

Multiple Linear Regression

```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error, r2_score, accuracy_score
```

Boston House Price Dataset

```
In [2]: df = pd.read_csv("E:\MCA\sem_3\ML_Lab\programs\week4\boston_house_prices.csv")
df.head()
```

Out[2]:

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT	MEDV
0	0.00632	18.0	2.31	0	0.538	6.575	65.2	4.0900	1	296	15.3	396.90	4.98	24.0
1	0.02731	0.0	7.07	0	0.469	6.421	78.9	4.9671	2	242	17.8	396.90	9.14	21.6
2	0.02729	0.0	7.07	0	0.469	7.185	61.1	4.9671	2	242	17.8	392.83	4.03	34.7
3	0.03237	0.0	2.18	0	0.458	6.998	45.8	6.0622	3	222	18.7	394.63	2.94	33.4
4	0.06905	0.0	2.18	0	0.458	7.147	54.2	6.0622	3	222	18.7	396.90	5.33	36.2

```
In [3]: df.isnull().sum()
```

```
Out[3]: CRIM      0
ZN          0
INDUS       0
CHAS        0
NOX         0
RM          0
AGE         0
DIS         0
RAD         0
TAX         0
PTRATIO     0
B           0
LSTAT       0
MEDV        0
dtype: int64
```

```
In [4]: df.shape
```

```
Out[4]: (506, 14)
```

```
In [5]: x = df.drop(['MEDV'],axis = 1).values  
x
```

```
Out[5]: array([[6.3200e-03, 1.8000e+01, 2.3100e+00, ..., 1.5300e+01, 3.9690e+02,  
              4.9800e+00],  
              [2.7310e-02, 0.0000e+00, 7.0700e+00, ..., 1.7800e+01, 3.9690e+02,  
              9.1400e+00],  
              [2.7290e-02, 0.0000e+00, 7.0700e+00, ..., 1.7800e+01, 3.9283e+02,  
              4.0300e+00],  
              ...,  
              [6.0760e-02, 0.0000e+00, 1.1930e+01, ..., 2.1000e+01, 3.9690e+02,  
              5.6400e+00],  
              [1.0959e-01, 0.0000e+00, 1.1930e+01, ..., 2.1000e+01, 3.9345e+02,  
              6.4800e+00],  
              [4.7410e-02, 0.0000e+00, 1.1930e+01, ..., 2.1000e+01, 3.9690e+02,  
              7.8800e+00]])
```

```
In [6]: y = df['MEDV'].values
y
```

```
Out[6]: array([24. , 21.6, 34.7, 33.4, 36.2, 28.7, 22.9, 27.1, 16.5, 18.9, 15. ,
18.9, 21.7, 20.4, 18.2, 19.9, 23.1, 17.5, 20.2, 18.2, 13.6, 19.6,
15.2, 14.5, 15.6, 13.9, 16.6, 14.8, 18.4, 21. , 12.7, 14.5, 13.2,
13.1, 13.5, 18.9, 20. , 21. , 24.7, 30.8, 34.9, 26.6, 25.3, 24.7,
21.2, 19.3, 20. , 16.6, 14.4, 19.4, 19.7, 20.5, 25. , 23.4, 18.9,
35.4, 24.7, 31.6, 23.3, 19.6, 18.7, 16. , 22.2, 25. , 33. , 23.5,
19.4, 22. , 17.4, 20.9, 24.2, 21.7, 22.8, 23.4, 24.1, 21.4, 20. ,
20.8, 21.2, 20.3, 28. , 23.9, 24.8, 22.9, 23.9, 26.6, 22.5, 22.2,
23.6, 28.7, 22.6, 22. , 22.9, 25. , 20.6, 28.4, 21.4, 38.7, 43.8,
33.2, 27.5, 26.5, 18.6, 19.3, 20.1, 19.5, 19.5, 20.4, 19.8, 19.4,
21.7, 22.8, 18.8, 18.7, 18.5, 18.3, 21.2, 19.2, 20.4, 19.3, 22. ,
20.3, 20.5, 17.3, 18.8, 21.4, 15.7, 16.2, 18. , 14.3, 19.2, 19.6,
23. , 18.4, 15.6, 18.1, 17.4, 17.1, 13.3, 17.8, 14. , 14.4, 13.4,
15.6, 11.8, 13.8, 15.6, 14.6, 17.8, 15.4, 21.5, 19.6, 15.3, 19.4,
17. , 15.6, 13.1, 41.3, 24.3, 23.3, 27. , 50. , 50. , 50. , 22.7,
25. , 50. , 23.8, 23.8, 22.3, 17.4, 19.1, 23.1, 23.6, 22.6, 29.4,
23.2, 24.6, 29.9, 37.2, 39.8, 36.2, 37.9, 32.5, 26.4, 29.6, 50. ,
32. , 29.8, 34.9, 37. , 30.5, 36.4, 31.1, 29.1, 50. , 33.3, 30.3,
34.6, 34.9, 32.9, 24.1, 42.3, 48.5, 50. , 22.6, 24.4, 22.5, 24.4,
20. , 21.7, 19.3, 22.4, 28.1, 23.7, 25. , 23.3, 28.7, 21.5, 23. ,
26.7, 21.7, 27.5, 30.1, 44.8, 50. , 37.6, 31.6, 46.7, 31.5, 24.3,
31.7, 41.7, 48.3, 29. , 24. , 25.1, 31.5, 23.7, 23.3, 22. , 20.1,
22.2, 23.7, 17.6, 18.5, 24.3, 20.5, 24.5, 26.2, 24.4, 24.8, 29.6,
42.8, 21.9, 20.9, 44. , 50. , 36. , 30.1, 33.8, 43.1, 48.8, 31. ,
36.5, 22.8, 30.7, 50. , 43.5, 20.7, 21.1, 25.2, 24.4, 35.2, 32.4,
32. , 33.2, 33.1, 29.1, 35.1, 45.4, 35.4, 46. , 50. , 32.2, 22. ,
20.1, 23.2, 22.3, 24.8, 28.5, 37.3, 27.9, 23.9, 21.7, 28.6, 27.1,
20.3, 22.5, 29. , 24.8, 22. , 26.4, 33.1, 36.1, 28.4, 33.4, 28.2,
22.8, 20.3, 16.1, 22.1, 19.4, 21.6, 23.8, 16.2, 17.8, 19.8, 23.1,
21. , 23.8, 23.1, 20.4, 18.5, 25. , 24.6, 23. , 22.2, 19.3, 22.6,
19.8, 17.1, 19.4, 22.2, 20.7, 21.1, 19.5, 18.5, 20.6, 19. , 18.7,
32.7, 16.5, 23.9, 31.2, 17.5, 17.2, 23.1, 24.5, 26.6, 22.9, 24.1,
18.6, 30.1, 18.2, 20.6, 17.8, 21.7, 22.7, 22.6, 25. , 19.9, 20.8,
16.8, 21.9, 27.5, 21.9, 23.1, 50. , 50. , 50. , 50. , 50. , 13.8,
13.8, 15. , 13.9, 13.3, 13.1, 10.2, 10.4, 10.9, 11.3, 12.3, 8.8,
7.2, 10.5, 7.4, 10.2, 11.5, 15.1, 23.2, 9.7, 13.8, 12.7, 13.1,
12.5, 8.5, 5. , 6.3, 5.6, 7.2, 12.1, 8.3, 8.5, 5. , 11.9,
27.9, 17.2, 27.5, 15. , 17.2, 17.9, 16.3, 7. , 7.2, 7.5, 10.4,
8.8, 8.4, 16.7, 14.2, 20.8, 13.4, 11.7, 8.3, 10.2, 10.9, 11. ,
9.5, 14.5, 14.1, 16.1, 14.3, 11.7, 13.4, 9.6, 8.7, 8.4, 12.8,
10.5, 17.1, 18.4, 15.4, 10.8, 11.8, 14.9, 12.6, 14.1, 13. , 13.4,
15.2, 16.1, 17.8, 14.9, 14.1, 12.7, 13.5, 14.9, 20. , 16.4, 17.7,
19.5, 20.2, 21.4, 19.9, 19. , 19.1, 19.1, 20.1, 19.9, 19.6, 23.2,
29.8, 13.8, 13.3, 16.7, 12. , 14.6, 21.4, 23. , 23.7, 25. , 21.8,
20.6, 21.2, 19.1, 20.6, 15.2, 7. , 8.1, 13.6, 20.1, 21.8, 24.5,
23.1, 19.7, 18.3, 21.2, 17.5, 16.8, 22.4, 20.6, 23.9, 22. , 11.9])
```

