

# Recursion in One Shot

# What and Why?

$$n! = n \times (n-1)!$$
  
 $f(n) = n \times f(n-1) \rightarrow \text{Reccurence kelation}$ 

#### Function calling itself

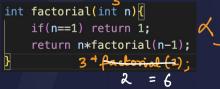
```
factorial (n) = n factorial (n-1);
int factorial (int n) {
                                        n1 = n + (n-1)1
   return no factorial (n-1);
```

# Ques: Make a function which calculates the factorial of n using recursion.

```
int main(){{
    int n;
    printf("Enter a number : ");
    scanf("%d",&n); n = Y
    int fact = factorial(*/);
    printf("%d", fact);
    return 0;
}
```

```
int factorial(int n){
    return n*factorial(n-1);
            3 * factorial (2):
int factorial(int n){
    return n*factorial(n-1);
           2* factorial (1)
int factorial(int n){
    return n*factorial(n-1);
            1+ factorial (0)
int factorial(int n){
    return n*factorial(n-1);
```

```
🦍 skills
int factorial(int n){
    if(n==1) return 1;
    return n*factorial(n-1);
                                        int factorial(int n){
int factorial(int n){
    if(n==1) return 1;
                                             if(n==1) return 1;
    return n*factorial(n-1);
```



int factorial(int n){
 if(n==1) return 1;
 return n\*factorial(n-1);
}

$$fact(5) \Rightarrow 5^{*} fact(4) 24 \longrightarrow 120$$

$$4^{*} fact(3) 6 = 24$$

$$3^{*} fact(2) 2 = 6$$

$$1 = 2$$

$$2^{*} fact(2)$$

$$1$$

#### Ques: Print n to 1

using recursion

int decreasing (int n) {

3

'n' times good morning

Output

7

E

6

4

3

2

1

```
void greeting(int n){
                                     void greeting(int n){
   \sqrt{1}f(n==0) return;
                                        /if(n==0) return;
   printf("Good Morning\n");
                                          printf("Good Morning\n");
   greeting(n-1);
                                          areeting(n-1):
   veturn:
void greeting(int<sup>1</sup>n){
                                     void greeting(int n){
   \sqrt{if(n==0)} return:
                                        \sqrt{if(n==0)} return:
  √printf("Good Morning\n");
                                        √printf("Good Morning\n");
   greeting(n=1);
                                       √greeting(n-1);
   return;
                                         veturn:
void greeting(int<sup>o</sup>n){
                                     void greeting(int n){
   \sqrt{if(n==0)} return:
                                       \sqrt{if(n==0)} return:

√printf("Good Morning\n");
                                       √printf("Good Morning\n");
  √greeting(n-1);
                                       qreeting(n-1);
  return;
                                       eturn;
```

Output

- · Good Morning

fun( ){ 1 base case code 1 recursive call code return

#### Ques: Print 1 to n

```
void increasing(int n){
                        if(n==0) return;
                        printf("%d\n",n);
                        increasing(n+1);
N=5
                        return;
               4
     Using extra
```

#### Ques: Print 1 to n (parameterized)

```
#include<stdio.h>
void increasing(int x, int n){
    if(x>n) return;
    printf("%d\n",x);
    increasing(x+1,n);
    return;
int main(){
    int n;
    printf("Enter a number : ");
                     n =5
    scanf("%d",&n);
    increasing(1,η);
    return 0;
```

### Output

- . 1
- 2
- 8 3
- 4
- 5
- •

#### Ques: Print 1 to n (after recursive call)

```
void increasing(int n){
  ✓if(n==0) return; // base case
  √increasing(n⇒1); // call
  /printf("%d\n",n); // code
 √return;
void increasing(int n){
  ✓if(n==0) return; // base case
  ✓increasing(n<sup>2</sup>₁); // call
  ✓printf("%d\n",n); // code
  return:
```

```
void increasing (int^0n)
   /if(n==0) return; // base case
    -increasing(n-1); // call
void increasing(int n){
   √if(n==0) return; // base case
   \sqrt{\text{increasing}(n^{0}1)}; // call
  printf("%d\n",n); // gode
  ✓ return;
void increasing(int n){
   √if(n==0) return; // base case
  ✓increasing(n 1); // call
  /printf("%d\n",n); // code
  return;
```

```
Output
```

