#### Monte Carlo Methods - Introduction

Prof. Dr. Narayan Prasad Adhikari Central Department of Physics Tribhuvan University Kirtipur, Kathmandu, Nepal

September 5, 2022



# **■**Warm up!!!

- Important Discoveries
- What is it?
- Why do we need it in Data Science?

#### ■Warm up - what is really it?!!!

You may face multidimensional integration. It comes in Mathematics as well as in Physics, Statistics ....

$$\int \int \dots \int f(x_1)f(x_2)\dots f(x_n)dx_1dx_2\dots dx_n \tag{1}$$

In above equation n may be huge ... 100,  $10^4$ , or  $10^6$ ,....? How to handle such a complex problem? Just think about it.... Does our ways of doing till now work?

## ■Warm up - what is really it?!!!

tivities 🧿 Google Chro	me 🔻		सितम्बर 4 22:26 ●
Monte Carlo" - Google Sc	× Estimation of Absorbed D × 9 Why the	Monte Carlo met   +	
→ C m scholar.goo	gle.com/scholar?hl=en&as_sdt=0%2C5&q="Monte+Carlo"	'&btnG=	
Gmail 🖸 YouTube 🤾	Maps		
Google Scholar	"Monte Carlo"		
Articles	About 4,740,000 results (0.06 sec)		
Any time Since 2022 Since 2021 Since 2018 Custom range	The monte carlo method  N Metropolis, S Ulam - Journal of the American statistical We shall present here the motivation and a general descr- class of problems in mathematical physics. The method is  Save 99 Cite Cited by 8220 Related articles All	iption of a method dealing with a s, essentially, a statistical approach	роғу hedibert.org
Sort by relevance Sort by date Any type	Monte Carlo theory and practice F James - Reports on progress in Physics, 1980 - iopscie in the Monte Carlo approach. The aim of this review is the "traditional" Monte Carlo and guassiMonte Carlo. and	, first, to lay a theoretical basis for both	[PDF] iop.org
Review articles  ☐ include patents ☐ include citations	☆ Save 97 Cite Cited by 723 Related articles All 1  [BOOK] Monte carlo methods  J Hammersley - 2013 - books.google.com	5 versions	
Create alert	This monograph surveys the present state of <b>Monte Carl</b> certain topics that have interested us Although personally.  \$\times\$ Save 99 Cite Cited by 6688 Related articles All	, we hope that our coverage of the	
	por Introduction to monte carlo simulation RL Harrison: AIP conference proceedings, 2010 aip soil. This page reviews the history and principles of Monte techniques commonly used in the simulation of medical in  Save 59 Cite Cited by 286 Related articles. All 8	Carlo simulation, emphasizing naging This paper gives an	[PDF] Scitation.org
	Related searches		
		monte carlo" dose	
		inetic "monte carlo" equential "monte carlo"	



Download Full Issue



Physica A: Statistical Mechanics and its
Applications
Volume 574, 15 July 2021, 126014



# A random walk Monte Carlo simulation study of COVID-19-like infection spread

...

S. Triambak <sup>a</sup>  $\stackrel{\triangle}{\sim}$   $\stackrel{\square}{\bowtie}$  D.P. Mahapatra <sup>b</sup>  $\stackrel{\square}{\bowtie}$ 

Show more

+ Add to Mendeley 💸 Share 🥦 Cite

https://doi.org/10.1016/j.physa.2021.126014

Get rights and content

#### Abstract

Recent analysis of early COVID-19 data from China showed that the number of confirmed cases follows: a subexponential power-law

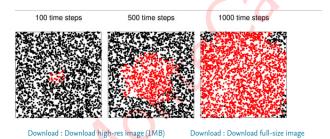
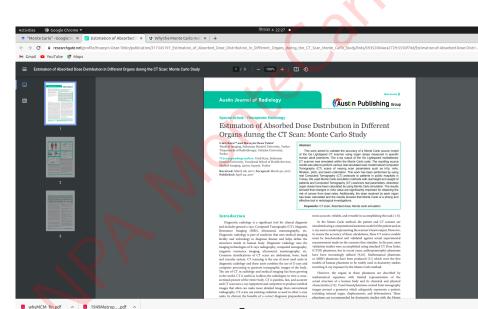


Fig. 1. An example of proximity-based infection spread obtained using the random walk Monte Carlo simulations described in this work. Each of the panels shown above has a population of 2.5k over a unit area. The average distance  $\langle r \rangle$  between any two points is =0.02 units. In this case every point (walker) takes randomly directed steps of length l=0.25  $\langle r \rangle$ . Further details are described in the text below.



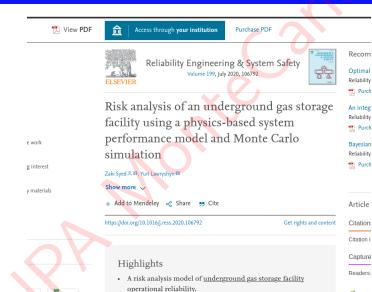
- Case of Siamese Twins
- Pharmacy
- MC dose calculation in the radiotherapy treatment

#### ■Warm up - Artificial intelligence



Monte Carlo methods are also pervasive in artificial intelligence and machine learning. Many important technologies used to accomplish machine learning goals are based on drawing samples from some probability distribution and using these samples to form a Monte Carlo estimate of some desired quantity.

