

```
import matplotlib.pyplot as plt
import numpy as np

def gradient_descent(f, learning_rate, initial_point):
    x_coordinate=[initial_point] #This list stores x_n's
    y_coordinate=[f(initial_point)] #This list stores y_n's

    def deriv(x):#using derivative to help with gradient descent
        return(f(x+0.0001)-f(x))/0.0001
    i=1 #setting index to 1
    while abs(deriv(x_coordinate[i-1]))>0.0001: #use a while loop to determine gradient descent for each function, loop will run until its 0.0001 away from minima
        xi=x_coordinate[i-1]-learning_rate*deriv(x_coordinate[i-1]) #initializing xi

        x_coordinate.append(xi) #creating list of x coordinates
        y_coordinate.append(f(x_coordinate[i])) #creating list of y coordinates
        i=i+1 #increment i

    plot_range = np.linspace(min(x_coordinate)-0.5,max(x_coordinate)+0.5,10000) #nice plot range
    function_range=[f(i) for i in plot_range]
    plt.plot(plot_range,function_range, label='F(x)')#plots function
    plt.plot(x_coordinate, y_coordinate, marker='o', color='y', label='Gradient Descent') #plots sequence of points x_n, f(x_n)
    plt.xlabel('x')
    plt.ylabel('f(x)')
    plt.title ('Gradient Descent')
    plt.legend()
    plt.show()
    return round(x_coordinate[-1],3), round(y_coordinate[-1],3) #returns last x_n and y_n, rounded to 3 decimals

#3d
def func_1(x):
    return x**2
```

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zygy.ca/jupyter/user/dhillj46/lab/tree/Untitled10.ipynb

All Tabs Settings Help

Discrete Time Dynamical S: X Untitled10.ipynb

#3d
def func_1(x):
 return x**2

gradient_descent(func_1, 0.9, 1)

