

# The Oort Cloud

*Hans Rickman*

# The seminal paper: Oort (1950)

THE STRUCTURE OF THE CLOUD OF COMETS SURROUNDING THE SOLAR SYSTEM,  
AND A HYPOTHESIS CONCERNING ITS ORIGIN,

BY J. H. OORT

The combined effects of the stars and of Jupiter appear to determine the main statistical features of the orbits of comets.

From a score of well-observed original orbits it is shown that the “new” long-period comets generally come from regions between about 50000 and 150000 A.U. distance. The sun must be surrounded by a general cloud of comets with a radius of this order, containing about  $10^{11}$  comets of observable size; the total mass of the cloud is estimated to be of the order of  $1/10$  to  $1/100$  of that of the earth. Through the action of the stars fresh comets are continually being carried from this cloud into the vicinity of the sun.

- Oort considered the *barycentric orbits of long-period comets before entry into the planetary system*, found by numerical integrations (E. Strömgren, G. Fayet):  
“*original orbits*”

# The Oort Spike

- Oort found a strong *pile-up in the  $1/a$  range next to the parabolic limit* for a sample of 19 orbits
- He concluded that *passing stars inject comets from a very distant “cloud”* into observable orbits

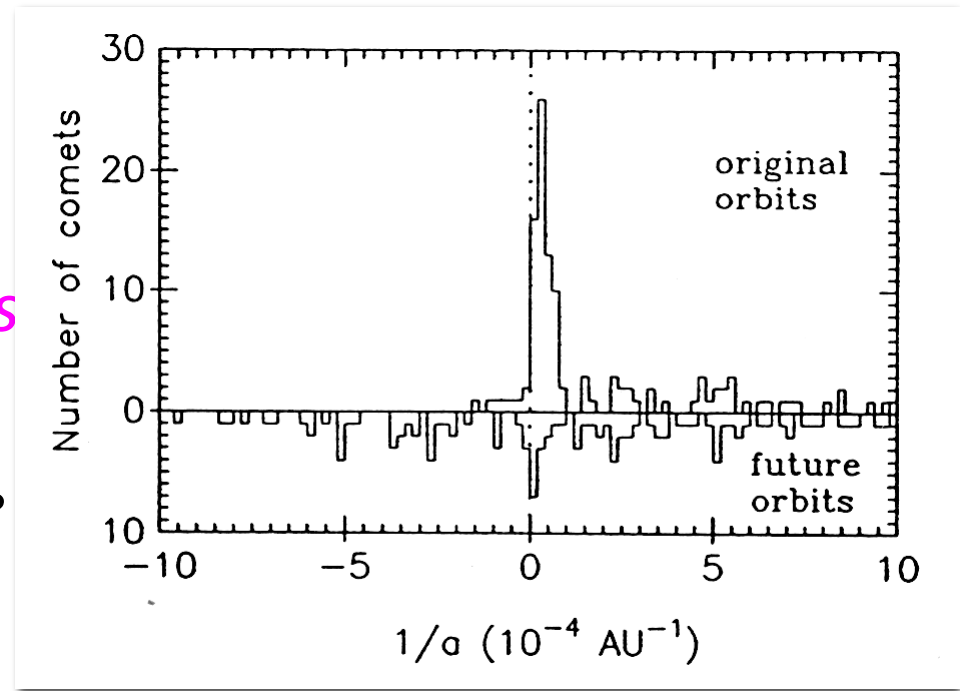
TABLE I  
Distribution of original semi-major axes  
( $a$  in Astronomical Units)

$1/a$	$n$
$< .000\ 05$	10
$.000\ 05 - .000\ 10$	4
$.000\ 10 - .000\ 15$	1
$.000\ 15 - .000\ 20$	1
$.000\ 20 - .000\ 25$	1
$.000\ 25 - .000\ 50$	1
$.000\ 50 - .000\ 75$	1
$> .000\ 75$	0

Oort (1950)

