# What the hell are math nerds talking about?

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Oftentimes, it is rough trying understand what the nerds are talking about	

Functional Programmers are often seen as nuts

## Purpose for this presentation

Distill some of the more difficult terms in functional programming, show it in Haskell and on as many possible languages of the JVM

## Part 1 of this presentation

- Higher order functions
- Type classes
- Ad-hoc Polymorphism,
- Types vs. kinds
- Functors

#### All Hail from Haskell!

#### Haskell

- "Pure" Functional Language
- Simon Peyton Jones, Lennart Augustsson, Eric Meijer, Philip Wadler
- Designed in 1990
- static, strong, and inferred
- Cross Platform
- Compiled & Interpreted

Shall we start with Hello World? Hell No!

#### Haskell Basic Types

- Int Bounded Integer
- Integer Unbounded Integer
- Float Floating Point
- Double Double Precision
- Bool Boolean
- Char Character (String are list of chars)
- Tuples Types surrounded by parenthesis

#### Basic Method in Haskell

```
isOdd :: Int -> Int
isOdd x = (x `mod` 2) /= 0
```

#### What is **mod** with the backticks?

First off, here is the signature. What the hell is a?

```
mod :: Integral a => a -> a
```

Take 2, and Returns 1

## Look at mod a different way

(mod 5 2)

This would work and return 1

Since it is a Take 2 and Return 1...

5 `mod` 2

#### Another Function!

Specifying the types before the method

## Combine with the implementation of sumThree

```
sumThree :: Int -> Int -> Int
sumThree x y z = x + y + z
```

To actually run sumThree

```
sumThree 1 2 3
```

Note: x, y, z is pattern matched

## Currying

Another way to look at sumThree is through currying...

```
sumThree :: Int -> Int -> Int
sumThree x y z = x + y + z
```

I can partially apply sumThree

```
let f = sumThree 2 1
```

```
f(4) -- 7
```

## Type Variables

```
myHead :: [a] -> a
myHead [] = error "empty list"
myHead [x] = x
myHead (x:xs) = x
```

This is analogous to in Java:

```
public A <A> myHead(List<A> list) {...}
```

# Filtering with Haskell lambdas

```
filter (\x -> x \ \mbox{mod} \ 2 /= 0) [1,2,3,4]
```

Becomes:

[1,3]

## Filtering with predefined functions

Remember this?

```
isOdd :: Int -> Int
isOdd x = (x `mod` 2) /= 0
```

We can apply it to as a function, since *it is* a function!

```
filter f [1,2,3,4]
```

Evaluates to...

```
[1,3]
```

# Mapping with Haskell Lambdas

```
map (\x -> x * 3) [1,2,3,4]
```

Becomes:

[3,6,9,12]

# Mapping with Haskell Postfix Lambdas

map (3\*) [1,2,3,4]

Becomes:

[3,6,9,12]

## Map is an interesting signature

```
map :: [a] -> (a -> b) -> [b]
```

This is a **higher order function!** 

Note: b can represent another type

## Looking at map again...

```
map (3*) [1,2,3,4]
```

Since b can be another type, therefore we can do...

```
map (\i -> "Hello " ++ show i) [1,2,3,4]
```

Evaluates to...

```
["Hello 1", "Hello 2", "Hello 3", "Hello 4"]
```

FYI: Show converts anything to String when it can.

#### Trying another higher order function

```
myZipWith :: (a -> b -> c) -> [a] -> [b] -> [c]
myZipWith _ [] _ = []
myZipWith _ _ [] = []
myZipWith f (x:xs) (y:ys) = f x y : myZipWith f xs ys
```

#### Simple Case:

```
myZipWith (+) [1,2,3] [4,5,6]
```

**Evaluates To:** 

```
[5, 7, 9]
```

Higher Difficulty Case:

```
let a = [1,2,3,4,5,6]
let b = ["Rock", "Jazz", "Country", "Salsa", "Polka", "Hip Hop"]
putStrLn (show $ myZipWith (\i s -> s ++ " " ++ show i) a b)
```

