

# Homework 6: Industrial Organisation

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*N.B. The code for this exercise was written in R and is available on my Github account. [www.github.com/dhananjayghei/io\\_estimation](http://www.github.com/dhananjayghei/io_estimation).*

## Some basics

1. Read the data into a statistical package and look at summary statistics to convince yourself that the data was read in correctly. Try a simple OLS regression of  $\log(\text{QUANTITY})$  on a constant,  $\log(\text{PRICE})$ , LAKES, and (twelve of) the seasonal dummy variables. If you were to view this as an estimate of a demand curve what would the price elasticity of demand be? Why does this number seem unreasonable?

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Table 1 shows the summary statistics from Porter's data set. The number are the same as in Table II of Porter. Thus, the data has been read in correctly. Figure 1 shows the plot of price as a function

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**Table 1** Summary statistics

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The table shows the summary statistics from Porter's data set.

	Mean	Sdev	Min	Max
Price	0.246	0.067	0.125	0.400
Quantity	25384.000	11633.000	4810.000	76407.000
Lakes	0.573	0.495	0.000	1.000
Collusion	0.619	0.486	0.000	1.000

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of time (in weeks). This replicates the Figure I from Porter.

Column I of Table 2 shows the OLS estimates of the demand equation. Demand elasticity from OLS is equal to 0.639. The demand is inelastic. This seems unreasonable because if we expect JEC to act as a monopolist, prices should go to infinity. One potential reason for this is that the price is endogenous which gives the estimate of elasticity to be biased towards zero.

2. Try doing the regression instead using instrumental variable with the COLLUSION variable as the instrument for PRICE. How does the reported price elasticity change. Is the estimate closer to that in Porter's paper or that in Ellison's paper and why? How do you interpret the coefficient on the LAKES variable? On the seasonal dummies? What is the R-squared of the regression and what do you make of it?

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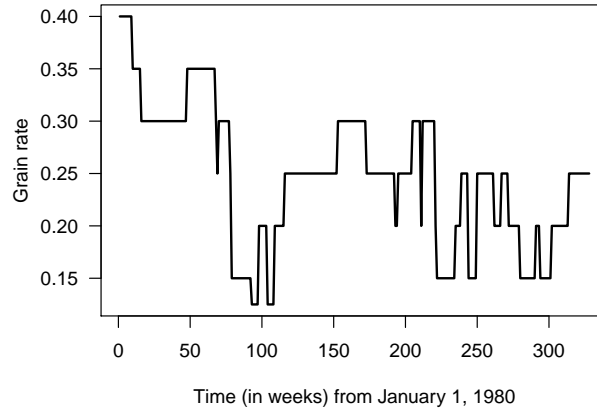
Column II of Table 2 shows the IV estimate using collusion as the instrument for price. Instrumenting increases the estimated demand elasticity from .639 to .867. This is closer to the Ellison's paper. For the Lakes variable, going from 0 to 1 indicates the opening of great lakes for navigation. The difference in expected log quantities is given by  $\log(Q_1) - \log(Q_0) = -.423$  which gives  $\frac{Q_1}{Q_0} = \exp(-.423) = .66$ .

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**Figure 1** Plot of price as a function of time

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The figure shows the plot of price as a function of time. The time is in weeks starting from Jan 1, 1980.



Thus, opening of lakes lead to a reduction of 34% in the quantity shipped given price. The interpretation on the seasonal dummies is similar to the one for lakes. In fact, there are some seasonal dummies which show statistical significance. In the IV case, the R-square coefficients do not hold much significance. This is the reason we do not get an F-stat for the two regressions.

3. Try the regression with the DM1-DM4 and COLLUSION as instruments for price. Do the estimates “improve” in any way?

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Column III of Table 2 shows the instrumental variable estimation using the collusion variable and the dummy variable as instrument. This does not help in changing the elasticity.

4. Estimate a supply equation as in Porter and Ellison using the LAKES variable as an instrument for quantity. What does the magnitude of the coefficient on COLLUSION tell us about the effect of collusion on prices? What might the coefficient on QUANTITY in this regression indicate about the nature of costs in the JEC?
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## Model derivation and interpretation

1. Suppose that rather than the log-log specification of demand you’ve been using so far, you tried others and found that a linear specification of demand like

$$Q_t = \alpha_0 + \alpha_1 P_t + \alpha_2 Lakes_t + u_t$$

seemed most appropriate. Show that for this demand curve the optimal price for a monopolist with a constant marginal cost of  $c$  to set is

$$P_t = c - \frac{1}{\alpha_1} Q_t$$

Given this result, what functional form would you choose for the supply curve in this model?

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The monopolist will solve:

$$\max_p (p - c)Q$$

**Table 2** Demand estimation

The table shows the demand estimation using OLS and instrumental variable estimation. Column I shows the results of OLS, Column II shows the results of IV using collusion as an instrument for price and Column III shows the results of IV using collusion and the dummies (DM1-DM4) as instruments for price.