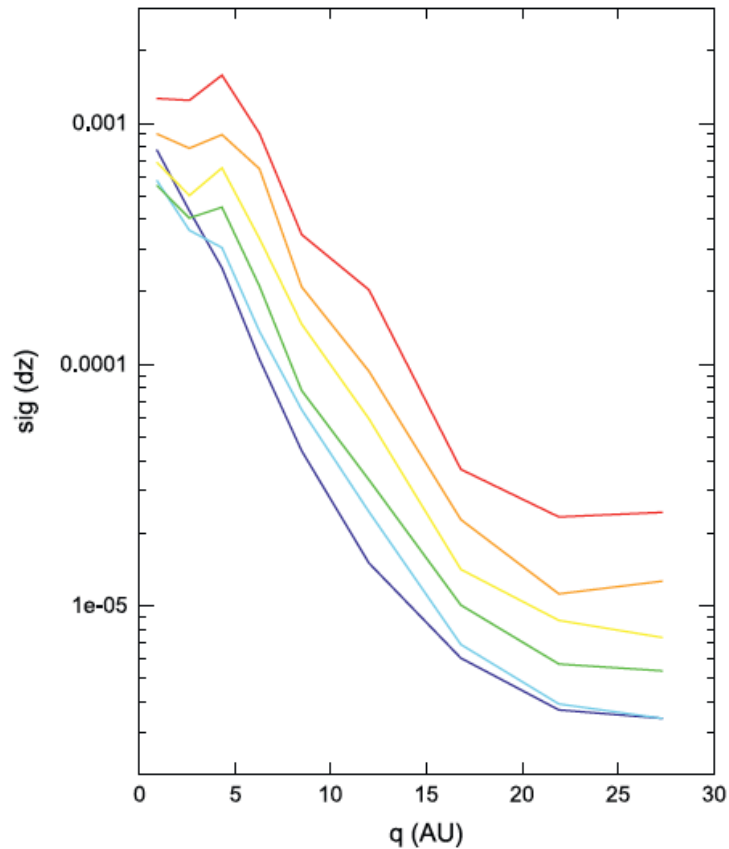
# The Oort Cloud

- *Entering into the planetary system, the comets have a strongly peaked distribution of  $1/a$*
  - *But planetary perturbations wipe out the spike*
  - *The comets of the spike are not returning – they are newcomers from a very distant reservoir*
- “New” and “Old” comets**