#### What does using a higher function look like in Java?

Not really a higher order function but close a function into a method...

```
static <A,B,C> Stream<C> zip(Stream<? extends A> a, Stream<? extends B> b, BiFunction<? super A,? super B,?
extends C> zipper)
```

How do we use it?

```
let a = Arrays.asList(1,2,3,4,5,6);
let b = Arrays.asList("Rock", "Jazz", "Country", "Salsa", "Polka", "Hip Hop");
Streams.zip(a.stream(), b.stream(), (x, y) -> y + " " + x).collect(Collectors.toList())
```

Note: Using it wasn't bad, but if you had to create your own zip, rough

#### Higher Order Functions in Scala

```
val a = List(1,2,3,4,5,6)
val b = List("Rock", "Jazz", "Country", "Salsa", "Polka", "Hip Hop")
a.zip(b).map{case (i,s) => s + " " + i}
```

## Higher Order Functions in Groovy

```
def a = [1,2,3,4,5,6]
def b = ["Rock","Jazz","Country","Salsa","Polka","Hip Hop"]
[a,b].transpose().collect{x -> x[1] + " " + x[0]}
```

## Higher Order Functions in Clojure

```
(def a [1,2,3,4,5,6])
(def b ["Rock" "Jazz" "Country" "Salsa" "Polka" "Hip Hop"])
(map #(str %1 " " %2) a b)
```

# Type Classes

Imagine...

#### That we can do this in Java

```
interface Eq <A> {
   public boolean equals (A a, A b);
   default public boolean notEquals (A a, A b) {
     return !equals(a,b)
   }
}
```

#### Lets Make an Instance for Eq and say for type Cow

```
package com.example.cowtypeclasses

public class CowEquivalenceByName implements Eq<Cow> {
    public boolean equals (Cow a, Cow b) {
        a.getName().equals(b.getName());
    }
}
```

#### Now lets say we can "bind" this in scope

In other words...

- By implementing an interface, we make this object available for anything that needs to use it.
- We have the power to import this CowEquivalence when ever we need to strategically use it.
- We can choose another implementation of Cow if we have another equivalence strategy
- Think of a Strategy Pattern that instead of setters we use imports!

#### Other ways to look at it

If we have the ability to create both classes in the same package (Java doesn't do this I know)

```
package com.example.cowtypeclasses
public class CowEquivalenceByName {...}
public class CowEquivalenceByWeight {...}
```

In some random method in some other package...I can do

```
public void foo(Cow a, Cow b) {
  import com.example.cowtypeclasses.CowEquivalenceByWeight
  a.equals(b); //true if equal weight!
}
```

That's a type class!

#### Coming back to Haskell

#### First off:

- There are no objects in Haskell. Get That?
- This is a functional language!
- Damn it! Listen to me I'm serious!

What Haskell has are "Algebraic Data Types"!

data GameResult = Win | Loss | Tie

## What does the **Eq** type class look like?

This is already built into Haskell

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
  x == y = not (x /= y)
  x /= y = not (x == y)
```

Warning: class is not a Java class. It is a type class!

#### Now we will make an **instance** of the type class:

```
instance Eq GameResult where
    Win == Win = True
    Loss == Loss = True
    Tie == Tie = True
    _ == _ = False
```

Warning: By instance we don't mean an object we mean "an implementation" of the type class

# Using the type class

```
(Win == Win) -- True
(Loss == Win) -- False
```

### Type Classes in Scala

```
trait Eq[a] {
  def eq(a1: a)(a2: a): Boolean
}
```

```
sealed abstract class GameResult
final case object Win extends GameResult
final case object Loss extends GameResult
final case object Tie extends GameResult
```

```
implicit class GameResult extends Eq[GameResult] {
   def eq(a1:GameResult, a2:GameResult) = (a1, a2) match {
      case (Win, Win) => true
      case (Loss, Loss) => true
      case (Tie, Tie) => true
      case _ => false
   }
}
```

