

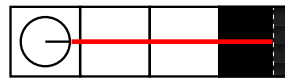
## Tutorial 5

Topic: Grid Maps & Mapping with Known Poses

Solutions will be discussed in class Monday 12:10-13:10, Week 50 of the calendar year.

### Q 1 – Occupancy Mapping

A robot has to build an occupancy grid map of a simple one-dimensional environment using a sequence of measurements from a range sensor.



Assume a simple inverse sensor model: every grid cell with a distance (based on its coordinate) smaller than the measured distance is assumed to be occupied with  $p = 0.3$ . Every cell behind the measured distance is occupied with  $p = 0.6$ . Every cell located more than 20cm behind the measured distance should not be updated. Additionally, the prior belief is set to 0.5.

Give the equation of the inverse sensor model  $l(m_i | z_t, x_t)$  and the value of the prior  $l(m_i)$  as used in the log-odds update equation.

Additionally, derive the equation to convert from log-odds to probabilities from the definition of the log odds ratio.

### Q 2 – Occupancy Mapping

Prove that in the occupancy grid mapping framework the occupancy value of a grid cell  $P(m_j | x_{1:t}; z_{1:t})$  is independent of the order in which the measurements are integrated.

## Q 3 – Counting Model

A robot applies the so-called simple counting approach to build a grid map of a 1D environment consisting of the cells  $c_0, \dots, c_3$ . While standing in cell  $c_0$ , the robot integrates four measurements  $z_{t_0}, \dots, z_{t_3}$ . After integrating these measurements, the resulting belief of the robot with regards to the occupancy of the four cells is  $b_0 = 0$ ,  $b_1 = \frac{1}{4}$ ,  $b_2 = \frac{2}{3}$ ,  $b_3 = 1$ . Given that the first three measurements are  $z_{t_0} = 1$ ,  $z_{t_1} = 2$ ,  $z_{t_2} = 3$ , compute the value of the last measurement  $z_{t_3}$ .