/*
Compiler's Lab :
* - Abhishek Goyal - 120101004
* - Dheeraj Khatri - 120101021
* - Ojas Deshpande - 120101046
*
*
*
* Input format - Regex must be well paranthesized. No need to give any symbol for
concatenation.
* Only 'or' () and 'kleene star' (*) operations are supported. Alphabet - {a,b}
*
*/

```
#include <bits/stdc++.h>
using namespace std;
struct trans {
  int vertex_from;
  int vertex_to;
  char trans_symbol;
};
class NFA {
public:
  vector<int> vertex;
  vector<trans> transitions;
  int final_state;
  NFA() {
```

```
}
int get_vertex_count() {
  return vertex.size();
}
void set_vertex(int no_vertex) {
  for(int i = 0; i < no_vertex; i++) {
     vertex.push_back(i);
  }
}
void set_transition(int vertex_from, int vertex_to, char trans_symbol) {
  trans new_trans;
  new_trans.vertex_from = vertex_from;
  new_trans.vertex_to = vertex_to;
```

```
new_trans.trans_symbol = trans_symbol;
  transitions.push_back(new_trans);
}
void set_final_state(int fs) {
  final_state = fs;
}
int get_final_state() {
  return final_state;
}
void display() {
  trans new_trans;
  cout<<"\n";
  for(unsigned int i = 0; i < transitions.size(); i++) {</pre>
```

```
new_trans = transitions.at(i);
       cout<<"q"<<new_trans.vertex_from<<" --> q"<<new_trans.vertex_to<<" :
Symbol - "<<new_trans.trans_symbol<<endl;
    }
     cout<<"\nThe final state is q"<<get_final_state()<<endl;</pre>
  }
  set<int> epsilon_closure(int index){
     set<int> myclous;
     myclous.insert(index);
     for(vector<trans> ::iterator it = transitions.begin(); it!=transitions.end(); ++it){
       if(it->vertex_from == index && it->trans_symbol == '^'){
          myclous.insert(it->vertex_to);
          set<int>temps = this->epsilon_closure(it->vertex_to);
```

```
for(set<int>::iterator itt = temps.begin();itt!=temps.end();++itt){
             myclous.insert(*itt);
          }
       }
     }
     return myclous;
  }
};
class DFA {
public:
  int vertex; // number of vertex
  vector<trans> transitions;
  vector<int> final_state;
```

```
void set_vertex(int count){
  vertex = count;
}
int get_vertex_count(){
  return vertex;
}
void set_final_state(int state){
  final_state.push_back(state);
}
bool is_final(int state){
  for(vector<int>::iterator it = final_state.begin();it!=final_state.end();++it){
     if(state == *it){
        return true;
```

```
}
  }
  return false;
}
void set_transition(int vertex_from,int vertex_to,char trans_symbol){
  trans new_trans;
  new_trans.vertex_from = vertex_from;
  new_trans.vertex_to = vertex_to;
  new_trans.trans_symbol = trans_symbol;
  transitions.push_back(new_trans);
}
void display() {
  trans new_trans;
```

```
cout<<"\n";
     for(unsigned int i = 0; i < transitions.size(); i++) {</pre>
        new_trans = transitions.at(i);
        cout<<"q"<<new_trans.vertex_from<<" --> q"<<new_trans.vertex_to<<" :
Symbol - "<<new_trans.trans_symbol<<endl;
     }
     // also print here final states
     cout<<"final states of dfa are"<<endl;
     for(vector<int>::iterator ift = final_state.begin();ift!=final_state.end();ift++){
        cout<<*ift<<" ";
     }cout<<endl;
  }
};
```

```
DFA nfa_to_dfa(NFA nfa){
  DFA dfa;
  int i,stateCounter,curState;
  stateCounter = curState = 0;
  map<set<int>,int >found_mapping; // map to record sets found till now
                                //queue to maintain all the set yet to be proceed
  queue<set<int> > todo;
  set<int> a_set;
  set<int> b_set;
  set<int> a_epsilon;
  set<int> b_epsilon;
  set<int> lol;
  bool isdone[20000];
  for(i=0;i<20000;i++)
```

```
isdone[i] = false;
set<int>temps = nfa.epsilon_closure(0);
//todoSet.push_back(temps);
found_mapping.insert(make_pair(temps,curState));
todo.push(temps);
while(!todo.empty()){
  temps.clear();
  a_set.clear();
  b_set.clear();
  a_epsilon.clear();
  b_epsilon.clear();
  lol.clear();
  temps = todo.front();
```

```
curState = found_mapping[temps];
     todo.pop();
     if(isdone[curState]==true)continue;
     isdone[curState] = true;