Gradient Descent

F(x)
Gradient Descent

2.0
1.5
1.0
0.5
0.0

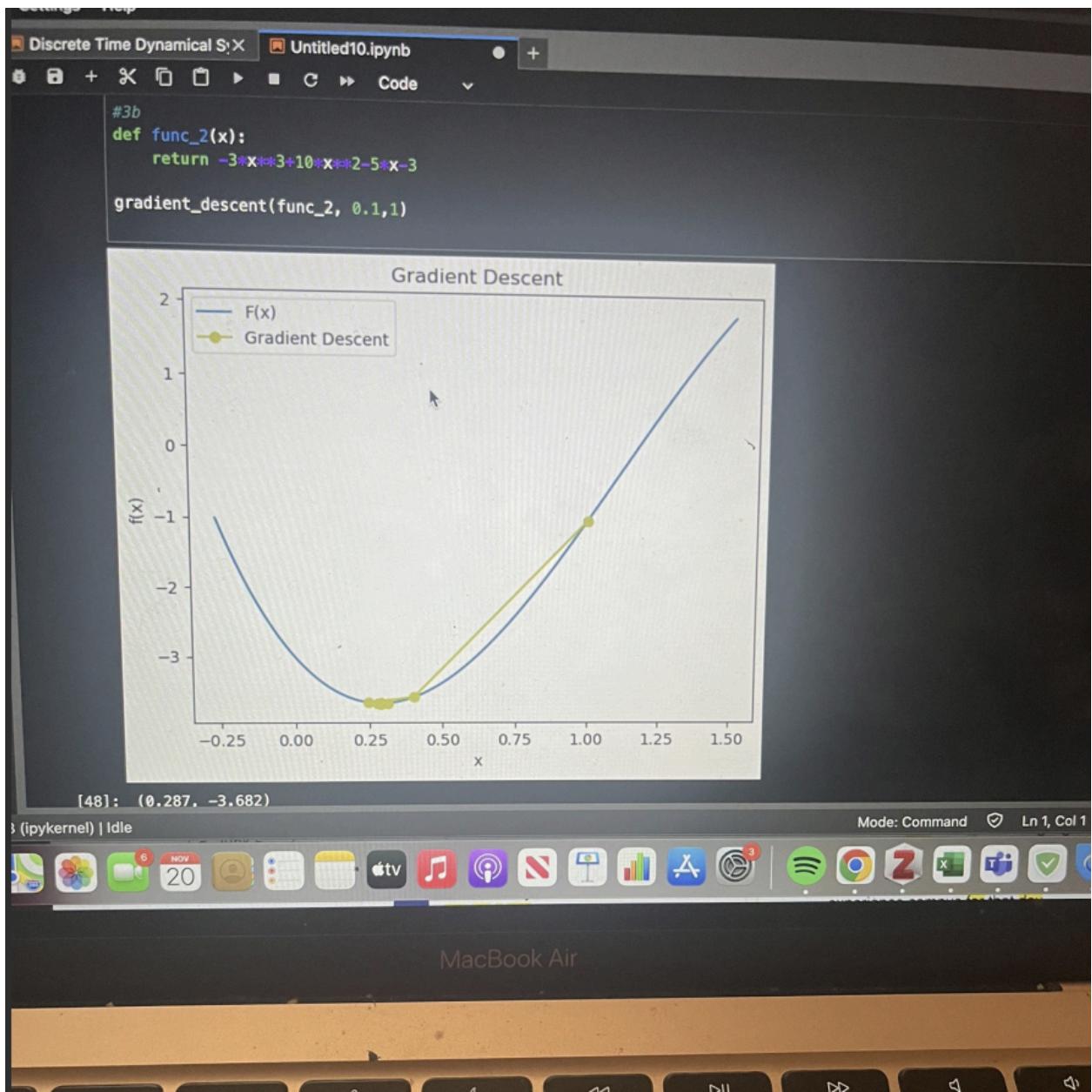
-1.0 -0.5 0.0 0.5 1.0 1.5

[38]: (-0.0, 0.0)

Python 3 (ipykernel) | Idle Mode: Edit Ln 30, Col 4 Untitled10.ipynb

The screenshot shows a Jupyter Notebook interface running on a MacBook Air. The code cell contains a Python function `func_1` that returns x^2 , and a call to the `gradient_descent` function with parameters `func_1`, `0.9`, and `1`. Below the code is a plot titled "Gradient Descent" showing a blue parabola labeled $F(x)$ and a yellow line with dots representing the gradient descent path. The x-axis ranges from -1.0 to 1.5, and the y-axis ranges from 0.0 to 2.0. The path starts at approximately (0.9, 1.0) and moves towards the minimum at (0, 0). The status bar at the bottom indicates "Mode: Edit" and "Ln 30, Col 4 Untitled10.ipynb".





Settings Help

Discrete Time Dynamical Syst... Untitled10.ipynb

Code

```
plt.xlabel('x')
plt.ylabel('f(x)')
plt.title ('Gradient Descent')
plt.legend()
plt.show()
return round(x_coordinate[-1],3), round(y_coordinate[-1],3) #returns last x_n and y_n, rounded to 3 decimal places
```

#3c

```
def func_3(x):
    if x>0:
        return x**x
    elif x==0:
        return 1
    else:
        return abs(x)**abs(x)

gradient_descent(func_3, 0.875,1)
```

