

# Statistical modelling of climate-sensitive diseases

Ania Kawiecki Peralta ([ania.kawiecki@bsc.es](mailto:ania.kawiecki@bsc.es))

Carles Milà Garcia ([carles.milagarcia@bsc.es](mailto:carles.milagarcia@bsc.es))

Global Health Resilience group

*Advanced Webinar Series on Spatiotemporal Modeling of Climate-Sensitive Diseases*  
*28st of January 2026*

# About us



**Barcelona  
Supercomputing  
Center**  
Centro Nacional de Supercomputación

**Ania Kawiecki Peralta**



I am a postdoc at the Global Health Resilience group at the BSC. My background is in Veterinary Medicine, and I have a PhD in Epidemiology studying dengue virus vector surveillance and control.

Currently I am working on developing R packages to facilitate disease risk modeling and prediction using Bayesian spatio-temporal models in INLA.

**Carles Milà**



I am a data scientist at the Global Health Resilience group at the BSC. My background is in statistics and geoinformatics, and I have a PhD in spatial modelling for exposure assessment.

I am currently working on developing R packages for climate-sensitive data processing and modelling.

1. Introduction: Linear model recap
2. Hierarchical generalized linear models (from a Bayesian perspective)
  - Introduction to generalized linear models
  - Basics of Bayesian inference
  - Hierarchical models
3. Model terms in a spatiotemporal context
4. Forecasting for early warning systems
5. Questions at the end!

# Linear model recap

# Linear model revisited

disease\_cases ~ rainfall + mean\_temperature

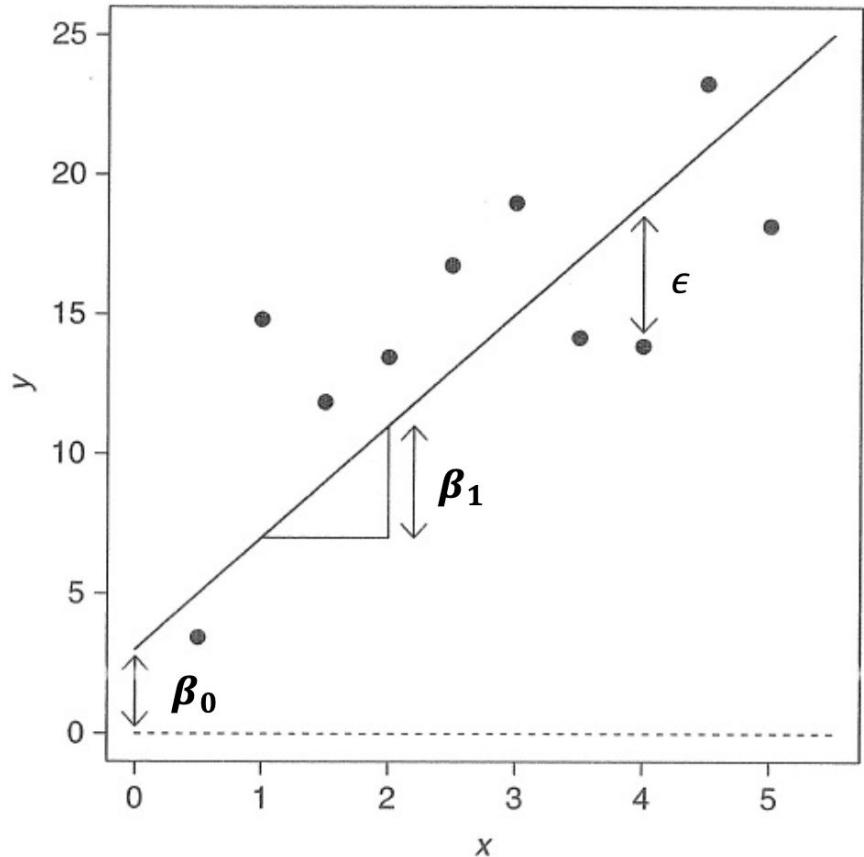
$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \epsilon_i$$

$\beta_0$  (intercept): number of dengue cases expected if rainfall = 0 and mean temperature = 0

$\beta_1$  = how many more cases you expect per 1 unit increase in rainfall, holding mean temperature constant

$\beta_2$  = how many more cases you expect per 1 unit increase in mean temperature, holding rainfall constant

$\epsilon_i$  = error term



$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \varepsilon_i \quad \text{where} \quad \varepsilon_i \sim N(0, \sigma)$$

What are (some) of the assumptions in this model?

- Linearity in the predictors: In the last webinar we saw that some variables have non-linear effects.
- Conditional independence of the observations: Our data are structured in space and time and therefore have autocorrelation.
- The response is Normally distributed conditional on the predictors and parameters: Not true for disease case counts.

$$Y_i | \mu_i, \sigma^2 \sim N(\mu_i, \sigma^2)$$

$\mu$ : mean of the distribution

$$\mu_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

$\sigma^2$ : variance of the distribution

disease\_cases ~ rainfall + mean\_temperature

## There's room for improvement!

How can we take into account the disease **seasonality**?

How can we account for differences and correlation between **spatial areas**?

Can we improve the model to reflect the **distribution** of the case count data?

How can we take into account the **interannual variation** in cases?

How can we incorporate **non-linear** relationships?

How do we use this model for **forecasting** and to account for **uncertainty**?

# Hierarchical generalized linear models (from a Bayesian perspective)

- Introduction to generalized linear models
- Basics of Bayesian inference
- Hierarchical models

# Generalised linear model: motivation

Our linear model:

$$Y_i | \mu_i, \sigma^2 \sim N(\mu_i, \sigma^2)$$

$$\mu_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

Some reasons this is problematic to predict disease case counts:

- We could predict negative cases (e.g. -2)
- We could predict non-integer cases (e.g. 4.3)
- Assumes that the variance is constant and is independent from the mean.
  - We know that the variance of a count scales with the mean: If the mean count  $\mu$  is large, the variance  $\sigma^2$  will also be larger.

# Generalised linear model: components

Enter the Generalized Linear Model (GLM)

$\mu$ : The mean of  
the distribution

$f$ : A distribution in the  
*Exponential family*

$\theta$ : Other parameters of  
the model

$$Y_i | \mu_i, \theta \sim f(\mu_i, \theta)$$

$$g(\mu_i) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

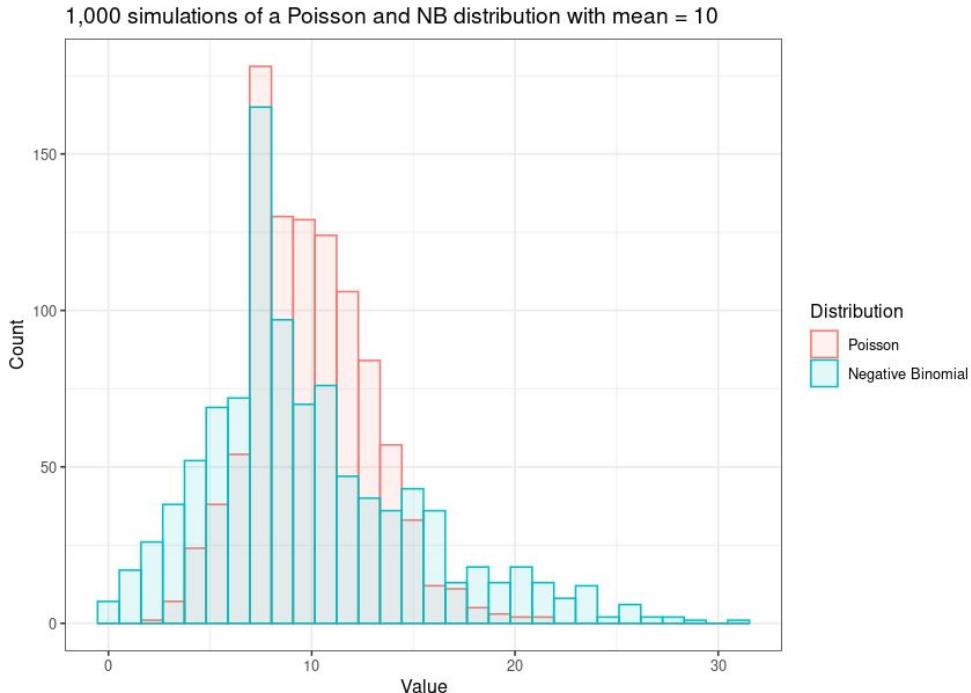
$g$ : Link function

Linear predictor

# Generalised linear model: distributions

Distributions suitable for count data  
(integer support):

- **Poisson:**  
variance = mean
- **Negative Binomial:**  
variance > mean  
(i.e. *overdispersion*)



Disease case counts usually exhibit *overdispersion*:  
Negative Binomial is often used

# Generalised linear model: link function

As a link function, we use the *log*. Therefore, our GLM tailored for case counts becomes:

$$Y_i | \mu_i, \theta \sim \text{NegBin}(\mu_i, \theta)$$

$$\log(\mu_i) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

Why use the *log* as link function?

