PHY2054 General Physics II

Section 611820

Prof. Douglas H. Laurence

Exam 1 (Chapters 19 - 21)
February 25, 2018

Name:

SOLUTIONS

Instructions:

This exam is composed of 10 multiple choice questions and 4 free-response problems. To receive a perfect score (100) on this exam, 3 of the 4 free-response problems must be completed. The fourth free-response problem may not be answered for extra credit. Each multiple choice question is worth 2.5 points, for a total of 25 points, and each free-response problem is worth 25 points, for a total of 75 points. This means that your exam will be scored out of 100 total points, which will be presented in the rubric below. Please do not write in the rubric below; it is for grading purposes only.

Only scientific calculators are allowed - do not use any graphing or programmable calculators.

For multiple choice questions, no work must be shown to justify your answer and no partial credit will be given for any work. However, for the free response questions, work must be shown to justify your answers. The clearer the logic and presentation of your work, the easier it will be for the instructor to follow your logic and assign partial credit accordingly.

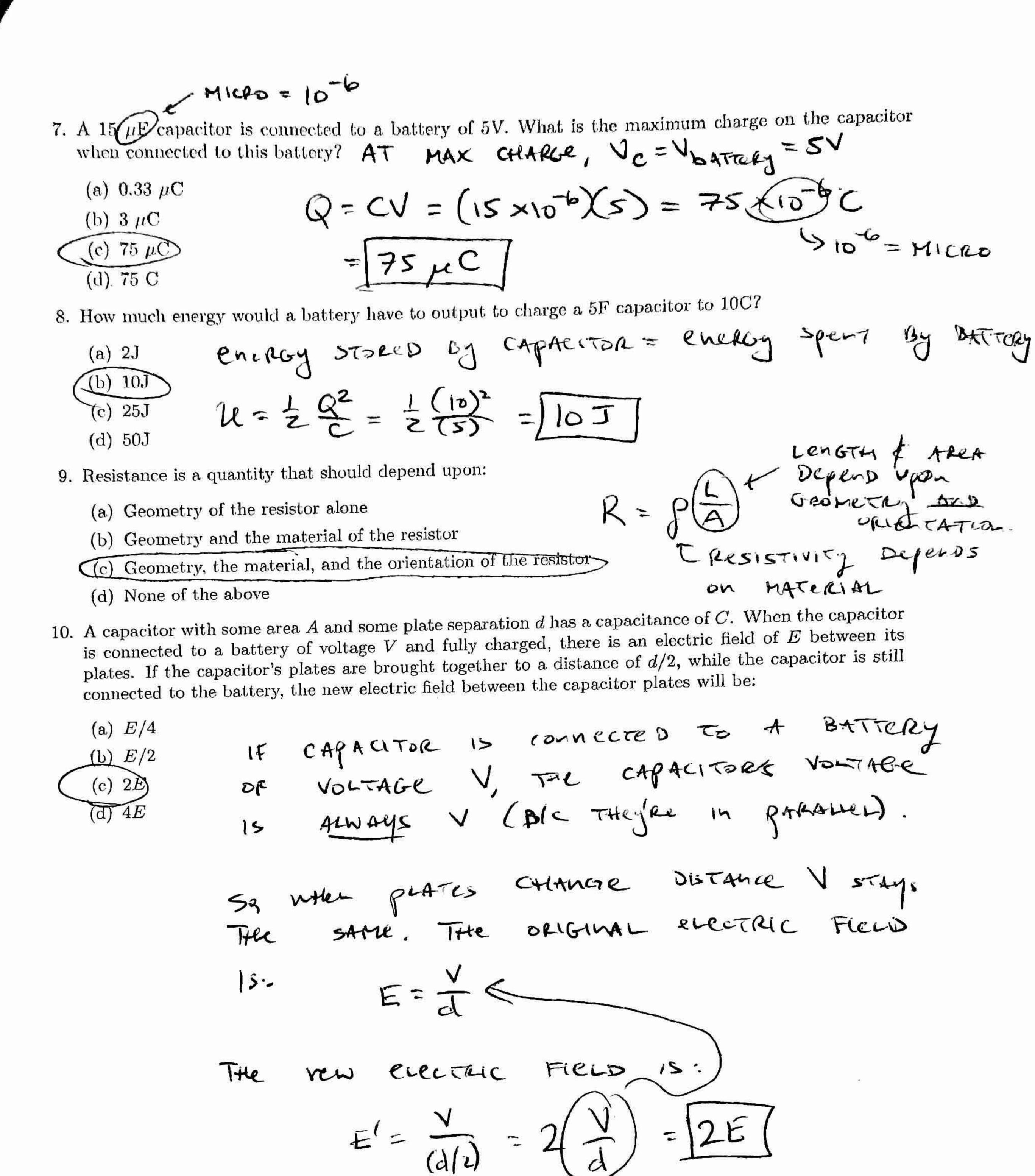
The exam begins on the next page. The formula sheet is attached to the end of the exam.

