

## Tutorial 4

Topic: Localization - Extended Kalman Filter

Solutions will be discussed in class Monday 12:10-13:10, Week 49 of the calendar year.

### Q 1 – Theoretical Considerations

The EKF is an implementation of the Bayes Filter.

#### 1.a

The Bayes filter processes three probability density functions, i. e.,  $p(x_t | u_t, x_{t-1})$ ,  $p(z_t | x_t)$ , and  $\text{bel}(x_t)$ . State the normal distributions of the EKF which correspond to these probabilities.

#### 1.b

Explain in a few sentences all of the components of the EKF, i. e.,  $\mu_t$ ,  $\Sigma_t$ ,  $g$ ,  $G_t$ ,  $h$ ,  $H_t$ ,  $R_t$ ,  $Q_t$ ,  $K_t$  and why they are needed. What are the differences and similarities between the KF and the EKF?

### Q 2 – EKF Prediction Step

We assume a differential drive robot operating on a 2-dimensional plane, i.e., its state is defined by  $\langle x, y, \theta \rangle$ . Its motion model is defined in the lecture "Probabilistic Motion Models - 2", slide 13, lines 4 - 6. Derive the Jacobian matrix  $G_t$  of the noise-free motion function  $g$ .

### Q 3 – EKF Correction Step

Derive the Jacobian matrix  $H_t$  of the noise-free measurement function  $h$  of a range-only sensor.