

Objective- Implement SGD to Linear Regression

Importing libraries

```
In [1]: import warnings
warnings.filterwarnings("ignore")
from sklearn.datasets import load_boston
from random import seed
from random import randrange
from csv import reader
from math import sqrt
from sklearn import preprocessing
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from prettytable import PrettyTable
from sklearn.linear_model import SGDRegressor
from sklearn import preprocessing
from sklearn.metrics import mean_squared_error
```

```
In [2]: # Loading of Boston dataset
from sklearn.datasets import load_boston
boston=load_boston()
```

```
In [3]: # Shape of data
print(boston.data.shape)

(506, 13)
```

```
In [4]: # Number of rows
print(boston.data.shape[0])
```

```
In [5]: # Number of columns
print(boston.data.shape[1])
```

13

```
In [6]: # Columns Name of Boston dataset
print(boston.feature_names)

['CRIM' 'ZN' 'INDUS' 'CHAS' 'NOX' 'RM' 'AGE' 'DIS' 'RAD' 'TAX' 'PTRATI
0'
 'B' 'LSTAT']
```

Importing Data

```
In [7]: # Dividing dataset into data(input variables) and target(output variable)
X = pd.DataFrame(boston.data)
Y = pd.DataFrame(boston.target)
```

```
In [8]: # Preprocessing of data
scaler = preprocessing.StandardScaler()
scaler.fit(X)
X_data=pd.DataFrame(scaler.transform(X))
```

```
In [9]: #Concatenating Input and output variables into a single DataFrame
data = pd.concat([X_data,Y], axis=1,ignore_index=True)
```

```
In [10]: #Printing Top 5 rows
data.head(5)
```

Out[10]:

	0	1	2	3	4	5	6	7	
0	-0.417713	0.284830	-1.287909	-0.272599	-0.144217	0.413672	-0.120013	0.140214	-0

	0	1	2	3	4	5	6	7	
1	-0.415269	-0.487722	-0.593381	-0.272599	-0.740262	0.194274	0.367166	0.557160	-0
2	-0.415272	-0.487722	-0.593381	-0.272599	-0.740262	1.282714	-0.265812	0.557160	-0
3	-0.414680	-0.487722	-1.306878	-0.272599	-0.835284	1.016303	-0.809889	1.077737	-0
4	-0.410409	-0.487722	-1.306878	-0.272599	-0.835284	1.228577	-0.511180	1.077737	-0

SGD regressor of Sklearn

```
In [11]: import warnings
warnings.filterwarnings("ignore")

#Applying SGDRegressor() and fitting the model on Data
clf = SGDRegressor()
clf.fit(X_data, Y)

#Printing the mean square error (Actual Y- Predicted Y)
print(mean_squared_error(Y, clf.predict(X_data)))

22.782371903483956
```

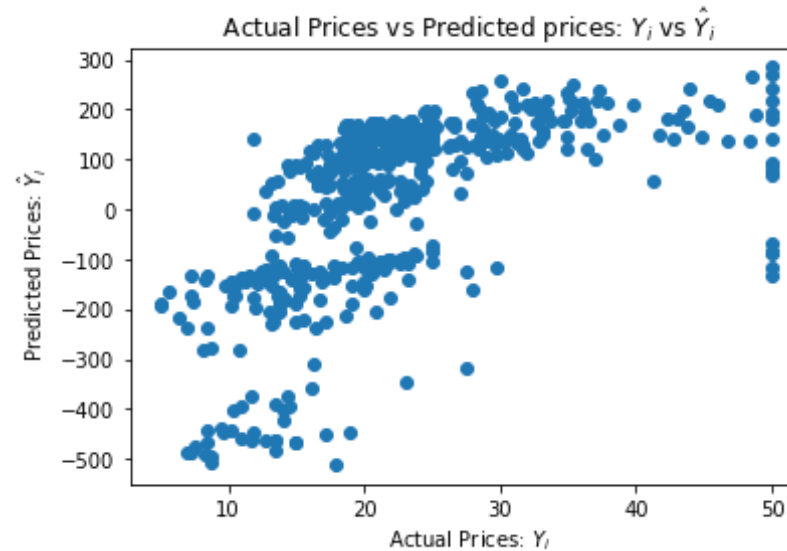
```
In [12]: # Finding the intercept value
clf.intercept_
```

```
Out[12]: array([22.35309641])
```

```
In [13]: # individual weights and storing as list in Dataframe
SGD_wght=pd.DataFrame(list(clf.coef_))
```

```
In [14]: #Plotting the Scatter plot of Predicted vs Actual price of Boston datas
et
plt.scatter(Y, clf.predict(X))
plt.xlabel(" Actual Prices: $Y_i$")
```

```
plt.ylabel(" Predicted Prices:  $\hat{Y}_i$ ")
plt.title(" Actual Prices vs Predicted prices:  $Y_i$  vs  $\hat{Y}_i$ ")
plt.show()
```



Manual SGD implementation

```
In [27]: #Taking random weight vector 'w' into Dataframe
w=pd.DataFrame(X_data.loc[0,:])

w=w.T      #Changing into row vector as default type is column vector
w          #Printing the weight vector 'w'
```

Out[27]:

	0	1	2	3	4	5	6	7	
0	-0.417713	0.28483	-1.287909	-0.272599	-0.144217	0.413672	-0.120013	0.140214	-0.98

```
In [28]: b=0      #Choosing Default value of intercept(scalar)
```

```
r=1 #Learning rate(r)
```

```
In [29]: # Reference: https://stackoverflow.com/questions/50328545/stochastic-gradient-descent-for-linear-regression-on-partial-derivatives
while(True):

    random_data=data.sample(100) #Taking the random data of 100 samples

    random_data=random_data.reset_index(drop=True)

    X=random_data.loc[:,0:12] #Taking all the input variables needed to predict the class label
    Y=random_data.loc[:,13] #Taking the output variable(class label)

    w_optimized=0.0
    b_optimized=0.0

    for k in range(100):
        #  $-2x * (y - (mx + b))$ 
        w_optimized= w_optimized+(-2*X.loc[k]*(Y.loc[k]-np.dot(X.loc[k],w.T)-b))

        #  $-2(y - (mx + b))$ 
        b_optimized=b_optimized+(float(-2*(Y.loc[k]-np.dot(X.loc[k],w.T)-b)))

    #updating the parameters
    w0=w-r*(w_optimized/100)
    b0=b-r*(b_optimized/100)

    r=r/2 #reducing the learning rate to half in each iteration

    #Comparing whether the obtained w is same as previous w
    if(np.array(w)==np.array(w0)).all():
        break;
    else:
        w=w0 #updating the value of w in each iteration
```

```
b=b0 #updating the value of b in each iteration
```

```
In [30]: # Obtained value of weight vector  
w0
```

```
Out[30]:
```

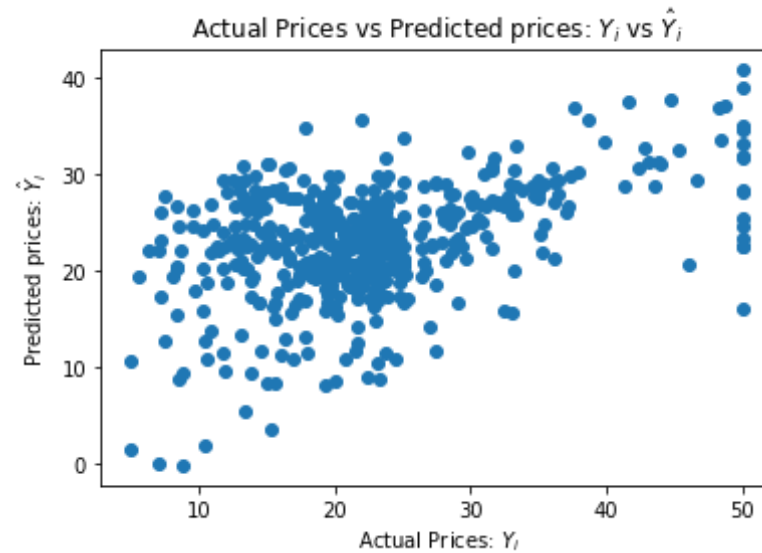
	0	1	2	3	4	5	6	7	
0	-3.239091	0.973096	-0.278184	-2.432222	-0.827658	4.525984	2.053458	-0.699801	1.4

```
In [31]: b0
```

```
Out[31]: 22.87076428299188
```

```
In [32]: y_pred=[]  
X=data.loc[:,0:12]  
y=data.loc[:,13]  
  
for i in range(506):  
    # Determining the hyperplane using the formula,  $y=mx+c$   
    # where  $m=w0.T(\text{vector})$ ,  $x=X[i]$   $i=0,1,2..506$  ,  $c=b0(\text{scalar})$   
    y_pred.append(np.dot(X.loc[i],w0.T)+b0)  
  
y_pred=np.asarray(y_pred)
```

```
In [33]: #Plotting the Scatter plot of Predicted vs Actual price of Boston datas  
et  
import matplotlib.pyplot as plt  
plt.scatter(y, y_pred)  
plt.xlabel(" Actual Prices:  $Y_i$ ")  
plt.ylabel("Predicted prices:  $\hat{Y}_i$ ")  
plt.title("Actual Prices vs Predicted prices:  $Y_i$  vs  $\hat{Y}_i$ ")  
plt.show()
```



```
In [36]: #Printing the mean square error (Actual Y- Predicted Y)
print(mean_squared_error(y,y_pred))
```

24.14143389935003

Summary

```
In [37]: #plotting the obtained results in Tabular form
from prettytable import PrettyTable
x = PrettyTable()
x.field_names = ["Parameters", "Manual SGD", "Sklearn SGD"]
x.add_row(["Mean Squared error", 24.1414, 22.7823])
x.add_row(["Intercept term ", 22.5334, 22.3530])
print(x)
```

Parameters	Manual SGD	Sklearn SGD
Mean Squared error	24.1414	22.7823
Intercept term	22.5334	22.3530

Intercept term	22.5334	22.353	
+-----+	+-----+	+-----+	+-----+

- The mean square error obtained from Manual SGD is almost similar to the mean square error obtained from the Sklearn SGD with small difference.
- The intercept term is also similar in both the cases.

In [38]: [#https://stackoverflow.com/questions/25698448/how-to-embed-html-into-ipynb-output](https://stackoverflow.com/questions/25698448/how-to-embed-html-into-ipynb-output)

```
from IPython.display import HTML, display
import tabulate
print("Manual SGD weights")
display(HTML(tabulate.tabulate(w0, tablefmt='html', showindex=False)))
print("Sklearn SGD weights")
display(HTML(tabulate.tabulate(SGD_wght.T, tablefmt='html', showindex=False)))
```

Manual SGD weights

-3.23909	0.973096	-0.278184	-2.43222	-0.827658	4.52598	2.05346	-0.699801	1.46954	1
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Sklearn SGD weights

-0.697901	0.695221	-0.453927	0.774562	-0.865385	3.08178	-0.0128706	-2.1502	0.95927
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