Exam Grade:

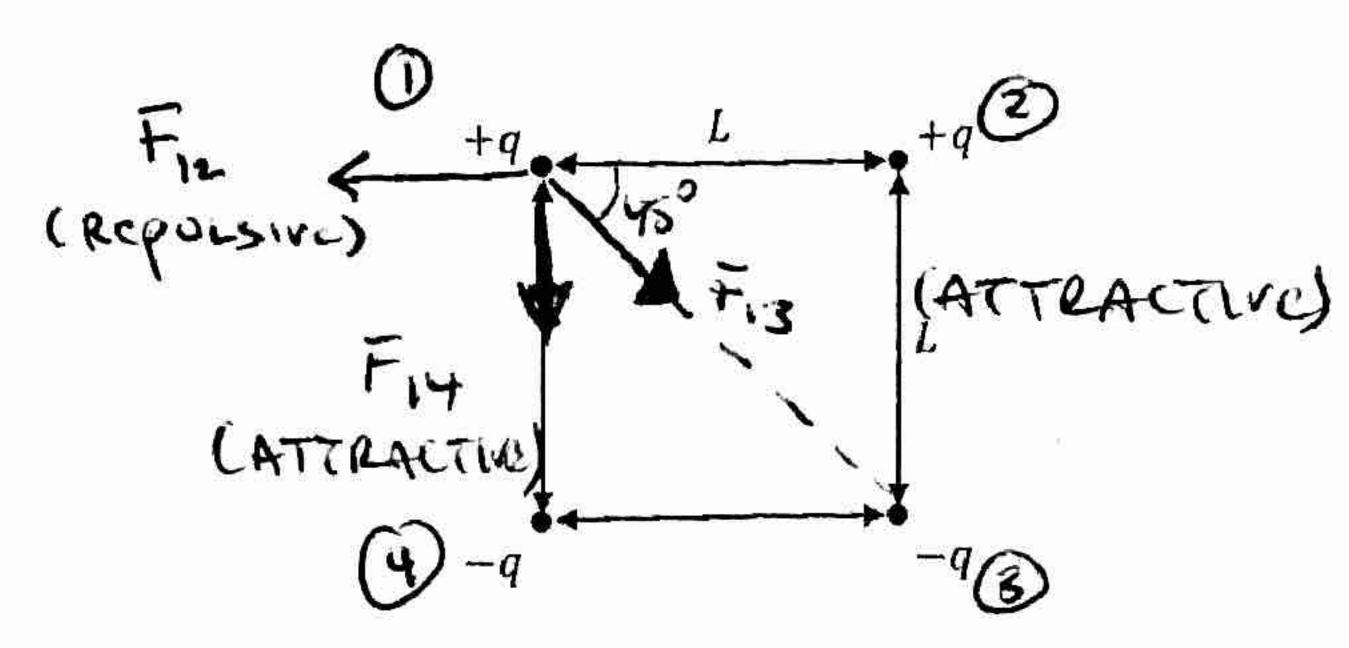
| Multiple Choice | |
|-----------------|--|
| Problem 1 | |
| Problem 2 | |
| Problem 3 | |
| Problem 4 | |
| Total | |