#3c

Gradient Descent

pykernel | Idle

Mode: Edit

MacBook Air

F10

F9

F8

F7

F6

F5

F4

F3

0

1

2

3

4

5

6

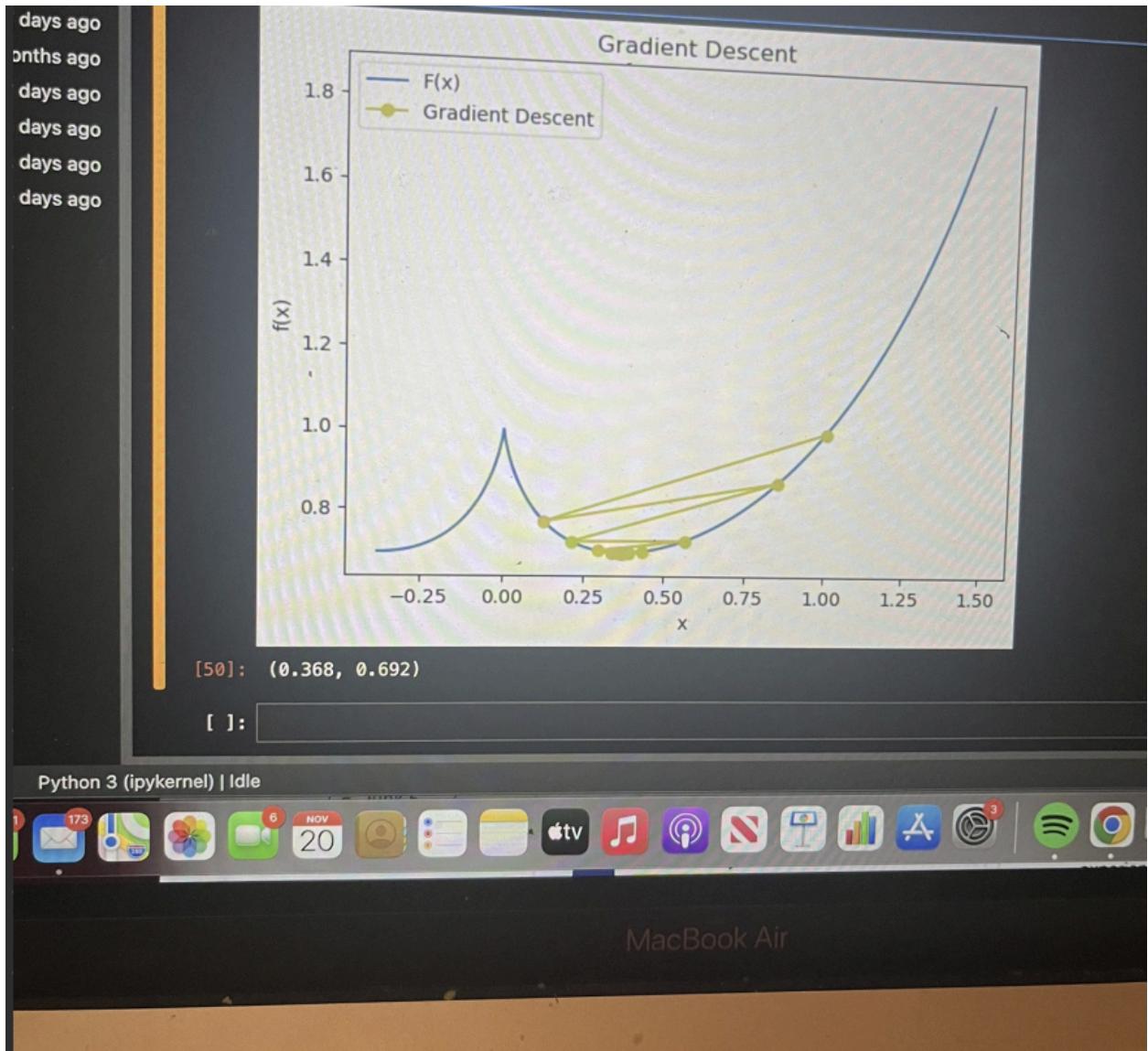
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Discrete Time Dynamical S:X Untitled10.ipynb

```
plt.xlabel('x')
plt.ylabel('f(x)')
plt.title ('Gradient Descent')
plt.legend()
plt.show()
return round(x_coordinate[-1],3), round(y_coordinate[-1],3) #returns last x_n and y_n, rounded to 3 decimals

#3d
def func_4(x):
    return abs(x)

gradient_descent(func_4, 0.1,1)

#When running this cell, there is no output no matter what the learning rate or initial point is.
#This is because the slope of what looks like a minimum is undefined,making the code not work.
```

[]: