

# Classification Metrics

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## 1. Confusion Matrix

Actual / Predicted	Positive (1)	Negative (0)
Positive (1)	TP (True Positive)	FN (False Negative)
Negative (0)	FP (False Positive)	TN (True Negative)

### Key terms:

- TP = Correctly predicted positive
  - TN = Correctly predicted negative
  - FP = Predicted positive but actually negative
  - FN = Predicted negative but actually positive
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## 2. Accuracy

Measures overall correctness of the model.

### Formula:

$$\text{Accuracy} = (TP + TN) / (TP + TN + FP + FN)$$

✅ Works well when classes are balanced.

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## 3. Precision (Positive Predictive Value)

Out of all predicted positives, how many are truly positive?

### Formula:

$$\text{Precision} = TP / (TP + FP)$$

High precision → few false positives.

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## 4. Recall (Sensitivity / True Positive Rate)

Out of all actual positives, how many did we correctly identify?

**Formula:**

$$\text{Recall} = \text{TP} / (\text{TP} + \text{FN})$$

High recall → few false negatives.

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## 5. F1-Score

Harmonic mean of Precision and Recall.

**Formula:**

$$\text{F1} = 2 \times (\text{Precision} \times \text{Recall}) / (\text{Precision} + \text{Recall})$$

Balances precision and recall.

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## 6. Specificity (True Negative Rate)

Out of all actual negatives, how many did we correctly predict?

**Formula:**

$$\text{Specificity} = \text{TN} / (\text{TN} + \text{FP})$$

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## 7. False Positive Rate (FPR)

Proportion of negatives incorrectly predicted as positive.

**Formula:**

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN})$$

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## 8. False Negative Rate (FNR)

Proportion of positives incorrectly predicted as negative.

**Formula:**

$$\text{FNR} = \text{FN} / (\text{FN} + \text{TP})$$

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## 9. ROC Curve (Receiver Operating Characteristic)

- Plots TPR (Recall) vs FPR at various thresholds.
  - Shows trade-off between sensitivity and specificity.
  - Ideal model curve → close to top-left corner.
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## 10. AUC (Area Under the ROC Curve)

Measures model's ability to distinguish classes.

**Range:** 0 to 1

Closer to 1 → better classifier.

0.5 → random guessing.

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## 11. Precision–Recall (PR) Curve

Plots Precision vs Recall at different probability thresholds.

Useful for **imbalanced data**.

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## 12. Log Loss (Cross-Entropy Loss)

Used in probabilistic classifiers (e.g., Logistic Regression).

**Formula:**

$$\text{Log Loss} = - (1/N) \times \sum [y_i \times \log(p_i) + (1 - y_i) \times \log(1 - p_i)]$$

Lower log loss = better model.

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## 13. Matthews Correlation Coefficient (MCC)

Balanced metric for binary or imbalanced data.

**Formula:**

$$\text{MCC} = (\text{TP} \times \text{TN} - \text{FP} \times \text{FN}) / \sqrt{((\text{TP} + \text{FP})(\text{TP} + \text{FN})(\text{TN} + \text{FP})(\text{TN} + \text{FN}))}$$

Range:

- +1 → perfect
  - 0 → random
  - -1 → completely wrong
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## 14. Cohen's Kappa

Measures agreement between predicted and actual labels, adjusted for chance.

**Formula:**

$$\text{Kappa} = (p_o - p_e) / (1 - p_e)$$

where

$p_o$  = observed accuracy

$p_e$  = expected accuracy (by chance)

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## 15. Balanced Accuracy

Average of Sensitivity and Specificity.

**Formula:**

$$\text{Balanced Accuracy} = (\text{Sensitivity} + \text{Specificity}) / 2$$

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## 16. Hamming Loss

Fraction of incorrectly predicted labels (for multi-label classification).

**Formula:**

$$\text{Hamming Loss} = (1/N) \times \sum \text{xor}(y_i, \hat{y}_i)$$

Lower value → better performance.

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## 17. Jaccard Index (Intersection over Union)

Measures similarity between predicted and true sets.

**Formula:**

$$\text{Jaccard} = \text{TP} / (\text{TP} + \text{FP} + \text{FN})$$

Used in **multi-label** and **image segmentation** tasks.

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## 18. Macro, Micro, and Weighted Averages (for Multi-class)

Type	Description	Formula
Micro Average	Aggregates all classes before computing metric.	Compute global TP, FP, FN → then Precision/Recall/F1.
Macro Average	Simple mean of metrics for each class.	$(\text{Metric}_1 + \text{Metric}_2 + \dots + \text{Metric}_n) / n$
Weighted Average	Weighted by number of samples per class.	$\sum (w_i \times \text{Metric}_i)$

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## 19. F $\beta$ -Score

Generalized F1-score;  $\beta$  controls importance of recall vs precision.

**Formula:**

$$F\beta = (1 + \beta^2) \times (\text{Precision} \times \text{Recall}) / ((\beta^2 \times \text{Precision}) + \text{Recall})$$

- $\beta > 1 \rightarrow$  focus on recall
  - $\beta < 1 \rightarrow$  focus on precision
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## 20. Top-K Accuracy

Used in multi-class problems (e.g., deep learning).

**Formula:**

$$\text{Top-K Accuracy} = (\text{Number of samples where true label} \in \text{Top K predictions}) / (\text{Total samples})$$