MULTIPLE CHOICE QUESTIONS

| 1. Most materials in nature are found to be: |
|--|
| (a) Positively charged |
| (b) Negatively charged |
| (c) Neutral |
| (d) It's random $hano = 10^{-9}$ |
| 2. A charge $Q = 1.6 \text{ nO}$ is composed of: $Q = Ne$ (FOR MAGNITUDE) (a) 10^{10} excess protons $\Rightarrow N = Q/e = (1.6 \times 10^{-9})/(1.6 \times 10^{-19})$ |
| (a) 10^{10} excess protons => $N = Q/e = (1.6 \times 10^{-10})$ |
| (b) 10^{-10} excess protons = 10^{10} |
| (c) 10^{10} excess electrons (d) 10^{-10} excess electrons Since $Q = \bigoplus 1.6nC$, These ARE [EXCESS PROTONS] |
| (U) 10 GACCOS CICCOLOTIO |
| 3. Consider a charge q_A producing an electric field. A second charge q_B feels the electric field with a magnitude E . If the distance between q_A and q_B is halved, and the charge q_B is doubled, what is the |
| magnitude E. If the distance between q_A and q_B is narrow, and we walke of the electric field felt by q_B ? $E = Felt By 9B$ is $Produce B$ 37 9A. |
| $I_{\alpha} \setminus F \setminus K$ |
| (a) E/Φ (b) $E/2$ $E_A = k \frac{g_A}{r^2 R}$ $F = \frac{1}{48} \text{ Is DoubleD, } E_A = \frac{1}{2} R + \frac{1}{2}$ |
| (c) 2E (c |
| (d) $4E \Rightarrow E_A = k \frac{74}{50} = -i \left(k \frac{94}{2}\right) = -i \left(k \frac{94}{2}$ |
| 4. Three possible surfaces enclose the same charge q . Surface S_1 is a sphere of radius 2cm with q at its center; surface S_2 is a sphere of radius 2cm with q 1cm off-center; surface S_3 is a cube of side-length center; surface S_2 is a sphere of radius 2cm with q 1cm off-center; surface S_3 is a cube of side-length |
| center; surface S_2 is a sphere of radius zell with q real spaces flux passing through it? 2cm with q at its center. Which surface has the greatest flux passing through it? |
| (a) SI GAUSS'LAW" FLUX THROUGH SURFACE PEPERDS DOLY |
| (b) So GAUSS CAN ON CHARGE ENCLOSED, MOT ON SHAPE |
| (c) S3 OF SURFALL OR POSITION OF CHARGE W/L+0 |
| (d) They all have the same flux through their surfaces |
| 5. Electrons will always move towards: every THING HONES TOWARDS LOW PORENTIAL |
| (a) High potential energy and high potential |
| (b) High potential energy but low potential $\Delta u = 9 \Delta \phi$ |
| (E) Low potential energy but high potential (-) (-) (-)(+) 30 1057 Re(+) |
| (d) Low potential energy and low potential (Following statements is true? |
| charges accumulate at some point B . Which of the following statements is true: |
| (a) The electric field points from A to B , with A being the point of low potential |
| (b) The electric field points from A to B, with B being the point of low potential |
| (c) The electric field points from B to A, with A being the point of low potential (d) The electric field points from B to A, with B being the point of low potential |
| (d) The electric field points from B to A, with B some From $\Theta \rightarrow \Theta$) From $A \tau_0 B$ |
| (A) = (A) |
| A D 3 - 3 - 3 B |
| 3 A & D |
| MONE TO B (THE G), SO B IS AT LOW POPULIAL) |
| More to B (THE 6), >0 12 12 to porter (AL) |



FREE-RESPONSE PROBLEMS



- 1. Imagine four charges arranged in the corners of an $L \times L$ square, as shown in the figure above. Consider the case of q=e and $L=10 \mathrm{cm}$.
 - (a) What is the electric force on the upper-left charge?
 - (b) What is the electric force on the lower-left charge? Hint: you can use symmetry arguments to answer this question based on how it relates to part (a).
 - (c) Imagine placing a fifth charge, +q, in the figure above. Where would it need to be placed so that the electric force on the upper-left charge is zero?

electric force on the upper-left charge is zero?

