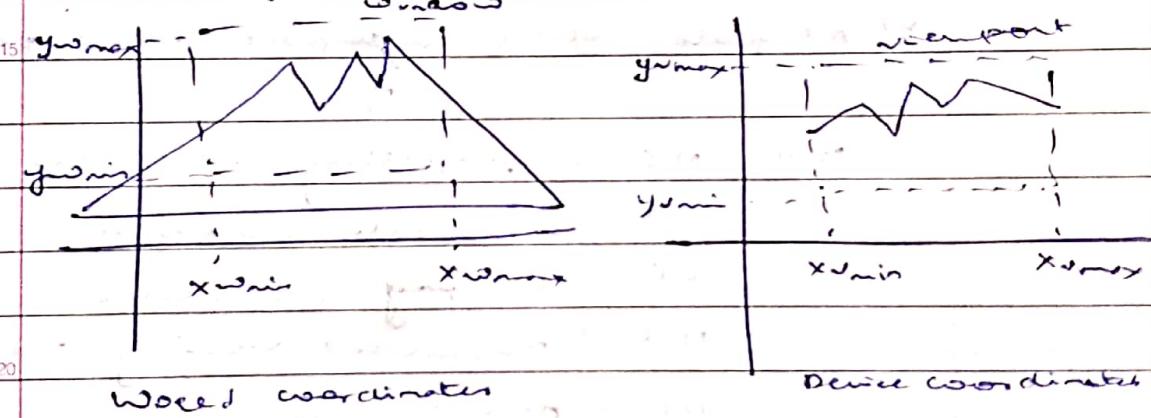


## 2D viewing

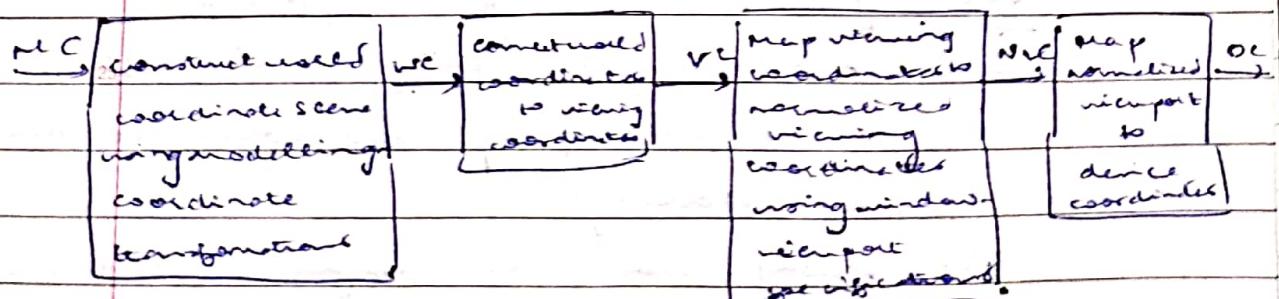
### Viewing pipeline

- Window: A world-coordinate area selected for display. Defines what is to be viewed.
- 5 → Viewport: Area of a display device to which a window is mapped. Defines where it is to be displayed.
- Windows and viewports are rectangles in standard position.
- 10 → Viewing transformation: Mapping of a part of a world-coordinate scene to device coordinates. Also called windowing transformation or window-to-viewport transformation.

### Window transformation



### 2-D viewing transformation pipeline



Process of viewing transformation:

- 1) Construct scene in world coordinates using output primitives and attributes.
- 2) Obtain particular orientation for window.
  - ↳ can create a 2D viewing coordinate system and define a window there.
  - ↳ for arbitrary representation of rectangular windows.
- 3) Once viewing reference frame is established, we can transform descriptions from world coordinates to viewing coordinates.
- 4) We then define viewpoint in normalized coordinates and map viewing coordinates description of the scene to normalized coordinates.
- 5) All parts outside viewpoint are clipped.

Note:

- MC → modelling coordinates
- WC → world coordinates
- VC → viewing coordinates
- NVC → normalized viewing coordinates
- DC → device coordinates

### Viewing coordinate reference frame

→ coordinate system provides the reference frame for specifying the world-coordinate window working.

- 1) A viewing-coordinate origin is selected at some world position:  $r_0 = (x_0, y_0)$ .
- 2) To establish the orientation, or rotation, of

this reference frame way to do this:

→ Specify a world vector  $v$  that defines the viewing  $y_v$  direction. vector  $v$  is called view up vector.

Now calculate components of unit vectors

$$v = (v_x, v_y) \text{ and}$$

$$u = (u_x, u_y)$$

for viewing  $y_v$  and  $x_v$  axes, respectively

→ These unit vectors are used to form

first and second rows of rotation matrix

$R$  that aligns the viewing  $x_v y_v$  axes with the world  $x_w y_w$  axes.

→ To form complete transformation matrix,

i) translate view to world

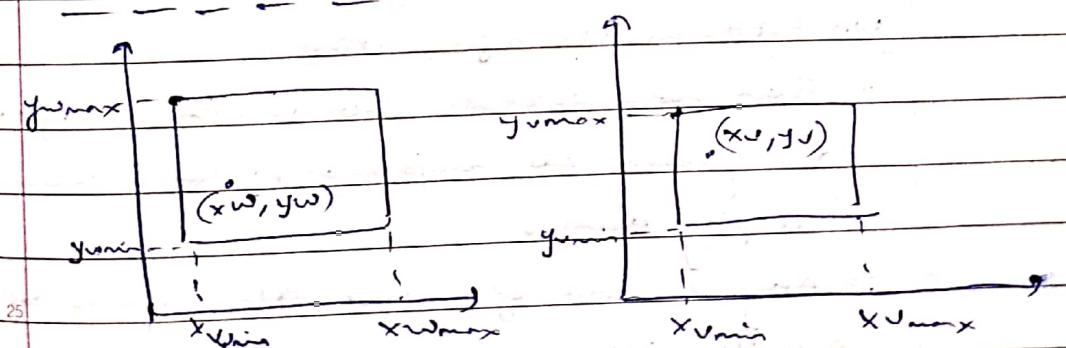
ii) rotate to align

$$M_{wc, vc} = R \cdot T$$

where  $T$  = Translation matrix

$R$  = rotation matrix

### Window - To - Viewport coordinate Transformation



→ A point at position  $(x_w, y_w)$  in the window is mapped into position  $(x_v, y_v)$  in the associated viewport. To maintain the same ~~viewport~~ as the ~~window~~, placement is the ~~same~~

window, we require that

$$x_v - x_{v\min} = x_w - x_{w\min}$$

$$\frac{x_{v\max} - x_{v\min}}{x_{w\max} - x_{w\min}} = \frac{x_w - x_{w\min}}{y_{w\max} - y_{w\min}} \quad (1)$$

$$\text{and } \frac{y_v - y_{v\min}}{y_{w\max} - y_{w\min}} = \frac{y_w - y_{w\min}}{y_{w\max} - y_{w\min}}$$

Solving these expressions for viewport position  $(x_v, y_v)$ , we have

$$x_v = x_{v\min} + (x_w - x_{w\min}) s_x \quad (2)$$

$$y_v = y_{v\min} + (y_w - y_{w\min}) s_y$$

where scaling factors are:

$$s_x = \frac{x_{v\max} - x_{v\min}}{x_{w\max} - x_{w\min}}$$

$$s_y = \frac{y_{v\max} - y_{v\min}}{y_{w\max} - y_{w\min}} \quad (3)$$

(2) can be described as the sequence:

(a) scaling (of  $(x_{v\min}, y_{v\min})$ ) that scales window area to size of viewport.

