# SCORECARD CREATION

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#### **Process Flow**

#### Data Collection

- Variable Selection
- Sample Size
- Sample / Performance Window

#### Data Cleaning

- Eliminate Duplicates
- Examine / Remove Outliers

#### Variable Grouping and Selection

- Weights of Evidence (WOE)
- Information Value (IV)
- Gini Criterion

#### Initial Scorecard Creation

- Logistic Regression
- Accuracy
- Threshold
- Assessment

#### Reject Inference

 Remove bias resulting from exclusion of rejects

#### Final Scorecard Creation

 Final Model Assessment

# INITIAL SCORECARD CREATION

#### **Initial Scorecard Model**

 The scorecard is (typically) based on a logistic regression model:

$$logit(p) = \log\left(\frac{p}{1-p}\right) = \beta_0 + \beta_1 x_1 + \dots + \beta_k x_k$$

p is the posterior probability of default (PD) given the inputs.

# Blasphemy!!!

 Wait, so I'm going through all that math just to throw things back into the logistic regression I was trying to avoid in the first place?!?!?!



## Different Inputs

 Instead of using the original variables for the model, scorecard models have the binned variables as their foundation.

Observation	Target	Bureau Score	Bureau Score Bin (R)	Bureau Score WOE (R)
1	0	757	716 – 765	1.0914
2	1	NA	Missing	-0.6972
3	0	626	605 – 629	-0.9586
4	0	693	665 – 716	0.1776
5	0	706	665 – 716	0.1776
6	0	673	665 – 716	0.1776
7	0	730	716 – 765	1.0914

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**Actual input into model!** 

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#### Different Inputs

 Instead of using the original variables for the model, scorecard models have the binned variables as their foundation.

**Actual input into model!** 

- Inputs are still treated as continuous.
- All variables now on same scale.
- Model coefficients are desired output for the scorecard.
- Coefficients now serve as measures of variable importance.

Bureau Score WOE (R) 1.0914 -0.6972-0.95860.1776 0.1776 0.1776 1.0914

```
smbinning.gen(df = train, ivout = result_all_sig$bureau_score, chrname = "bureau_score_bin")
```

smbinning.gen(df = train, ivout = result\_all\_sig\$bureau\_score, chrname = "bureau\_score\_bin")

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7	0	730	716 – 765	1.0914

```
for (i in 1:length(train)) {
   bin_name <- "bureau_score_bin"
   bin <- substr(train[[bin_name]][i], 2, 2)

woe_name <- "bureau_score_woe"

if(bin == 0) {
   bin <- dim(result_all_sig$bureau_score$ivtable)[1] - 1
   train[[woe_name]][i] <- result_all_sig$bureau_score$ivtable[bin, "woe"]
} else {
   train[[woe_name]][i] <- result_all_sig$bureau_score$ivtable[bin, "woe"]
}
}</pre>
```

Observation	Target	Bureau Score	Bureau Score Bin (R)	Bureau Score WOE (R)
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## Initial Scorecard – Example