     // finding a_set and b_set
     for(vector<trans>::iterator its =
(nfa.transitions).begin();its!=(nfa.transitions).end();++its){
       if(temps.find(its->vertex_from)!=temps.end()){
          if(its->trans_symbol == 'a'){
             a_set.insert(its->vertex_to);
          }else if(its->trans_symbol == 'b'){
             b_set.insert(its->vertex_to);
          }
```

```
}
}
//set dfa transitions
if(a_set.empty()){
  dfa.set_transition(curState,-1,'a');
} else{
  // find clousure of all the states in set
  for(set<int>::iterator aits = a_set.begin();aits!=a_set.end();aits++){
     lol.clear();
     lol = nfa.epsilon_closure(*aits);
     for(set<int>::iterator ilol = lol.begin(); ilol!=lol.end();++ilol){
        a_epsilon.insert(*ilol);
     }
```

```
}
      //HERE ALSO CHECK WHETHER THE STATE IS ALREADY PRESENT OR
NOT THEN INSERT IN VECTOR MAPPING
      if(found_mapping.find(a_epsilon)==found_mapping.end()){
        found_mapping.insert(make_pair(a_epsilon,++stateCounter));
      }
      todo.push(a_epsilon);
      dfa.set_transition(curState,found_mapping[a_epsilon],'a');
    }
    //INSERT EPSILON CLOSURE FOR A_sET AND B_sET
    if(b_set.empty()){
      dfa.set_transition(curState,-1,'b');
    } else{
```

```
for(set<int>::iterator bits = b_set.begin();bits!=b_set.end();bits++){
         lol.clear();
         lol = nfa.epsilon_closure(*bits);
         for(set<int>::iterator ilols = lol.begin(); ilols!=lol.end();++ilols){
            b_epsilon.insert(*ilols);
         }
       }
       //HERE ALSO CHECK WHETHER THE STATE IS ALREADY PRESENT OR
NOT THEN INSERT IN VECTOR MAPPING
       if(found_mapping.find(b_epsilon)==found_mapping.end()){
         found_mapping.insert(make_pair(b_epsilon,++stateCounter));
       }
       todo.push(b_epsilon);
```

```
dfa.set_transition(curState,found_mapping[b_epsilon],'b');
     }
     //check for final state temps is current set, check whether final state of johnson
algo is there?
     if(temps.find(nfa.get_final_state())!=temps.end()){
        dfa.set_final_state(curState);
     }
  }
  int total_vertex = found_mapping.size();
  cout << total_vertex << "\n";</pre>
  int flag1=0;
  for(vector<struct trans>::iterator ajeeb =
dfa.transitions.begin();ajeeb!=dfa.transitions.end();ajeeb++){
```

```
if(ajeeb->vertex_to == -1){
     ajeeb->vertex_to=total_vertex;
     flag1=1;
  }
}
if(flag1==1){
  dfa.set_transition(total_vertex,total_vertex,'a');
  dfa.set_transition(total_vertex,total_vertex,'b');
}
if(flag1==1) dfa.set_vertex(total_vertex+1);
else dfa.set_vertex(total_vertex);
return dfa;
```

}

```
NFA concatenation(NFA a, NFA b) {
  NFA result;
  result.set_vertex(a.get_vertex_count() + b.get_vertex_count());
  unsigned int i;
  trans new_trans;
  for(i = 0; i < a.transitions.size(); i++) {</pre>
     new_trans = a.transitions.at(i);
     result.set_transition(new_trans.vertex_from, new_trans.vertex_to,
new_trans.trans_symbol);
  }
  result.set_transition(a.get_final_state(), a.get_vertex_count(), '^');
  for(i = 0; i < b.transitions.size(); i++) {</pre>
     new_trans = b.transitions.at(i);
```

```
result.set_transition(new_trans.vertex_from + a.get_vertex_count(),
new_trans.vertex_to + a.get_vertex_count(), new_trans.trans_symbol);
  }
  result.set_final_state(a.get_vertex_count() + b.get_vertex_count() - 1);
  return result;
}
NFA kleene_star(NFA a) {
  NFA result;
  unsigned int i;
  trans new_trans;
  result.set_vertex(a.get_vertex_count() + 2);
  result.set_transition(0, 1, '^');
  for(i = 0; i < a.transitions.size(); i++) {</pre>
```

```
new_trans = a.transitions.at(i);
     result.set_transition(new_trans.vertex_from + 1, new_trans.vertex_to + 1,
new_trans.trans_symbol);
  }
  result.set_transition(0, a.get_vertex_count() + 1, '^');
  result.set_transition(a.get_vertex_count(), a.get_vertex_count() + 1, '^');
  result.set_transition(a.get_vertex_count(), 1, '^');
  result.set_final_state(a.get_vertex_count() + 1);
  return result;
}
NFA or_function(NFA n1, NFA n2) {
