## Notes

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# Contents

Inti	oduction	2
1.1	Motivation	2
1.2		3
		3
	1.2.2 Local Phylodynamics	3
Me	thods	5
2.1	Coalescent Preliminaries	5
2.2	Inhomogenous Coalescent	6
		6
2.3	Coalescent with Local Population Structure	6
Res	ults	7
3.1	Implementation Notes	7
3.2		7
		7
		7
3.3		7
		7
	3.3.2 MCMC inference	7
Dis	cussion	8
Bib	liography	9
	1.1 1.2  Met 2.1 2.2 2.3  Res 3.1 3.2	1.2 Existing Work  1.2.1 Phylodynamic Methods 1.2.2 Local Phylodynamics   Methods  2.1 Coalescent Preliminaries 2.2 Inhomogenous Coalescent 2.2.1 Exponential Growth 2.3 Coalescent with Local Population Structure  Results  3.1 Implementation Notes 3.2 Exponential Growth 3.2.1 Phylogeny Simulation 3.2.2 MCMC inference 3.3 Coalescent with Local Population Structure  3.3.1 Phylogeny Simulation Structure 3.3.1 Phylogeny Simulation

### Introduction

#### 1.1 Motivation

In epidemiology, it is often desired to be able to reconstruct the history of a pathogen population and it's structure. The problem of reconstructing the history of a pathogen population can be tackles using phylodynamics. Phylodynamics utilises genomic data to assemble phylogenies, which are then used to infer the population size history. This is possible by viewing a phylogeny as a realisation of a coalescent process, wit appropriately rescaled time. This claim can be justified by viewing the coalescent as a Moran model, run backwards in time with the time rate equal to the population size [1].

Within this report we will first introduce the coalescent process for phylodynamic inference, review it's inhomogenous generalisation, and finally introduce the main result of this work, a new model capable of doing local phylodynamic inference, i.e. on a subset of the whole population capable of detecting and modelling clonal expansions.

Clonal expansions are a process in which a particular subsest of a given bacterial strain undergoes explosive population growth that can be traced back to a particular individual [2]. The presence of clonal expansions in bacterial populations have been of long-standing interest and is implicated in epidemic processes, were an outbreak can be traced to a single ancestor [2, 3, 4, 5]. This often happens when a particular strain or individual obtains a variant of a particular gene that confers evolutionary advantange, for example, antibiotic resistance [6, 7, 5].

The presence of clonal expansions leaves an imprint in the overall population structure of a given bacterial strain, the particular topology associated with this often being referred to as star-like [2, 3]. The problem of detecting hidden population structure corresponding to clonal expansions has become a problem of interest in epidemiology and outbreak surveillance [8].

While methods to detect inhomogeneities in the population structure and size have been of interest since the early days of genetic sequencing [2, 3], the in-

terest in the problem increased with whole genome sequencing becoming more accessible and affordable [6, 9, 10].

Despite the problems of inferring population size from a genealogy and detecting heterogeneities in the population size of the entire population being intrinsically tied, all but one method [8], to our knowledge, rely either on manual detection or indirect detection. We aim to propose a simulation for the formation of clonal expansions in genealogy using the structured coalescent process, and devise a fully bayesian method for joint estimation and detection of relative population size and clonal expansions.

#### 1.2 Existing Work

#### 1.2.1 Phylodynamic Methods

Kingman's Coalescent is a continuous time markov chain stochastic process, defined on the statespace 1, 2, 3, ..., K which can be interpreted as a set of j particles, where each pair of particles independently coalesces at a constant rate. This gives transition rates:

$$g(j, j-1) = \binom{j}{2} \lambda \quad \lambda \in \mathbb{R}^+$$
 (1.1)

[11]

By taking a backwards in time approximation of the Wright-Fisher model, the coalescent process can be modified to model evolution of genealogies, i.e. how do the ancestors of a set of individuals relate to each other backwards in time. Denote the relative population size at time t by  $\alpha(t)$ . Under such modification the transition rates become:

$$g(j, j-1) = \binom{j}{2} \cdot \frac{1}{\alpha(t)} \tag{1.2}$$

[1]

One way to interpret this is as a rescaling of time inversely proportional to the population size under Wright-Fisher model [12].

As the transition rates depend on the relative population size, it is possible to utilise this model for the inverse problem of determining the history of the size of a population, based on genealogies reconstructed from genomic samples. Such methods are often referred to as SkyGrid methods, have been first introduced in [13] and [14].

The framework has then been extended to allow for piecewise continuous population size functions, referred to as SkyGrid [15] and to include covariates [16].

#### 1.2.2 Local Phylodynamics

Whereas phylodynamics considers the size history of an entire population, the idea behind local phylodynamics is to consider the histories of selected subsets

of related individuals, where each subset can be traced to a single ancestor. This can for example be practical when trying to detect hidden outbreaks, or clonal expansions due to a particular strain of a bacteria gaining a fitness advantage. This idea has been investigated in [8], where a null hypothesis based testing framework is developed to identify subsets of individuals that seem to have a significantly different opulation history than the the rest of the phylogeny. Recently, a birth-death type model that allows for heterogenous growth rate parameters has been introduced in [17].

### Methods

#### 2.1 Coalescent Preliminaries

The coalescemt process can be characterised as a time-inhomogenous pure-death markov process. We now conduct a brief analysis of the process and re-derive some properties.

The waiting times can be derived as follows. For an inhomogenous CTMC, let  $E_j(t)$  be the total exit rate from state j at time t. By the markov property individual exit events from a given state only depend on the state and given time, i.e. they form a time-inhomogenous poisson process. As such the probability of no events in an interval [t, t+s]  $s \in \mathbb{R}^+$  is

$$\exp\left(-\int_{t}^{t+s} E_{j}(\tau)d\tau\right) = \exp\left(-\int_{0}^{s} E_{j}(t+\tau)d\tau\right)$$
 (2.1)

The waiting times are defined as

$$W_j(t) = \inf\{s : X(t+s) \neq j \mid X(t) = j\}$$
 (2.2)

As such

$$W_i(t) > s \Rightarrow \forall \tau \in [t, t+s] \quad X(\tau) = j$$
 (2.3)

Furthermore the above relation holds iff no exit event have occured in the time interval [t, t + s]. As such:

$$P[W_j(t) > s] = P[\text{no exit events in } [t, t+s]] = \exp\left(-\int_0^s E_j(t+\tau)d\tau\right)$$
$$P[W_j(t) < s] = 1 - \exp\left(-\int_0^s E_j(t+\tau)d\tau\right)$$

In the case of phylodynamic coalescent this becomes

$$P[W_j(t) \le s] = 1 - \exp\left(-\int_0^s \frac{\binom{j}{2}}{\alpha(t+\tau)} d\tau\right)$$
 (2.4)

- 2.2 Inhomogenous Coalescent
- 2.2.1 Exponential Growth
- 2.3 Coalescent with Local Population Structure

## Results

- 3.1 Implementation Notes
- 3.2 Exponential Growth
- 3.2.1 Phylogeny Simulation
- 3.2.2 MCMC inference
- 3.3 Coalescent with Local Population Structure
- 3.3.1 Phylogeny Simulation
- 3.3.2 MCMC inference

Discussion

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