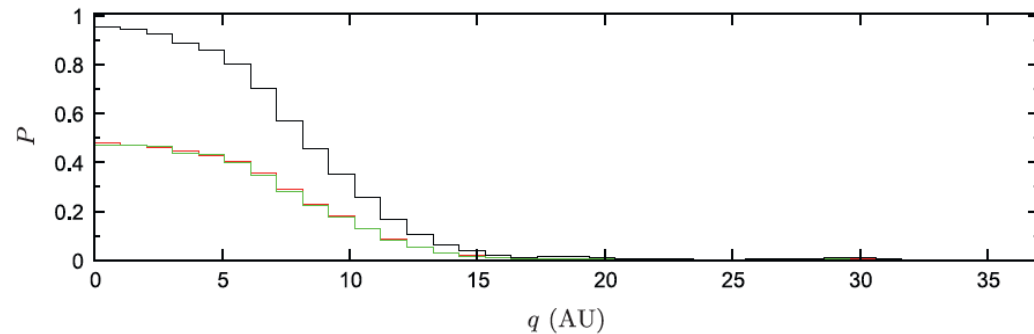
*More recent sample  
of orbits*

# The Loss Cone



$\sigma(\Delta(1/a))$  vs  $q$  for different inclination ranges

***Loss cylinder (loss cone)***



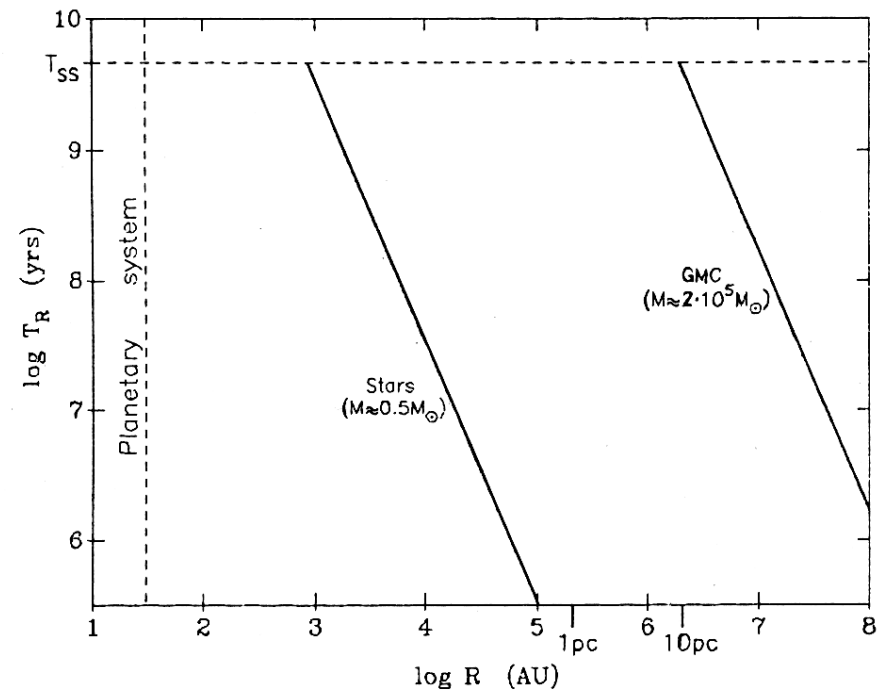
Probability for new comets to be kicked out of the defining range of  $1/a$  vs  $q$

*Fouchard et al (2013)*

# Stellar encounters

*Why do the new comets have  $a > 10^4$  AU?*

- Stellar encounters then occur on the time scale of one orbital period, injecting comets deep inside the loss cylinder
- For much smaller orbits the stellar encounter time scale is much longer than the period

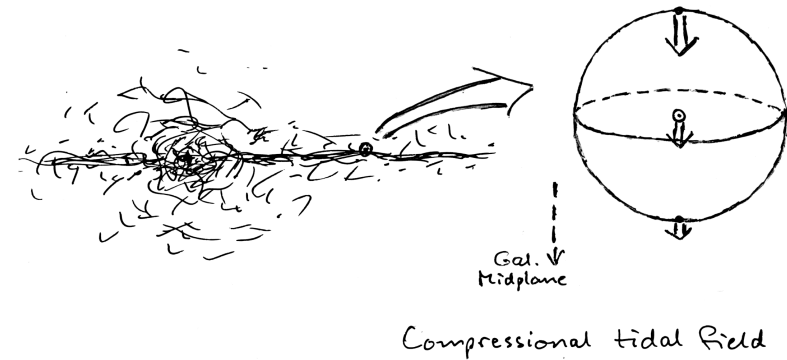


*Encounter time scales vs  
minimum distance*

# Galactic tides

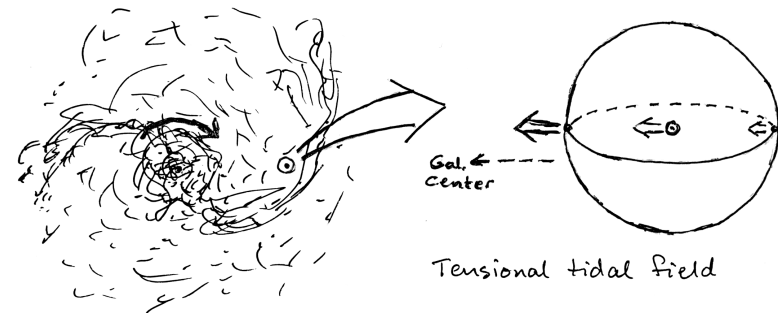
- **The disk tide**

- Gravitational potential of the Galactic disk
- Induces *regular oscillations of  $q$  and  $i_G$*  (small enough  $a$ )