  NFA result;
  int vertex_count = 2;
```

```
int i;
unsigned int j;
NFA med;
trans new_trans;
vertex_count += n1.get_vertex_count();
vertex_count += n2.get_vertex_count();
result.set_vertex(vertex_count);
int adder_track = 1;
for(i = 0; i < 2; i++) {
  result.set_transition(0, adder_track, '^');
  med = i==0?n1:n2;
  for(j = 0; j < med.transitions.size(); j++) {</pre>
     new_trans = med.transitions.at(j);
```

```
result.set_transition(new_trans.vertex_from + adder_track, new_trans.vertex_to
+ adder_track, new_trans.trans_symbol);
     }
     adder_track += med.get_vertex_count();
     result.set_transition(adder_track - 1, vertex_count - 1, '^');
  }
  result.set_final_state(vertex_count - 1);
  return result;
}
string infix_to_postfix(string re){
  stack<char> operators;
  stack<string> variables;
  int reg_l = re.length();
```

```
for(int i=0;i<reg_l;i++){</pre>
  string tem="";
  tem+=re[i];
  if(re[i]=='('){\{}
     operators.push(re[i]);
     variables.push(tem);
  }
  else if(re[i]==')'){
     while(!operators.empty() && operators.top()!='('){
        string t1 = variables.top();
        variables.pop();
        string t2 = variables.top();
        variables.pop();
```

```
char op = operators.top();
  operators.pop();
  variables.push(t2+t1+op);
}
string temp = variables.top();
variables.pop();
operators.pop();
if(!variables.empty() && variables.top()!="(") temp+='&';
while(!variables.empty() && variables.top()!="("){
  string temp2 = variables.top();
  variables.pop();
  if(variables.top()!="(") temp=temp2+'&'+temp;
  else temp=temp2+temp;
```

```
}
  variables.pop();
  variables.push(temp);
}
else if(re[i]=='*'){
  string temp = variables.top();
  variables.pop();
  temp+='*';
  variables.push(temp);
}
else if(re[i]=='|') operators.push(re[i]);
else{
  if(!operators.empty() && operators.top()!='(' && !variables.empty()){
```

```
string temp = variables.top();
       variables.pop();
       temp+=re[i];
       temp+=operators.top();
       operators.pop();
       variables.push(temp);
     }
     else variables.push(tem);
  }
}
if(!operators.empty()){
  while(!operators.empty()){
     string t1 = variables.top();
```

```
variables.pop();
     string t2 = variables.top();
     variables.pop();
     char op = operators.top();
     operators.pop();
     variables.push(t2+t1+op);
  }
}
re=variables.top();
variables.pop();
if(!variables.empty()) re+='&';
while(!variables.empty()){
  string temp2=variables.top();
```

```
variables.pop();
     if(!variables.empty()) re = temp2+'&'+re;
     else re = temp2 + re;
  }
  reg_l = re.length();
  cout << re << "\n";
  return re;
}
NFA re_to_nfa(string re) {
  stack<char> operators;
  stack<NFA> operands;
  char cur_sym;
  NFA *new_sym;
```

```
for(string::iterator it = re.begin(); it != re.end(); ++it) {
    cur_sym = *it;
     if(cur_sym != '(' && cur_sym != ')' && cur_sym != '*' && cur_sym != '|' &&
cur_sym != '.' && cur_sym != '&') {
       new_sym = new NFA();
       new_sym->set_vertex(2);
       new_sym->set_transition(0, 1, cur_sym);
       new_sym->set_final_state(1);
       operands.push(*new_sym);
       delete new_sym;
    } else {
       if(cur_sym == '*') {
          NFA star_sym = operands.top();
```

```
operands.pop();
  operands.push(kleene_star(star_sym));
} else if(cur_sym == '.' || cur_sym == '&') {
  NFA op1,op2;
  op2 = operands.top();
  operands.pop();
  op1 = operands.top();
  operands.pop();
  operands.push(concatenation(op1, op2));
} else if(cur_sym == '|') {
  vector<NFA> selections;
  NFA n2=operands.top();
  operands.pop();
```

```
NFA n1=operands.top();
          operands.pop();
          operands.push(or_function(n1,n2));
       }
     }
  }
  return operands.top();
}
//minimization using myhill nerode theorem
DFA dfa_minimize(DFA dfa){
  int states,i,j,iatrans,ibtrans,jatrans,jbtrans; // iatrans = $(i,a); ibtrans = $(i,b)
  states = dfa.get_vertex_count();
```

bool change = false; // to check whether is there any change in table if not then stop