Iteration 1

i. test_size=0.3 random_state=0

```
In [7]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.3,random_state = 0)
```

```
In [8]: model= LinearRegression()
```

```
In [9]: model.fit(x_train,y_train)
```

```
Out[9]: ▾ LinearRegression
LinearRegression()
```

```
In [10]: y_predict = model.predict(x_test)
```

```
In [11]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)
```

```
print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 27.20
R-squared: 0.67

```
In [12]: model.score(x,y)
```

```
Out[12]: 0.7378284679886178
```

```
In [13]: y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})
pred_y_df
```

```
Out[13]:
```

	Actual Values	predicted values	Difference
0	22.6	24.935708	-2.335708
1	50.0	23.751632	26.248368
2	23.0	29.326383	-6.326383
3	8.3	11.975346	-3.675346
4	21.2	21.372725	-0.172725
...
147	36.2	27.811077	8.388923
148	11.0	14.506816	-3.506816
149	7.2	7.573699	-0.373699
150	22.8	28.334807	-5.534807
151	28.7	25.043412	3.656588

152 rows × 3 columns

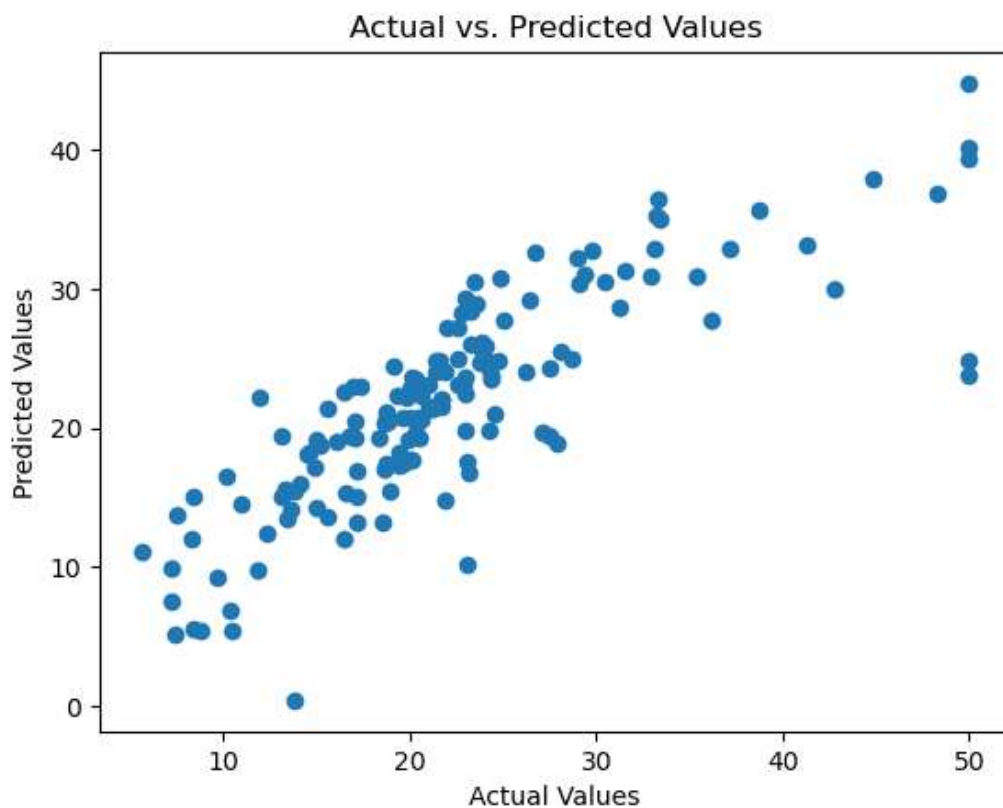
```
In [14]: model.coef_
```