- Ensures that the mean is positive.

$$\mu_i = \exp(\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2})$$

- Multiplicative effect of covariates, useful to capture skewed case counts.

$$\mu_i = \exp(\beta_0) \cdot \exp(\beta_1 x_{i1}) \cdot \exp(\beta_2 x_{i2})$$

# Generalised linear model: interpreting coefficients

How can we interpret the model coefficients  $\square_1$  and  $\square_2$ ?

$$Y_i | \mu_i, \theta \sim \text{NegBin}(\mu_i, \theta)$$
$$\log(\mu_i) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

- $\square_1$ : increasing the temperature by 1 makes the  $\log(\mu_i)$  increase by  $\square_1$ 
  - $\square_1 < 0$  means a decrease in risk while  $\square_1 > 0$  means an increase in risk.
- $\exp(\square_1)$ : can be interpreted as the multiplicative factor on the mean count per unit increase in temperature. Why?

$$\begin{aligned}\mu_i(x_{i1} + 1) &= \exp(\beta_0 + \beta_1(x_{i1} + 1) + \beta_2 x_{i2}) \\ &= \exp(\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}) \cdot \exp(\beta_1) \\ &= \mu_i(x_{i1}) \cdot \exp(\beta_1)\end{aligned}$$

# Generalised linear model: population offset

We have disease case counts that vary in space and time:

- The population at risk varies in time and space so it's difficult to compare counts.
- Could we standardize them somehow?



Population  
at risk

$$Y_i | \mu_i, \theta \sim \text{NegBin}(\mu_i, \theta)$$

$$\log\left(\frac{\mu_i}{P_i}\right) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

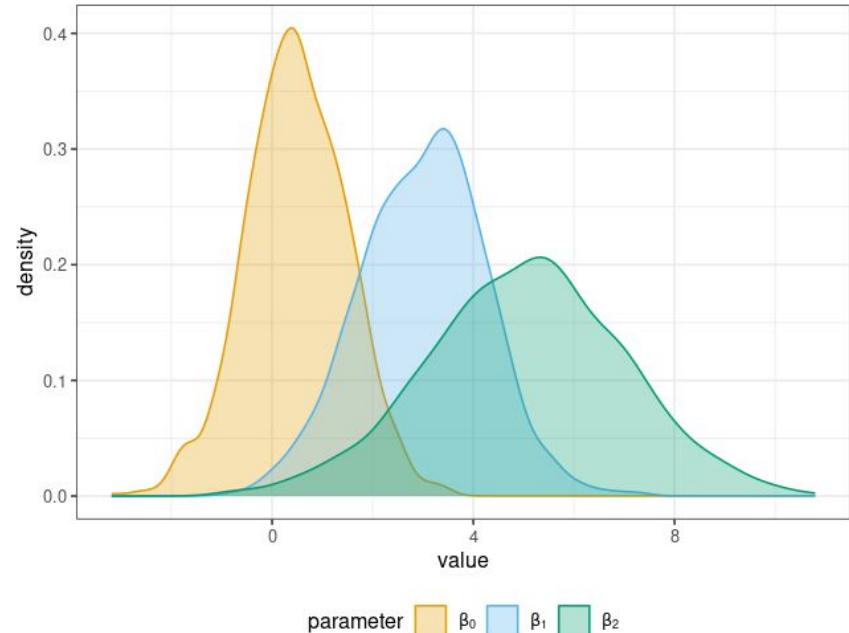
$$\log(\mu_i) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \log(P_i)$$

We add a population offset  
to model rates rather than  
counts

# Bayesian inference

Bayesian inference allows us to estimate model parameters while characterizing their uncertainty through their **full probability distributions**.

$$Y_i|\mu_i, \theta \sim \text{NegBin}(\mu_i, \theta)$$
$$\log(\mu_i) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \log(P_i)$$

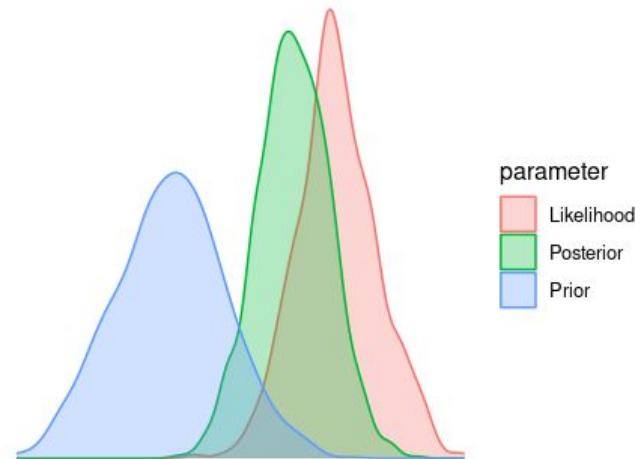


# Bayesian inference : likelihood, priors and posteriors

3 main components in Bayesian estimation:

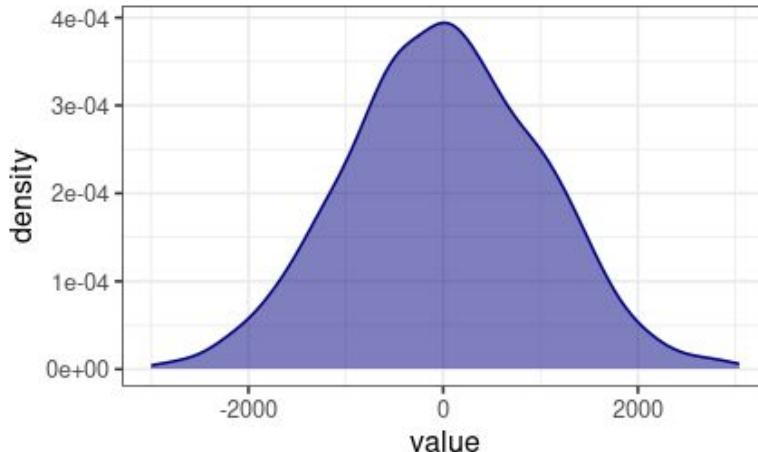
- Prior distribution: Our **prior beliefs** about the parameters before observing the data.
- Likelihood: How probable the **observed data** are given the model parameters.
- Posterior distribution: **Updated beliefs** about the parameter after observing the data.

Bayesian inference updates the prior using the information in the data (likelihood) to get the posterior.



# Bayesian inference : how to choose priors

- Priors are specified **before fitting the model** to the current data
- Unless we have very strong evidence, weakly informative priors are often a good default.
- Weakly informative priors:
  - Allow the data to dominate when information is strong.

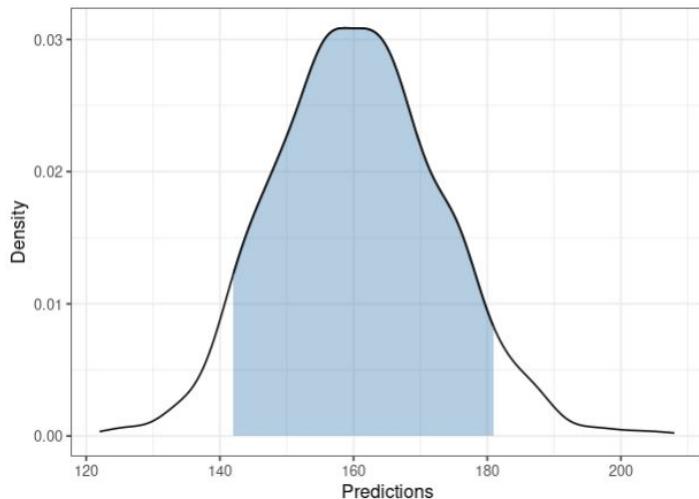


Weakly informative prior for □

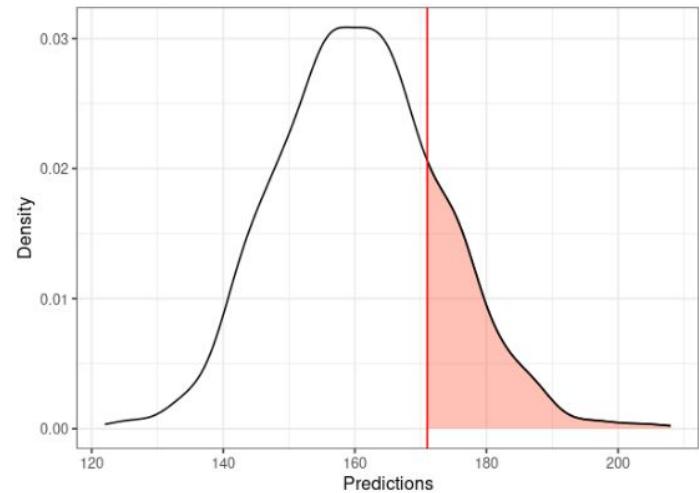
# Bayesian inference : posterior predictive distribution

Why Bayesian in early warning systems?