(b) Translate the scaled window area to position of viewport.

### Workstation Transformation

→ For normalized coordinates, object descriptions are mapped to the various display devices

→ Any source of output devices, can be open in a particular application and another window-to-viewport transformation can be performed for each output device.

→ This mapping is accomplished by selecting a window area in normalized space and a

viewport area in the coordinates of the display device.

### 2D - Viewing functions

- 1) evaluateViewOrientationMatrix ( $x_0, y_0, x_V, y_V, \text{error, viewMatrix}$ )

→  $x_0, y_0$  : coordinates of viewing origin

→  $x_V, y_V$  = world - coordinate position for view up vector

→ error : generated if input parameters are in error. otherwise the

→ viewMatrix for world - to - viewing transformation is calculated

\* Defines a viewing reference system in

- 2) to set up elements of window - to - viewport mapping matrix:

evaluateViewMappingMatrix ( $x_{wmin}, y_{wmax},$

$y_{wmin}, y_{wmax}, x_{vmin}, x_{vmax}, y_{vmin}, y_{vmax}, \text{error, viewMappingMatrix}$ )

→  $x_{wmin}, x_{wmax}, y_{wmin}, y_{wmax}$ : window limits

→  $x_{vmin}, x_{vmax}, y_{vmin}, y_{vmax}$ : viewport limits

- 3) store combination of viewing and window - viewport mappings for various representations in a viewing table

setViewRepresentation ( $ws, viewIndex, viewArea, viewMappingMatrix, xclipmin, xclipmax, yclipmin, yclipmax, clipxy$ )

→ ws: output workstation

→ viewIndex : integer identifier for this particular window-viewport pair.

→ winMatrix and viewMappingMatrix can be concatenated and referenced by viewIndex

→ clipxy : clip or noclip

4) Selects a particular set of options from given table

setViewIndex (viewIndex)

5) Apply workstation transformation by selecting workstation - window-viewport pair:

setWorkstationWindow (ws, xwsWinmin,

xwsWinmax, ywsWinmin, ywsWinmax)

setWorkstationViewport (ws, xwsVpmin,

xwsVpmax, ywsVpmin, ywsVpmax)

### 20 Clipping Operations

→ Any procedure that identifies those portions of a picture that are either inside or outside of a specified region of space is referred to as a clipping algorithm or simply clipping.

→ Region against which an object is to be clipped is called a clip window.

→ Applications of clipping:

(i) extracting part of a defined scene for viewing

(ii) identifying visible surfaces in 3D scene

- (iii) articulating some segments or object boundaries
- (iv) creating objects using solid-modelling procedures
- 5 (v) displaying a multiwindow environment
- (vi) drawing and painting operations that allow parts of a picture to be selected for copying, moving, erasing or duplicating.

10 → Types:

- (1) point clipping
- (2) line clipping
- (3) Area clipping
- (4) curve clipping
- (5) Text clipping

### 15 Point Clipping

→ point  $P(x, y)$  is clipped from a clip window

$(x_{w\min}, x_{w\max}, y_{w\min}, y_{w\max})$  if it does not satisfy any one of the following:

$$x_{w\min} \leq x \leq x_{w\max}$$

$$y_{w\min} \leq y \leq y_{w\max}$$

### Line Clipping

→ for a given line segment to detect if it is either completely inside the clipping window or completely outside.

→ If above condition is not satisfied, perform intersection calculations with one or more clipping boundaries and calculation of multiple intersection points.

→ To avoid execution, derive below algorithms

$$x = x_1 + u(x_2 - x_1)$$

$$y = y_1 + u(y_2 - y_1)$$

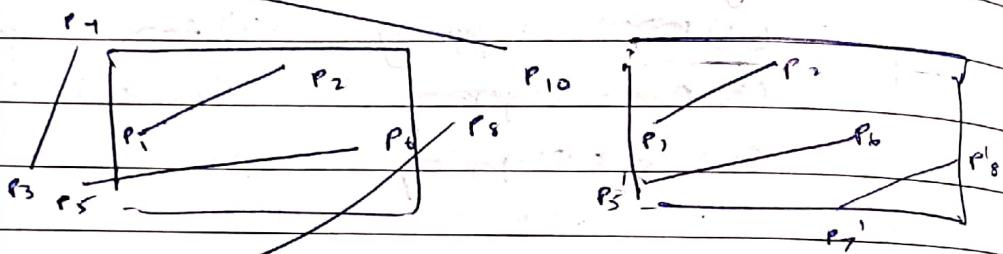
At  $(x, y)$ , values for  $u$  are calculated by  
check for intersection.

5 If  $u \neq 0.001$ , line does not enter interior of window at boundary.

If  $u = 0.001$ , line does cross into clipping area.  
line segments that are parallel to window edges can be handled as special cases.

10

eg.



15

Before clipping

after clipping

### Cohen-Sutherland and line clipping

→ oldest and most popular.

20 → speeds up processing of line segments by performing initial tests that reduce the number of intersections that must be calculated.

→ Every line endpoint in a picture is assigned

25 a 4-digit binary code, called region code  
that identifies the location of particular  
the boundaries of the clipping rectangle.

bit	4	3	2	1
pos	above	below	right	left

→ → point is in that relative position.

$\rightarrow 0000$  : window

1001 | 1000 | 1010

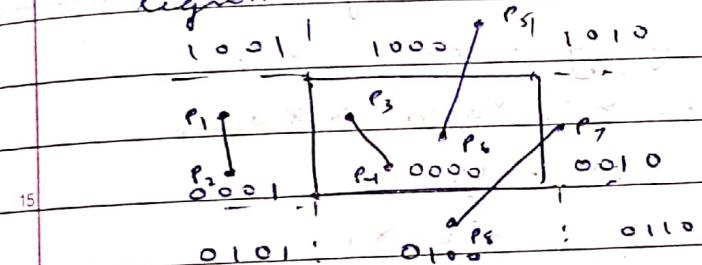
0001 | 0000 | 0010

0101 | 0100 | 0110

Bit 1 :  $x < x_{min}$  Bit 3 :  $y < y_{min}$   
 $(x_{min} - x)$   
 Bit 2 :  $x > x_{max}$  Bit 4 :  $y > y_{max}$   
 $(x_{max} - x)$   
 $(y_{max} - y)$

1) calculate differences b/w endpoint coordinates  
 and clipping boundaries

2) use the constant sign bit of each difference  
 calculation to set corresponding value in the  
 region code.