```
Out[14]: array([-1.21310401e-01,  4.44664254e-02,  1.13416945e-02,  2.51124642e+00,
                -1.62312529e+01,  3.85906801e+00, -9.98516565e-03, -1.50026956e+00,
                 2.42143466e-01, -1.10716124e-02, -1.01775264e+00,  6.81446545e-03,
                -4.86738066e-01])
```

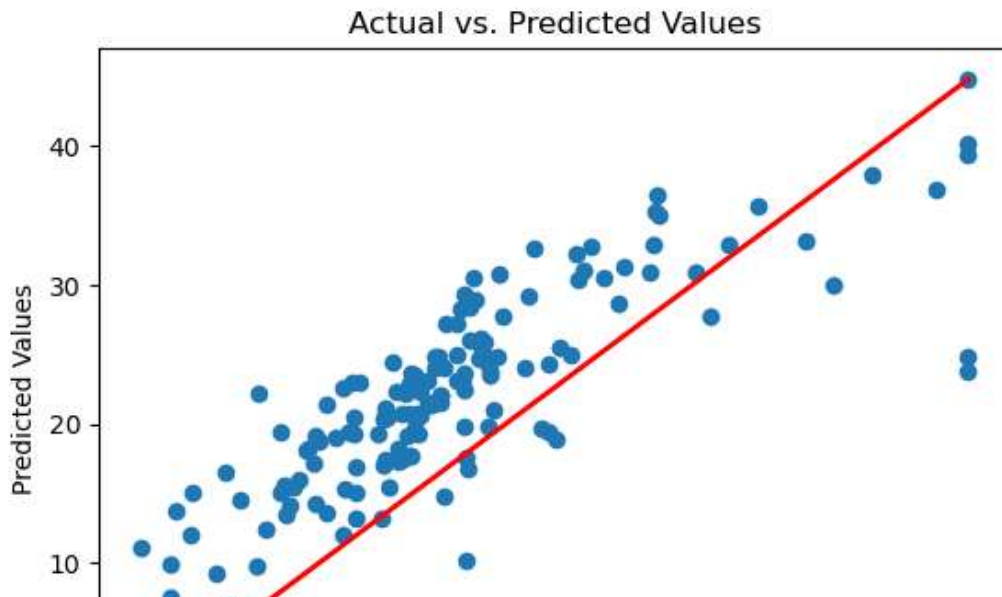
```
In [15]: model.intercept_
```

```
Out[15]: 37.93710774183272
```

```
In [16]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



```
In [17]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



ii. test_size=0.3 random_state=42

```
In [18]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.3,random_state = 42)
```

```
In [19]: model= LinearRegression()
```

```
In [20]: model.fit(x_train,y_train)
```

```
Out[20]: LinearRegression
LinearRegression()
```

```
In [21]: y_predict = model.predict(x_test)
```

```
In [22]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)

print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 21.52
R-squared: 0.71

```
In [23]: model.score(x,y)
```

```
Out[23]: 0.7365934508044951
```

```
In [24]: y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})
pred_y_df
```

Out[24]:

	Actual Values	predicted values	Difference
0	23.6	28.648960	-5.048960
1	32.4	36.495014	-4.095014
2	13.6	15.411193	-1.811193
3	22.8	25.403213	-2.603213
4	16.1	18.855280	-2.755280
...
147	17.1	17.403672	-0.303672
148	14.5	13.385941	1.114059
149	50.0	39.983425	10.016575
150	14.3	16.682863	-2.382863
151	12.6	18.285618	-5.685618

152 rows × 3 columns

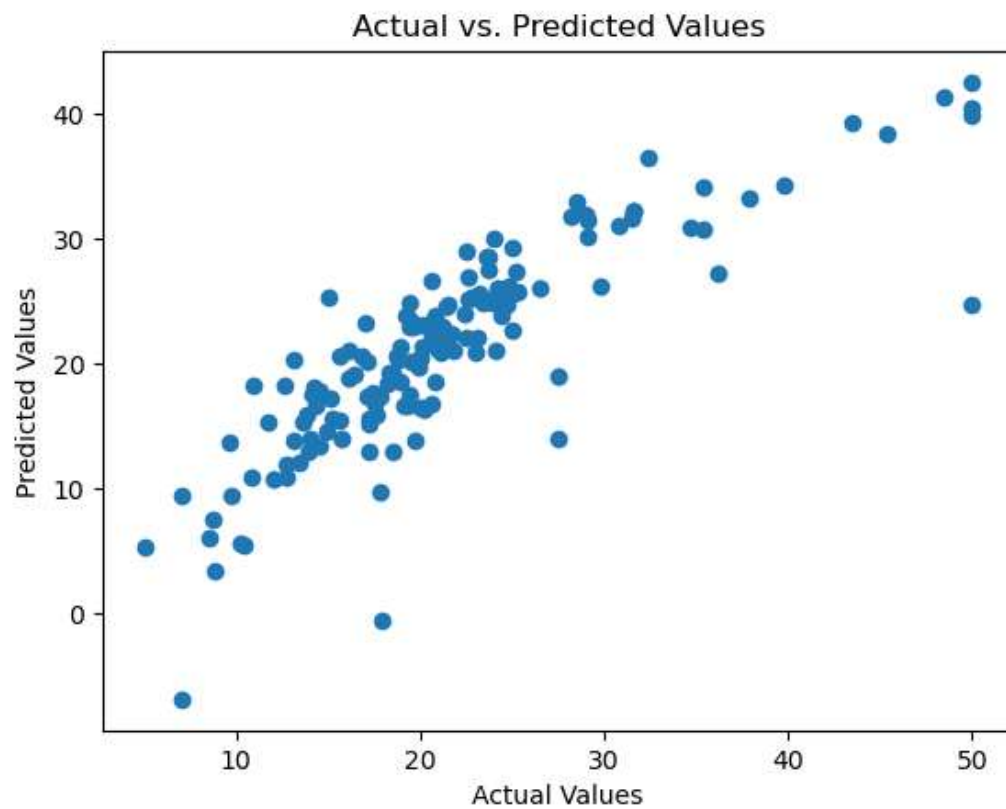
```
In [25]: model.coef_
```

```
Out[25]: array([-1.33470103e-01,  3.58089136e-02,  4.95226452e-02,  3.11983512e+00,
                -1.54170609e+01,  4.05719923e+00, -1.08208352e-02, -1.38599824e+00,
                 2.42727340e-01, -8.70223437e-03, -9.10685208e-01,  1.17941159e-02,
                -5.47113313e-01])
```

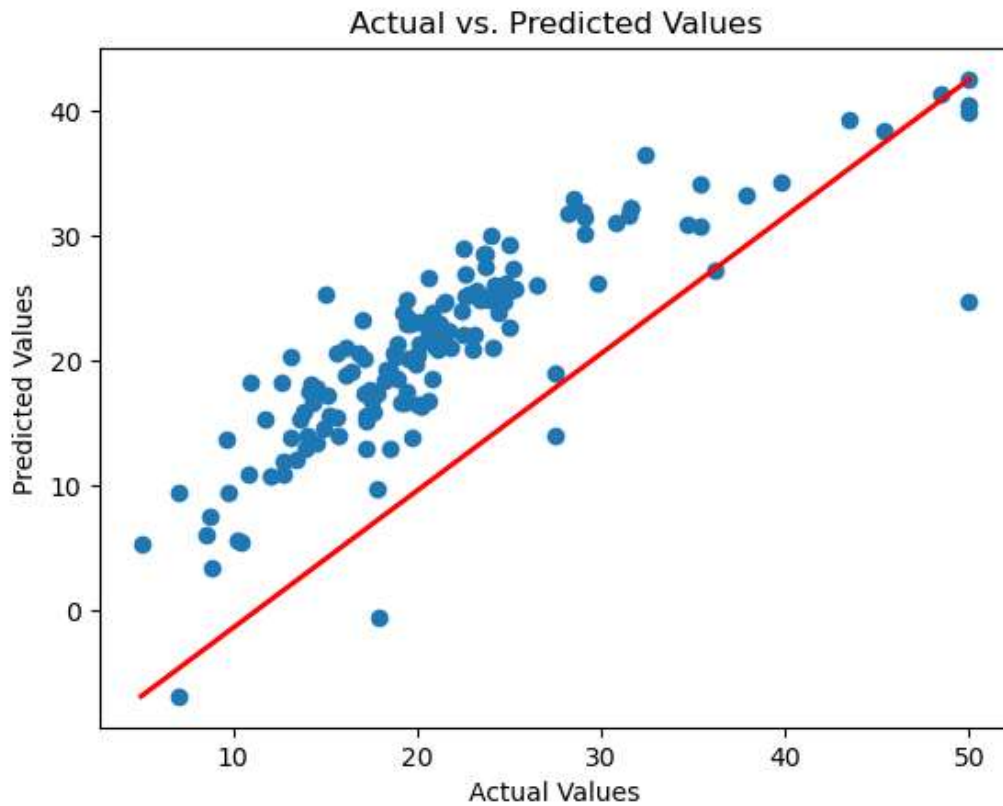
```
In [26]: model.intercept_
```

```
Out[26]: 31.63108403569373
```

```
In [27]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```




```
In [28]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



Iteration 2

i. test_size=0.4 random_state=0

```
In [29]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.4,random_state = 0)
```

```
In [30]: model= LinearRegression()
```

```
In [31]: model.fit(x_train,y_train)
```

```
Out[31]: LinearRegression
LinearRegression()
```

```
In [32]: y_predict = model.predict(x_test)
```

```
In [33]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)

print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 25.79
R-squared: 0.69

