

# Divide & Conquer

Merge Sort ( $n \log n$ )  $\rightarrow$  T.C  $O(n) \rightarrow$  S.C

```
public static void printArr (int arr[]) {  
    for (int i = 0; i < arr.length; i++) {  
        System.out.print (arr[i] + " ");  
    }  
    System.out.println();  
}
```

```
public static void mergeSort (int arr[], int si, int ei) {  
    if (si >= ei) {  
        return;  
    }  
    int mid = si + (ei - si) / 2; // (si + ei) / 2  
    mergeSort (arr, si, mid); // left part  
    mergeSort (arr, mid + 1, ei); // right part  
    merge (arr, si, mid, ei);  
}
```

```
public static void merge (int arr[], int si, int mid, int ei) {  
    int temp[] = new int [ei - si + 1];  
    int i = si; // iterator for left part  
    int j = mid + 1; // iterator for right part  
    int k = 0; // iterator for temp arr
```

```
while (i <= mid && j <= ei){
```

```
    if (arr[i] < arr[j]){
```

```
        temp[k] = arr[i];
```

```
        i++;
```

```
    } else {
```

```
        temp[k] = arr[j];
```

```
        j++;
```

```
    }
```

```
    k++;
```

```
}
```

```
// left part
```

```
while (i <= mid){
```

```
    temp[k++] = arr[i++];
```

```
}
```

```
// right part
```

```
while (j <= ei){
```

```
    temp[k++] = arr[j++];
```

```
}
```

```
// copy temp to original arr
```

```
for (k = 0, i = si; k < temp.length; k++, i++){
```

```
    arr[i] = temp[k];
```

```
}
```

```
}
```

---

```
main
```

```
int arr[] = {6, 3, 9, 5, 2, 8};
```

```
mergeSort(arr, 0, arr.length - 1);
```

```
printArr(arr);
```

Quick Sort :  $O(n \log n) \rightarrow$  average } T.C  
pivot & partition  $O(n^2) \rightarrow$  worst }  
space  $\rightarrow O(1)$

```
public static void printArr (int arr[]) {  
    for (int i=0; i<arr.length; i++) {  
        Syso (arr[i] + " ");  
    }  
    Sysoln();  
}
```

```
public static void quickSort (int arr[], int si, int ei) {  
    if (si >= ei) {  
        return;  
    }  
    //last element  
    int pIdx = partition (arr, si, ei);  
    quickSort (arr, si, pIdx-1); // left  
    quickSort (arr, pIdx+1, ei); // right  
}
```

```
public static int partition (int arr[], int si, int ei) {  
    int pivot = arr[ei];  
    int i = si-1; // to make place for ele smaller than pivot  
    for (int j=si; j<ei; j++) {  
        if (arr[j] <= pivot) {  
            i++;  
        }  
    }  
}
```



// swap

```
int temp = arr[j];
```

```
arr[j] = arr[i];
```

```
arr[i] = temp;
```

```
}
```

```
}
```

```
i++;
```

```
int temp = pivot;
```

```
arr[ei] = arr[i];
```

```
arr[i] = temp;
```

```
return i;
```

```
}
```

— main —

```
int arr[] = {6, 3, 9, 8, 2, 5};
```

```
quickSort(arr, 0, arr.length - 1);
```

```
printArr(arr);
```

```
}
```

Worst case occurs when pivot is always the smallest or the largest element

## Search in rotated sorted array

input: sorted, rotated array with distinct numbers  
(in ascending order) it is rotated at a pivot point.  
Find the index of given element.

4	5	6	7	0	1	2
---	---	---	---	---	---	---

target: 0

output: 4

```
public static int search (int arr[], int tar, int si, int ei) {  
    if (si > ei) {  
        return -1;  
    }  
    int mid = si + (ei - si) / 2; // (si + ei) / 2  
    // case FOUND  
    if (arr[mid] == tar) {  
        return mid;  
    }  
    // mid on L1  
    if (arr[si] <= arr[mid]) {  
        // case a: left  
        if (arr[si] <= tar && tar <= arr[mid]) {  
            return search(arr, tar, si, mid - 1);  
        } else {  
            // case b: right  
            return search(arr, tar, mid + 1, ei);  
        }  
    }  
}
```

```
// mid on L2
```

```
else {
```

```
    // case c : right
```

```
    if (arr[mid] <= tar && tar <= arr[ei]) {
```

```
        return search(arr, tar, mid+1, ei);
```

```
    } else {
```

```
        // case d : left
```

```
        return search(arr, tar, si, mid-1);
```

```
    }
```

```
}
```

```
main
```

```
int arr[] = {4, 5, 6, 7, 0, 1, 2};
```

```
int target = 0; // output = 4
```

```
int tarIdx = search(arr, target, 0, arr.length-1);
```

```
System.out.println(tarIdx);
```

```
}
```