case (1)  $P_1$  and  $P_2$

$0001 \rightarrow N_2$

&  $0001 \rightarrow N_2$

$0001 \rightarrow N_2$

completely outside  $\Rightarrow$  reject

case (2) :  $P_3$  and  $P_4$

$0000 \rightarrow Z$

$0000 \rightarrow Z$

$0000 \rightarrow Z$

accept the same (no clipping)

case (3) :  $P_5$  and  $P_6$

$1010 \quad N_2 \quad$  clipping

$0000 \quad Z$

$0000 \quad Z$

(partially inside)

Case (4) :  $P_7$  and  $P_8$

$$\begin{array}{r} 0010 \\ 0100 \\ \hline 0000 \end{array} \rightarrow N2$$

$$\begin{array}{r} 0000 \\ \hline 0000 \end{array} \rightarrow N2 \quad \} \text{clipping}$$

partially inside

Intersection points with a clipping boundary can be calculated using the slope-intercept form of the line equation. For a line with endpoint coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$ , the y coordinates of the intersection point with a vertical boundary can be obtained as:

$$y = y_1 + m(x - x_1)$$

where  $x = x_{\min}$  or  $x_{\max}$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

// by x coordinate with horizontal boundary

$$x = x_1 + \frac{y - y_1}{m}$$

where  $y = y_{\min}$  or  $y_{\max}$

In case (3):  $P_5'$  needs to be calculated.

$$P_5' = \underline{\underline{0000}}_2$$

$$\underline{\underline{0000}}_2$$

$\underline{\underline{0000}}_2 \rightarrow \text{accept}$

clip  $P_5'$  and  $P_5$ .

Algorithm:

Step 1: For each end point, region code is assigned

Step 2: The line is accepted if both end points

var region code, 0000

step 3: Block, logical AND operator is performed for both region code.

step 3.1: If result is not 0000, then reject the line.

step 3.2: Else clipping is required.

Step 3.2.1: An end point of line is

selected that is outside the window

Step 3.2.2: Find the intersection

point of the window boundary

Step 3.2.3: The end point is replaced

with the intersection

point and the region

code is updated.

Step 3.2.4: Repeat step 2 until we

find a clipped line

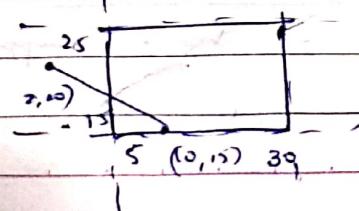
either logically accepted

or logically rejected

Step 4: Repeat steps for other lines.

- Q1) Clip the line with the coordinates  $(x_1, y_1) = (2, 20)$  and  $(x_2, y_2) = (10, 15)$  against a window having lower left corner at  $(5, 15)$  and upper right corner at  $(13, 25)$  using Cohen Sutherland line clipping algorithm.

Ans



1) Region code for  $(x_1, y_1) = (2, 20)$

$$\text{bit 1: } x - x_{\min} = 2 - 5 = -3 \quad (\text{+ve}) \quad 1$$

$$\text{bit 2: } x_{\max} - x = 30 - 2 = 28 \quad (\text{+ve}) \quad 0$$

$$\text{bit 3: } y - y_{\min} = 20 - 15 = 5 \quad (\text{+ve}) \quad 0$$

$$\text{bit 4: } y_{\max} - y = 25 - 20 = 5 \quad (\text{+ve}) \quad 0$$

Region code = 0001

2) Region code for  $(x_2, y_2) = (10, 15)$

$$\text{bit 1: } x - x_{\min} = 10 - 5 = 5 \quad (\text{+ve}) = 0 \quad 1$$

$$\text{bit 2: } x_{\max} - x = 30 - 10 = 20 \quad (\text{+ve}) \quad 0$$

$$\text{bit 3: } y - y_{\min} = 15 - 15 = 0 \quad (\text{+ve}) \quad 0$$

$$\text{bit 4: } y_{\max} - y = 25 - 15 = 10 \quad (\text{+ve}) \quad 0$$

Region code = 0000

$$0001 \rightarrow N2$$

$$0000 \rightarrow Z$$

$$\underline{0000} \rightarrow Z$$

clipping at point 1 vertical intersect

$$y = y_1 + m(x - x_1)$$

$$= 20 + \frac{5}{8}(5-2)$$

$$= 18.125 \quad \therefore m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$(5, 18.125)$$

3) Region code for  $(x'_1, y'_1) = (5, 18.125)$

$$\text{bit 1: } x - x_{\min} = 5 - 5 = 0 \quad 0 \quad \frac{-5}{5}$$

$$\text{bit 2: } x_{\max} - x = 30 - 5 = 25 \quad 0$$

$$\text{bit 3: } y - y_{\min} = 18.125 - 15 = 3.125 \quad 0 \quad x = x_{\min}$$

$$\text{bit 4: } y_{\max} - y = 25 - 18.125 \quad 0 \quad \therefore \text{ intersects at } x_{\min}$$

Region code = 0000

hence, we have clipped one segment

Q2) window : LL ( $5, 15$ )  $x_{max}, y_{max}$   
 $UR (30, 25)$

$$(x_1, y_1) = (2, 16) \quad (x_2, y_2) = (10, 15)$$

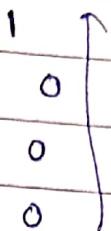
At  $(2, 16)$

Bit 1:  $2 - 5 = -3 < 0$

2:  $30 - 16 = 14 > 0$

3:  $16 - 16 = 0$

4:  $25 - 16 = 9$



Region code = 0000

At  $(10, 15)$

Bit 1:  $10 - 5 = 5 \rightarrow 1$  (0)

2:  $30 - 10 = 20 \rightarrow 0$  (0)

3:  $15 - 15 = 0 \rightarrow 0$  (0)

4:  $25 - 15 = 10 \rightarrow 0$  (0)



Region code = 0000

0001  $\rightarrow N2$

0000  $\rightarrow Z$

0000  $\rightarrow Z$

Point 1 does not have to be clipped.

Equation:  $y = y_1 + m(x - x_1)$

$= 16 + \frac{15-16}{10-2} (5 - 2)$

$= 16 - 0.6 \cdot 3$

$= 15.625$

$(5, 15.625)$

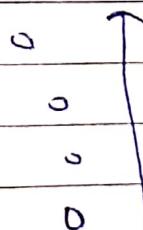
Region at  $(5, 15.625)$

Bit 1:  $5 - 5 = 0$

Bit 2:  $30 - 5 = 0$

Bit 3:  $15.625 - 15 = 0.625$

Bit 4:  $25 - 15.625$



Region code = 0001

$\Rightarrow$  successfully clipped.