```
In [34]: model.score(x,y)
```

Out[34]: 0.7361196190442469

```
In [35]: y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})
```

Out[35]:

	Actual Values	predicted values	Difference
0	22.6	24.581552	-1.981552
1	50.0	24.516293	25.483707
2	23.0	29.713799	-6.713799
3	8.3	12.511327	-4.211327
4	21.2	21.349654	-0.149654
...
198	22.1	27.219549	-5.119549
199	46.0	40.065076	5.934924
200	22.9	29.489264	-6.589264
201	20.2	16.588711	3.611289
202	43.1	37.210154	5.889846

203 rows × 3 columns

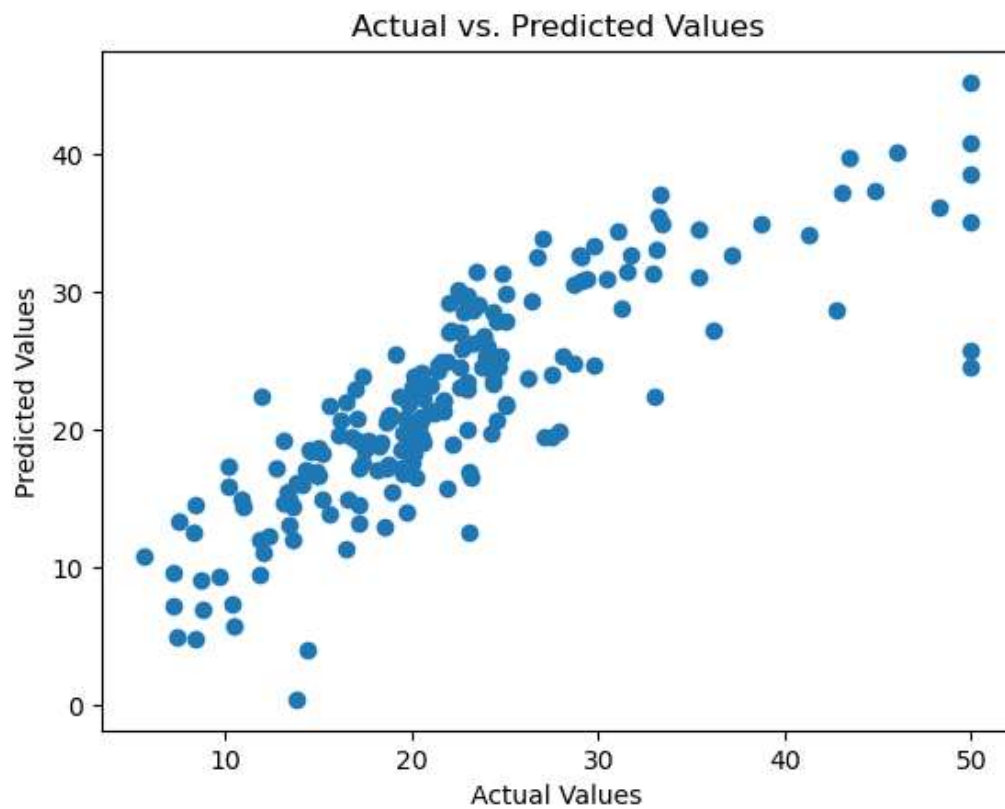
```
In [36]: model.coef_
```

Out[36]: array([-1.03747356e-01, 5.58589924e-02, 5.88240770e-02, 2.50523544e+00,
-1.90284888e+01, 3.25353601e+00, -3.22150522e-03, -1.57603462e+00,
 2.58716068e-01, -1.14681299e-02, -1.10777478e+00, 5.50051783e-03,
-5.59569992e-01])

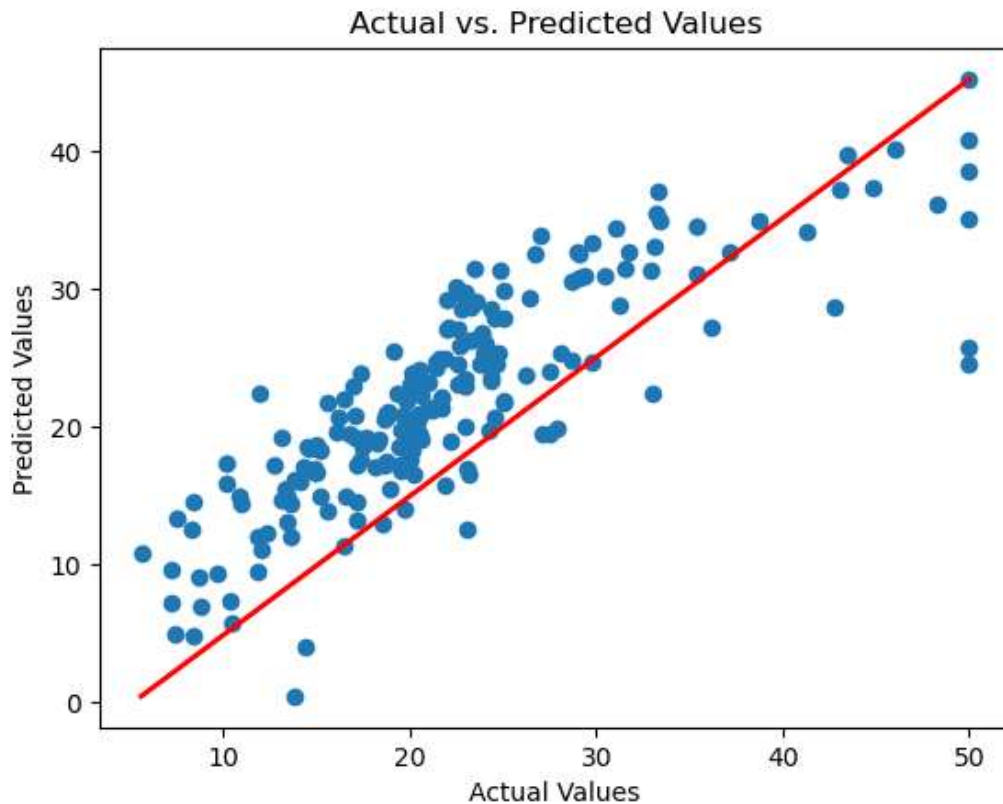
```
In [37]: model.intercept_
```

Out[37]: 45.481419593251005

```
In [38]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



```
In [39]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



ii.test_size=0.4 random_state=42

```
In [40]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.4,random_state = 42)
```

```
In [41]: model= LinearRegression()
```

```
In [42]: model.fit(x_train,y_train)
```

```
Out[42]: LinearRegression
LinearRegression()
```

```
In [43]: y_predict = model.predict(x_test)
```

```
In [44]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)

print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 21.83
R-squared: 0.71

```
In [45]: model.score(x,y)
```

```
Out[45]: 0.7362442925015322
```

```
In [46]: y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})
pred_y_df
```

```
Out[46]:
```

	Actual Values	predicted values	Difference
0	23.6	28.700257	-5.100257
1	32.4	37.275424	-4.875424
2	13.6	14.450663	-0.850663
3	22.8	25.734356	-2.934356
4	16.1	18.497639	-2.397639
...
198	16.7	19.366259	-2.666259
199	13.8	11.536608	2.263392
200	22.9	28.982763	-6.082763
201	15.3	21.744787	-6.444787
202	27.5	32.575230	-5.075230