We also obtain a probability distribution for the predictions: **the posterior predictive distribution.**



We can calculate uncertainty intervals directly in the distribution: *credible intervals*



We can calculate the probability of exceeding a threshold: *outbreak probability*

# Hierarchical models

date	micro_name	dengue_cases	tmin	pdsi	meso_name	water_network
2001-01-01	Alto Taquari	0	22.33064	-0.67288578	Centro Norte De Mato Grosso Do Sul	86.21000
2001-02-01	Alto Taquari	2	22.09503	-0.79167610	Centro Norte De Mato Grosso Do Sul	86.21000
2001-03-01	Alto Taquari	6	21.65975	0.19557676	Centro Norte De Mato Grosso Do Sul	86.21000
⋮						
2001-01-01	Aquidauana	1	22.94171	1.60573995	Pantanais Sul Mato-Grossense	84.18500
2001-02-01	Aquidauana	0	22.75295	2.24432206	Pantanais Sul Mato-Grossense	84.18500
2001-03-01	Aquidauana	5	22.04041	1.54781866	Pantanais Sul Mato-Grossense	84.18500
⋮						
2001-01-01	Baixo Pantanal	0	23.50009	0.08895861	Pantanais Sul Mato-Grossense	84.18500
2001-02-01	Baixo Pantanal	1	23.27970	0.25999102	Pantanais Sul Mato-Grossense	84.18500
2001-03-01	Baixo Pantanal	1	22.71204	0.26609710	Pantanais Sul Mato-Grossense	84.18500

# Hierarchical models

*i*: individual-level

*j*: group-level

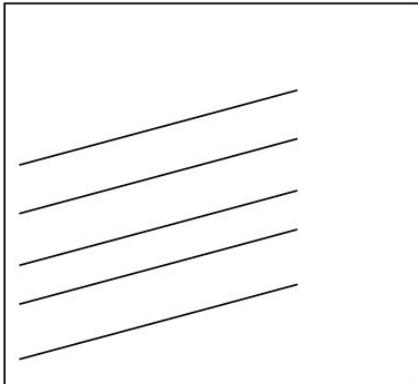
date	micro_name	dengue_cases	tmin	pdsi	meso_name
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2001-03-01	Baixo Pantanal	1	22.71204	0.26609710	Pantanais Sul Mato-Grossense

meso_name	water_network
Centro Norte De Mato Grosso Do Sul	86.21000
Pantanais Sul Mato-Grossense	84.18500
Sudoeste De Mato Grosso Do Sul	78.20667
Leste De Mato Grosso Do Sul	79.41250

## How to handle variation between groups

### Single-level/non-hierarchical approach

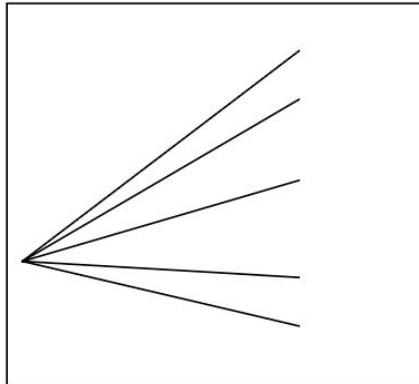
#### Varying intercepts



$$y_i = \alpha_{j[i]} + \beta x_i + \epsilon_i$$

The average number of cases observed at the mean temperature in each region varies, but the effect of temperature on dengue cases is the same

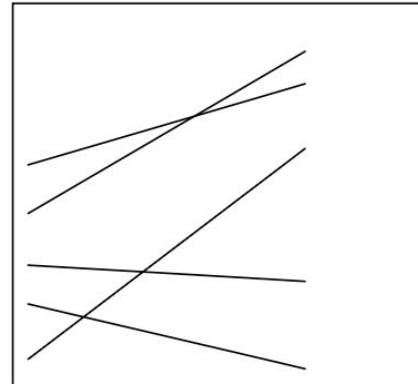
#### Varying slopes



$$y_i = \alpha + \beta_{j[i]} x_i + \epsilon_i$$

The average number of cases observed at the mean temperature in each region is the same, but the effect of temperature on dengue cases varies

#### Varying intercepts and slopes



$$y_i = \alpha_{j[i]} + \beta_{j[i]} x_i + \epsilon_i$$

The average number of cases observed at the mean temperature in each region varies, AND the effect of temperature on dengue cases varies

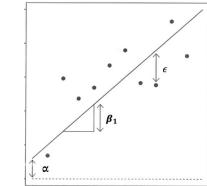
where  $j[i]$  is the group corresponding to individual  $i$

## How to handle variation between groups

**(1) Complete pooling:** assumes there are no differences between the groups. (Equivalent to taking the average number of cases over the entire population or simple linear regression).

$$y_i \sim N(\mu_i, \sigma^2)$$

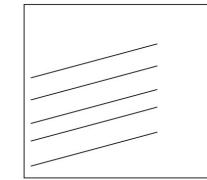
$$\mu_i = \alpha + \beta x_i$$



**(2) No pooling:** assumes that each group tells us nothing about any other group. (Equivalent to a separate linear regression for each group or a varying intercept model).

$$y_i \sim N(\mu_i, \sigma^2)$$

$$\mu_i = \alpha_{j[i]} + \beta x_i$$



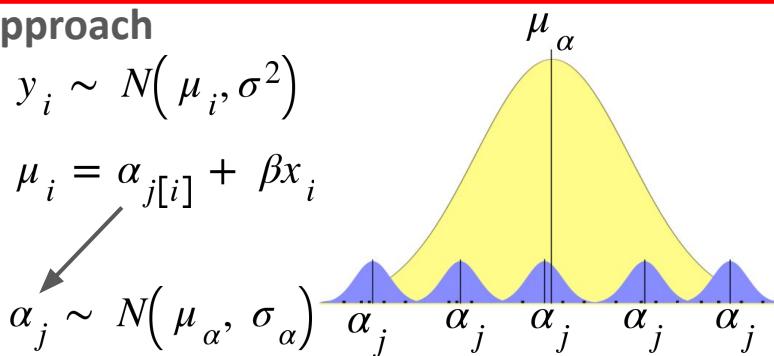
**(3) Partial pooling:** pools information across groups by assigning a probability distribution to each group intercept, pulling the group intercept towards the total mean, but allows it to vary by group. (Allows variation of the group-level mean around the total mean).

### Multilevel/hierarchical approach

$$y_i \sim N(\mu_i, \sigma^2)$$

$$\mu_i = \alpha_{j[i]} + \beta x_i$$

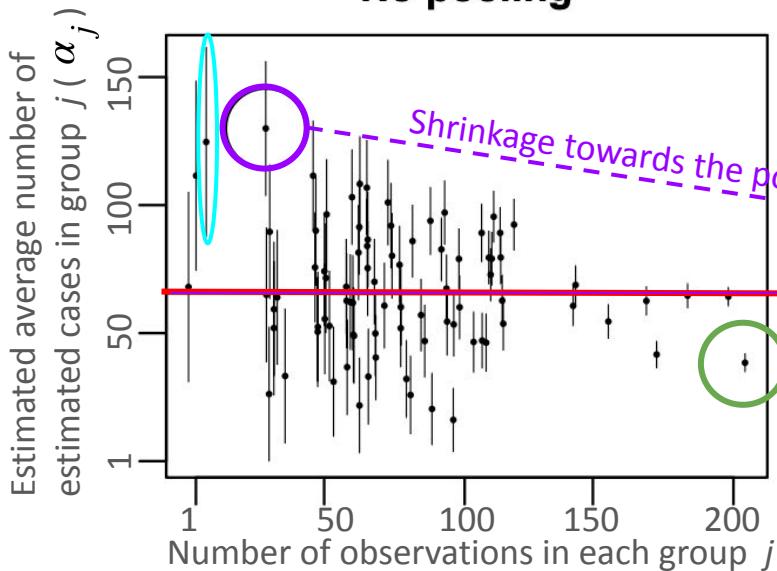
$$\alpha_j \sim N(\mu_\alpha, \sigma_\alpha)$$