there

```
bool isfalse; // to check whether table entry already checked or not
DFA m_dfa; // final minimized dfa
bool table[states][states];
for(i=0;i<states;i++){</pre>
  for(j=0;j<states;j++){</pre>
     table[i][j] = true;
  }
}
//first loop for ticking
for(i=0;i<states;i++){
  for(j=0;j<states;j++){
```

```
if(i \le j)
          continue; // only lower half table needed to be filled
                     // chceck whether one of i and j found in final state
        } else{
          if( ( (find(dfa.final_state.begin(),dfa.final_state.end(),i)!=dfa.final_state.end())
&& (find(dfa.final_state.begin(),dfa.final_state.end(),j)==dfa.final_state.end())) ||
             ((find(dfa.final_state.begin(),dfa.final_state.end(),j)!=dfa.final_state.end())
&& (find(dfa.final_state.begin(),dfa.final_state.end(),i)==dfa.final_state.end()))
          ){
             table[i][j] = false;
          }
        }
     }
  }
```

```
// loop until there is no change in table
  do{
     change = false;
     for(i=0;i<states;i++){</pre>
        for(j=0;j<states;j++){</pre>
           if(i<=j || table[i][j]==false){</pre>
              continue;
           }else{
              //iterate over all transitions and find i and j's transitions
              //if pair goes to such state on a or b which is having false in table
              for(vector<trans>::iterator its =
(dfa.transitions).begin();its!=dfa.transitions.end();its++){
                 if(its->vertex_from == i){
```

```
if(its->trans_symbol == 'a')
       iatrans = its->vertex_to;
     else if(its->trans_symbol == 'b')
       ibtrans = its->vertex_to;
  }else if(its->vertex_from == j){
     if(its->trans_symbol == 'a')
       jatrans = its->vertex_to;
     else if(its->trans_symbol == 'b')
       jbtrans = its->vertex_to;
  }
} // for pair i j found the a and b transitions
// FOR SOME STATE I IF THERE IS NO TRANSITION THEN WE ARE
```

SETTING THAT TRANSITION IN -1 STATE

```
check whether any trans lead to FALSE entry in table
             //
             if((iatrans!=-1 && jatrans!=-1) && iatrans!=jatrans){
               isfalse = iatrans > jatrans ? table[iatrans][jatrans]:table[jatrans][iatrans];
                if(!isfalse) {
                  change = true;
                  table[i][j] = false;
               }
               // if any one (i or j)is -1 and other is final state then set table enrty
             }else if((iatrans==-1 && jatrans!=-1 &&
(find(dfa.final_state.begin(),dfa.final_state.end(),jatrans)!=dfa.final_state.end()))||
                (jatrans==-1 && iatrans!=-1 &&
(find(dfa.final_state.begin(),dfa.final_state.end(),iatrans)!=dfa.final_state.end()))){
```

FALSE

```
table[i][j] = false;
             }
             if((ibtrans!=-1 && jbtrans!=-1) && ibtrans!=jbtrans){
                isfalse = ibtrans > jbtrans ? table[ibtrans][jbtrans]:table[jbtrans][ibtrans];
                if(!isfalse) {
                  change = true;
                  table[i][j] = false;
                }
             }else if((ibtrans==-1 && jbtrans!=-1 &&
(find(dfa.final_state.begin(),dfa.final_state.end(),jbtrans)!=dfa.final_state.end()))||
                (jbtrans==-1 && ibtrans!=-1 &&
(find(dfa.final_state.begin(),dfa.final_state.end(),ibtrans)!=dfa.final_state.end()))){
```

change = true;

```
change = true;
             table[i][j] = false;
           }
        } // end of i>j else
     } // end of j loop
  } // end of i loop
}while(change);
cout<<"FINAL MINIMIZED TABLE IS "<<endl;</pre>
for(i=0;i < states;i++)\{
  for(j=0;j<states;j++){
     if(i<=j)cout<<"- ";
     else cout<<table[i][j]<<" ";
  }
```

```
cout<<endl;
}
//make sets and maps them to new states
bool checked[states];
map<set<int>,int>final_mapping; // merged set will be mapped to new given states
int curCount=0; // counter for new merged set to map a new state
set<int>aisehi,temps;
map<set<int>,int>::iterator to_erase;
set<int>::iterator sit;
