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1. Cards = 52
Diamond = 13
Heart = 13
Spade = 13

Required Probability = $\frac{13C_1 \times 13C_1 \times 13C_1}{52C_3}$

$$= \frac{13 \times 13 \times 13}{52 \times 51 \times 50} = \frac{2197}{182600} = 0.0165$$

2. Action movies = 42% $\rightarrow P(A)$
Comedy movies = 54% $\rightarrow P(B)$
Drama movies = 36% $\rightarrow P(C)$
Horror movies = 12% $\rightarrow P(D)$

a) Either action or drama

$$P(A \cup C) = P(A) + P(C) - P(A \cap C)$$

$$= 42 + 36 - 0$$

$$P(A \cup C) = 78/100$$

b) Either comedy or horror

$$P(B \cup D) = P(B) + P(D) - P(B \cap D)$$

$$= 54 + 12 - 0$$

$$P(B \cup D) = 66/100$$

3. Bag A Bag B

Red - 3 white - 4

Black - 5 black - 7

$$P(A) = \frac{1}{2}, \quad P(B) = \frac{1}{2}$$

$$P\left(\frac{\text{Black}}{A}\right) = \frac{5}{8}, \quad P\left(\frac{\text{Black}}{B}\right) = \frac{7}{11}$$

$$P\left(\frac{B}{\text{Black}}\right) = \frac{P(B) \times P\left(\frac{\text{Black}}{B}\right)}{P(A) \times P\left(\frac{\text{Black}}{A}\right) + P(B) \times P\left(\frac{\text{Black}}{B}\right)}$$
$$= \frac{\frac{1}{2} \times \frac{7}{11}}{\left(\frac{1}{2} \times \frac{5}{8}\right) + \left(\frac{1}{2} \times \frac{7}{11}\right)}$$

$$= \frac{\frac{7}{22}}{\frac{5}{16} + \frac{7}{22}} = \frac{\frac{7}{22}}{\frac{110 + 112}{352}} = \frac{\frac{7}{22}}{\frac{222}{352}}$$

$$P\left(\frac{B}{\text{Black}}\right) = 0.5045$$

6. $z = \frac{x - \mu}{\sigma}$

$$0.675 = \frac{x - 350870}{12405}$$

$$x = 350870 + (0.675 \times 12405)$$

$$x = 359237.045$$

$$75^{\text{th}} \text{ Percentile} = 359237.045$$

(4) a)

450 applications in 1 hour

$$\lambda = \frac{450}{60}$$

$$\lambda = 15/2,$$

$$x = 10$$

$$P(X=7) = \frac{e^{-15/2} \cdot (15/2)^{10}}{10!}$$
$$= 0.0858$$

b)

$$P(X=x) = \frac{e^{-15/2} \cdot (15/2)^{17}}{17!}$$

$$= 0.6824.$$