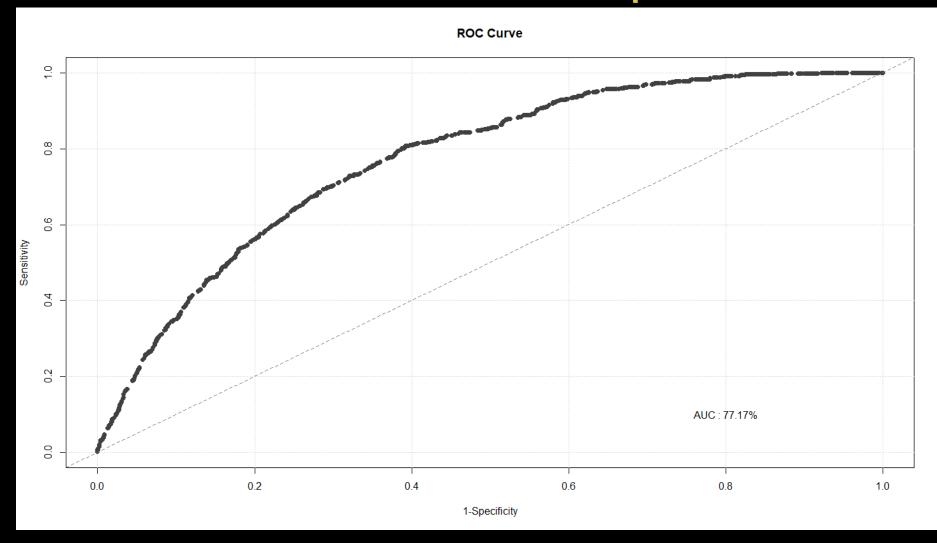
#### Initial Scorecard – Example

> summary(initial\_score) call: glm(formula = bad ~ age\_oldest\_tr\_WOE + tot\_rev\_line\_WOE + rev\_util\_WOE + bureau\_score\_WOE + down\_pyt\_WOE + ltv\_WOE, family = "binomial", data = train, weights = train\$weight) Deviance Residuals: Min 10 Median 30 Max -1.6599 -0.7457 -0.4245 -0.1655 3.3717 Coefficients: Estimate Std. Error z value Pr(>|z|) 0.04098 - 72.729 < 0.00000000000000002 \*\*\*(Intercept) -2.98073 age\_oldest\_tr\_WOE -0.25059 0.08328 -3.009 0.00262 \*\* tot\_rev\_line\_WOE -0.43244 0.07139 -6.057 0.0000000138 \*\*\* rev\_util\_woe -0.23988 0.07647 -3.137 0.00171 \*\* down\_pyt\_woe -0.38994 0.14825 -2.630 0.00853 \*\* ltv\_woe -0.86347 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1 (Dispersion parameter for binomial family taken to be 1) Null deviance: 6910.4 on 4376 degrees of freedom Residual deviance: 6083.5 on 4370 degrees of freedom AIC: 6184.2 Number of Fisher Scoring iterations: 6

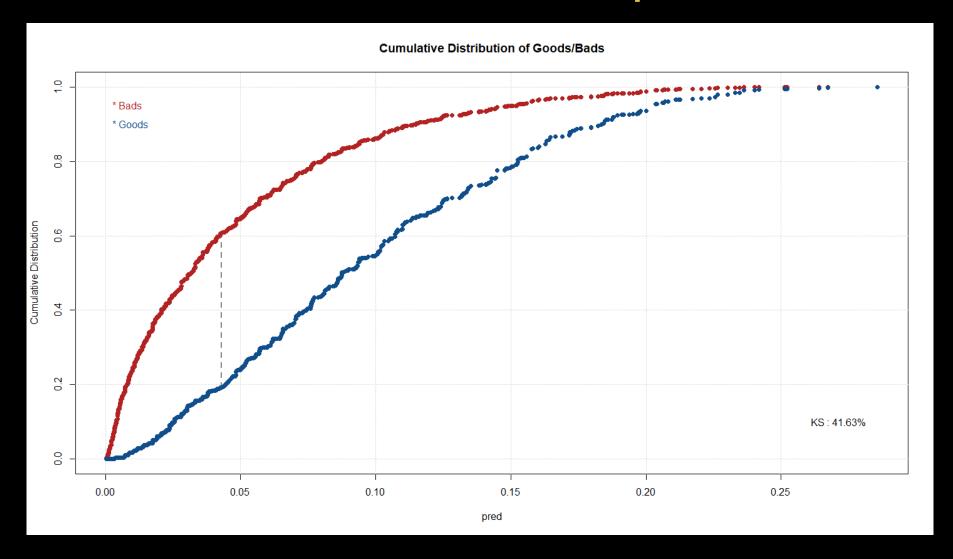
#### Model Evaluation

- Variable significance review using "standard" output of logistic regression, but don't forget business logic.
- Overall performance of model AUC (area under ROC curve, also called c) is the most popular criterion.
- This is only a preliminary scorecard.
- Final scorecard is created after reject inference is performed.