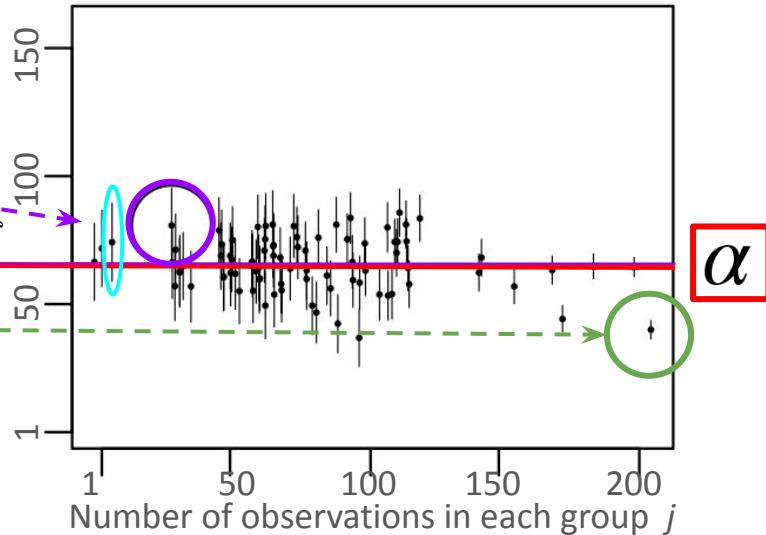
# Hierarchical models

## How to handle variation between groups

### No pooling



### Partial pooling



Complete pooling

- Estimates in groups with fewer observations are more variable with higher standard errors.
- Estimates in groups with many observations are close to estimate resulting from partial pooling.

Estimates in groups with fewer observations are closer to the complete pooling estimate.

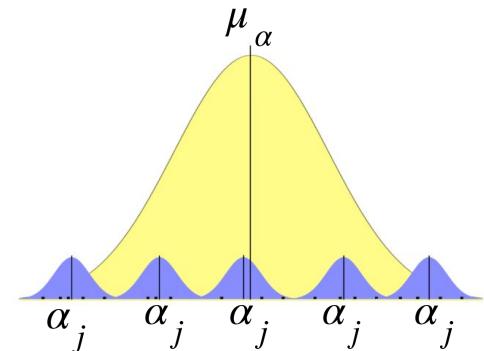
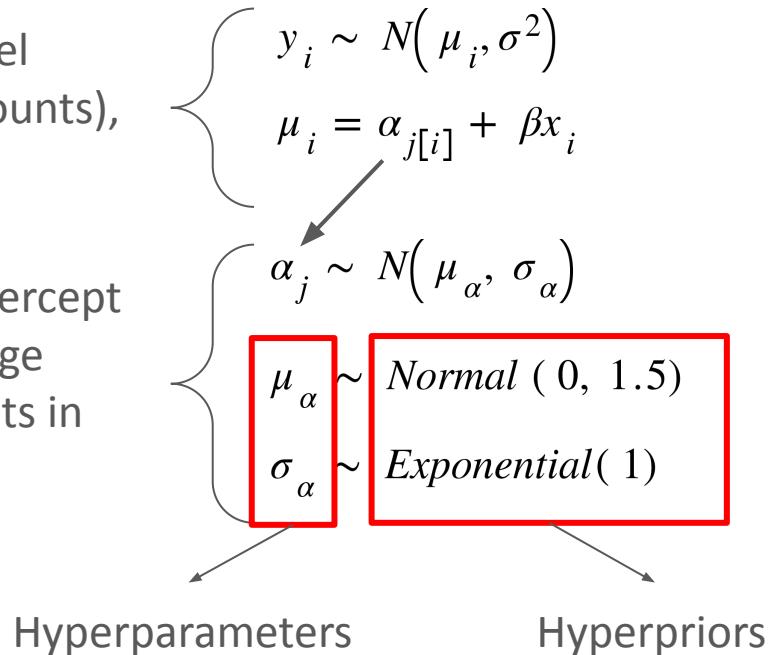
## Advantages of hierarchical models

- **Improved estimates for repeated sampling:** When more than one observation arises from the same group (individual, location, or time), then traditional, single-level models either underfit or overfit the data.
- **Improved estimates for imbalance in sampling:** When some groups are sampled more than others, multilevel models prevent over-sampled groups from unfairly dominating inference.
- **Estimates of variation:** multilevel models model variation explicitly, allowing the exploration of individual-level and group-level variation.
- **Avoid averaging, retain variation:** Frequently, scholars pre-average some data to construct variables for a regression analysis. This can be dangerous, because averaging removes variation. Multilevel models allow us to preserve the uncertainty in the original, pre-averaged values, while still using the average to make predictions.

## Multilevel/hierarchical approach

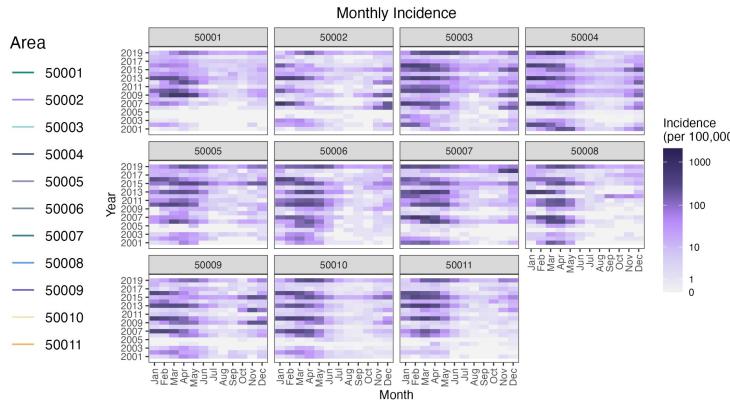
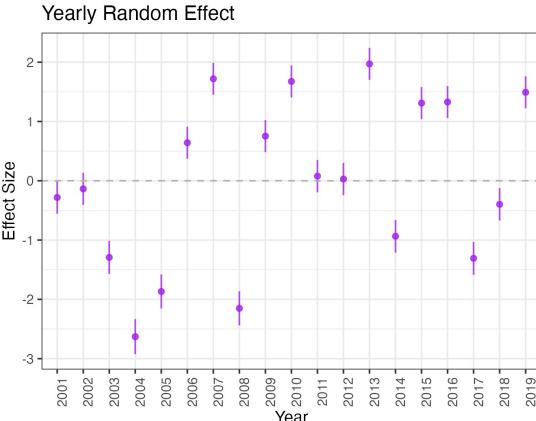
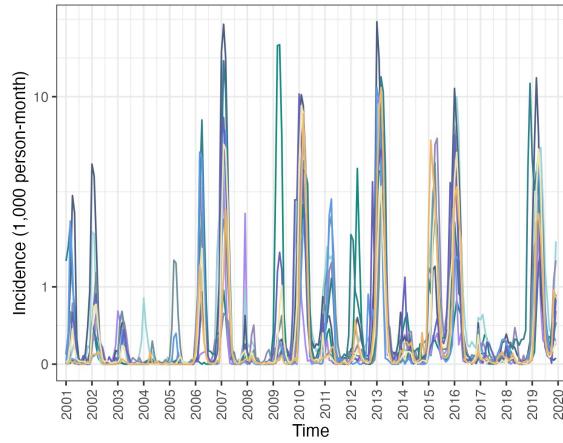
Estimates  $y$ , the model outcome (e.g. case counts), for each observation

Estimates  $\alpha_j$ , the intercept per group (e.g. average number of case counts in each region)