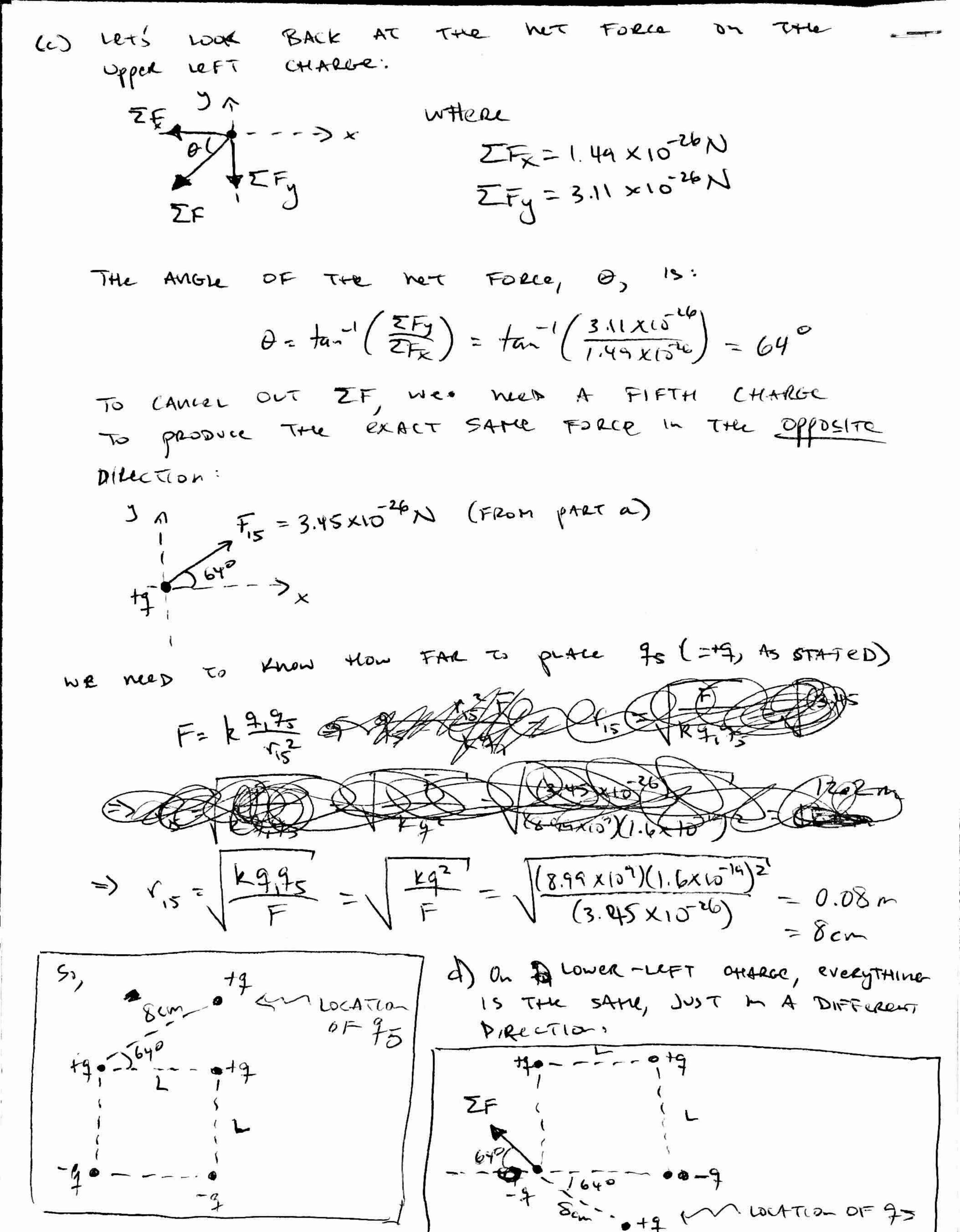
(a) ALL ELECTRIC FORCES ARE GIVEN BY CONDUMS: LAW. $\begin{bmatrix}
F_{12} = k \frac{q_1 q_2}{y_2^2} \\
F_{12} = k \frac{q_2 q_2}{y_2^2} \\
F_{13} = k \frac{q_2}{p_3^2} \\
F_{14} = k \frac{q_1 q_2}{p_3^2} \\
F_{14} = k \frac{q_2}{p_3^2} \\
F_{15} = k \frac{q_2}{p_3^2} \\
F_{16} = k \frac{q_2}{p_3^2} \\
F_{17} = k \frac{q_2}{p_3^2} \\
F_{18} = k \frac{q_2}{p_3^2} \\
F_{19} = k \frac{q_3}{p_3^2} \\
F_{19} = k$

Let's compute $F = k \frac{q^2}{L^2} = (8.99 \times 10) \frac{(1.6 \times 10^{14})^2}{(0.1)^2}$