```
def newIsEquals(x:GameResult, y:GameResult)(implicit val eq:Eq[GameResult]) = {
   eq(x)(y)
}
```

### Type classes in Clojure

```
(defprotocol Eq
   (equal-to [x y])
   (not-equal-to [x y])
)

(extend-type clojure.lang.Keyword
   Eq
   (equal-to [x y] (= x y))
   (not-equal-to [x y] (not= x y))
)

(println (equal-to :Win :Win))
(println (equal-to :Loss :Loss))
(println (equal-to :Tie :Tie))
(println (equal-to :Win :Loss))
```

### Ad Hoc Polymorphism

- Something badass you can tell your boss to get a raise
- It actually has to do with the ability of types
- Also known as "overloading"
- Definition that we can use the Eq type class for various types!

### More about Ad Hoc Polymorphism

```
(1 == 4)
```

This works because there is an instance of Eq Int

```
("Hello" == "Hello")
```

This works because there is an instance of Eq String

```
(Win == Win)
```

This works because we said so and is an instance of Eq GateResult

# Extending Type Classes

```
class (Eq a) => Ord a where

(<), (<=), (>=), (>) :: a -> a -> Bool

max, min :: a -> a -> a
```

# Kinds Vs. Types

# Types

• Type are what are classes in Java

```
Prelude> :t 4
4 :: Num a => a
```

```
Prelude> :t "What is love? Baby don't hurt me"
"What is love? Baby don't hurt me" :: [Char]
```

#### Kinds

Kinds are a description of the type

```
Prelude> :k Int
Int :: *
```

"In order to create a type Int, how many extra things do we need?"

### Introduction to the Maybe Type

Algebraic Data Type of Maybe

```
data Maybe a = Nothing | Just a
Prelude> Just 3
Just 3

Prelude> Just "Blueberry Pancakes"
Just "Blueberry Pancakes"

Prelude> Nothing
Nothing
Prelude> Just 10 :: Maybe Double
Just 10.0
```

# The Type of Maybe

```
Prelude> :t Just "Blueberry Pancakes"
Just "Blueberry Pancakes" :: Maybe [Char]
```

```
Prelude> :t Just 90
Just 90 :: Num a => Maybe a
```

# The Kind of Maybe

First off, remember this signature...

```
data Maybe a = Nothing | Just a

Prelude> :k Maybe
Maybe :: * -> *

Prelude> :k Maybe Int
Maybe Int :: *
```

## The Either type

```
data Either a b = Left a | Right b
```

```
Prelude> Left 10
Left 10
Prelude> :t Left 10
Left 10 :: Num a => Either a b
```

What do you think the unsatisfied kind is of Either?

#### The Kind of Either

```
Prelude> :k Either
Either :: * -> * -> *

Prelude> :k Either Int
Either Int :: * -> *

:k Either Int [Char]
Either Int [Char] :: *
```

### The List Type

```
Prelude> :t []
[] :: [a]
```

```
Prelude> :t [1,2,3,4]
[1,2,3,4] :: Num t => [t]
```

What is the kind of []?

# Kind of []

```
Prelude> :k []
[] :: * -> *

Prelude> :k [Int]
[Int] :: *
```

## Functor Type Class

This is where things get "kind" of hard

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

f has a requirement, what kind does f have to be?

# Discovering Kinds in Functor

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

f a means whatever f is it requires an a f b also means whatever f is, it requires a b

Because f requires one thing \*, therefore we know that f is \* -> \*

Quick! It's up to us now to find a kind of \* -> \*!

## Plugging in a kind of Maybe

Reminder #1:

```
data Maybe a = Nothing | Just a
```

Reminder #2:

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

Reminder #3:

```
Prelude> :k Maybe
Maybe :: * -> *
```

Well that's what we need a kind of \* → \*!