- **The radial tide**

- In-plane, central force field of the Galaxy
- Changes also the semimajor axis and *may eject comets*



# Tidal theories of the 1980's

- Several authors identified the ***q oscillations of the disk tide*** as an important mechanism to inject comets into the loss cylinder
- Heisler & Tremaine (1986) developed an ***analytic theory of the regular disk tide*** by orbital averaging

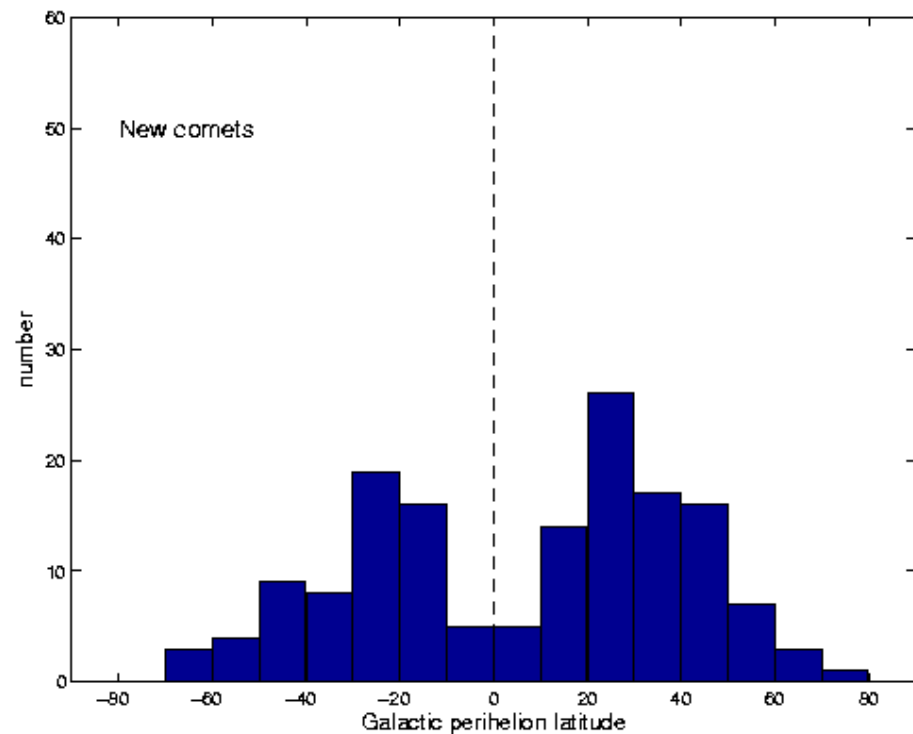
$$|\Delta q| \propto q^{1/2} \cdot a^{7/2} \cdot |\sin 2\beta_G|$$

*Tidal change of q per orbital revolution due to the disk tide*



# Imprint of the disk tide

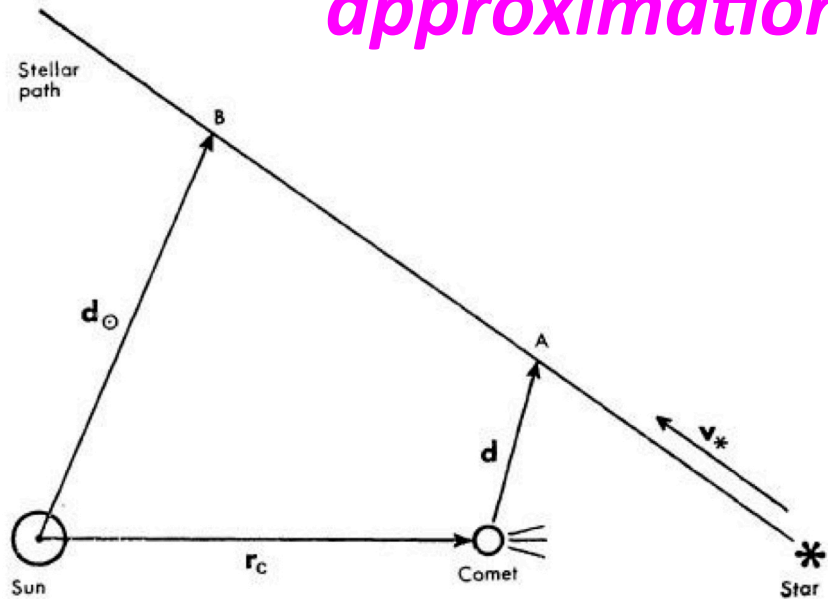
- Delsemme (1987) recognized a *double-peaked distribution of Galactic latitudes of perihelia* of new comets, indicating the *importance of the disk tide for comet injection*