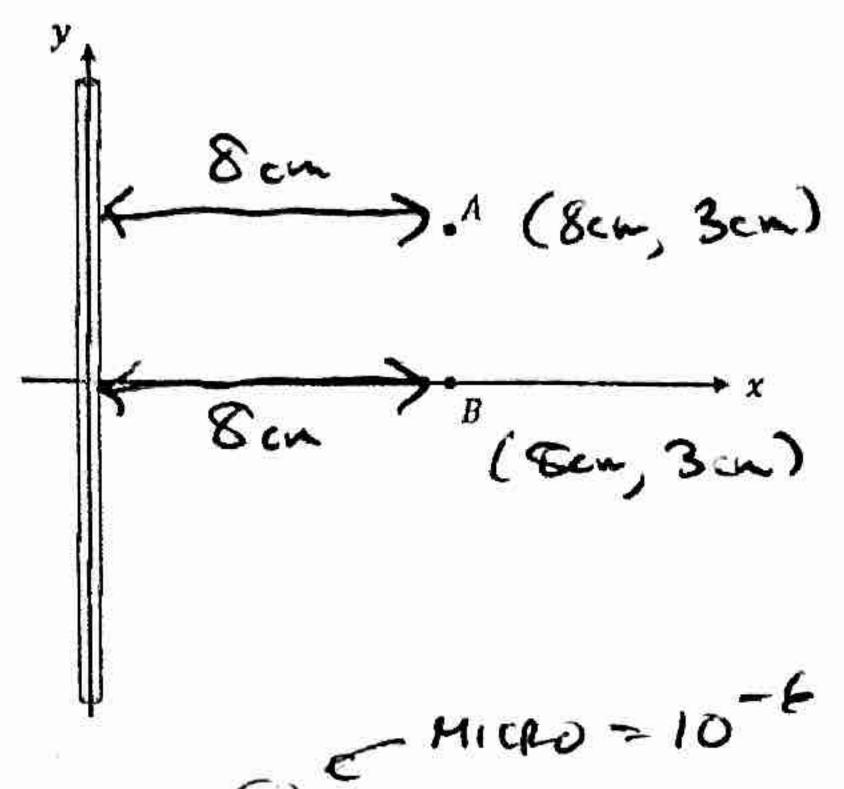
= 2.3x10⁻²⁶N

(a) Continued DRAWING THE FORCES ACTING ON Upper-LEFT CHARGE then we need to BREAK FIS OF INTO ITS X & Fis The TOTAL FORCE " $F_{13,jx} = F_{13} cos45 = \sqrt{2} F_{13}$ The same: $F_{13,jy} = F_{13} sin45 = \sqrt{2} F_{13} = \sqrt{2} \left(\frac{1}{2} k \frac{9^2}{L^2}\right)$ $=\frac{\sqrt{2}}{4}L\frac{3^2}{1^2}$ Fig Figy So, The Net Force, IF, MAS Components: ZFx=F12-F13,x= k92-12k92 2 (1-经) L 至2 EFG = Fi4 + Fisy = k== + 12 + 12 k== 2 (FROM PREV. PAGE) 323 Using F= k = 2.3 x10²⁶N, ZFx= (1-4)(2.3x1526)=1.49x1026N ZFy= (1+5)(2.3 ×10-26) = 3.11 ×10-26) => ZF= VZFx2+ ZFz2 = 10.49x1542+(3.11x15") = 3.45 x10 36 N THIS IS IDENTICAL TO PART (a), DUST W/ THE FORCES pointine in PIFFERENT PIRECTIONS. 150

TF = 3.45 × 10-26 N Next page



FOR WIFE, ALL THAT MATTERS IS THE HORIZONIA DISTANCE:



2. A very long wire has a total charge of $15(\mu C)$ and a length of 1.2m. The center of the wire is placed at the origin of a coordinate system, and the wire runs along the y-axis, as shown in the figure above.

(a) What is the electric field at the point A in the above figure, located at (8cm, 3cm)?

(b) What is the electric field at the point B in the above figure, located at (8cm, 0)?

(c) If a charge q = 5 nC was placed at point A, what would the electric force on q be?

(d) If the same charge q was placed at point B, instead, what would the electric force on q be?