# Model terms

# Capturing group-level uncertainty - Interannual



$$Y_{s,t} \mid \mu_{s,t}, \theta \sim \text{NegBin}(\mu_{s,t}, \theta)$$

$$\log(\mu_{s,t}) = \alpha + \gamma_{a(t)}$$

$$\gamma_a \sim \text{Normal}(0, \tau_a^{-1})$$

$$\log(\tau_a) = \theta_a$$

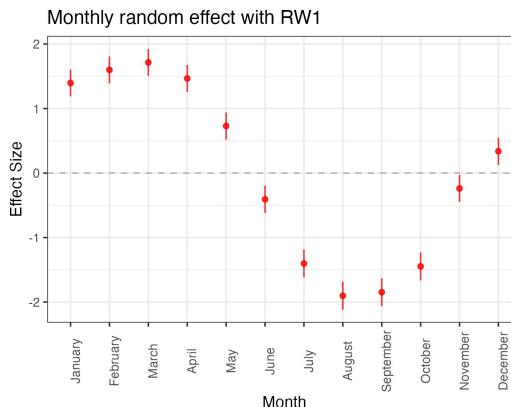
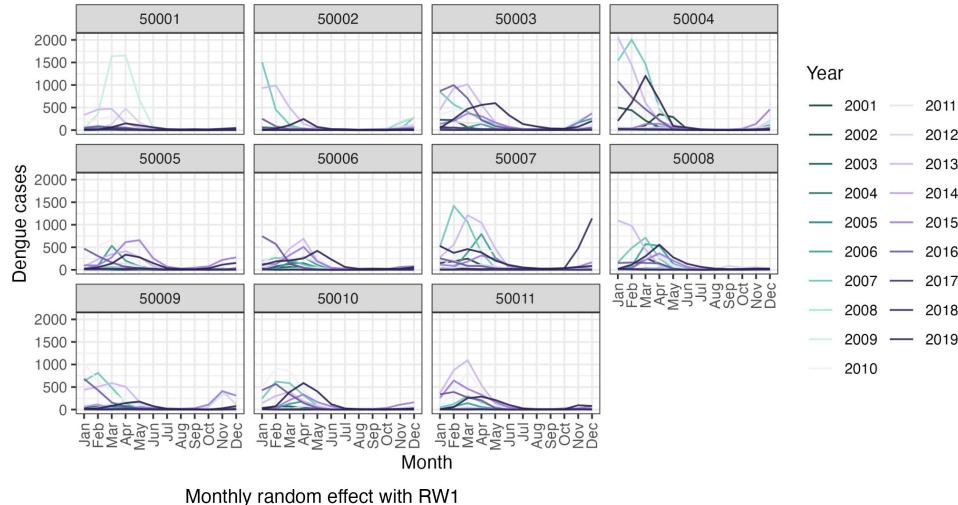
$$\theta_a \sim \text{LogGamma}(0.01, 0.01)$$

**Interannual patterns:** is there a common pattern in case incidence every several years, e.g. does every third year usually have more cases on average than July?

**Autocorrelation:** Are years close to each other more likely to have similar values?

Here we assume years are *iid*, that is, independent from each other. Other approaches: random walk order 1 or 2.

# Capturing group-level uncertainty - Seasonal



**Seasonality:** is there a common pattern in case incidence every year, e.g. does January usually have more cases on average than July?  
**Autocorrelation:** Are years close to each other more likely to have similar values?

$$Y_{s,t} \mid \mu_{s,t}, \theta \sim \text{NegBin}(\mu_{s,t}, \theta)$$

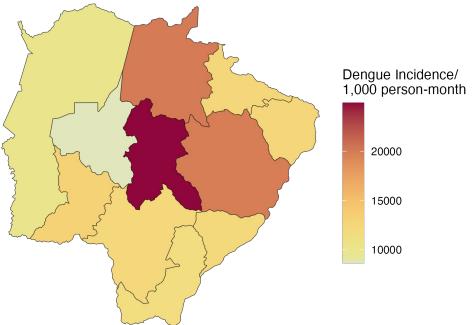
$$\log(\mu_{s,t}) = \alpha + \delta_{m(t)}$$

$$\delta_m - \delta_{m-1} \sim \mathcal{N}(0, \tau^{-1})$$

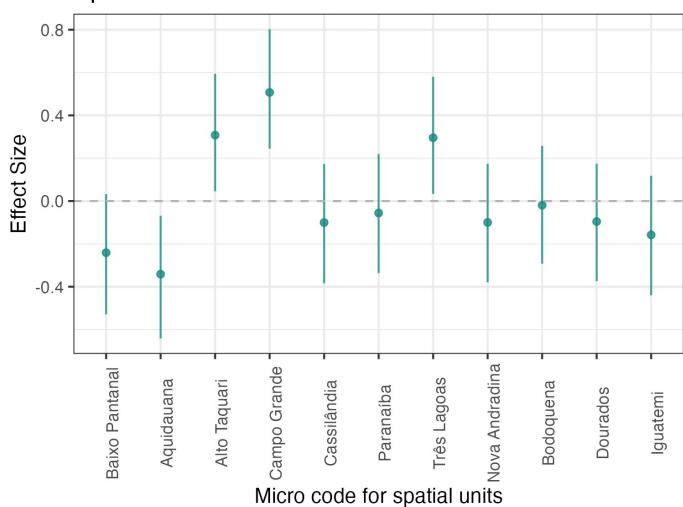
$$\tau \sim \text{Gamma}(0.01, 0.01)$$

Here we use a random walk order 1.  
 Other approaches:  
 random walk order 2.

# Capturing group-level uncertainty - Spatial

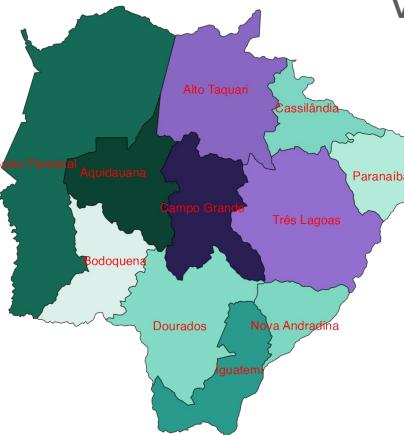


Spatial random effects



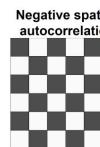
**Regional patterns:** is there a common pattern in case incidence in certain regions, e.g. do the northern regions usually have more cases on average than the southern ones?

Spatial random effects

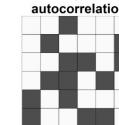


**Autocorrelation:** Are regions close to each other more likely to have similar values?

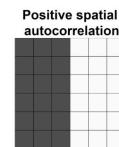
Median of the random effect  
0.40  
0.20  
0.00  
-0.20



Negative spatial autocorrelation



No spatial autocorrelation

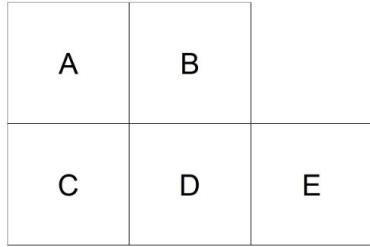


Positive spatial autocorrelation

FIGURE 8.1: Examples of configurations of areas showing different types of spatial autocorrelation.

Moraga Chapman and Hall/CRC 2019

# Capturing group-level uncertainty - Spatial



	A	B	C	D	E	Sum
A	0	1	1	1	0	3
B	1	0	1	1	1	4
C	1	1	0	1	0	3
D	1	1	1	0	1	4
E	0	1	0	1	0	2

FIGURE 7.7: Left: Areas of the study region. Right: Spatial weight matrix calculated by assuming neighboring areas share a common boundary, and sum of weights for each area.

ICAR model

$$u_i | \mathbf{u}_{-i} \sim N\left(\bar{u}_{\delta_i}, \frac{\sigma_u^2}{n_{\delta_i}}\right)$$

$$\bar{u}_{\delta_i} = n_{\delta_i}^{-1} \sum_{j \in \delta_i} u_j$$

$\delta_i$  = neighbors of area  $i$

$n_{\delta_i}$  = number of neighbors of area  $i$

**g** is an adjacency matrix used to calculate the ICAR (Intrinsic Conditional Auto-Regressive) model used for the prior of the structured spatial effect.

The effect of each area  $i$  is normally distributed with a mean equal to the average of its neighbors and a variance decreasing with the number of neighbors.