203 rows × 3 columns

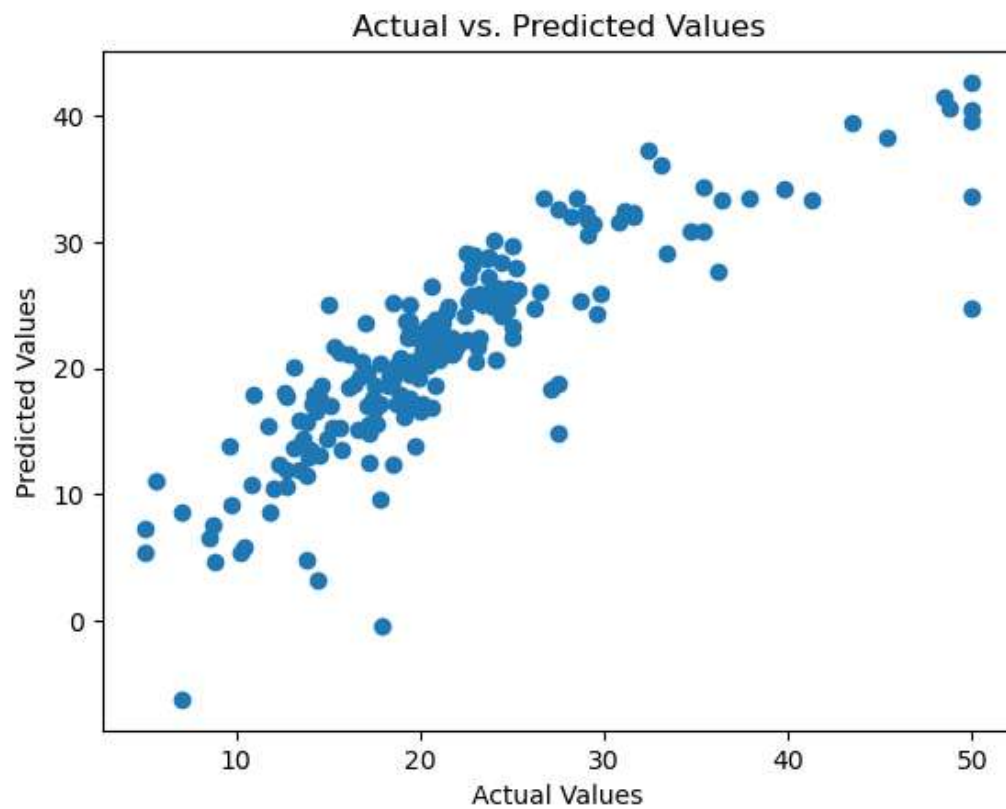
```
In [47]: model.coef_
```

```
Out[47]: array([-1.13498178e-01,  3.79976868e-02,  2.99876109e-02,  3.51131977e+00,
                -1.44513558e+01,  3.80534175e+00, -1.79553906e-02, -1.48968845e+00,
                 2.53016064e-01, -1.00262729e-02, -8.86408743e-01,  1.08462004e-02,
                -5.75917903e-01])
```

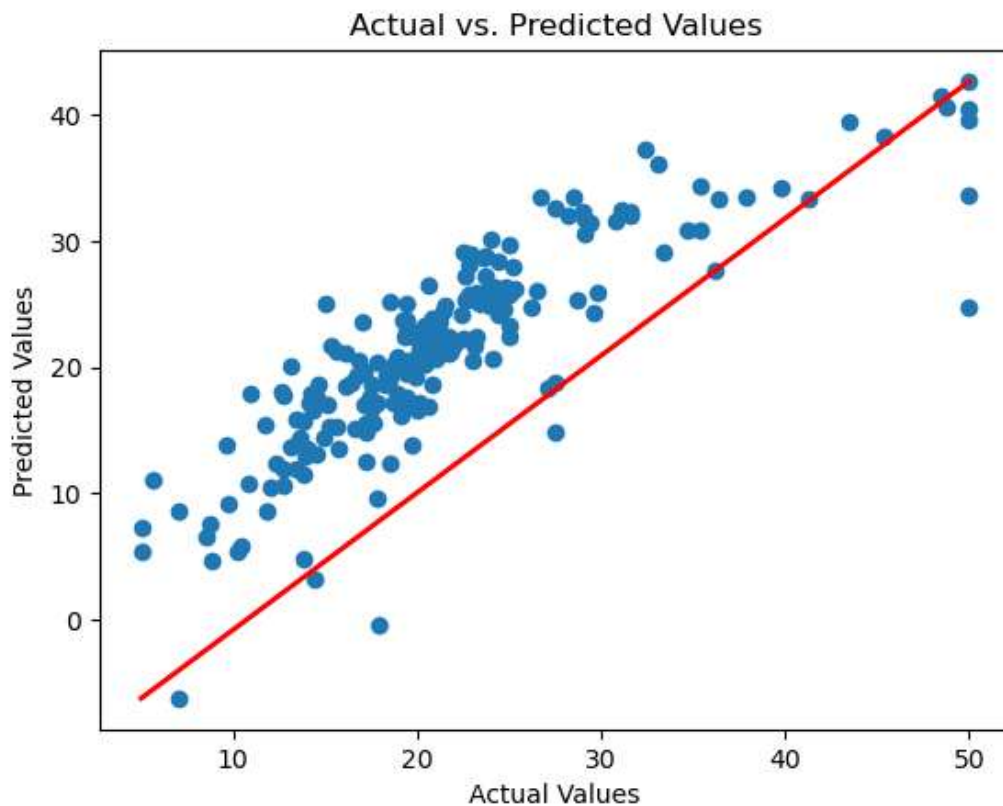
```
In [48]: model.intercept_
```

```
Out[48]: 34.33026076546706
```

```
In [49]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