```
instance Functor Maybe where
  fmap f (Just x) = Just (f x)
  fmap f Nothing = Nothing
```

# Using a Maybe Functor

```
fmap (\x -> x * 14) (Just 19)
```

Results in:

Just 266

I could've written it like this...

fmap (14\*) (Just 19)

Now, trying with Nothing

fmap (22+) Nothing

Results in:

Nothing

It's about find the right types and the right kinds

#### List Functor

Reminder of the kind of []

```
Prelude> :k []
[] :: * -> *
```

It works! Therefore to make it a Functor:

```
instance Functor [] where
fmap f xs = map f xs
```

or

```
instance Functor[] where
fmap = map
```

Therefore fmap and map should work the same

```
Prelude> fmap (12*) [1,2,3,4,5] [12,24,36,48,60] Prelude> map (12*) [1,2,3,4,5] [12,24,36,48,60]
```

#### Either Functor

Reminder of the Algebraic Data Type

```
data Either a b = Left a | Right b
```

The problem with Either is that it's kind is..

```
Prelude> :k Either
Either :: * -> * -> *
```

and it is not \* -> \* like we need it to be, therefore we need satisfy one half of the kind pattern.

```
instance Functor (Either a) where
  fmap f (Right x) = Right (f x)
  fmap f (Left x) = Left x
```

Reminder:

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

# Using the Either Functor

```
Prelude> fmap ("Nice " ++) (Right "Code")
Right "Nice Code"
Prelude> fmap (20*) (Left 30)
Left 30
```

### Intermission

# Part 2 of this presentation

- Some More Functors
- Applicatives
- Monoids
- Monads

### What do Functors look like in Java?

### Imagine...

### ...if we had the ability to do this in Java

```
public F<B> <A, B, F extends Functor> fmap(x:A, f:F<A>) {
   ....
}
```

But we can't. We cannot do F<B> because F is unknown, and java needs that. F is what is known as a **Higher Kinded Type** 

### Scala has Higher Kinded Types!

```
trait Functor[F[_]] { self =>
  def map[A, B](fa: F[A])(f: A => B): F[B]
implicit object ListFunctor extends Functor[List] {
  override def map[A, B](fa: List[A])(f: (A) \Rightarrow B): List[B] = fa.map(f)
}
implicit object OptionFunctor extends Functor[Option] {
  override def map[A, B](fa: Option[A])(f: (A) => B): List[B] = fa match {
     case Some(x) \Rightarrow Some(f(x))
     case None => None
  }
/* Power play! I only need to declare once! Remember ad-hoc polymorphism! */
def fmap[A, B, C[_]](f:A => B)(coll:C[A])(implicit functor:Functor[C]) =
       functor.map(coll)(f)
fmap(x \Rightarrow x + 2)(List(1,2,3,4)) //List(3,4,5,6)
fmap(x => x + 2)(Some(100)) //Some(102)
                         //None
fmap(x \Rightarrow x + 19)(None)
```

### Winner! Winner! Chicken Dinner!

# Applicatives

- Beefed up functor
- Functors take one param
- Consider:

```
fmap (*) (Just 10)
```

Turns into:

```
(Just ((+) 10))
```

Which is the same as:

```
(Just (10+)
```

Where the type is:

```
:t Maybe(Int -> Int)
```

### Other Partial Maps

```
fmap (+) [1,2,3,4,5]
```

Where the type is...

```
:t [Integer -> Integer]
```

or

```
fmap (x y z -> x + y + z) [1,2,3,4,5]
```

Where the type is...

```
:t [Integer -> Integer]
```

What if we wanted to do...

```
op Just(4*) Just(5)
```

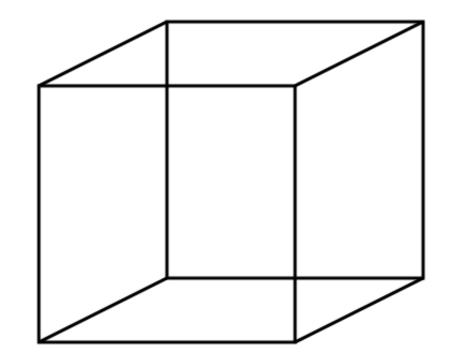
so we can get Just(9)?

## Applicative Functors Definition