#### ■Warm up - Risk Analysis



· Physics-based performance model combined with Monte

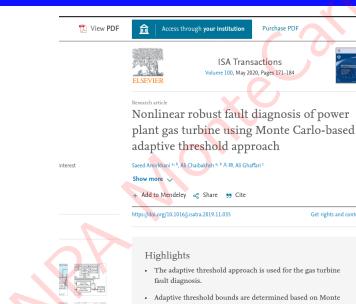
Carlo simulation of dispuptions.

**⊘**PLUM

# ■Warm up - Sensitivity



#### ■Warm up - powerplant



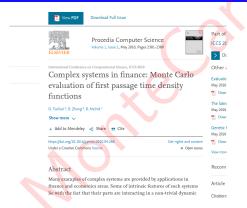
Purchase PDF



Get rights and content

- · Adaptive threshold bounds are determined based on Monte Carlo simulations.
- The robustness of fault detection is analysed through

#### **■Warm up - Finance**



Monte Carlo analysis is useful in risk analysis because many investment and business decisions are made on the basis of one outcome. In other words, many analysts derive one possible scenario and then compare that outcome to the various impediments to that outcome to decide whether to proceed.

# ■Warm up - Physics

diffusion Limited Aggregation

#### ■Warm up - what is really it?!!!

- Monte Carlo methods, or Monte Carlo experiments, are a broad class of computational algorithms that rely on repeated random sampling to obtain numerical results. The underlying concept is to use randomness to solve problems that might be deterministic in principle.
- In a Monte Carlo simulation (method) we attempt to follow the 'time dependence' of a model for which change, or growth, does not proceed in some rigorously predefined fashion (e.g. according to Newton's equation of motion) but rather in a stochastic manner which depends on a sequence of random numbers which is generated during the simulation

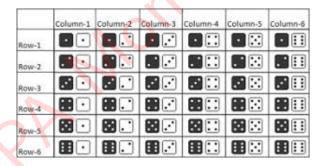
#### ■Warm up - what is really it?!!!

- Monte Carlo method is used to estimate the possible outcomes of an uncertain event. The Monte Carlo Method was invented by John von Neumann and Stanislaw Ulam during World War II to improve decision making under uncertain conditions. It was named after a well-known casino town, called "Monte Carlo" in Monaco, since the element of chance is core to the modeling approach, similar to a game of roulette.
- Monte Carlo Simulations have assessed the impact of risk in many real-life scenarios, such as in artificial intelligence, stock prices, sales forecasting, project management, and pricing.

- When Ulam was in hospital he was playing cards (just for time passing) and got the idea of random sampling. He then applied this idea along with Neuman to solve the problem of "neutron diffusion" in the Manhattan project
- Monte Carlo algorithms are simple, flexible, and scalable. When applied to physical systems, Monte Carlo techniques can reduce complex models to a set of basic events and interactions, opening the possibility to encode model behavior through a set of rules which can be efficiently implemented on a computer.
- However he published paper about MC simulation only in 1949 from LANL (Los Alamos National Lab)

- Take a random sample of given population. Calculate many different outcomes and their probabilities of occurrence
- This outcome represents the desired results.

 Consider a simple example of rolling dice. Assume that you want to determine the probability of rolling a seven using two dice with values one through six. There are 36 possible combinations for the two dice, six of which will total seven, as shown in the following image.



- This means that mathematical probability of rolling a seven is six in 36, or 16.67 percent.
- But is the mathematical probability the same as the actual probability? Or are there other factors that might affect the mathematical probability, such as the design of the dice themselves, the surface on which they are thrown, and the technique that is used to roll them?
- To determine the actual probability of rolling a seven, you might physically roll the dice 100 times and record the outcome each time. Assume that you did this and rolled a seven 17 out of 100 times, or 17 percent of the time. Although this result would represent an actual, physical result, it would still represent an approximate result. If you continued to roll the dice again and again, the result would become less and less approximate.

 A Monte Carlo simulation is the mathematical representation of this process. It allows you to simulate the act of physically rolling the dice and lets you specify how many times to roll them. Each roll of the dice represents a single iteration in the overall simulation; as you increase the number of iterations, the simulation results become more and more accurate. For each iteration, variable inputs are generated at random to simulate conditions such as dice design, rolling surface, and throwing technique. The results of the simulation would provide a statistical representation of the physical experiment described above.

- Bayesian Statistics is fundamentally all about modifying conditional probabilities – it uses prior distributions for unknown quantities which it then updates to posterior distributions using the laws of probability. In fact Bayesian statistics is all about probability calculations!
- MC method is some how based on the Bayesian Statistics