# Model Evaluation – Example



# Model Evaluation – Example





# SCALING THE SCORECARD

## Scaling the Scorecard

 The relationship between odds and scores is represented by a linear function:

$$Score = Offset + Factor \times \log(odds)$$

 If the scorecard is developed using "odds at a certain score" and "points to double the odds" (PDO), Factor and Offset can be calculated using the simultaneous equations:

$$Score = Offset + Factor \times \log(odds)$$
$$Score + PDO = Offset + Factor \times \log(2 \times odds)$$

## Scaling the Scorecard

 Solving the equations for PDO, you get the following results:

$$PDO = Factor \times \log(2)$$

Therefore,

$$Factor = \frac{PDO}{\log(2)}$$

$$Offset = Score - Factor \times \log(odds)$$

 If a scorecard were scaled where the developer wanted odds of 50:1 at 600 points and wanted the odds to double every 20 points (PDO = 20), Factor and Offset would be:

$$Factor = \frac{20}{\log(2)} = 28.8539$$

$$Offset = 600 - (28.8539 \times \log(50)) = 487.123$$

 Therefore, each score corresponding to each set of odds can be calculated as follows:

$$Score = 487.123 + 28.8539 \times \log(odds)$$

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$$Factor = \frac{20}{\log(2)} = 28.8539$$

$$Offset = 600 - (28.8539 \times \log(50)) = 487.123$$

 Therefore, each score corresponding to each set of odds can be calculated as follows:

$$Score = 487.123 + 28.8539 \times \log(odds)$$

This is predicted value from logit function.

Score	Odds
600	50.0
601	51.8
604	57.4
-	
-	
-	
-	
620	100.0

#### Points Allocation

 The points allocated to attribute i of characteristic j are computed as follows:

$$Points_{i,j} = -\left(WOE_{i,j} \times \hat{\beta}_j + \frac{\hat{\beta}_0}{L}\right) \times Factor + \frac{Offset}{L}$$

- $\overline{WOE_{i,j}}$ : Weight of evidence for attribute i of characteristic j
- $\hat{\beta}_i$ : Regression coefficient for characteristic j
- $\hat{\beta}_0$ : Intercept term from model
- L: Total number of characteristics
- Points typically rounded to nearest integer.

#### Points Allocation – Example

```
# Add Scores to Initial Model #
pdo <- 20
score <- 600
odds <- 50
fact <- pdo/log(2)
os <- score - fact*log(odds)
var_names <- names(initial_score$coefficients[-1])</pre>
for(i in var_names) {
  beta <- initial_score$coefficients[i]</pre>
  beta0 <- initial_score$coefficients["(Intercept)"]</pre>
  nvar <- length(var_names)</pre>
  WOE_var <- train[[i]]</pre>
  points_name <- paste(str_sub(i, end = -4), "points", sep="")
  train[[points_name]] <- -(WOE_var*(beta) + (beta0/nvar))*fact + os/nvar
colini <- (ncol(train)-nvar + 1)
colend <- ncol(train)</pre>
train$Score <- rowSums(train[, colini:colend])</pre>
hist(train$Score, breaks = 50, main = "Distribution of Scores", xlab = "Score")
```



# REJECT INFERENCE

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#### Reject Inference

- Reject inference is the process of inferring the status of the rejected applicants based on the accepted applicants model in an attempt to use their information to build a scorecard that is representative of the entire applicant population.
- Reject inference is about solving sample bias so that the development sample is similar to the population to which the scorecard will be applied.

#### Rejected Inference

- Can we develop a scorecard without rejected applications? YES!
- Is it legally permissible to develop a scorecard without rejected applications? YES!
- If yes, then how biased would the scorecard model be?
- "My suggestion is to develop the scorecard using what data you have, but start saving rejected applications ASAP."
  - Raymond Anderson, Head of Scoring at Standard Bank Africa, South Africa

# Why Reject Inference?

- Initial scorecard used only known good and bad loans (accepted applicants only) – also called "behavioral scoring"
- Reduce bias in model and provide risk estimates for the "through-the-door" population — also called "application scoring"
- Comply with regulatory requirements (FDIC, Basel)
- Provide a scorecard that is able to generalize better to the entire credit application population.