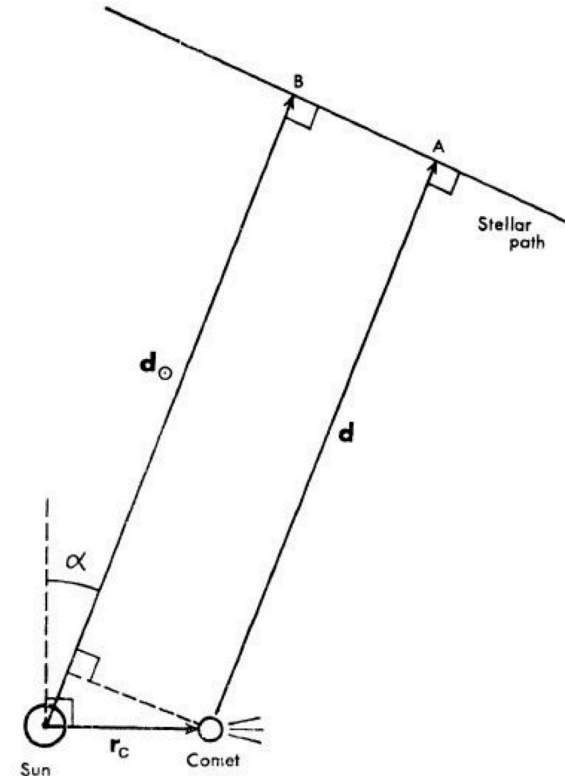
*recent orbital statistics*

# Stellar encounters

## Classical impulse approximation



$$\Delta \mathbf{V}_c = \frac{2GM_*}{V_*} \left\{ \frac{\hat{\mathbf{d}}_c}{d_c} - \frac{\hat{\mathbf{d}}_\odot}{d_\odot} \right\}$$