	<i>Dependent variable:</i>		
	OLS (1)	IV (2)	IV (3)
Constant	9.176*** (0.135)	8.865*** (0.196)	9.045*** (0.180)
Log(Price)	-0.639*** (0.082)	-0.867*** (0.132)	-0.735*** (0.120)
Lakes	-0.448*** (0.120)	-0.423*** (0.122)	-0.437*** (0.120)
SEAS1	0.200* (0.106)	0.222** (0.108)	0.209* (0.107)
SEAS2	0.244** (0.106)	0.267** (0.108)	0.254** (0.107)
SEAS3	0.288*** (0.108)	0.283*** (0.109)	0.286*** (0.108)
SEAS4	0.242* (0.131)	0.205 (0.134)	0.226* (0.132)
SEAS5	0.180 (0.164)	0.125 (0.168)	0.157 (0.165)
SEAS6	0.255 (0.164)	0.191 (0.169)	0.228 (0.166)
SEAS7	-0.102 (0.164)	-0.163 (0.168)	-0.128 (0.166)
SEAS8	0.136 (0.164)	0.073 (0.169)	0.109 (0.166)
SEAS9	0.302* (0.165)	0.217 (0.172)	0.266 (0.169)
SEAS10	0.348** (0.164)	0.283* (0.169)	0.320* (0.167)
SEAS11	0.352** (0.163)	0.310* (0.166)	0.334** (0.165)
SEAS12	0.133 (0.111)	0.131 (0.112)	0.132 (0.111)
Observations	328	328	328
R <sup>2</sup>	0.313	0.296	0.310
Adjusted R <sup>2</sup>	0.282	0.264	0.279
Residual Std. Error (df = 313)	0.397	0.402	0.398
F Statistic	10.169*** (df = 14; 313)		

Note:

\*p<0.1; \*\*p<0.05; \*\*\*p<0.01

**Table 3** Supply estimation

The table shows the supply side estimation using OLS and instrumental variable estimation. Column I shows the results of OLS, Column II shows the results of IV using the lakes variable as an instrument for quantity.

	<i>Dependent variable:</i>	
	OLS (1)	IV (2)
Constant	−0.934*** (0.284)	−3.945** (1.758)
D1	−0.241*** (0.046)	−0.202*** (0.055)
D2	−0.199*** (0.069)	−0.173** (0.081)
D3	−0.308*** (0.048)	−0.319*** (0.065)
D4	−0.332*** (0.106)	−0.208 (0.172)
SEAS1		0.063 (0.070)
SEAS2		0.100 (0.073)
SEAS3		−0.030 (0.088)
SEAS4		−0.072 (0.070)
SEAS5		−0.073 (0.077)
SEAS6		−0.113 (0.071)
SEAS7		0.043 (0.110)
SEAS8		0.011 (0.084)
SEAS9		−0.140** (0.070)
SEAS10		−0.126* (0.069)
SEAS11		−0.013 (0.070)
SEAS12		−0.030 (0.072)
Collusion	0.296*** (0.027)	0.368*** (0.054)
Log(Quantity)	−0.044 (0.027)	0.253 (0.173)
Observations	328	328
R <sup>2</sup>	0.455	0.316
Adjusted R <sup>2</sup>	0.445	0.276
Residual Std. Error	0.215 (df = 321)	0.246 (df = 309)
F Statistic	44.638*** (df = 6; 321)	
<i>Note:</i> *p<0.1; **p<0.05; ***p<0.01		

The first order condition is given by:  $(p - c)\frac{\partial Q}{\partial p} + Q = 0$ . From the demand function, we know that  $\frac{\partial Q}{\partial p} = \alpha_1$ , so we have  $p = c - \frac{1}{\alpha}Q$ .

2. What pricing rule would result with this demand curve if the industry instead consisted of perfectly competitive firms with total costs of the form  $c(Q_t) = c_0Q_t + c_1Q_t^2$  setting price equal to marginal cost? Could one use an approach like Porter's to distinguish between these two models of behavior? Talk about why this is an important question.

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If the industry was perfectly competitive, then the firms would price at marginal cost. Therefore, the supply equation will be:  $p_t = c_0 + 2c_1Q_t$ .

## Causes of price wars

1. Using the collusion variable generate an indicator variable for the start of a price war. Perform a probit regression with this indicator as a dependent variable and with QUANTITY, LAKES, and DM1-DM4 (or a subset thereof) as explanatory variables. What inferences might you want to draw about whether price wars are more likely to occur in booms from the coefficients on the first two variables? Why are these variables not really the right ones to be using in the equation?

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Table 4 shows the estimation from probit results.

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**Table 4** Cause of price wars

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The table shows the results from probit estimation.

	<i>Dependent variable:</i>
	Price war
Constant	−5.351*** (0.202)
Quantity	−0.00001 (0.00001)
Lakes	−0.379 (0.290)
D1	3.818*** (0.279)
D2	4.423*** (0.524)
D3	4.268*** (0.241)
D4	−0.220* (0.122)
Observations	328
Log Likelihood	−45.106
Akaike Inf. Crit.	104.211
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

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