Q3)  $(10, 12)$  and  $(34, 27)$  for window

$$UR = \left( \frac{max}{30}, 25 \right) \quad LL = \left( \frac{min}{5}, 15 \right)$$

ans - At  $(10, 12)$

$$Bit 1: 10 - 5 = 5 \quad 0$$

$$2: 30 - 10 = 20 \quad 0$$

$$3: 12 - 15 = -3 \quad 1$$

$$4: 15 - 12 = 3 \quad 0$$

Region code = 0100

At  $(34, 27)$

$$1: 34 - 5 = 29 \quad 0$$

$$2: 30 - 34 = -4 \quad 1$$

$$3: 27 - 15 = 12 \quad 0$$

$$4: 25 - 27 = -2 \quad 1$$

Region code = 1010

$0100 \rightarrow N2$

$1010 \rightarrow N2$

$0000 \rightarrow Z$

perform clipping at both points.

(a) point 1  $(10, 12)$  cut horizontally.

$$y = y_{min} = 15 \quad [ \because below ]$$

$$x = x_1 + \frac{y_{min} - y_1}{m}$$

$$m = \frac{27 - 12}{34 - 10} = \frac{15}{24} = \frac{5}{8}$$

$$x = 10 + \frac{(15 - 12) \times 8}{5}$$

$$= 14.8$$

Point =  $(14.8, 15)$

UBRL

1010

(b) point 2  $(34, 27)$

$$x = x_{max} = 30$$

$$y = y_1 + m(x - x_1)$$

$$= 27 + \frac{5}{8}(30 - 34)$$

$$= 24.5$$

$$(30, 24.5)$$

Region code at (14.8, 15)

$$\text{Bit 1: } 14.8 - 5 \quad 0$$

$$\text{Bit 2: } 30 - 14.8 \quad 0$$

$$\text{Bit 3: } 15 - 15 \quad 0$$

$$\text{Bit 4: } 25 - 15 \quad 0$$

Region code = 0000

$\Rightarrow$  clipping successive.

At (30, 24.5)

$$\text{Bit 1: } 30 - 5 \quad 0$$

$$\text{Bit 2: } 30 - 30 \quad 0$$

$$\text{Bit 3: } 24.5 - 15 \quad 0$$

$$\text{Bit 4: } 25 - 24.5 \quad 0$$

Region code = 0000

$R \Rightarrow$  clipping successive.

Q4) Clip the line P1P2 with coordinates  $(x_1, y_1)$

$= (-13, 5)$  and  $(x_2, y_2) = (17, 11)$  against a

window having lower left corner at  $(-8, -4)$

and upper right corner at  $(12, 8)$  using

Cohen-Sutherland line clipping algorithm.

$$\text{Ans: } (x_1, y_1) = (-13, 5) \quad (x_2, y_2) = (17, 11)$$

$$LL = (-8, -4)$$

$$UR = (12, 8)$$

At (-13, 5)

$$\text{Bit 1: } -13 + 8 = -5 \quad 1$$

$$\text{Bit 2: } 12 + 13 = 25 \quad 0$$

$$\text{Bit 3: } 5 + 4 = 9 \quad 0$$

$$\text{Bit 4: } 8 - 5 = 3 \quad 0$$

Region code = 0001

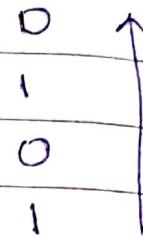
At (17, 11)

$$B \cap 1 = 17 + 8$$

$$2: 12 - 17$$

$$3: 11 + 4$$

$$4: 8 - 11$$



Region code = 1010

$$0001 \rightarrow N_2$$

$$1010 \rightarrow N_2$$

$$0000 \rightarrow Z$$

point 1 and 2 to be clipped.

(a) For point 1: (-13, 5)

$$y = y_1 + m(x_{min} - x_1)$$

$$= 5 + \frac{11-5}{17+13}(-8+13)$$

$$z = 5$$

Point = (-8, 5)

Region code will be as:

$$B \cap 1: 12 - 8 + 8$$

$$2: 12 + 8$$

$$3: 5 + 4$$

$$4: 8 - 5$$

Region code = 0000

$\Rightarrow$  successfully clipped.

(b) For point 2: (17, 11)

Assume surface intersection

$$y = y_1 + m_{\max}(x - x_1)$$

$$= 11 + \frac{11-5}{17+13}(12-17)$$

$$= 10$$

(12, 10)

Bit 1:  $12 + 8$  0

2:  $12 - 12$  0

3:  $10 + 4$  0

4:  $8 - 10$  1

Region code = 1000

$\Rightarrow$  not successful.

Assume horizontal intersection:

$$x = \frac{x_1 + y - y_1}{m} \quad [y = y_{max}]$$

$$= 17 + (8 - 11) \cdot 30$$

16

$\approx 20.0$

(24, 8)

Bit 1:  $2 + 8$  0

2:  $12 - 2$  0

3:  $8 + 4$  0

4:  $8 - 8$  0

Region code = 0000

$(-8, 5) \rightarrow (2, 8)$  is successful.

Points are  $(-8, 5)$  and  $(2, 8)$ .

Q5) Find the region codes for a given line segment:

PC with the endpoints given as P(-1, 5) and

Q(3, 8) and then clip the line w.r.t a rectangular

window with lower-left corner at (-3, 1) and

upper-right corner at (2, 6) using Cohen

and Sutherland line clipping algorithm.

Ans-  $(x_1, y_1) = (-1, 5)$   $(x_2, y_2) = (3, 8)$

LL = (-3, 1)

UR = (2, 6)

At (-1, 5)

$$\text{Bit 1: } -1 + 3$$

$$2: 2 + 1$$

$$3: 5 - 1$$

$$4: 6 - 5$$

Region code = 0001

At (3, 8)

$$\text{Bit 1: } 3 + 3$$

$$\text{Bit 2: } 2 - 3$$

$$3: 8 - 1$$

$$4: 6 - 8$$

Region code = 1010

0001

1010 } 2

0000 → 2

Both points P and Q need to be clipped

(a) Clipping P (-1, 5) at left vertical.

$$y = y_1 + m(x_{min} - x_1)$$

$$= 5 + \frac{8-5}{-3+1}(-3+1)$$

$$(x_{min}, y_{min}) = (3, 3+1)$$

$$= 3.5$$

$$P' = (-3, 3.5)$$

$$\text{Bit 1: } -3 + 3$$

$$2: 2 + 3$$

$$3: 3.5 - 1$$

$$4: 6 - 3.5$$

Region code = 0000

$\therefore P' (-3, 3.5)$

and successfully clipped

(b) Clipping (3, 8)

Let us assume horizontal clipping

$$x = x_1 + \underline{y - y_1}$$

m

$$= 3 + \frac{(6 - 8)(4)}{3}$$

$$= 0.333$$

$$(0.333, 6)$$

$$\text{Box 1: } 0.333 + 3 \quad 0$$

$$2: \quad 2 - 0.333 \quad 0$$

$$3: \quad 6 - 1 \quad 0$$

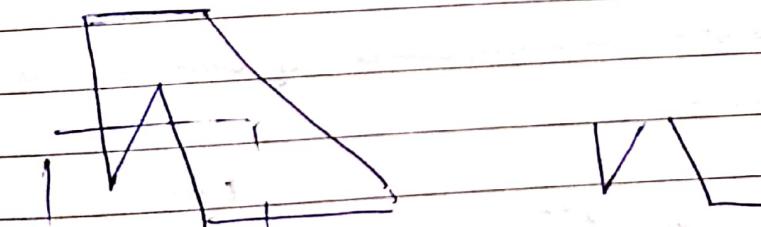
$$4: \quad 6 - 6 \quad 0$$

$$\text{Region code} = 0000$$

$$\therefore Q' = (0.333, 6)$$

and successively clipped.

### Polygon Clipping



Before clipping

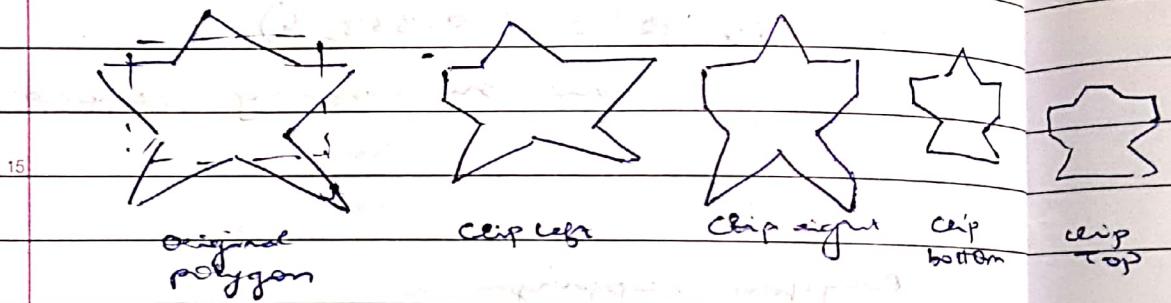
After clipping

→ an algorithm that will generate one or more closed areas that are then scan converted for the appropriate area fill.

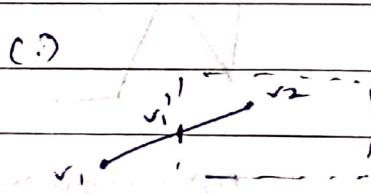
→ order of polygon clipped should be a sequence of vertices that defines the clipped polygon boundaries.

Sutherland-Hodgeman Polygon Clipping  
 → processing all polygon vertices against each clip rectangle boundary.

i.e. we first clip the polygon against the left rectangle boundary to produce a new sequence of vertices. The new set of vertices could then be successively passed to a right boundary clipper, a bottom boundary clipper, and a top boundary clipper. At each step, a new sequence of output vertices is generated and passed to the next window boundary clipper.



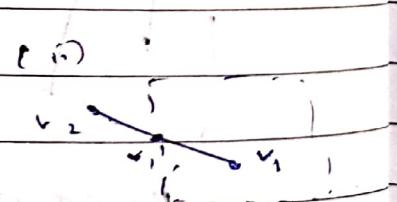
To find new sequence of vertices we have 4 cases:



outside  $\rightarrow$  inside

O/P:  $v_1, v_2$

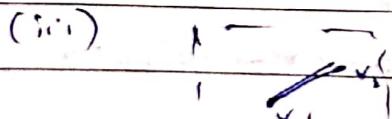
(intersect + det)



inside  $\rightarrow$  outside

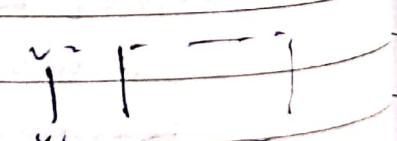
O/P:  $v_2$

$-v_1'$



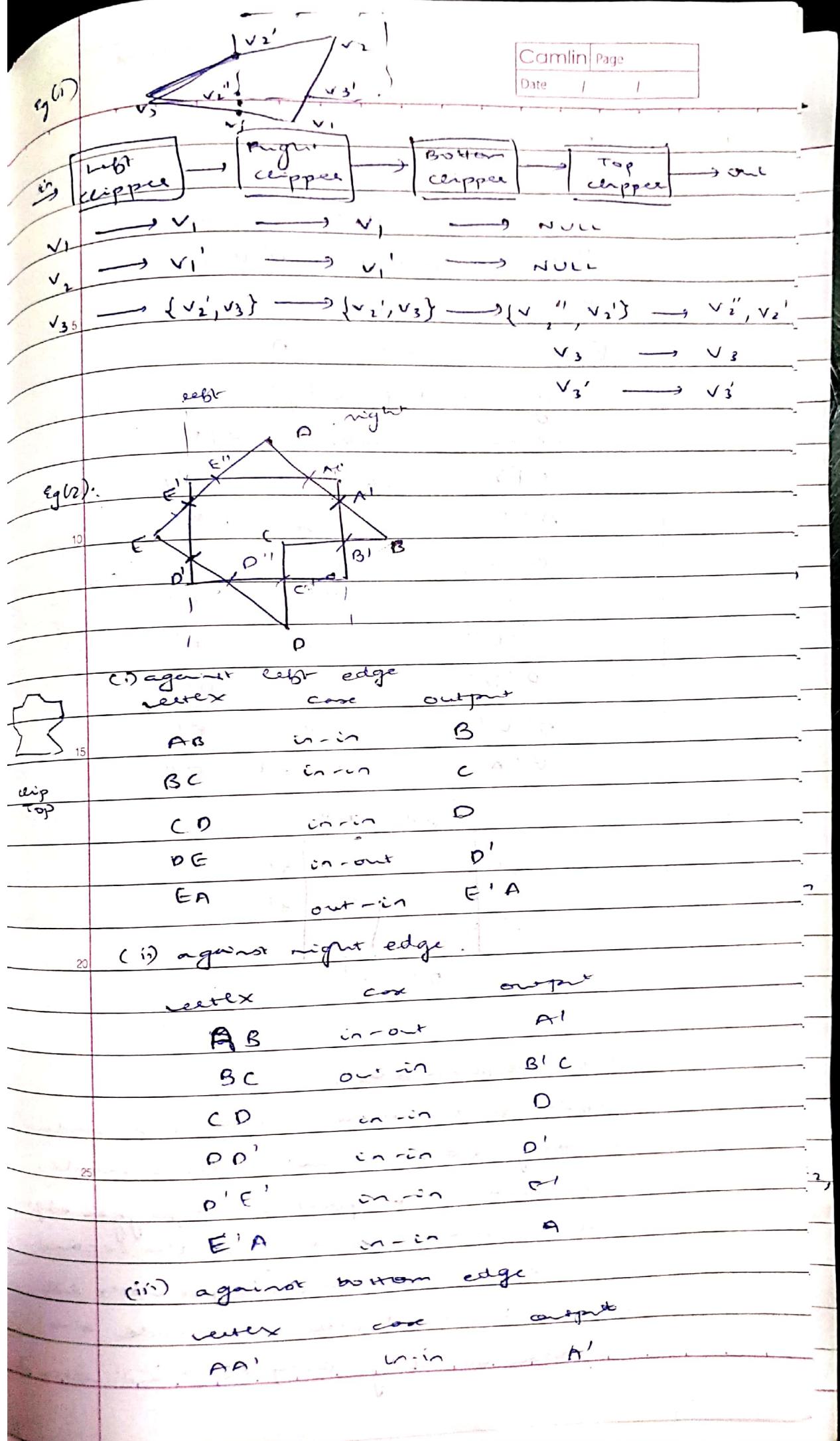
in  $\rightarrow$  in

O/P det:  $v_2$



out  $\rightarrow$  out

O/P: null



$A'B'$  in-in  $B'$   
 $B'C$  in-in  $C$   
 $C'D$  in-out  $C'$   
 $DD'$  out-in  $D''D$   
 $D'E'$  in-in  $E'$   
 $E'A$  in-in  $A$

(iv) against top edge

vertex case O/P

$AA'$  in-in  $A''A'$

$A'B'$  in-in  $B'$

$B'C$  in-in  $C$

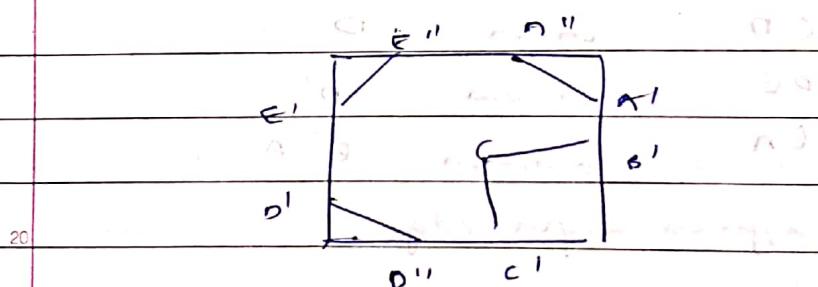
$C'C'$  in-in  $C'$

$C'D''$  in-in  $D''$

$D''D'$  in-in  $D''$

$D'E'$  in-in  $E'$

$E'A$  in-out  $E''$



cases are explained as:

(1) If the first vertex is outside the window boundary and the second vertex is inside, both the intersection point of the polygon edge with the window boundary and the second vertex are added to the output vertex list.

(2) If both input vertices are inside the window boundary, only the second vertex is

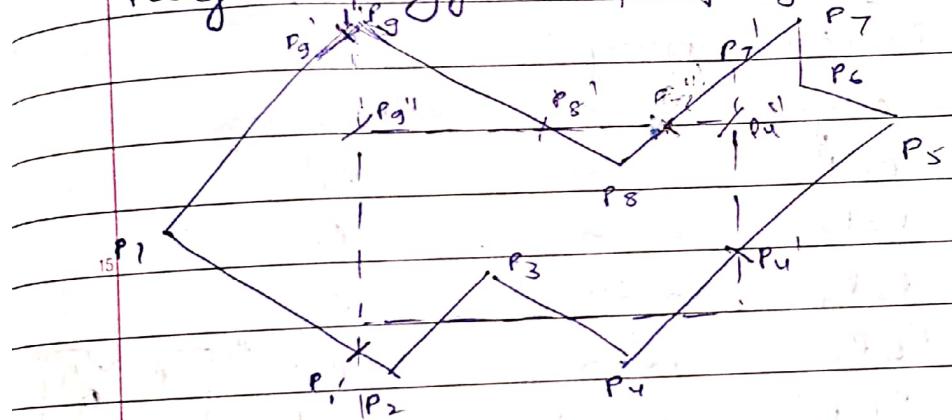
added to the output vertex list.

(3) If the first vertex is inside the window boundary and the second vertex is outside,

only the edge intersection with the window boundary is added to the output vertex list.

(4) If both input vertices are outside the window boundary, nothing is added to the output list.

a) Clip the following polygon using Sutherland-Hodgeman polygon clipping algorithm



Ans (i). left clipping

edge	case	O/P vertex
P <sub>1</sub> P <sub>2</sub>	out → in	P' <sub>1</sub> P <sub>2</sub>
P <sub>2</sub> P <sub>3</sub>	in → in	P <sub>3</sub>
P <sub>3</sub> P <sub>4</sub>	"	P <sub>4</sub>
P <sub>4</sub> P <sub>5</sub>	"	P <sub>5</sub>
P <sub>5</sub> P <sub>6</sub>	"	P <sub>6</sub>
P <sub>6</sub> P <sub>7</sub>	"	P <sub>7</sub>
P <sub>7</sub> P <sub>8</sub>	"	P <sub>8</sub>
P <sub>8</sub> P <sub>9</sub>	"	P <sub>9</sub>
P <sub>9</sub> P <sub>1</sub>	in → out	P' <sub>9</sub>

(ii) right clipping

edge      case      O/P vertex

$P_1'P_2$

in-in

$P_1'$

$P_2P_3$

"

$P_2$      $P_3$

$P_3P_4$

"

$P_3$      $P_4'$

$P_4P_5$

in-out

$P_4'$

$P_5P_6$

out-out

—

$P_6P_7$

out-out

—

$P_7P_8$

out-in

$P_7'P_8$

$P_8P_9$

in-in

$P_8$

$P_9P_9'$

in-in

$P_9$

$P_9'P_1'$

in-in

$P_9'$

(i) top clipping

edge      case      O/P vertex

$P_1'P_2$

in-in

$P_1'$

$P_2P_3$

in-in

$P_2$

$P_3P_4$

in-in

$P_3$

$P_4P_4'$

in-in

$P_4$

$P_4'P_7'$

in-out

$P_4''P_7'$

$P_7'P_8$

out-in

$P_7''P_8$

$P_8P_9$

in-out

$P_8'$

$P_9P_9'$

out-out

—

$P_9'P_1'$

out-in

$P_9''P_1'$

(ii) bottom clipping

edge      case      O/P vertex

$P_1'P_2$

out-out

—

$P_2P_3$

out-in

$P_2'P_3$

$P_3P_4$

in-out

$P_3'$

$P_4P_4'$

out-in

$P_4''P_4'$

$P_4'P_4''$

in-in

$P_4'$

$P_4''P_7''$

in-in

$P_4''$

$P_7'P_8$

in-in

$P_7'P_8$

$P_8P_9$

in-in

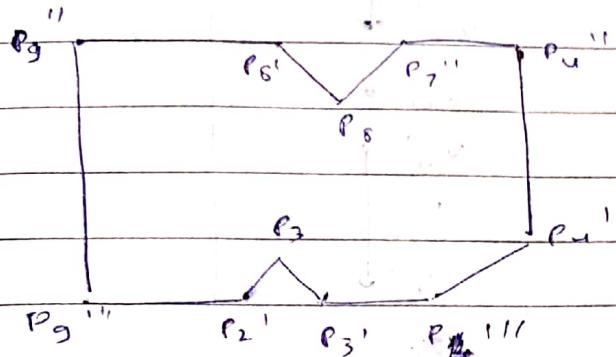
$P_8$

$P_9P_9'$

in-in

$P_9$

$P_7'' P_8''$  in-in  $P_7'$   
 $P_8 P_5'$  "  $P_8$   
 $P_8' P_9''$  "  
 $P_9'' P_1'$  in-out  $P_9'''$



Orientation: only correctly clipped convex polygon ( $\omega < 180^\circ$ )

### Wuille Atherton Polygon clipping

→ follow the window boundaries: path type

follow depends on polygon processing direction (clockwise or counterclockwise)

and whether the pair of polygon vertices

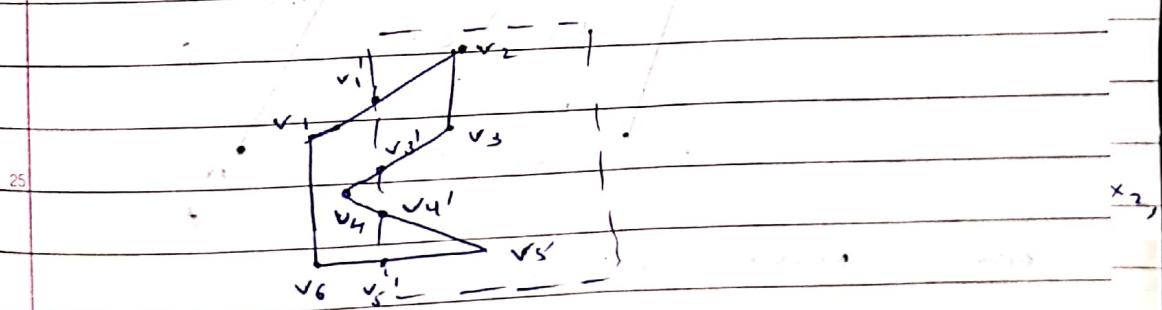
currently being processed represents an

out-in pair or in-out pair. For clockwise

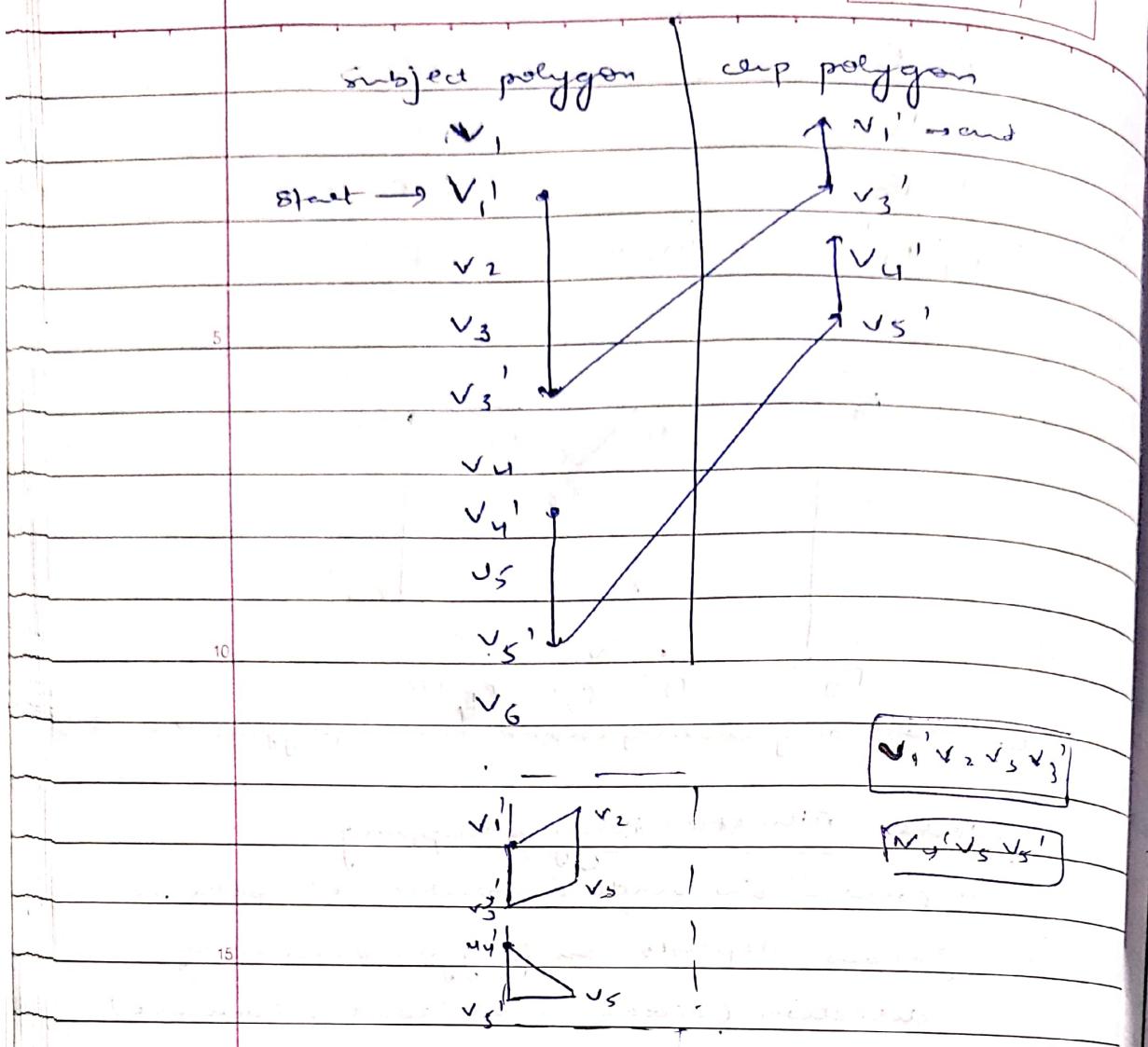
processing, use following rules:

1) out-out: follow polygon boundary.

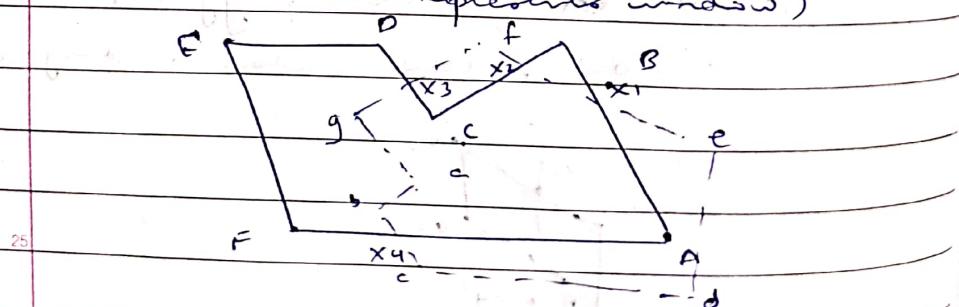
2) in-out, follow window boundary in clockwise



