

Probability Basics - Session 2

Practice Exercise Solutions

1. The mean outcome for this game is calculated as follows:

$$\mu = (-1 \cdot 0.3) + (0 \cdot 0.4) + (3 \cdot 0.2) + (10 \cdot 0.1) = -0.3 + 0.6 + 0.5 = 0.8$$

the player can expect to win about 80 cents playing this game.

2. Expected Value: $\mu = E(X) = \sum x \cdot P(x)$

$$= 4 \times 0.32 + 5 \times 0.47 = 3.63.$$

$$\text{Variance: } \sum x^2 \cdot P(x): \sum x^2 \cdot P(x) = 16 \times 0.32 + 25 \times 0.47 = 16.87.$$

$$\text{Therefore, } \text{Var}(X) = \sum x^2 P(x) - \mu^2 = 16.87 - 13.17 = 3.7.$$

3. Here the events are Loss, Break Even, and Profit with respective \$ values. Thus, this is a discrete case.

Compute the Expected Return for Project A (in case of loss the amount will be -ve)

$$\text{Project A: } -71000 \cdot 0.2 + 0 \cdot 0.65 + 0.15 \cdot 143000 = \$7250$$

4. Divide the data in the infants who survived and those who did not and compare the mean weight of the both groups.

Survived: 23 and Not Survived: 27

$$E[\text{Survived}] = 1.130 + 1.575 + \dots + 3.005 / 23 = 2.307 \text{ kg}$$

$$E[\text{NotSurvived}] = 1.050 + 1.175 + \dots + 2.730 / 27 = 1.692 \text{ kg}$$

- 5.

a) # get cumulative probability for values

```
for i in range(int(df['Spending Score (1-100)'].min()),int(df['Spending Score (1-100)'].max()+10, 10):
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    print('P(x< %s): %.3f'%(i, ecdf(i)))
```

P(x< 1): 0.010

P(x< 11): 0.085

P(x< 21): 0.180

P(x< 31): 0.235

P(x< 41): 0.335

P(x< 51): 0.530

P(x< 61): 0.700

P(x< 71): 0.735

P(x< 81): 0.860

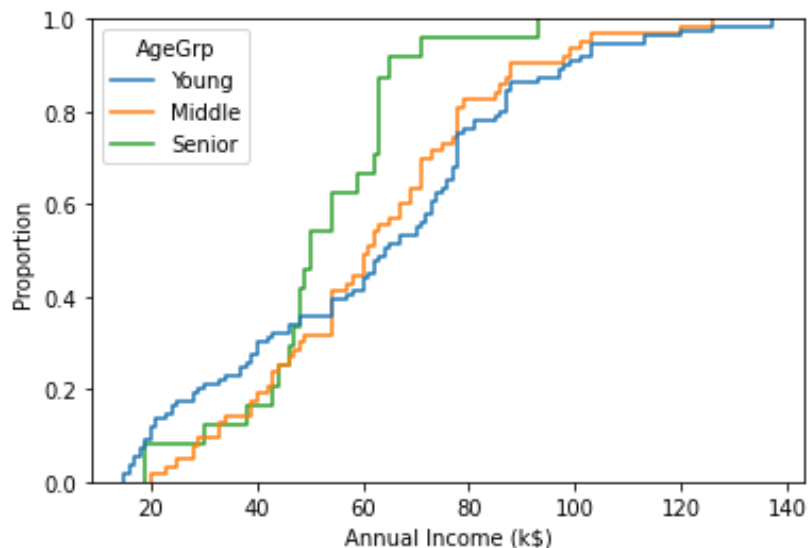
P(x< 91): 0.940

P(x< 101): 1.000

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b) min = df['Age'].min()
middle1 = df['Age'].mean()
middle2= df['Age'].mean()+df['Age'].mean()/2
max= df['Age'].max()

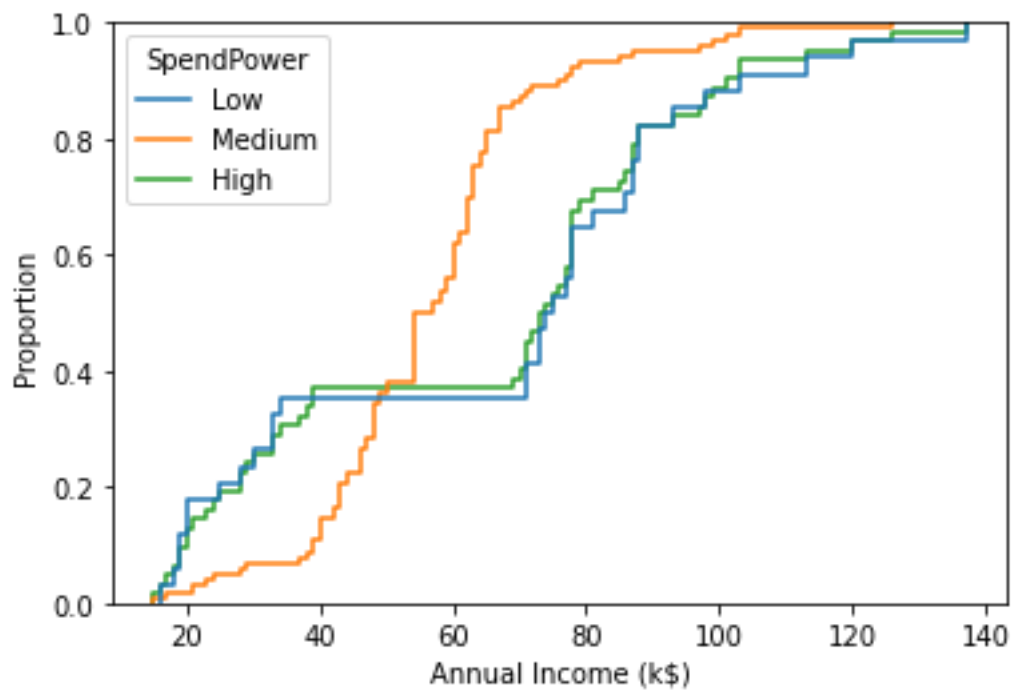
df['AgeGrp'] = pd.cut(x=df['Age'],
                      bins=[min,middle1,middle2,max],
                      labels=['Young', 'Middle', 'Senior'])

sns.ecdfplot(data=df, x="Annual Income (k$)",hue='AgeGrp')
```



65% Seniors have low income as compared to young and middle aged group

In general young people earn more than middle aged group (62%)



c)