## Reject Inference Techniques

- Three common techniques for reject inference:
  - Hard Cutoff Augmentation
  - 2. Parceling Augmentation
  - 3. Fuzzy Augmentation (DEFAULT in SAS)

#### Hard Cutoff Augmentation

- Build a scorecard model using the known good/bad population (accepted applications)
- 2. Score the rejected applications with this model to obtain each rejected applicant's probability of default and their score on the scorecard model.
- 3. Create weighted cases for the rejected applicants weight applied is the "rejection rate" which adjusts the number of sampled rejects to accurately reflect the number of rejects from population.

## Hard Cutoff Augmentation

- 4. Set a cut-off score level above which applicant is deemed good and below applicants deemed bad.
- 5. Add inferred goods and bads with known goods and bads and rebuild scorecard.

# Hard Cutoff Augmentation – Example

```
# Reject Inference - Hard Cut-off #
rejects_scored$pred <- predict(initial_score, newdata=rejects_scored, type='response')
rejects$bad <- as.numeric(rejects_scored$pred > 0.0603)
rejects$weight <- ifelse(rejects$bad == 1, 2.80, 0.59)
rejects$good <- abs(rejects$bad - 1)
comb_hard <- rbind(accepts, rejects) # New Combined Data Set #</pre>
```

# Hard Cutoff Augmentation – Example

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# Parceling Augmentation

- Build a scorecard model using the known good/bad population (accepted applications)
- 2. Score the rejected applications with this model to obtain each rejected applicant's probability of default and their score on the scorecard model.
- 3. Create weighted cases for the rejected applicants weight applied is the "rejection rate" which adjusts the number of sampled rejects to accurately reflect the number of rejects from population.

# Parceling Augmentation

- 4. Define score ranges manually or automatically with simple bucketing.
- 5. The inferred good/bad status of the rejected applicants will be assigned **randomly** and proportional to the number of goods and bads in the accepted population within each score range.
- If desired, apply the event rate increase factor to P(bad) to increase the proportion of bads among the rejects (oversampling with the rejects)
- 7. Add the inferred goods and bads back in with the known goods and bads and rebuild the scorecard.

	Accepted Applicants				Rejected Applicants		
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	?	?

	Accepted Applicants				Rejected Applicants		
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	5	0

Assume bad if no information to prove otherwise

	Į.	Accepted A	Applicant	Rejected Applicants			
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	5	0
655 <b>–</b> 665	300	360	45.5%	54.5%	190	?	?

	Accepted Applicants				Rejected Applicants		
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	5	0
655 <b>–</b> 665	300	360	45.5%	54.5%	190	86	?

 $0.455\times190\approx86$ 

Randomly assign!

	Accepted Applicants				Rejected Applicants		
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	5	0
655 – 665	300	360	45.5%	54.5%	190	86	114
							•

