

Step	<b>Algorithm:</b> $[C] := \text{SYRK\_AC\_BLK\_VAR3}(A, C)$
1a	$\{C = \widehat{C}$
4	$A \rightarrow \left( A_L \middle  A_R \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right)$ <p>where <math>A_R</math> has 0 columns, <math>C_{BR}</math> is <math>0 \times 0</math></p>
2	$\left\{ \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} \widehat{C}_{TL} & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & A_R^T A_R + \widehat{C}_{BR} \end{array} \right) \right\}$
3	<b>while</b> $n(A_R) < n(A)$ <b>do</b>
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} \widehat{C}_{TL} & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & A_R^T A_R + \widehat{C}_{BR} \end{array} \right) \wedge n(A_R) < n(A) \right\}$
5a	<p><b>Determine block size <math>b</math></b></p> $\left( A_L \middle  A_R \right) \rightarrow \left( A_0 \middle  A_1 \middle  A_2 \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$ <p>where <math>A_1</math> has <math>b</math> columns, <math>C_{11}</math> is <math>b \times b</math></p>
6	$\left\{ \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & A_2^T A_2 + \widehat{C}_{22} \end{array} \right) \right\}$
8	$C_{12} = A_1^T A_2 + C_{12}$ $C_{11} = A_1^T A_1 + C_{11}$
7	$\left\{ \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & A_1^T A_1 + \widehat{C}_{11} & A_1^T A_2 + \widehat{C}_{12} \\ \hline C_{20} & C_{21} & A_2^T A_2 + \widehat{C}_{22} \end{array} \right) \right\}$
5b	$\left( A_L \middle  A_R \right) \leftarrow \left( A_0 \middle  A_1 \middle  A_2 \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$
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1b	$\{[C] = \text{syrk\_ac}(A, \widehat{C})$

Step	Algorithm: $[C] := \text{SYRK\_AC\_BLK\_VAR3}(A, C)$
1a	{
4	
	where
2	{
3	while do
2,3	{
	$\wedge$
5a	Determine block size $b$
	where
6	{
8	
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	endwhile
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6	$\left\{ \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & A_2^T A_2 + \widehat{C}_{22} \end{array} \right) \right\}$
8	$C_{12} = A_1^T A_2 + C_{12}$ $C_{11} = A_1^T A_1 + C_{11}$
7	$\left\{ \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right) = \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & A_1^T A_1 + \widehat{C}_{11} & A_1^T A_2 + \widehat{C}_{12} \\ \hline C_{20} & C_{21} & A_2^T A_2 + \widehat{C}_{22} \end{array} \right) \right\}$
5b	$\left( A_L \mid A_R \right) \leftarrow \left( A_0 \mid A_1 \mid A_2 \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} \widehat{C}_{TL} & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & A_R^T A_R + \widehat{C}_{BR} \end{array} \right) \right\}$
	<b>endwhile</b>
2,3	$\left\{ \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left( \begin{array}{c c} \widehat{C}_{TL} & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & A_R^T A_R + \widehat{C}_{BR} \end{array} \right) \wedge \neg(n(A_R) < n(A)) \right\}$
1b	$\{[C] = \text{syrk\_ac}(A, \widehat{C})$

	Algorithm: $[C] := \text{SYRK\_AC\_BLK\_VAR3}(A, C)$
	$A \rightarrow \left( A_L \middle  A_R \right), C \rightarrow \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right)$ <p>where <math>A_R</math> has 0 columns, <math>C_{BR}</math> is <math>0 \times 0</math></p>
	while $n(A_R) < n(A)$ do
	<p><b>Determine block size <math>b</math></b></p> $\left( A_L \middle  A_R \right) \rightarrow \left( A_0 \middle  A_1 \middle  A_2 \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$ <p>where <math>A_1</math> has <math>b</math> columns, <math>C_{11}</math> is <math>b \times b</math></p>
	$C_{12} = A_1^T A_2 + C_{12}$ $C_{11} = A_1^T A_1 + C_{11}$
	$\left( A_L \middle  A_R \right) \leftarrow \left( A_0 \middle  A_1 \middle  A_2 \right), \left( \begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$
	endwhile

**Algorithm:**  $[C] := \text{SYRK\_AC\_BLK\_VAR3}(A, C)$

$$A \rightarrow \left( A_L \left| A_R \right. \right), C \rightarrow \left( \begin{array}{c|c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right)$$

**where**  $A_R$  has 0 columns,  $C_{BR}$  is  $0 \times 0$

**while**  $n(A_R) < n(A)$  **do**

**Determine block size**  $b$

$$\left( A_L \left| A_R \right. \right) \rightarrow \left( A_0 \left| A_1 \left| A_2 \right. \right. \right), \left( \begin{array}{c|c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|c|c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$$

**where**  $A_1$  has  $b$  columns,  $C_{11}$  is  $b \times b$

$$C_{12} = A_1^T A_2 + C_{12}$$

$$C_{11} = A_1^T A_1 + C_{11}$$

$$\left( A_L \left| A_R \right. \right) \leftarrow \left( A_0 \left| A_1 \left| A_2 \right. \right. \right), \left( \begin{array}{c|c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|c|c} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ \hline C_{20} & C_{21} & C_{22} \end{array} \right)$$

**endwhile**