- . 1
- 2
- 3
- L

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 $H_{\underline{omework}}$ : Print Decreasing - Increasing  $n=4 \rightarrow 4$ 

# Hint: Call se pehle, Call ke boad

H-M. N=3 > DRY KNN

🚯 SKILLS

#### n = 4, S = 0

#### Ques: Print sum from 1 to n (Parameterised)

```
void sum(int^{1}n, int^{0}s){ void sum(int^{1}n, int^{1}s){
  ✓if(n==0){
        printf("%d",s);
        return;
  √return:
void sum(int 3, in (s){
  \sqrt{if(n==0)}
        printf("%d",s);
         return;
  ✓return;
```

```
✓if(n==0){
        printf("%d",s);
         return;
 √sum(n-1,s+n); 
√return;
void sum(int<sup>2</sup>n, int s){

✓if(n==0){
        printf("%d",s);
         return;
```

```
Output
\sqrt{if(n==0)}
    /printf("%d",s);
     return;
```

#### Ques: Print sum from 1 to n (Return type)

$$Sum(n) = n + Sum(n-1);$$

$$Sum(5)=1+2+3+4+5 = 5 + Sum(4)$$

$$4 + Sum(3)$$

$$3 + Sum(2)$$

$$2 + Sum(4)$$

factorial (n) = n+ factorial (n-1);

# Ques: Make a function which calculates 'a' raised to the power 'b' using recursion.

```
a^b = a \times a \times a \times a \cdot \cdot \cdot
int power = 1;
        int a, b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             b times
for(int i=1; i < b; i++)
                                                                            power = power * a; if (b==0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                              power (a,b) = a^* power (a,b-1);
                                                            2^{4} = 2^{2} + 2^{3} \rightarrow 2^{3} = 2^{2} + 2^{2} \rightarrow 2^{2} = 2^{2} + 2^{3} \rightarrow 2^{2} = 2^{2} + 2^{2} \rightarrow 2^{2} \rightarrow 2^{2} = 2^{2} + 2^{2} \rightarrow 2^{2} \rightarrow 2^{2} = 2^{2} + 2^{2} \rightarrow 2^{2
```



#### \*Multiple Calls

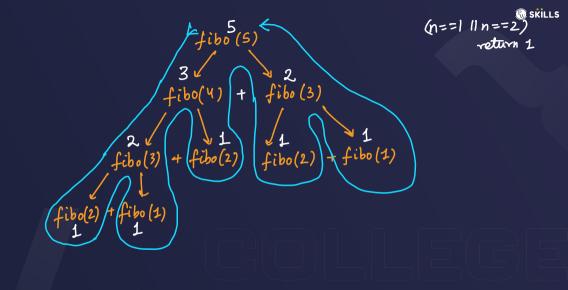
## Ques: Write a function to calculate the nth fibonacci number using recursion.

112358 |3213455 89...

12345678910

fibo(n) = fibo(n-1) + fibo(n-2);

if 
$$n=1$$
 or  $n=2$ ) return 1



#### Ques: Stair Path - 1

single step, double step
no. of ways, so that
the person readles nth
ctair.

 $n \rightarrow n-1, n-2$ 

5 steps

11111 1121

2 2

5

# Ques: Stair Path - 2 H.W. nth stair single step, double step, triple step

no . of ways, so that the person reaches nth ctair.