190 - 86 = 114

	Į.	Accepted A	Applicant	Rejected Applicants			
Score Range	# Bad	# Good	% Bad	%Good	Rejects	# Inferred Bad	# Inferred Good
< 655	0	0	0%	0%	5	5	0
655 <b>–</b> 665	300	360	45.5%	54.5%	190	86	114
665 – 675	450	700	39.1%	60.9%	250	98	152

```
# Reject Inference - Parcelling #
parc <- seq(500, 725, 25)
accepts_scored$score_parc <- cut(accepts_scored$score, breaks = parc)
rejects_scored$Score_parc <- cut(rejects_scored$Score, breaks = parc)
table(accepts_scored$score_parc, accepts_scored$bad)
parc_perc <- table(accepts_scored$score_parc, accepts_scored$bad)[,2]/rowSums(table(accepts_scored$score_parc, accepts_scored$bad))</pre>
rejects$bad <- 0
rej_bump <- 1.25
for(i in 1:(length(parc)-1)) {
  for(j in 1:length(rejects_scored$score)) {
    if((rejects_scored$score[j] > parc[i]) &
        rejects_scored$Score[j] < parc[i+1] &
        (runif(n = 1, min = 0, max = 1) < (rej_bump*parc_perc[i]))) {
      rejects$bad[j] <- 1
table(rejects_scored$score_parc, rejects_scored$bad)
rejects\( weight <- ifelse(rejects\) bad == 1, 2.80, 0.59)
rejects$good <- abs(rejects$bad - 1)
comb_parc <- rbind(accepts, rejects) # New Combined Data Set #</pre>
```

```
# Reject Inference - Parcelling #
parc <- seq(500, 725, 25)
accepts_scored$score_parc <- cut(accepts_scored$score, breaks = parc)
rejects_scored$5core_parc <- cut(rejects_scored$5core, breaks = parc)
table(accepts_scored$score_parc, accepts_scored$bad)
parc_perc <- table(accepts_scored$score_parc, accepts_scored$bad)[,2]/rowSums(table(accepts_scored$score_parc, accepts_scored$bad))</pre>
rejects$bad <- 0
rej_bump <- 1.25
for(i in 1:(length(parc)-1)) {
  for(j in 1:length(rejects_scored$score)) {
    if((rejects_scored$Score[j] > parc[i]) &
        rejects_scored$Score[j] < parc[i+1] &
        (runif(n = 1, min = 0, max = 1) < (rej_bump*parc_perc[i]))) {
      rejects$bad[i] <- 1
table(rejects_scored$score_parc, rejects_scored$bad)
rejects\( weight <- ifelse(rejects\) bad == 1, 2.80, 0.59)
rejects$good <- abs(rejects$bad - 1)
comb_parc <- rbind(accepts, rejects) # New Combined Data Set #</pre>
```

## Fuzzy Augmentation

- Build a scorecard model using the known good/bad population (accepted applications)
- 2. Score the rejected applications with this model to obtain each rejected applicant's probability of being good, P(Good), and probability of being bad, P(Bad).
- 3. Do not assign a reject to a good/bad class create two weighted cases for each rejected applicant using P(Good) and P(Bad).

## **Fuzzy Augmentation**

- 4. Multiply P(Good) and P(Bad) by the user-specific rejection rate to form frequency variables.
- 5. For each rejected applicant, create **two observations** one observation has a frequency variable (rejection weight × P(Good)) and a target variable of 0; other observation has a frequency variable (rejection weight × P(Bad)) and a target variable of 1.
- 6. Add inferred goods and bads back in with the known goods and bads and rebuild the scorecard.

# Fuzzy Augmentation – Example

```
# Reject Inference - Fuzzy Augmentation #
rejects_scored$pred <- predict(initial_score, newdata=rejects_scored, type='response')
rejects_g <- rejects
rejects_b <- rejects
rejects_g$bad <- 0
rejects_g$weight <- (1-rejects_scored$pred)*2.80
rejects_g$good <- 1
rejects_b$bad <- 1
rejects_b$bad <- 1
rejects_b$weight <- (rejects_scored$pred)*0.59
rejects_b$good <- 0|
comb_fuzz <- rbind(accepts, rejects_g, rejects_b)</pre>
```

# Reject Inference Techniques

- Three common techniques for reject inference:
  - Hard Cutoff Augmentation
  - 2. Parceling Augmentation
  - Fuzzy Augmentation (DEFAULT in SAS)
- There are other techniques as well, but are not as highly recommended.

- Assign all rejects to bads.
- Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
- 3. Similar in-house model on different data.
- 4. Approve all applicants for certain period of time.
- 5. Clustering
- Memory based reasoning

- 1. Assign all rejects to bads
  - Appropriate only if approval rate is very high (ex. 97%) and there is a high degree of confidence in adjudication process.
- 2. Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
- 3. Similar in-house model on different data.
- 4. Approve all applicants for certain period of time.
- Clustering
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- 1. Assign all rejects to bads.
- Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
  - Assignment done completely at random!
  - Valid only if current system has no consistency.
- 3. Similar in-house model on different data.
- 4. Approve all applicants for certain period of time.
- Clustering
- 6. Memory based reasoning

- 1. Assign all rejects to bads.
- 2. Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
- 3. Similar in-house model on different data.
  - Performance on similar products used as proxy.
  - Hard to pass by regulators.
- 4. Approve all applicants for certain period of time.
- Clustering
- 6. Memory based reasoning