for(i=0;i<states;i++) checked[i] = false; // to check all states are checked or not
for(i=0;i<states;i++){</pre>
  if(checked[i]==false){
     aisehi.clear();
```

```
aisehi.insert(i);
  }
  for(j=i+1;j<states;j++){</pre>
     if(table[j][i]==1 && checked[i]==false){
        aisehi.insert(j);
        checked[j] = true;
     }
  }
  if(checked[i]==false)final_mapping[aisehi] = curCount++;
  checked[i] = true;
m_dfa.set_vertex(curCount);
set<int>::iterator ist;
```

}

```
int atra, btra;
  for(map<set<int>,int>::iterator ift = final_mapping.begin(); ift!=final_mapping.end();
ift++){}
     // set final states
     for(ist = ift->first.begin(); ist!=ift->first.end();ist++){
        if(find(dfa.final_state.begin(),dfa.final_state.end(),*ist)!=dfa.final_state.end()){
           m_dfa.set_final_state(ift->second);
           break; //necessary otherwise multiple copy in final state vector
        }
     }
     // now set transitions
     ist = (ift->first).begin();
     //iterate over dfa.transitions and find the a and b transition state
```

```
for(vector<trans>::iterator itr = dfa.transitions.begin(); itr!=dfa.transitions.end();
itr++){
        if(itr->vertex_from == *ist && itr->trans_symbol == 'a'){
          atra = itr->vertex_to;
        }
        if(itr->vertex_from == *ist && itr->trans_symbol == 'b'){
          btra = itr->vertex_to;
        }
     }
     if(atra==-1){
        m_dfa.set_transition(ift->second,-1,'a');
     }
     if(btra==-1){
```

```
m_dfa.set_transition(ift->second,-1,'b');
     }
     // now check in which set atra and btra are and accordingly set the transition of
final dfa
     for(map<set<int>,int>::iterator ifft =
final_mapping.begin();ifft!=final_mapping.end();ifft++){
        for(set<int>::iterator isst = ifft->first.begin();isst!=ifft->first.end();isst++){
          if(atra!=-1 && *isst == atra ){
             m_dfa.set_transition(ift->second,ifft->second,'a');
          }
          if(btra!=-1 && *isst == btra){
             m_dfa.set_transition(ift->second,ifft->second,'b');
          }
```

```
}
     }
  }
  m_dfa.display();
  return m_dfa;
}
bool simulate(DFA dfa, string s){
  unsigned int i;
  int curstate=0;
  if(s!="^"){
     for(i=0;i<s.length();i++){}
        for(vector<trans>::iterator its =
dfa.transitions.begin();its!=dfa.transitions.end();its++){
```

```
if(its->vertex_from == curstate && its->trans_symbol == s[i] && its->vertex_to
== -1)return false;
          else if(its->vertex_from == curstate && its->trans_symbol == s[i]){
             curstate = its->vertex_to;
             break;
          }
     }
  }
  // now check cur state if final or not
  for(vector<int>::iterator it = dfa.final_state.begin(); it!=dfa.final_state.end();it++){
     if(*it == curstate)return true;
  }
```

```
return false;
}
int main() {
  string re;
  cout<<"\n\nEnter the regular expression - \n\n";
  cin>>re;
  cout<<"-----The postfix expression for the regex : -----"<<endl;
  re = infix_to_postfix(re);
  cout<<"-----The required NFA has the transitions: -----"<<endl;
  NFA required_nfa;
  required_nfa = re_to_nfa(re);
  required_nfa.display();
  string to_simulate;
```

```
cout<<"-----"<<endl;
cout<<"now nfa->dfa will be shown"<<endl;
DFA required_dfa = nfa_to_dfa(required_nfa);
required_dfa.display();
cout<<"-----"<<endl;
cout<<"here goes minimization table for required dfa"<<endl;
DFA tempdfa = dfa_minimize(required_dfa);
cout<<"enter the strings to simulate and press q to quit"<<endl;
cin>>to_simulate;
while(to_simulate!="q"){
  bool flag = false;
  if(to_simulate!="^")
    for(unsigned int I = 0; I<to_simulate.length();I++)</pre>
```

```
if(to_simulate[l]!='a' && to_simulate[l]!='b'){
             flag=true;
             break;
          }
     if(flag){
        cout << "rejected\n";</pre>
        cin>> to_simulate;
        continue;
     }
     simulate(tempdfa,to_simulate) == true ? cout<<"accepted"<<endl :</pre>
cout<<"rejected"<<endl;
     cin>>to_simulate;
  }
```

```
cout<<"-----"<<endl;
return 0;
```