(a)
$$E = \frac{\lambda}{2\pi \xi r}$$
 FOR A VORY LONG (INFINITE) WIRE.

$$\lambda = \frac{Q}{L} = \frac{15\mu C}{1.2m} = 12.5 \times 10^{-6} \frac{C}{m}$$
(12.5 × 10⁻⁶)

=) $E_{A} = \frac{(12.5 \times 10^{6})}{2\pi (8.85 \times 15^{19})(0.08)} = \frac{2.81 \times 10^{6} \text{ N}}{2}$ 8cm = 0.08m

(6) Point B 15 LOCKTED AT THE SAME

HORIETAL DISTANCE TO A) SO /Eg = 2.81 X10 C

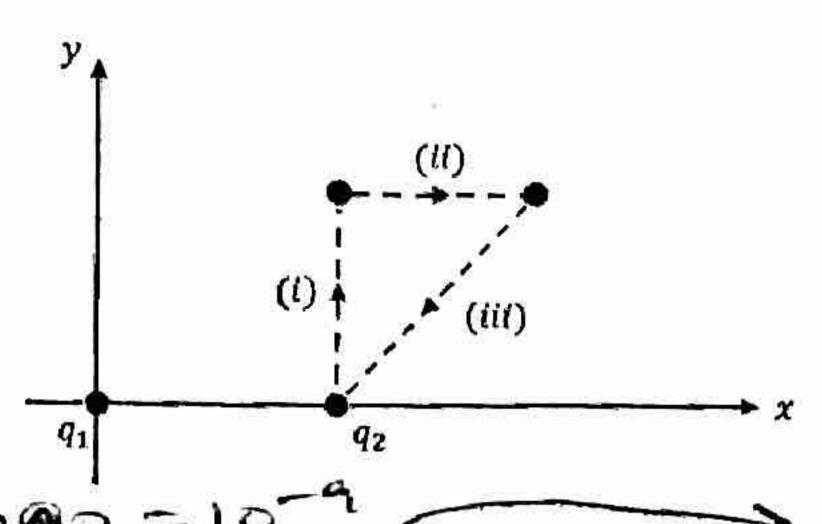
(e) Farce possible Given by F=qE

=> FA = 9 EA = (5x151)(2.81 X186) = [0.014N]

(d) since EB=EA,

THE FORCES ARE THE SAME AS WELL:

1FB - 0014N



- 3. A charge $q_1 = -10$ kC is fixed at the origin. A second charge $q_2 = 25$ in the moved along the following path, as shown in the figure above: (i) q_2 is moved from (10cm, 0) to (10cm, 5cm); (ii) q_2 is then moved from (10cm, 5cm) to (15cm, 5cm); (iii) q_2 is then moved back to its starting point.
 - (a) How much work does the electric force do on q_2 along path (i)?
 - (b) How much work does the electric force do on q_2 along path (ii)?
 - (c) How much work does the electric force do on q_2 along path (iii)?
 - (d) What is the work done along the entire path? What does this answer signify about the electric force? Hint: the total path taken by the charge is a closed loop.

$$\frac{1}{3}$$
 $\frac{1}{3}$ $\frac{1}$

ALL CALCULATIONS ARE GOING TO DEPEND on?

$$W_{ii} = k 4.9 \cdot 2 \left(\frac{1}{r_i} - \frac{1}{r_f} \right) = (-2.25 \times 10^4) \left(\frac{1}{0.1} - \frac{1}{0.112} \right) = \left[-2.41 \times 10^6 \right]$$

$$92 \frac{15^{2}+52}{42} = 15.8 \text{ cm}$$
 $92 \frac{15^{2}+52}{42} = 0.158 \text{ m}$
 150 m

$$W_{(ii)} = kq_{1}q_{2}\left(\frac{1}{r_{i}} - \frac{1}{r_{4}}\right) = \left(-2.25 \times 10^{6}\right)\left(\frac{1}{.112} - \frac{1}{.158}\right) = \left[-5.85 \times 10^{6}\right]$$

$$W_{(iii)} = 6 kq_{1}q_{2} \left(\frac{1}{r_{i}} - \frac{1}{r_{f}}\right) = \left(-2.25 \times 10^{-6}\right) \left(\frac{1}{.158} - \frac{1}{.1}\right)$$

$$= + \sqrt{8.26 \times 10^{-6} \text{ J}}$$

(d) $W_{tot} = W_{(ii)} + W_{(iii)} + W_{(iii)} = -2.41 \times 10^{-6} - 5.85 \times 10^{-6}$ = 100

The Contract of the Contract o

Energy), Then The Work Done By THAT FORCE
ALOUND Any CLOSED LOOP IS ZERO. THE ELECTRIC
FORCE IS, INDEED, CONSERVATIVE, SO WE SHOULD

EXPECT THIS ALSWER.

