	10	11	12	13
Instruction	1	FI	DA	FO	EX									
	2		FI	DA	FO	EX								
(Branch)	3			FI	DA	FO	EX							
	4				FI	-	-	FI	DA	FO	EX			
	5					-	-	-	FI	DA	FO	EX		
	6									FI	DA	FO	EX	
	7										FI	DA	FO	EX