```
class (Functor f) => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
```

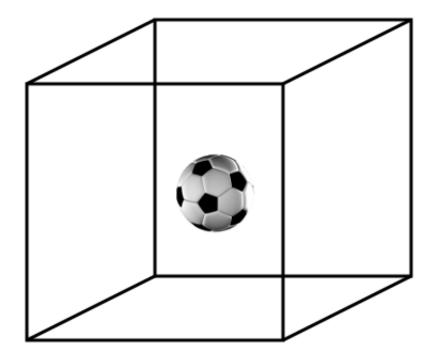
Note: Applicatives are Functors

It's pure baby





It's pure baby



# More pure:

pure 3 :: Either String Int

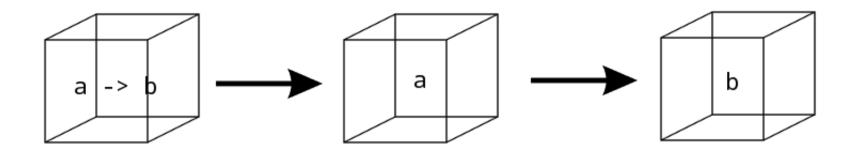
Will return:

Right 3

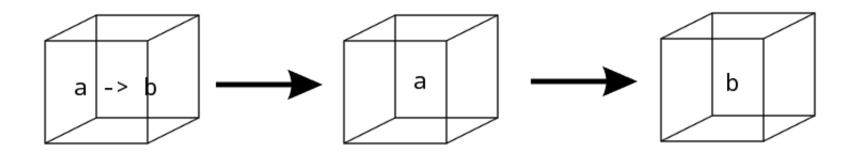
# Contrasting and Comparing <\*> and fmap

```
fmap :: (a -> b) -> f a -> f a
```

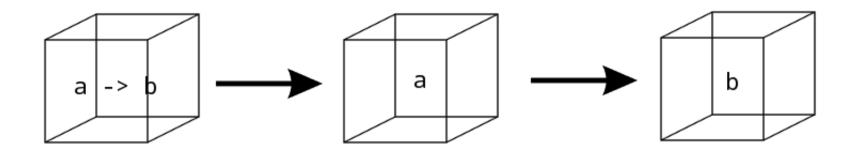
Envisioning what <\*> looks like



Envisioning what <\*> looks like



Envisioning what <\*> looks like



# Building another applicative



pure (+) <\*> Just 3 <\*> Just 5

## Building another applicative



pure (\*) <\*> Nothing <\*> Just 9

## List Applicatives

```
instance Applicative [] where
  pure x = [x]
  fs <*> xs = [f x | f <- fs, x <- xs]</pre>
```

## Pure List Applicatives

```
pure 3 :: [Int]

Converts to:

[3]

pure "Dance" : [String]

Converts to:

["Dance"]
```

Note: String is an alias for [Char]

## So how do we read List Applicative's <\*>?

The signature is

This is called a for comprehesion

## A slightly complicated Applicative chain

```
[(+), (*)] <*> [4,5] <*> [1,9]
```

Taking it in parts

```
[(+4), (+5), (*4), (*5)] <*> [1,9]
[5, 13, 6, 14, 4, 36, 5, 45]
```

#### What does Applicative look like in Scala?

```
trait Applicative[F[_]] {
   def pure[A](a:A):F[A]
   def apply[A, B](fa: F[A])(f:F[A=>B]):F[B]
}
implicit object ListApplicative extends Applicative[List] {
  override def pure[A] (a:A) = List(a)
  override def apply[A, B](xs: List[A])(fs: List[A => B]): List[B] =
    for (f <- fs;
         x < -xs) yield f(x)
}
implicit object OptionApplicative extends Applicative[Option] {
  override def pure[A] (a:A) = Some(a)
  override def apply[A, B](fa: Option[A])(f: Option[A \Rightarrow B]): Option[B] = (f, fa) match {
     case (None, _) => None
     case (Some(f), item) => fmap(f)(item)
  }
}
def applicate [A, B, C[_]](f:C[A => B])(coll: C[A])(implicit applicative:Applicative[C]) = {
       applicative.apply(coll)(f)
}
println(applicate(Some((x:Int) => x * 4):Option[Int => Int])(Some(5):Option[Int]))
println(applicate(List((x => x + 1), (x => x + 4)):List[Int => Int])(List(3, 9)))
```

#### Monoids

- Monoids combines things that are associative, regardless of order or parenthetical categorization:
- Examples

