

Let, degree of  $p^x(\cdot), p^y(\cdot) < s$  where  $p^x(\cdot)$  and  $p^y(\cdot)$  are encodings of  $x$  and  $y$  respectively, where  $x = (x_1, \dots, x_l)$  and  $y = (y_1, \dots, y_l)$ .

Let,  $S = \{\eta_1, \dots, \eta_{2s}\}$ . Consider  $3l < s$  and  $t < \frac{N}{3}$ .  $S_1, \dots, S_N$  is a partition of  $S$ .

For the privacy,  $t \cdot |S_i| < s - l$ , to choose a partition such that  $S_i$  such that  $|S_i| < \frac{2s}{N}$ .

Let  $P_i$  is the  $i^{th}$  prover contains a share of  $p^x(\cdot)$  and  $p^y(\cdot)$ , say  $p^{x_i}(\cdot)$  and  $p^{y_i}(\cdot)$ . The provers do the following protocol to get the share of the polynomial  $p^{xy}(\cdot) = p^x(\cdot) \cdot p^y(\cdot)$ :

- $P_i$  evaluates  $p^{x_i}(\eta)$  and  $p^{y_i}(\eta)$  and sends this to  $P_j$  if  $\eta \in S_j$
- $P_j$  computes  $\sum_{i \in [N]} p^{x_i}(\eta) = p^x(\eta)$  and  $\sum_{i \in [N]} p^{y_i}(\eta) = p^y(\eta) \forall \eta \in S_j$
- $P_j$  computes  $p^x(\eta) \cdot p^y(\eta) = p^{xy}(\eta) \forall \eta \in S_j$
- $P_j$  construct shares  $p^{xy}(\eta)_1, \dots, p^{xy}(\eta)_N$  such that  $p^{xy}(\eta) = \sum_{i \in [N]} p^{xy}(\eta)_i$  and sends  $p^{xy}(\eta)_i$  to  $P_i$ .

**Privacy:** If  $t$  corrupted provers come together they can get the evaluation of  $p^{x_i}$  on  $t \times \frac{2s}{N} < \frac{N}{3} \times \frac{2s}{N} = \frac{2s}{3} < \frac{3s-3l}{3} = s - l$