```
In [50]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



Iteration 3

test_size=0.5 random_state=0

```
In [51]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.5,random_state = 0)
```

```
In [52]: model= LinearRegression()
```

```
In [53]: model.fit(x_train,y_train)
```

```
Out[53]: 

LinearRegression



LinearRegression()


```

```
In [54]: y_predict = model.predict(x_test)
```

```
In [55]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)

print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 25.30
R-squared: 0.67

```
In [56]: model.score(x,y)
```

Out[56]: 0.733888612575677

```
In [57]: y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})
```

Out[57]:

	Actual Values	predicted values	Difference
0	22.6	24.709603	-2.109603
1	50.0	25.126314	24.873686
2	23.0	30.765033	-7.765033
3	8.3	12.414055	-4.114055
4	21.2	21.295995	-0.095995
...
248	32.2	32.604891	-0.404891
249	13.5	12.787651	0.712349
250	17.9	1.206608	16.693392
251	13.3	19.442771	-6.142771
252	11.7	15.319865	-3.619865

253 rows × 3 columns

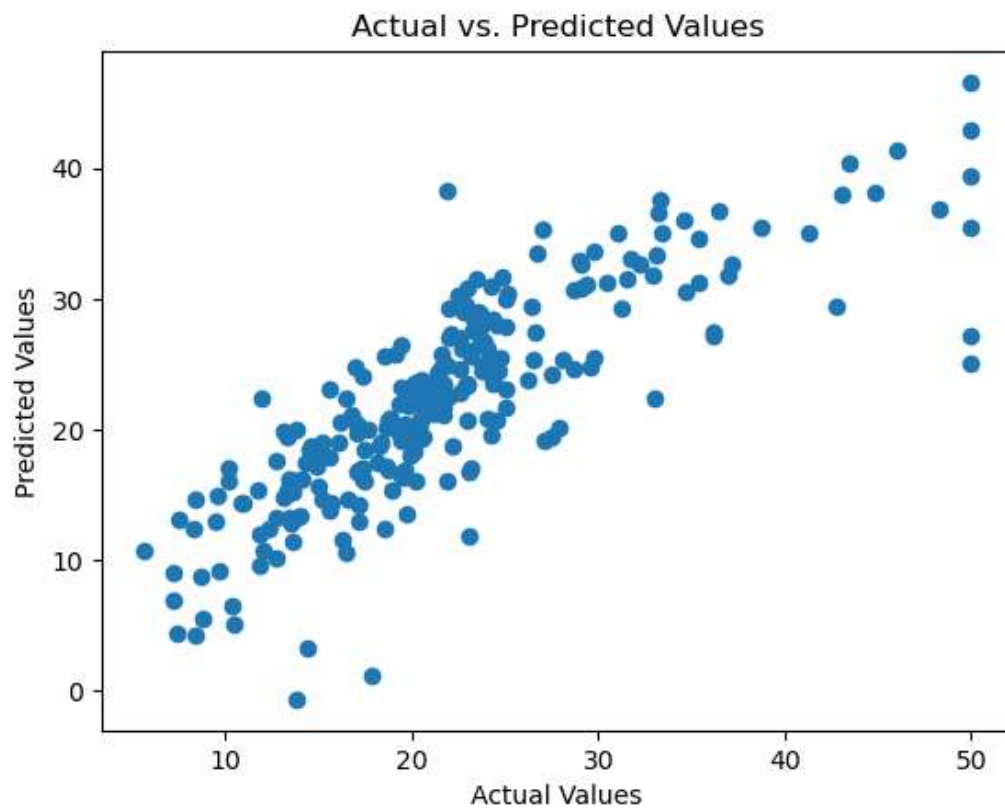
```
In [58]: model.coef_
```

Out[58]: array([-1.22697052e-01, 5.76835439e-02, 7.42047961e-02, 3.38949970e+00,
-1.65391519e+01, 3.57730248e+00, -2.98033902e-03, -1.55759520e+00,
 2.50098217e-01, -9.73850155e-03, -1.12527834e+00, 6.85073312e-03,
-5.92410460e-01])

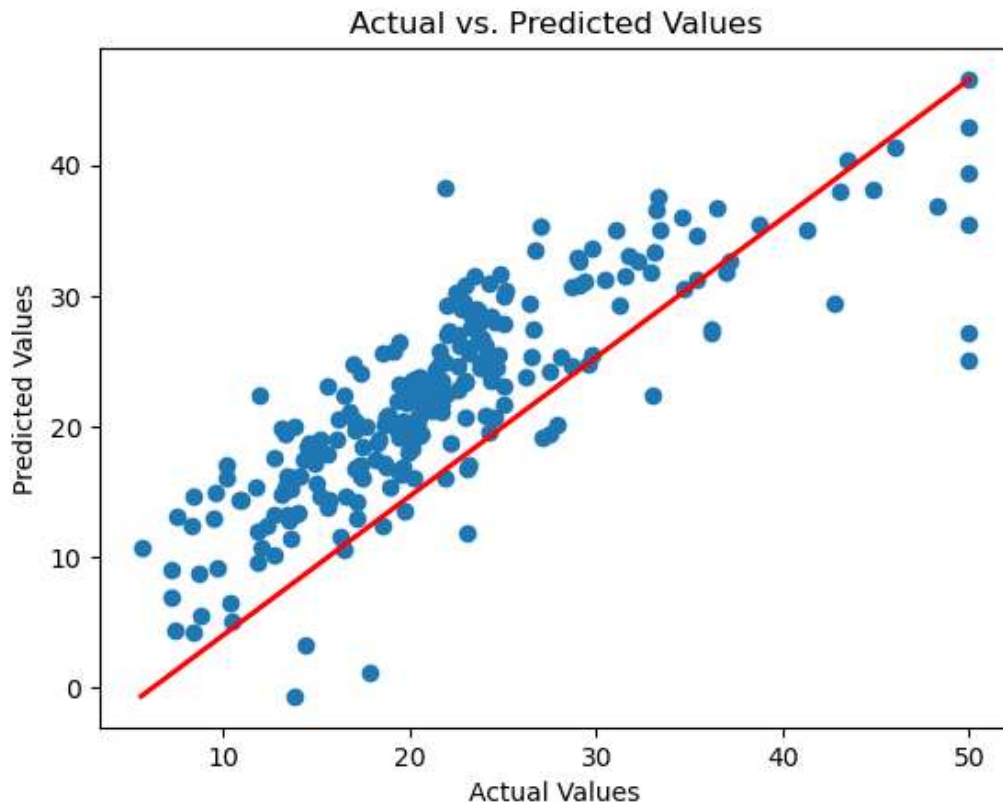
```
In [59]: model.intercept_
```

Out[59]: 41.58607683099513