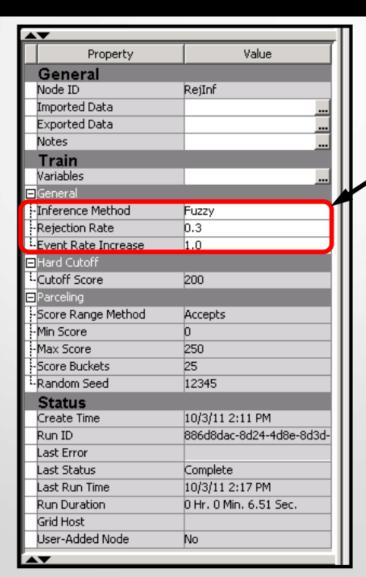
- 1. Assign all rejects to bads.
- Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
- 3. Similar in-house model on different data.
- 4. Approve all applicants for certain period of time.
  - Provides actual performance of rejects instead of inferred.
  - Might be "legal" problems....
- 5. Clustering
- 6. Memory based reasoning

- 1. Assign all rejects to bads.
- Assign rejects in the same proportion of goods to bads as reflected in the accepted data set.
- 3. Similar in-house model on different data.
- 4. Approve all applicants for certain period of time.
- Clustering
- Memory based reasoning



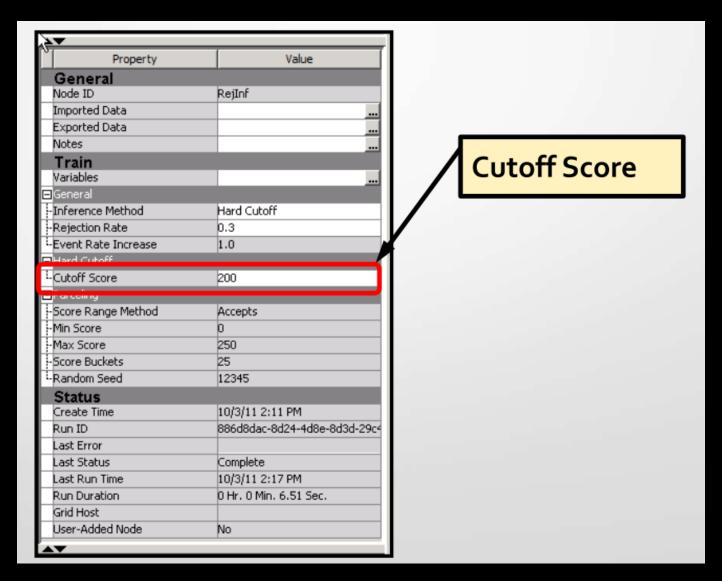
# REJECT INFERENCE NODE IN SAS EM

# **General Options**

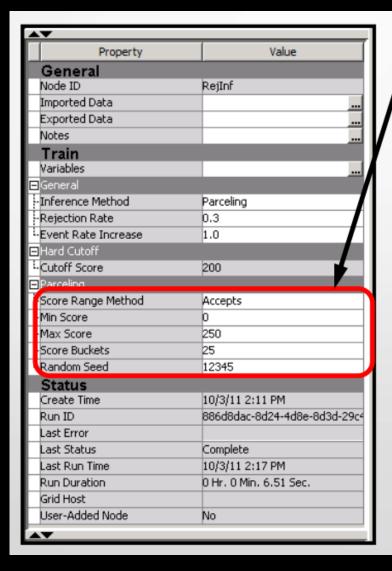


Inference Method Rejection Rate Event Rate Increase

# Hard Cut-off Options



# Parceling Options



Score Range Method Min Score Max Score Score Buckets Random Seed



# FINAL SCORECARD CREATION

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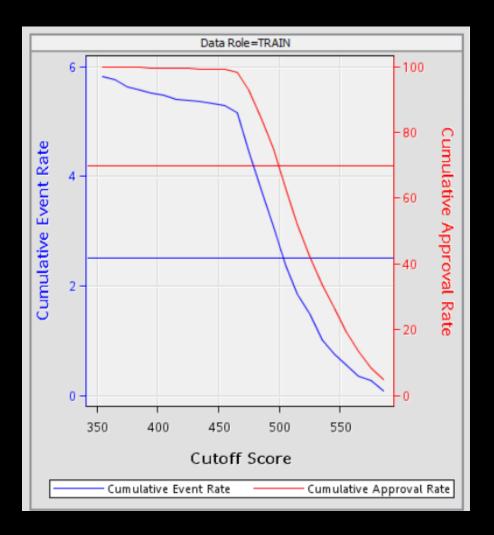
 Final Model Assessment

### Final Scorecard Creation

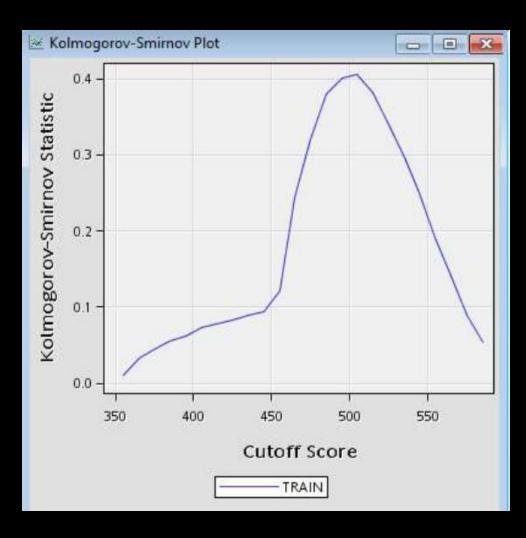