Note: Potential energies only exist Form Conservative Forces, so by using W=-AM, we Actually Assumed the Force was conservative to show that Whom =0. This Arbument is Technically Carcular, since we that to Assume the Force was conservative in order to Show that It was conservative in order to Show that It was conservative.

- 4. A cylindrical resistor, made of an unknown material, has a radius of 1mm and a length of 5cm. If, when connected to a 10V battery, the current through the resistor is measured to be 0.5A,
 - (a) What is the resistance of the resistor?
 - (b) What is the resistivity of the resistor?
 - (c) What electric field is produced within the resistor?
 - (d) How much heat is the resistor producing each second?
- (a) Since The RESISTOR IS Connected to the BATTERY,
 THEY ARE IN PARALLEL => THE VOLTAGE OF THE
 RESISTOR IS 10 V. Usine Ohin'S LAW, WE CAN

FIND THE RUSISTAMCE.

V=iR => R= (0.5) (0.5) (me were TOLD CURRENT=0.54)

(b) FOR A CYLINDRICAL DESISTOR. $A = \pi r^2 = \pi (0.001)^2 = 3.14 \times 10^6 \text{ m}^2$ $1 \times 10^2 = 0.001 \text{ m}^2$

R= PA -> P= RA - (20)(3.14x10)

=1.26 x 10 2m

- (a) $E = \frac{V}{L} = \frac{(10)}{(0.5)} = \sqrt{\frac{20V}{10.5}}$
- (d) Power = energy/The, & HEAT IS THE ENERGY EMITTED

 By A PLSISTOR.
 - $\Rightarrow P = V_{\tilde{c}} = (10)(0.5) = 5W = 5T \text{ of HeAT}$ $\Rightarrow P = V_{\tilde{c}} = (10)(0.5) = 5W = 5T \text{ of HeAT}$

FORMULA SHEET

Vectors:

$$|\vec{A} \cdot \vec{B}| = AB \cos \theta = A_x B_x + A_y B_y + A_z B_z$$
$$|\vec{A} \times \vec{B}| = AB \sin \theta$$

• Physics I Formulae:

$$\sum \vec{F} = m\vec{a}$$

$$W = \vec{F} \cdot \Delta \vec{x}$$

$$W_{tot} = \Delta K$$

$$W_{cons} = -\Delta U$$

$$K = \frac{1}{2}mv^{2}$$

$$K_{i} + U_{i} = K_{f} + U_{f}$$

• Electric Forces:

$$e = 1.6 \times 10^{-19} \text{ C}$$
 $k = 8.99 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$ $\epsilon_0 = 8.85 \times 10^{-12} \frac{\text{F}}{\text{m}}$ $k = \frac{1}{4\pi\epsilon_0}$ $Q = Ne$ $F = k\frac{q_1q_2}{r^2}$ $\vec{F} = q\vec{E}$

• Electric Fields:

$$E = k \frac{q}{r^2} \text{ (point charge)}$$

$$E = \frac{\lambda}{2\pi\epsilon_0} \text{ (infinite line of charge)}$$

$$E = \frac{\sigma}{2\epsilon_0} \text{ (infinite sheet of charge)}$$

$$\Phi_E = \vec{E} \cdot \vec{A}$$

$$\Phi_{tot} = \frac{q_{enc}}{\epsilon_0}$$

$$\lambda = \frac{Q}{L} \quad \text{or} \quad \sigma = \frac{Q}{A} \quad \text{or} \quad \rho = \frac{Q}{V} \quad \text{(charge densities)}$$

• Electric Potential Energy and Electric Potential:

$$U = k \frac{q_1 q_2}{r}$$
 $\phi = k \frac{q}{r}$
 $U = q \phi$ and $\Delta U = q \Delta \phi$
 $E_{av} = \frac{\Delta \phi}{\Delta x}$

 $V = \Delta \phi$

• Capacitors:

$$Q = CV$$

$$C = \epsilon_0 \frac{A}{d}$$

$$E = \frac{V}{d}$$

$$U = \frac{1}{2} \frac{Q^2}{C}$$

$$u = \frac{1}{2} \epsilon_0 E^2$$

• Resistors:

$$R =
ho rac{L}{A}$$
 $V = iR$
 $E = rac{V}{L}$
 $P = Vi$