Here we use a BYM2 prior for the spatial effect. Other approaches include BYM, ICAR, CAR models

$$Y_{s,t} | \mu_{s,t}, \theta \sim \text{NegBin}(\mu_{s,t}, \theta)$$

$$\log(\mu_{s,t}) = \alpha + u_s + v_s$$

Structured  
spatial effect

Unstructured  
spatial effect

$$u_s + v_s = \sqrt{\frac{1-\phi}{\tau}} v_s^* + \sqrt{\frac{\phi}{\tau}} u_s^*$$

$$u_s^* \sim \text{ICAR}(\mathbf{g}) \quad v_s^* \sim \text{Normal}(0, 1)$$

$$\tau \sim \text{PC-Precision}(\sigma = 0.5/0.31, \alpha = 0.01)$$

$$\phi \sim \text{PC-Mixing}(\phi_0 = 0.5, \alpha = 2/3)$$

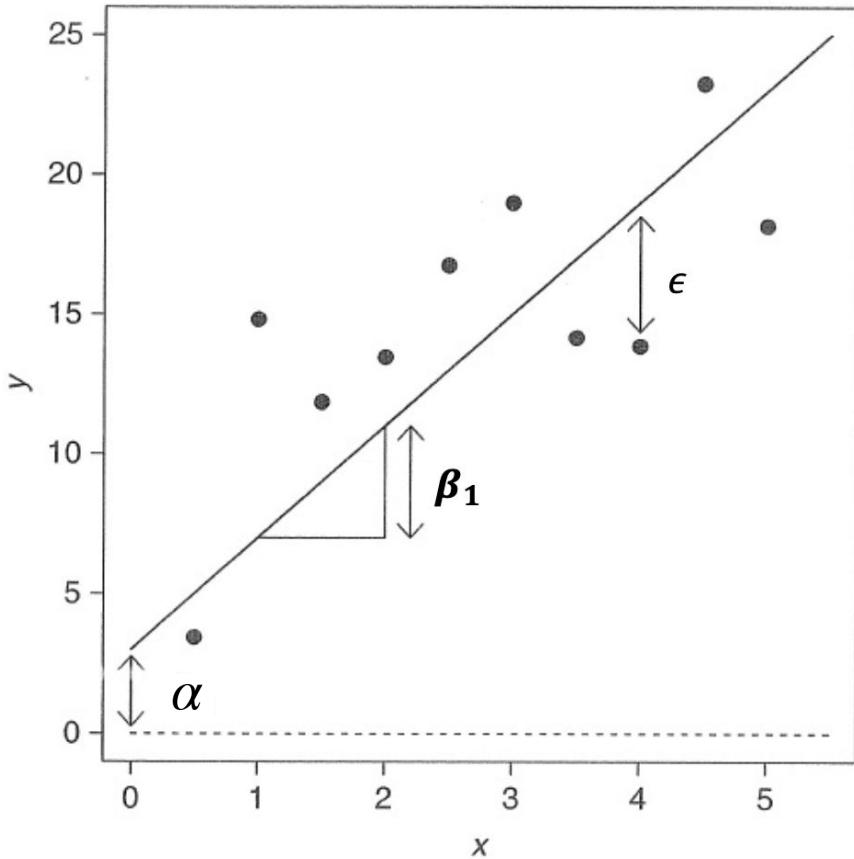
## Predictor effects - Linear

$$y_i = \alpha + \beta_1 x_{i1} + \varepsilon_i$$



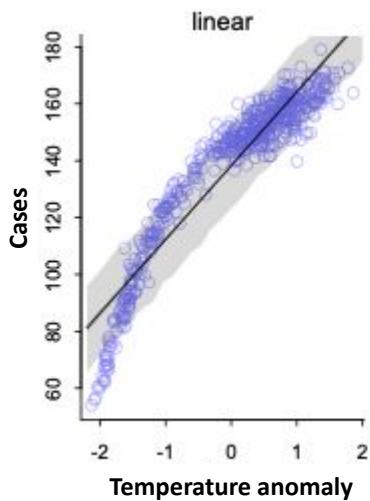
$$y_i \sim N(\mu_i, \sigma^2)$$

$$\mu_i = \alpha + \beta x_i$$

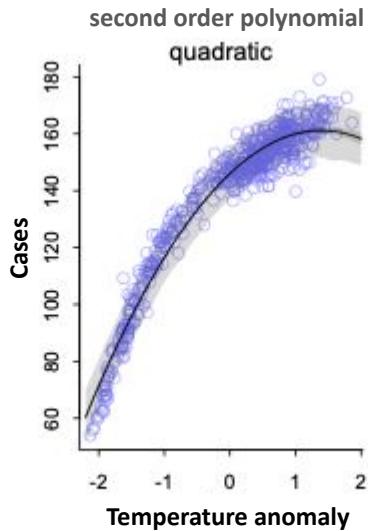


# Predictor effects - Non-linear

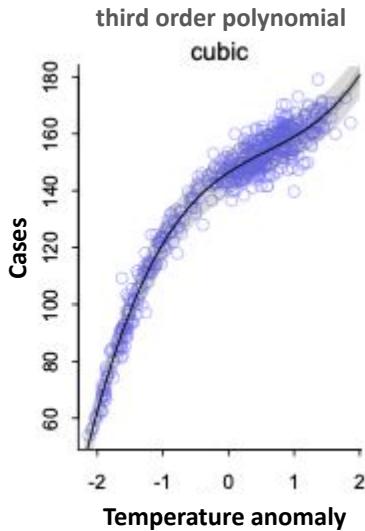
## Polynomials



$$\mu_i = \alpha + \beta_1 x_{i1}$$



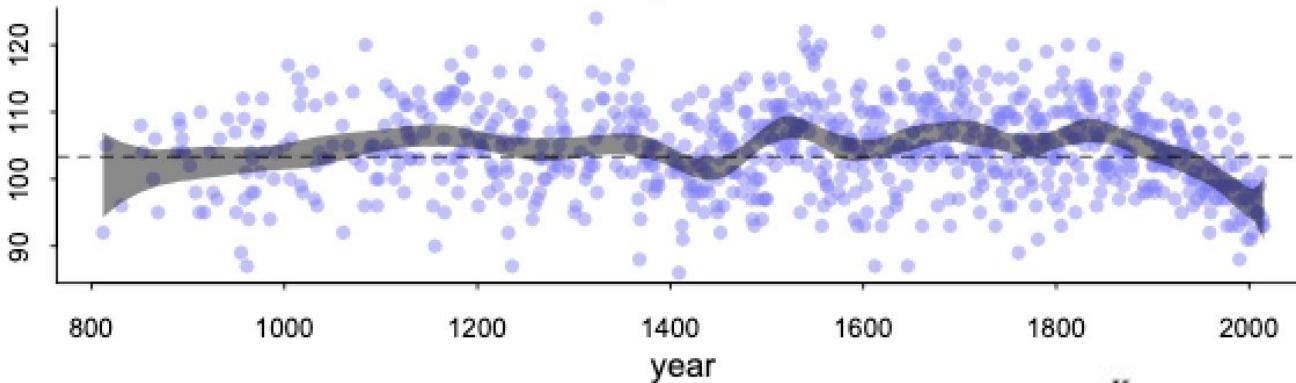
$$\mu_i = \alpha + \beta_1 x_{i1} + \beta_2 x_{i1}^2$$



$$\mu_i = \alpha + \beta_1 x_{i1} + \beta_2 x_{i1}^2 + \beta_3 x_{i1}^3$$

# Predictor effects - Non-linear

## Splines



$$\mu_i = \alpha + w_1 B_{i,1} + w_2 B_{i,2} + w_3 B_{i,3} + \dots \longrightarrow \mu_i = \alpha + \sum_{k=1}^K w_k B_{k,i}$$

parameter      basis function

Divide the range of  $x$  variable into parts.

Each part has:

**B: basis function:** a “synthetic” predictor variable

**w: weight parameter:** acts like a slope, adjusting the influence of each basis function on the mean  $\mu_i$

# Predictor effects - Non-linear

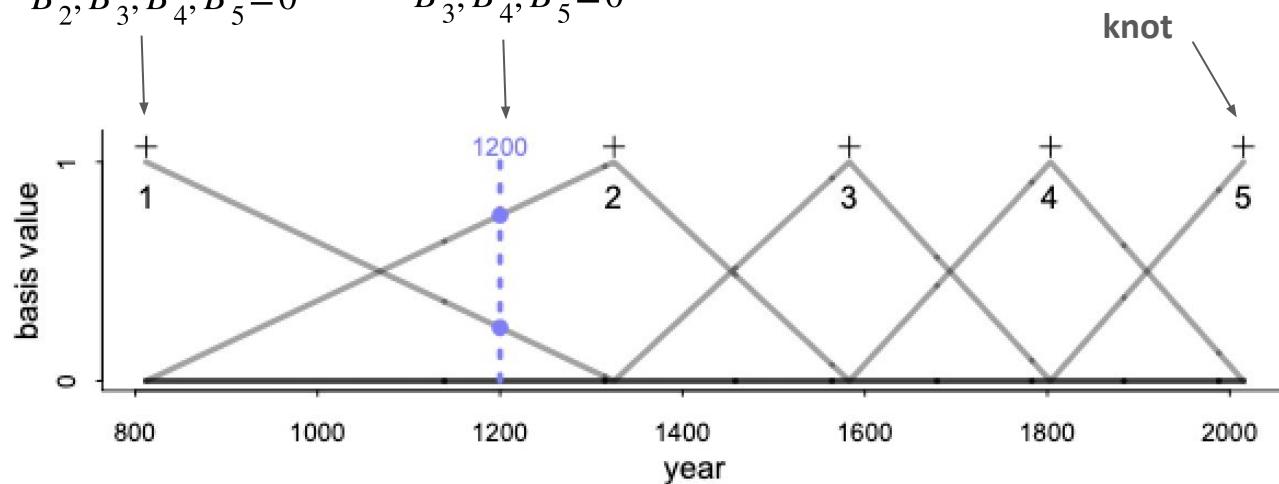
## Splines

$$B_1 = 1$$

$$B_2, B_3, B_4, B_5 = 0$$

$$B_1 \neq 0 ; B_2 \neq 0$$

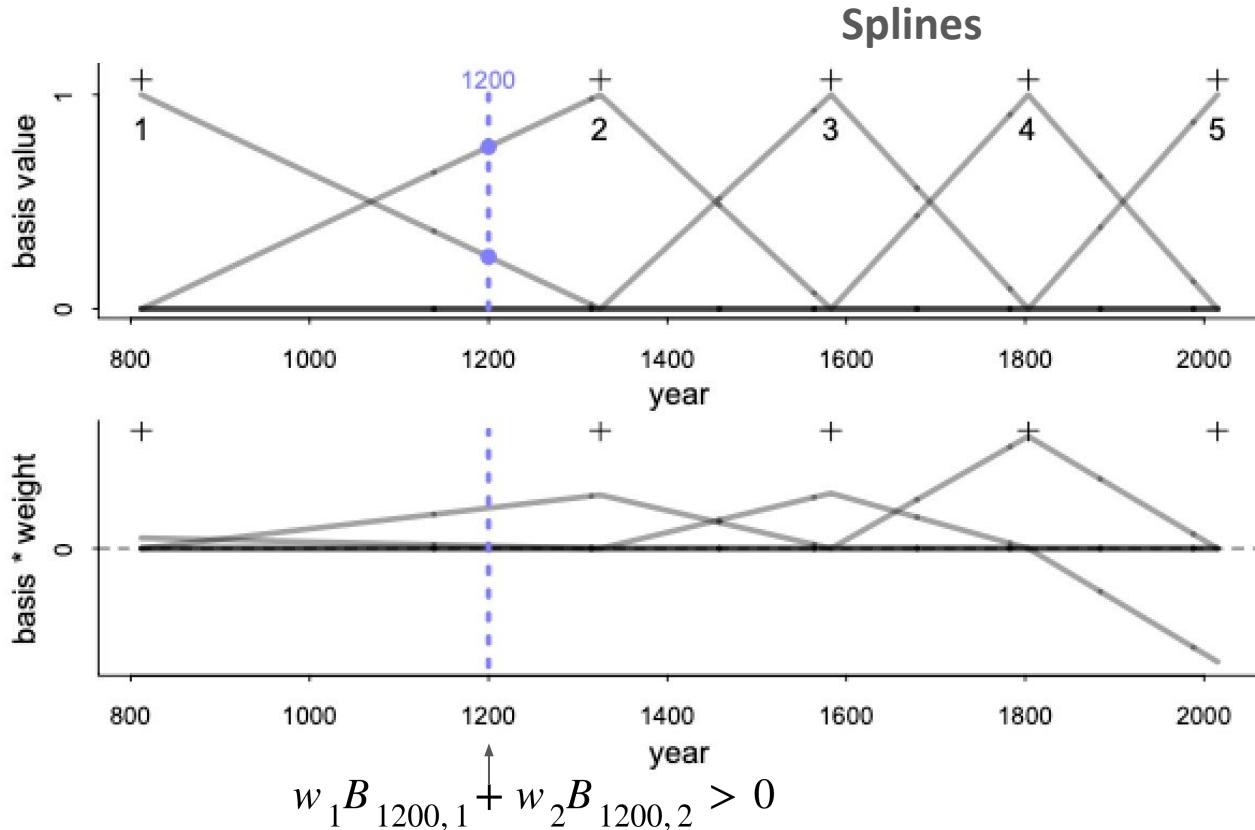
$$B_3, B_4, B_5 = 0$$



Divide the range of  $x$  variable into 4 parts using 5 **knots** placed at even quartiles of the data.

**B:** basis function:  
tells you how close  
you are to each knot.

## Predictor effects - Non-linear

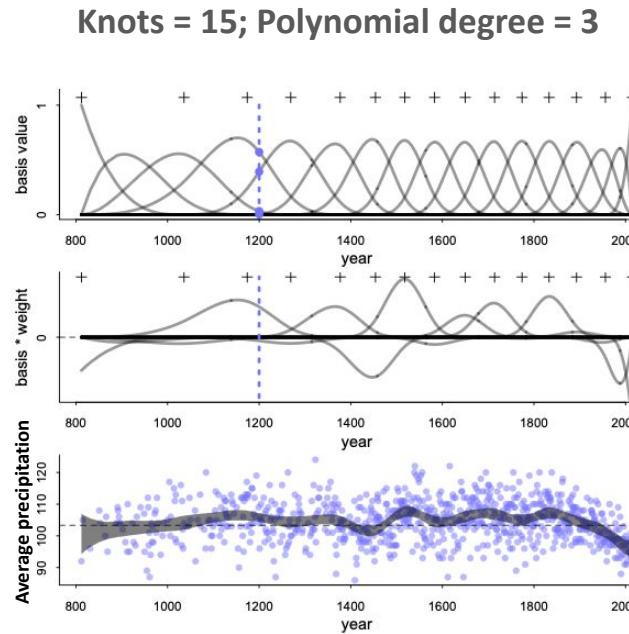
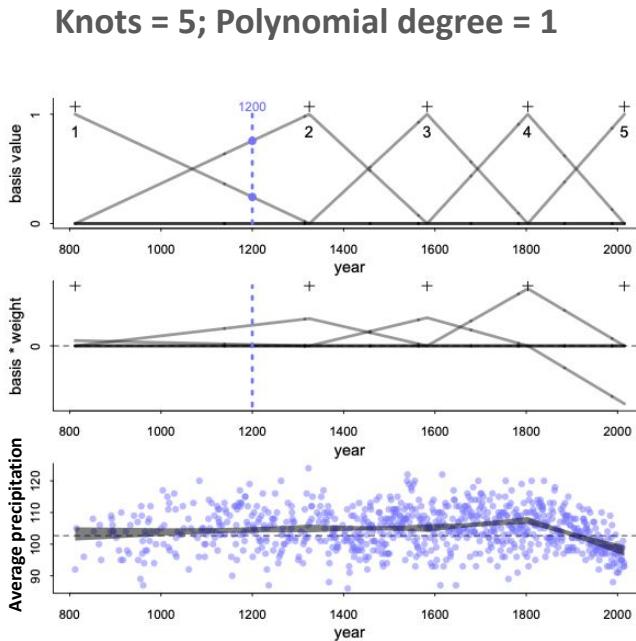


**w: weight parameters:**  
are estimated by fitting  
the model to the data.  
They can be positive or  
negative.

Each basis function ( $B$ ) is  
multiplied by its  
corresponding weight  
parameter ( $w$ ).  
To predict for a given  
value of  $x$ , add the  
weighted basis functions  
for that value.

