

# ARTIFICIAL INTELLIGENCE



## N-QUEENS PROBLEM

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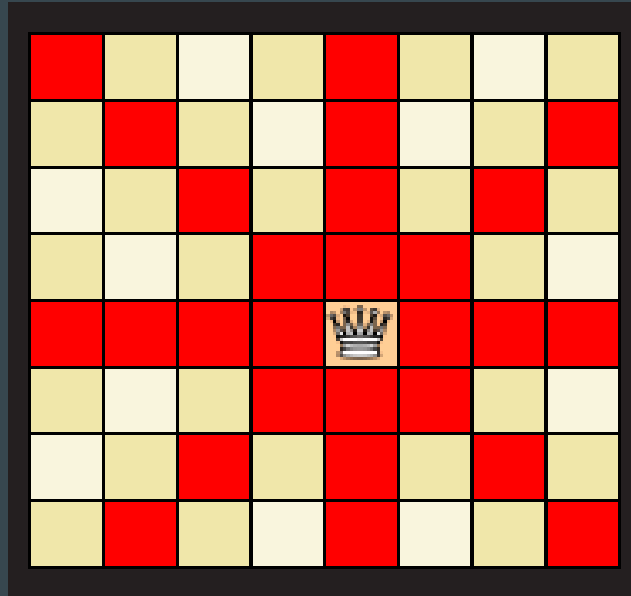
(17BCS009)

PRIYA A TIRU (17BCS021)

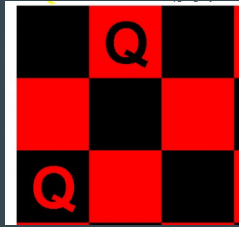
VIVEK DAL (17BCS022)

# PROBLEM STATEMENT/ HARDNESS

Using a regular chess board, the challenge is to place 8 queens on the board such that no queen is attacking any of the other.

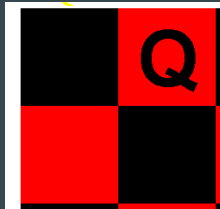


# SOLVING N-QUEENS PROBLEM



$N < 4$

Cannot use  $N$  Queens



**Search Space:** The set of objects among which we search for the solution

Example: N-queen configurations

**Goal condition:** This is the characteristics of the object we want to find in the search space?

Example: Non-attacking n-queen configuration

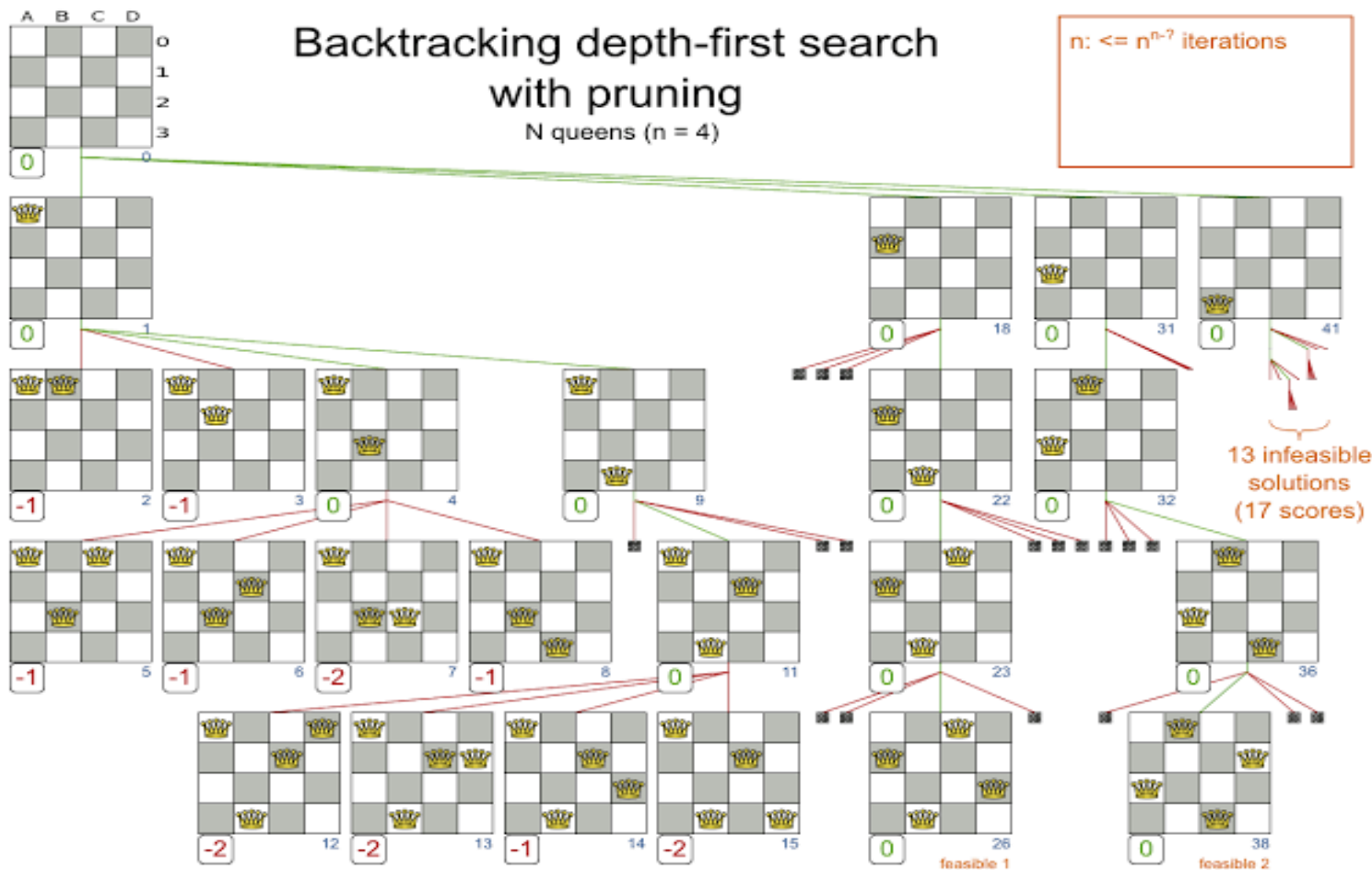
# SOLUTION USING BACKTRACKING

- One of the approach that guarantees a solution, though it can be slow
- Can be seen as a form of intelligent depth-first search

# Backtracking depth-first search with pruning

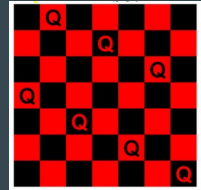
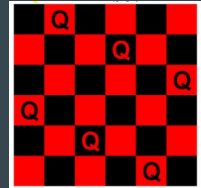
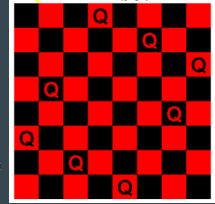
N queens (n = 4)

n:  $\leq n^{n-1}$  iterations



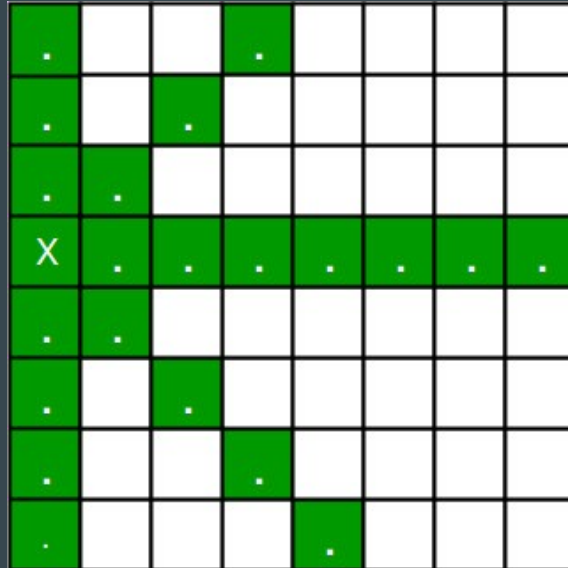
# MATHEMATICAL FORMULATION Iterative (non-search)

- For  $N > 4$  only
- $N$  is even except  $N \neq 6K+2$  :
  - Row 1 to  $N/2$ : Queen on  $2*\text{Row}$
  - Row  $N/2+1$  to  $N$ : Queen on  $2*\text{Row}-N-1$
- $N$  is even,  $N = 6K+2$ 
  - Row 1 to  $N/2$ : Queen on  $(2*\text{Row} + N/2 - 3) \bmod N + 1$
  - Row  $N/2+1$  to  $N$ : Queen on  $N - (2*(N-\text{Row}+1) + N/2 - 3) \bmod N$
- $N$  is odd:
  - When  $N$  is even, no queen is placed on position  $(1,1)$ .
  - So this just places the first  $N-1$  queens as on an  $N-1$  (even) sized board, then places the last queen on the bottom right position  $(N,N)$ .



# CONSTRAINTS

1. There can be only one queen in a column , and another constraint prohibits two queens on the same diagonal.
2. No queens on the same row.





Thank you