- The mechanics of building the final scorecard model are identical with the initial scorecard creation except that analysis is performed after reject inference.
- Accuracy Measurements:
  - Repeat review of the logistic model estimated parameters, life, KS, ROC, etc.

- A new scored should be better than the last in terms of one of the following:
  - Lower bad rate for the same approval rate.
  - Higher approval rate while holding the bad rate constant.

- Trade-off Plots:
  - The reference lines of approval rate and event (bad) rate are predefined by analyst.
  - How much risk are you willing to take on?

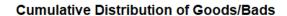


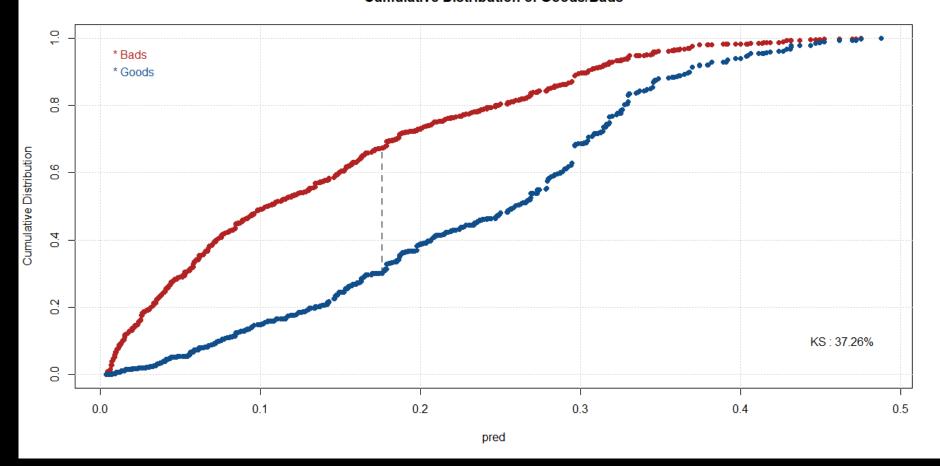
- KS Statistic Plot:
  - KS Statistic is how well your model separates the 1's and 0's goods and bads.
  - Cut-off that maximizes the KS value.



- Setting Multiple Cut-offs Example:
  - Anyone who scores above 210 points is accepted automatically.
  - Anyone who scores below 190 is declined.
  - Any scores in between 190 and 210 are referred to manual adjudication.

# Final Scorecard – Example





# Final Scorecard – Example