4

1 3

3 |

+ pow(a, b/2)

#### **Ques**: Power function (logarithmic)

$$a^{b} = a^{+} a^{b-1};$$
 if  $(b = 0)$  return 1; pow(a,b) = pow(a,b/2)

 $2^{64} = 2^{+} 2^{63}$ 
 $2^{63} = 2^{+} 2^{62}$ 
 $2^{64} = 2^{2} \times 2^{32}$ 
 $2^{64} = 2^{32} \times 2^$ 

#### **Ques**: Power function (logarithmic)

$$a^{b} = a^{b/2} * a^{b/2}$$
# Problem:
$$2^{\frac{7}{4}} = 2^{\frac{3}{4}} * 2^{\frac{3}{4}} = 16$$

$$2^{\frac{3}{4}} = 2^{\frac{3}{4}} * 2^{\frac{3}{4}} = 16$$

```
# Solution:
          if bis even
                 \alpha^{b} = \alpha^{b/2} \times \alpha^{b/2}
         if bis odd
                 a^{b} = a^{b/2} * a^{b/2} * a.
b=S
a^{5}=a^{5/2}\times a^{5/2}\times a
```

 $= a^2 \times a^2 \times a$ 

```
int powerlog(int a, int b){
    if(b==0) return 1;
    int x = powerlog(a,b/2);
    if(b%2==0)
        return x*x;
    else
        return x*x*a;
}
```

$$b = 9$$

$$a^{b} \Rightarrow b \text{ calls}$$

$$2^{100} = 100 \text{ calls}$$

a = 2

$$2^{9} = 2^{9} \times 2^{9} \times 2^{9}$$

$$2^{9} = 2^{2} \times 2^{2};$$

$$2^{2} = 2^{1} \times 2^{1};$$

$$2^{1} = 2^{0} \times 2^{0} \times 2;$$

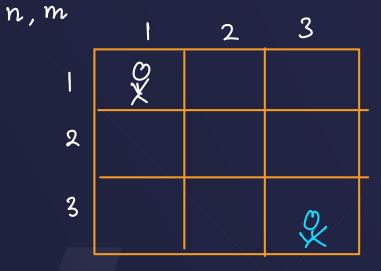
$$2^{1} = 2^{0} \times 2^{0} \times 2;$$

$$2^{1} = 2^{0} \times 2^{0} \times 2;$$

## Ques : Maze path

no. of ways 'Down, Right'

"I step at a time"