→ create 2 lists: one for project polygon and the other for clipping polygon

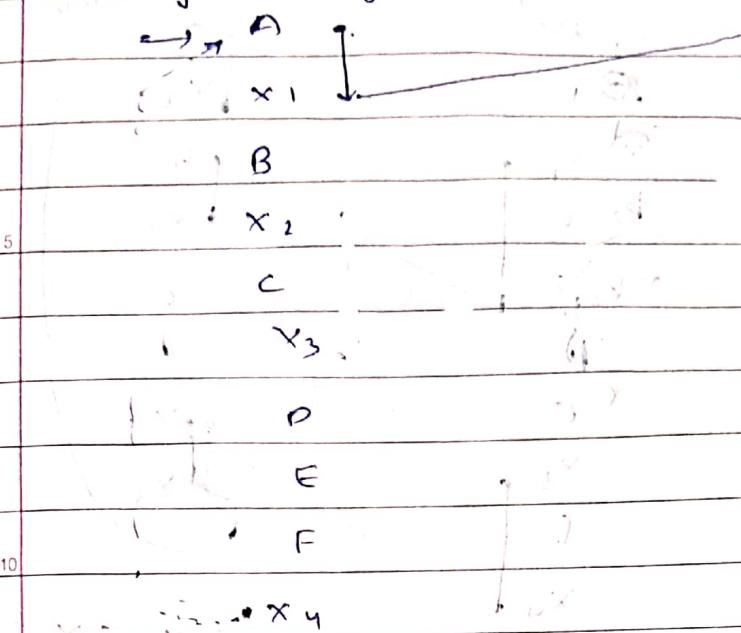


(Q2) Explain how polygon in Figure 1 will be clipped using the window intersection polygon clipping algorithm (solid line represents polygon and dashed line represents window)

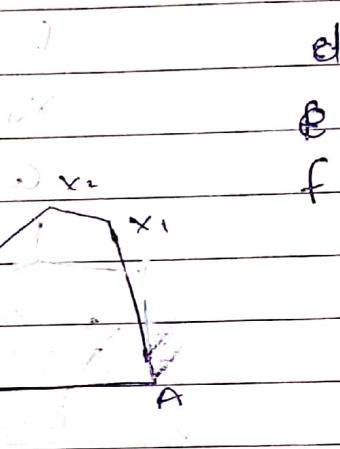
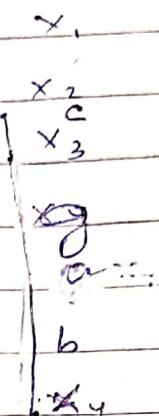


Ans - mark intersections with window co-  
 $x_2, x_3$  and  $x_4$  as marked in the figure.  
 create lists.

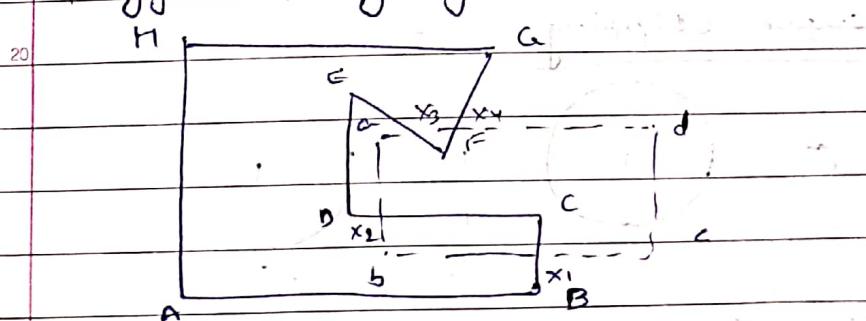
subject Polygon



clip polygon



(e) clip the following polygon using weiler astels  
polygon clipping algorithm.



Ans - mark intersections with indices as  $x_1, x_2, x_3, x_4$  as shown.

Open 2 lists as below:

Subject Polygon

A  
B

5

x<sub>1</sub>  
c  
x<sub>2</sub>  
b  
d

Clip Polygon

a  
x<sub>2</sub>

b  
v<sub>1</sub>  
c  
d

10

E  
x<sub>3</sub>  
F  
x<sub>4</sub>

x<sub>4</sub>  
x<sub>3</sub>

(x<sub>1</sub> < x<sub>2</sub>, b)

15

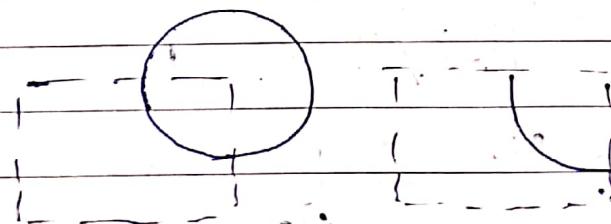
x<sub>1</sub> x<sub>4</sub>  
x<sub>2</sub> F c  
b x<sub>1</sub>

(x<sub>3</sub> > x<sub>4</sub>)

20

Curve Clipping

25



before clipping      after clipping

→ clipping access with curved boundaries

→ requires more processing than for objects with linear boundaries.

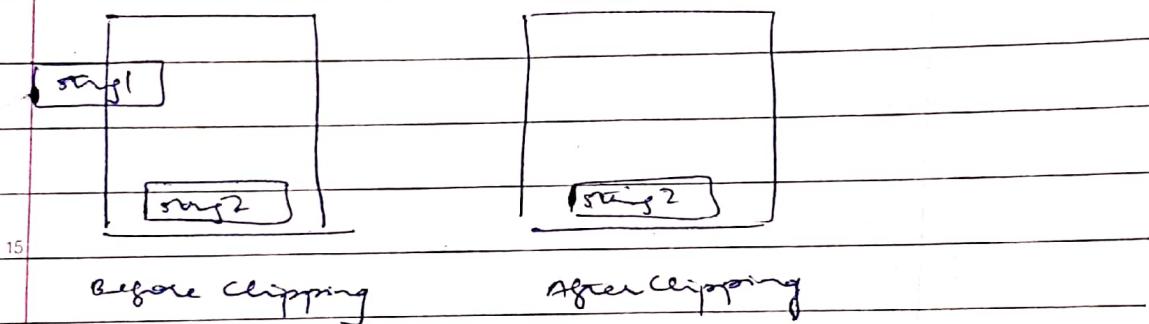
→ bounding rectangle for curved object can be used just to test for overlap with a rectangular clip window.

→ If bounding rectangle for the object is completely inside the window, we save the object.

→ If rectangle is determined to be completely outside the window, we discard the object.

→ For others, we can use coordinate extrema of individual quadrants for circles and ellipses.

## 10. Text Clipping



→ technique used depends on methods used to generate characters and the requirements of a particular application.

→ all-or-none string-clipping strategy: If all of the string is inside a clip window, we keep it. Otherwise, the string is discarded. The procedure is implemented by considering a bounding rectangle around the text pattern. produces faster text clipping.

→ all-or-some character-clipping strategy: Here, we discard only those characters that are not completely inside the window. In this case, the boundary units of individual characters are compared to the window.

→ clip components of individual character:

each character is treated in a way like lines.

If an individual character encloses a clip

window boundary, we clip off the parts of the character that are outside the window.

Characters defined with bit maps would be clipped by comparing the relative position of the individual pixels in the character grid patterns to the clipping boundaries.