# Predictor effects - Non-linear

## How to define spline flexibility?

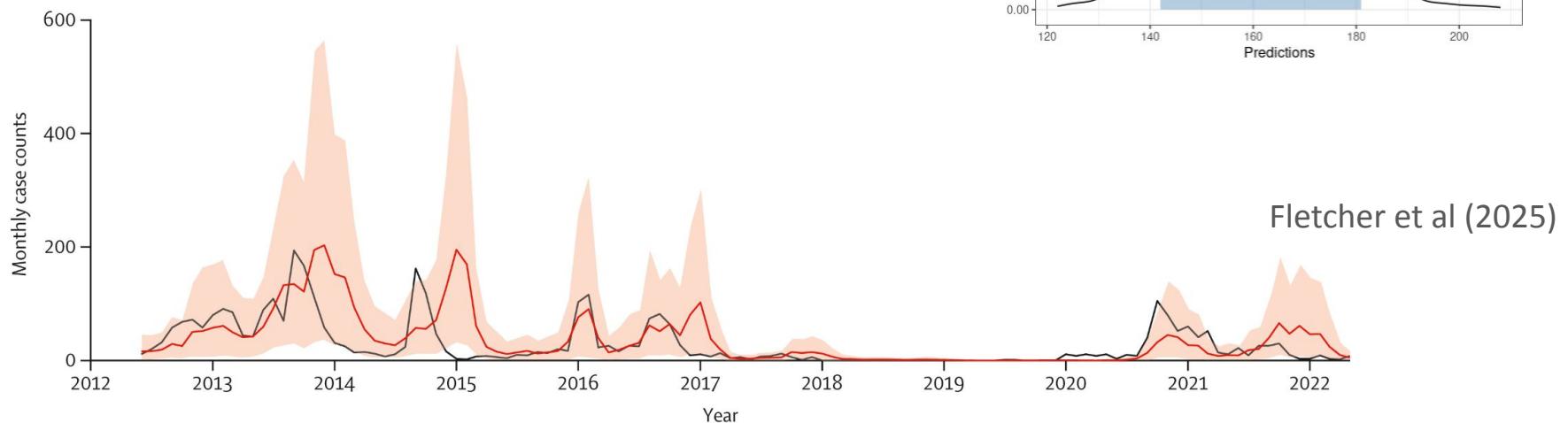


- **Number of knots**
- **Placement of knots:**  
Usually at evenly spaced intervals (equal number of  $x$  values) or quantiles (equal number of observations)
- **Polynomial degree:**  
defines how many basis functions combine at each point (value of  $x$ ), that is, how many parameters interact to produce the spline.

# Forecasting for early warning systems

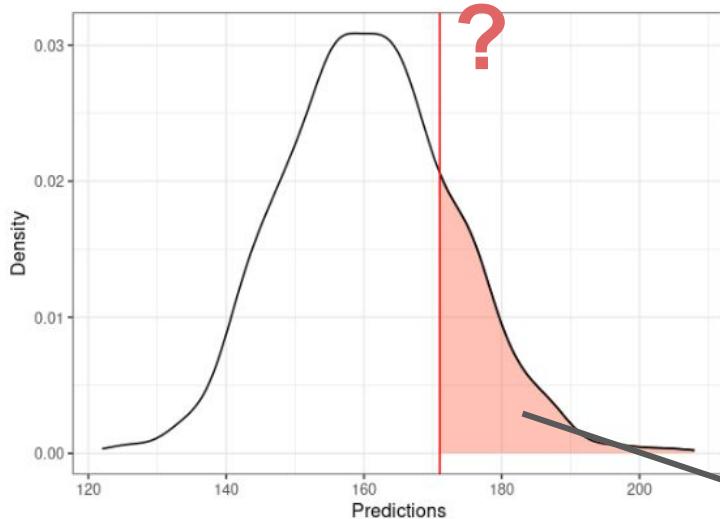
# Early warning systems: Predicting case counts

With the fitted model, we can predict case counts (posterior predictive distribution).



Alternatively, we can communicate our predictions in terms of outbreaks (yes/no) that can trigger the early warning system.

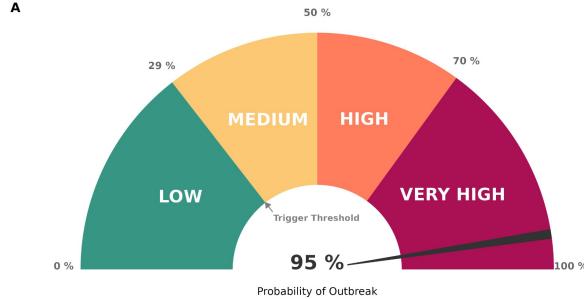
How do we define the outbreak threshold?



- A quantity defined with the stakeholders.
- A certain quantile of the observed cases.
- Mean +  $\phi \cdot SD$ .

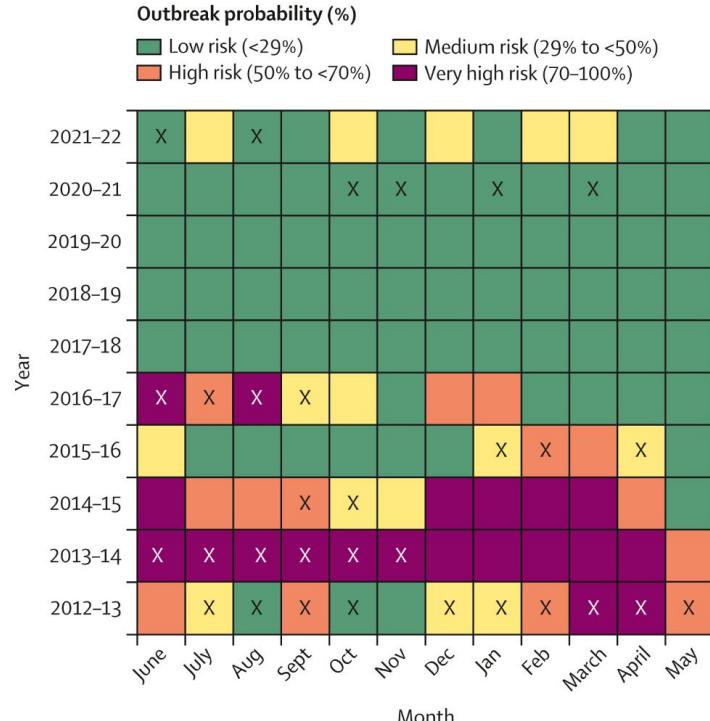
We can calculate the probability of exceeding a threshold: *outbreak probability*

# Early warning systems: computing probability trigger threshold



We can communicate the probability of outbreaks using different ranges

We can also see how our systems performs using cross-validation





# Acknowledgements

The GHR team!!



PROF RACHEL LOWE  
LEADING RESEARCHER



DR GIOVENALE MOIRANO  
VISITING  
RESEARCHER



DR MARTIN LOTTO  
RESEARCHER



CHLOE FLETCHER  
PHD CANDIDATE

# Time for questions

**Ania Kawiecki Peralta** ([ania.kawiecki@bsc.es](mailto:ania.kawiecki@bsc.es))

**Carles Milà Garcia** ([carles.milagarcia@bsc.es](mailto:carles.milagarcia@bsc.es))

# Useful resources if you want to know more

Gelman, A., & Hill, J. (2006). *Data Analysis Using Regression and Multilevel/Hierarchical Models*. Cambridge University Press.  
<https://doi.org/10.1017/CBO9780511790942>

McElreath, R. (2020). *Statistical Rethinking: A Bayesian Course with Examples in R and STAN* (2nd ed.). Chapman and Hall/CRC.  
<https://doi.org/10.1201/9780429029608>

Moraga, P. (2019). *Geospatial Health Data: Modeling and Visualization with R-INLA and Shiny*. Chapman & Hall/CRC Biostatistics Series.  
<https://www.paulamoraga.com/book-geospatial/index.html> (FREE ONLINE RESOURCE)

Dogucu, M., Ott, M. Q. O., Johnson, A. A. (2021). *Bayes Rules! An Introduction to Applied Bayesian Modeling*.  
<https://www.bayesrulesbook.com/> (FREE ONLINE RESOURCE)

Rowe, F. and Arribas-Bel, D. (2024) *Spatial Modelling for Data Scientists* <https://gdsl-ul.github.io/san/>  
<https://doi.org/10.17605/OSF.IO/8F6XR> (FREE ONLINE RESOURCE)

Morris, M. (2019) *Bayesian hierarchical spatial models: Implementing the Besag York Mollié model in stan*. Spatial and Spatio-Temporal Epidemiology <https://doi.org/10.1016/j.sste.2019.100301> (FREE ONLINE RESOURCE [here](#))

Fletcher, C., Moirano, G., Alcayna, T., Rollock, L., Van Meerbeeck, C. J., Mahon, R., Trotman, A., Boodram, L.-L., Browne, T., Best, S., Lührsen, D., Diaz, A. R., Dunbar, W., Lippi, C. A., Ryan, S. J., Colón-González, F. J., Stewart-Ibarra, A. M., & Lowe, R. (2025). Compound and cascading effects of climatic extremes on dengue outbreak risk in the Caribbean: An impact-based modelling framework with long-lag and short-lag interactions. *The Lancet Planetary Health*, 9(8), 101279. <https://doi.org/10.1016/j.lanplh.2025.06.003> (OPEN SOURCE)