```
In [60]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



```
In [61]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



ii.test_size=0.5 random_state=42

```
In [62]: x_train, x_test, y_train, y_test = train_test_split(x,y,test_size = 0.5,random_state = 42)
```

```
In [63]: model= LinearRegression()
```

```
In [64]: model.fit(x_train,y_train)
```

```
Out[64]: LinearRegression
```

```
In [65]: y_predict = model.predict(x_test)
```

```
In [66]: mse = mean_squared_error(y_test, y_predict)
r2 = r2_score(y_test, y_predict)

print(f"Mean Squared Error: {mse:.2f}")
print(f"R-squared: {r2:.2f}")
```

Mean Squared Error: 25.18
R-squared: 0.69

In [67]: `model.score(x,y)`

Out[67]: 0.7325693559556025

In [68]: `y_test = np.array(y_test).flatten()
y_predict = np.array(y_predict).flatten()
pred_y_df = pd.DataFrame({"Actual Values":y_test, "predicted values": y_predict, "Difference": y_test - y_predict})`

Out[68]:

	Actual Values	predicted values	Difference
0	23.6	28.280203	-4.680203
1	32.4	37.739436	-5.339436
2	13.6	15.407600	-1.807600
3	22.8	25.441452	-2.641452
4	16.1	18.605815	-2.505815
...
248	19.3	20.360373	-1.060373
249	23.9	26.435753	-2.535753
250	24.7	23.326693	1.373307
251	19.8	18.110622	1.689378
252	23.8	22.463210	1.336790

253 rows × 3 columns

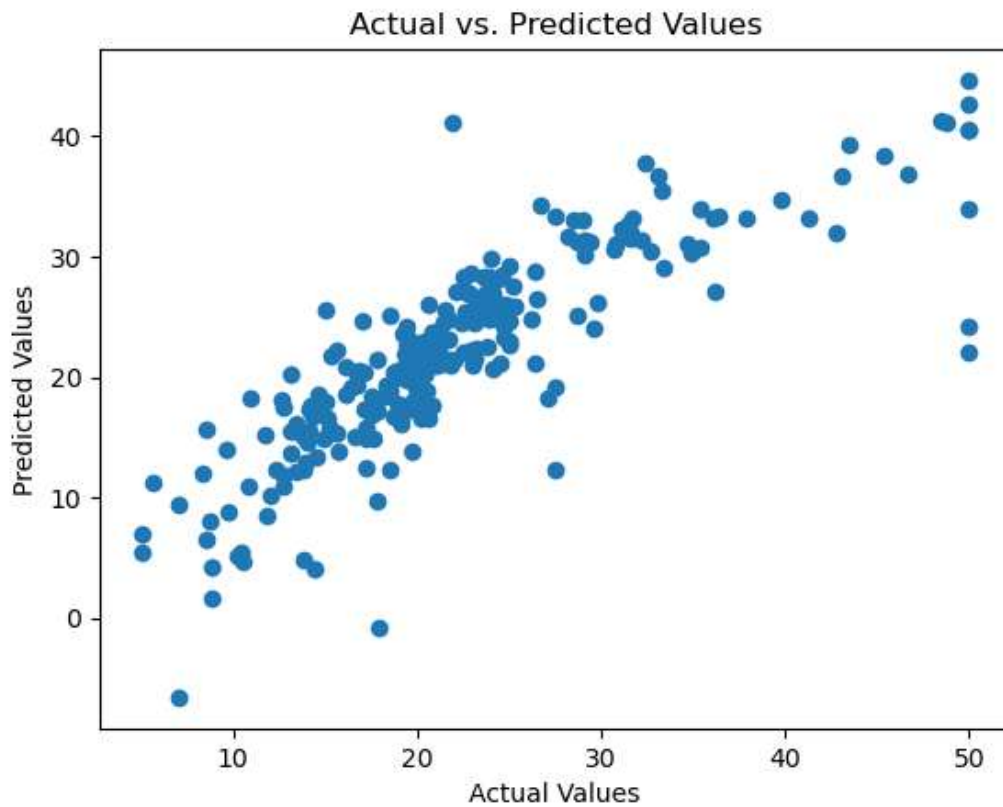
In [69]: `model.coef_`

Out[69]: `array([-1.17646736e-01, 3.32466019e-02, 3.05213436e-02, 4.40864134e+00,
 -1.34354334e+01, 4.54696921e+00, -2.19317442e-02, -1.44431337e+00,
 1.98900056e-01, -8.07440421e-03, -8.09040596e-01, 1.11002543e-02,
 -5.15546338e-01])`

In [70]: `model.intercept_`

Out[70]: 26.60863720541145

```
In [71]: plt.scatter(y_test, y_predict)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```



```
In [72]: plt.scatter(y_test, y_predict)
plt.plot([min(y_test), max(y_test)], [min(y_predict), max(y_predict)], color='red', linewidth=2)
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values')
plt.show()
```