```
`3 * 4`

`2 + 10`

((r + s) + t) or (r + (s + t))
```

- A higher abstract to append one item to another, but in a type class way
- Functional Programmers are obsessive about using one method to work with many types

### Monoid Definition

```
class Monoid m where
  mempty :: m
  mappend :: m -> m -> m
  mconcat :: [m] -> m
  mconcat = foldr mappend mempty
```

### Monoid Rules

```
mempty `mappend` x = x
x `mappend` mempty = x
(x `mappend` y) `mappend` z = x `mappend` (y `mappend` z)
```

#### List Monoids

```
instance Monoid [a] where
  mempty = []
  mappend = (++)
```

```
Prelude> [1,2,3] `mappend` [4,5,6]
[1,2,3,4,5,6]
Prelude> "What's" `mappend` "cool"
What'scool
Prelude> mempty::[String]
[]
Prelude> mempty::[Int]
[]
Prelude> mempty::String
""
Prelude> mconcat [[1,2], [3,5,6,7,10], [12, 19]]
[1,2,3,5,6,7,10,12,19]
```

### foldr?

```
Prelude> let g = foldr (+) 0
Prelude> g [1,2,3,4,5]
15
```

Repeating from the previous slide

```
Prelude> mconcat [[1,2], [3,5,6,7,10], [12, 19]] [1,2,3,5,6,7,10,12,19]
```

#### What does a monoid look like in Scala?

```
trait Monoid[A] {
    def op(a1: A, a2: A): A
    def zero: A
}

val stringMonoid= new Monoid[String] {
    def op(a1: String, a2: String) = a1 + a2
    val zero = ""
}

def listMonoid[A] = new Monoid[List[A]] {
    def op(a1: List[A], a2: List[A]) = a1 ++ a2
    val zero = Nil
}
```

#### So far we have discovered..

```
fmap :: (Functor f) => (a -> b) -> f a -> f b
```

```
(<*>) :: (Applicative f) => f (a -> b) -> f a -> f b
```

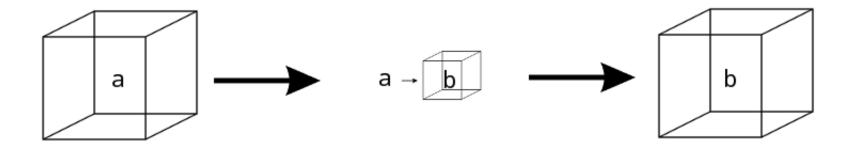
#### ..and now Monads!

```
fmap :: (Functor f) => (a -> b) -> f a -> f b
```

```
(<*>) :: (Applicative f) => f (a -> b) -> f a -> f b
```

```
(>>=) :: (Monad m) => m a -> (a -> m b) -> m b
```

### Monads in Visual Form



(>>=) :: (Monad m) => m a -> (a -> m b) -> m b

## The complete Monad typeclass

```
class Monad m where
  return :: a -> m a

(>>=) :: m a -> (a -> m b) -> m b

(>>) :: m a -> m b -> m b
  x >> y = x >>= \_ -> y

fail :: String -> m a
  fail msg = error msg
```

### return?

• Same is pure in Applicative, take an item and put into a context or container

```
return 4 :: Maybe Int

Evaluates To...
```

Just 4

return 4 :: [Int]

Evaluates To..

[4]

### Bind method

```
(>>=) :: m a -> (a -> m b) -> m b
```

How we will invoke as such:

```
ma >>= (a -> m b)
```

Bind will take one monad, and a function that will return a monad of another type, and provide some result

## fail

- Monads provide an option for failure as a monad.
- Whereas return will provide a Monad of it's simplest form
- fail will return a monad representing failure

### The "move-along" function

- (>>) will take two monads, and determine with one to pass on down.
- By default will accept a the two monads, and return the second one.

The signature is:

```
(>>) :: m a -> m b -> m b
x >> y = x >>= \_ -> y
```

## Maybe Monad

```
instance Monad Maybe where
  return x = Just x
  Nothing >>= f = Nothing
  Just x >>= f = f x
  fail _ = Nothing
```

```
Prelude> Just 4 >>= \x -> return (3*x)
12
Prelude> Nothing >>= \x -> return(x + 100)
Nothing
Prelude> fail "Help" :: Maybe Int
Nothing
```

### What is the point?

```
Prelude> Just 10 >>= (\x -> Just (show x ++ "!"))
Just "10!"
```

```
Prelude> Just 10 >>= (\x -> Just "!" >>= (\y -> Just (show x ++ y)))
Just "10!"
```

Both of the above, are longer than...

```
Prelude> let x = 3; y = "!" in show x ++ y
```

### Monads have built in short circuit error handling

```
Prelude> Nothing >>= (\x -> Just "!" >>= (\y -> Just (show x ++ y)))
Nothing
Prelude> Just 3 >>= (\x -> Nothing >>= (\y -> Just (show x ++ y)))
Nothing
Prelude> Just 3 >>= (\x -> Just "!" >>= (\y -> Nothing))
Nothing
```

### Because Haskell and other programming languages rely on monads...

We are able to convert this...

```
monadStack :: Maybe String
monadStack = Just 3 >>= (\x ->
    Just "!" >>= (\y ->
    Just (show x ++ y)))
```

to this...

This is called "Monad Comprehension"

## We can even do pattern matching as a Monad Comprehension

#### List Monads

Here is the definition of a list monad...

```
instance Monad [] where
  return x = [x]
  xs >>= f = concat (map f xs)
  fail _ = []
```

And here is how we use it...

```
[3,4,5] >>= \x -> [x,-x]
[3,-3,4,-4,5,-5]
```

#### Failure in List Monads

Should be very similar to the Maybe Monad

```
Prelude> [] >>= \x -> [1,2,3]
[]
Prelude> [1,2,3] >>= \x -> []
[]
```

## As a list monad, does this operation look familiar?

```
Prelude> [10,11,12] >>= (x -> [x + 1, x + 2, x + 3]) [11,12,13,12,13,14,13,14,15]
```

## Flat Map!

Here is Flat Map in Java 8!

```
Arrays.asList(10, 11, 12).stream().flatMap(x -> Arrays.asList(x + 1, x + 2, x +
3).stream()).collect(Collectors.toList());
```

```
[11, 12, 13, 12, 13, 14, 13, 14, 15]
```

# Flat Map in Scala!

```
List(10, 11, 12).flatMap(x => List(x + 1, x + 2, x + 3))
```

```
[11, 12, 13, 12, 13, 14, 13, 14, 15]
```

## Flat Map in Scala is used for a variety of things

Like a Maybe Monad

```
Some(4).flatMap(x => Some(3 + x))
Some(7)
```

#### IO Monad?

```
main = do
    x <- return("Hello ")
    y <- return("World")
    putStrLn (x ++ y)</pre>
```

is the same as

```
main = do
    return("Hello ") >>= \x ->
    return("World") >>= \y ->
    putStrLn(x ++ y)
```

Note: This is perhaps the single reason why Haskell is always so hard to get started!

#### Futures Monad in Scala

#### Rube Goldbergs and XMonad

### Thank you!

#### Sources:

- Learn you a Haskell for A Greater Good http://learnyouahaskell.com/
- Functional Programming in Scala http://www.manning.com/bjarnason/
- Math World Wolfram Alpha http://mathworld.wolfram.com
- Wikipedia http://www.wikipedia.org

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