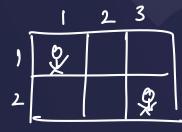
DDRR DRDR

DRRD

RRDD

RDRD

RDDR



DRR

RRD

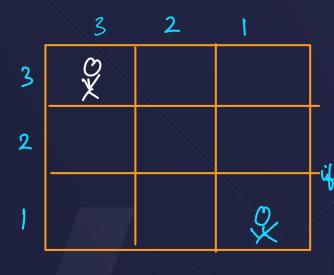
RDR



DR RD

#### Ques: Maze path n=3, m=3

$$n=3$$
,  $m=3$ 



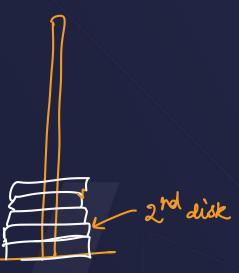
Down 
$$\rightarrow (n-1,m)$$
  
Right  $\rightarrow (n,m-1)$ 

if 
$$(n==1)$$
 2 k  $m==1$ ) return 1  
if  $(n==1)$ 4 // Can't go down  
rightwayl  $+=$ 

```
int maze(int cr, int cc, int er, int ec){
                                                               2
    int rightWays = 0;
    int downWavs = 0:
    if(cr==er && cc==ec) return 1:
                                                 2
    if(cr==er){ // only rightWays call
        rightWays += maze(cr.cc+1,er.ec);
                                            int maze(int cr, int cc, int er, int ec){
    if(cc==ec){ // only downwards call
                                                int rightWays = 0;
        downWays += maze(cr+1.cc.er.ec);
                                                int downWays = 0;
                                                if(cr==er && cc==ec) return 1;
    if(cr<er && cc<ec){
                                                if(cr==er){ // only rightWays call
    rightWays += maze(cr,cc+1,er,ec);
                                                    rightWays += maze(cr,cc+1,er,ec);
        downWavs += maze(cr+1.cc.er.ec);
                                                if(cc==ec){ // only downwards call
    int totalWays = rightWays + downWays;
                                                    downWays += maze(cr+1,cc,er,ec);
    return totalWays;
                                                                       2 2 2 2
                                                if(cr<er && cc<ec){
                                                    rightWays += maze(cr,cc+1,er,ec);
                                                    downWays += maze(cr+1,cc,er,ec);
                                                int totalWays = rightWays + downWays;
                                                return totalWays;
```

#### Call Stack

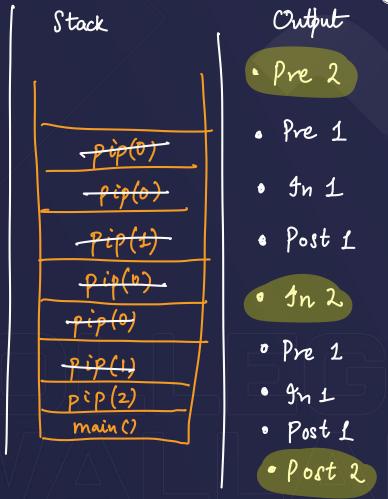
CD Rack





#### **Pre In Post**

```
n=2
void preInPost(int n){
    if(n==0) return;
    printf("Pre %d\n",n);
    preInPost(n-1);
    printf("In %d\n",n);
    preInPost(n-1);
    printf("Post %d\n",n);
    return;
```



#### **Pre In Post**

Tree Diagram

propip(2)

propip(2)

propip(1)

propip(1)

propip(1)

```
void preInPost(int n){
    if(n==0) return;
    printf("Pre %d\n",n);
    preInPost(n-1);
    printf("In %d\n",n);
    preInPost(n-1);
    printf("Post %d\n",n);
    return;
}
```

pip(0)

#### Output

- · Pre 2
- · Pre 1
- In 1
- · Post 1
- 4n 2
- · Pre 1
- In 1
- · Post 1
- · Post 2

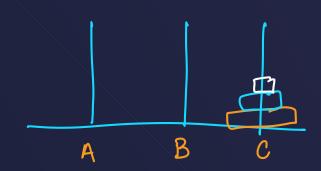


```
Ques: Print zig-zag
```

Input Output

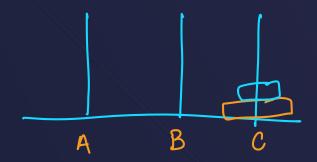
- 1 111
- 2 211121112
- 3 321112111232111211123





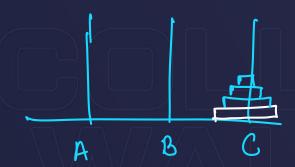
Griput > 
$$n \rightarrow n \cdot of$$
 disker  
disks min moves  
 $3 \rightarrow 2^3 - 1 = 7$   
 $4 \rightarrow 2^4 - 1 = 15$   
 $5 \rightarrow 2^5 - 1 = 31$ 

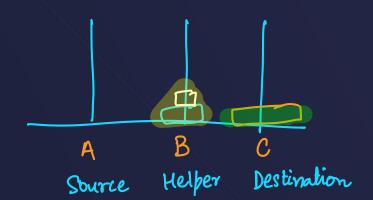
$$A \rightarrow B$$
 $C \rightarrow B$ 



$$A \rightarrow B$$
 $A \rightarrow C$ 
 $B \rightarrow C$ 

$$n = 2$$
  
 $m. moves \rightarrow 2^2 - 1 = 3$ 







**SKILLS** 