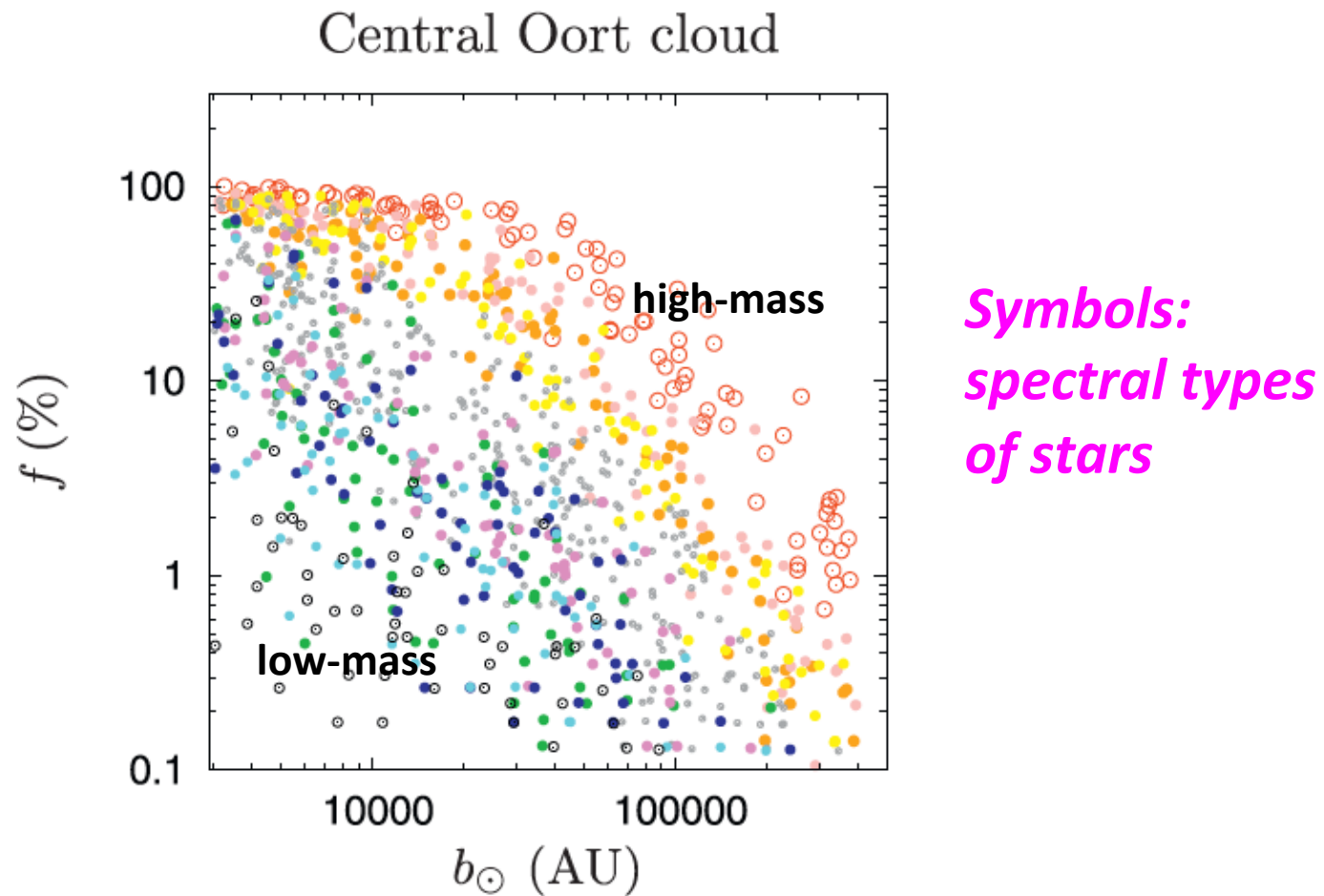
$$\Delta \mathbf{V}_c \approx \frac{2GM_* r_c \sin \alpha}{V_* d_\odot^2} \cdot \hat{\mathbf{d}}_\odot$$

**Thus, a change in angular momentum and perihelion distance**

# Basics of Oort Cloud dynamics

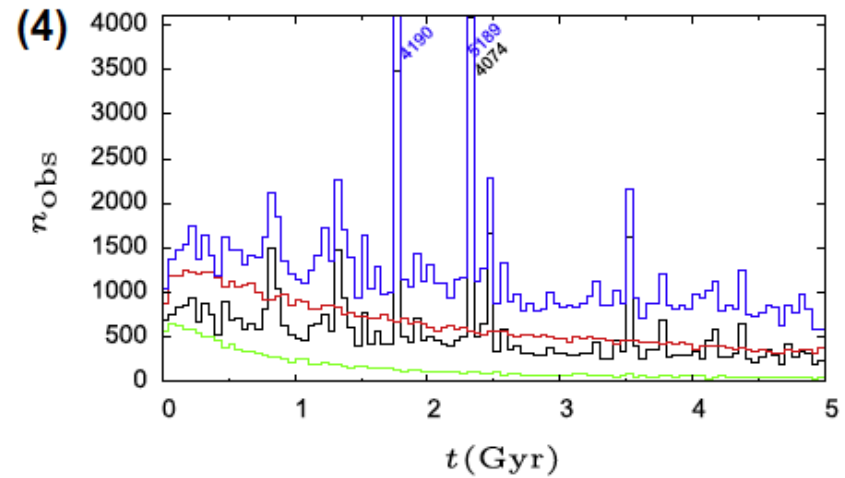
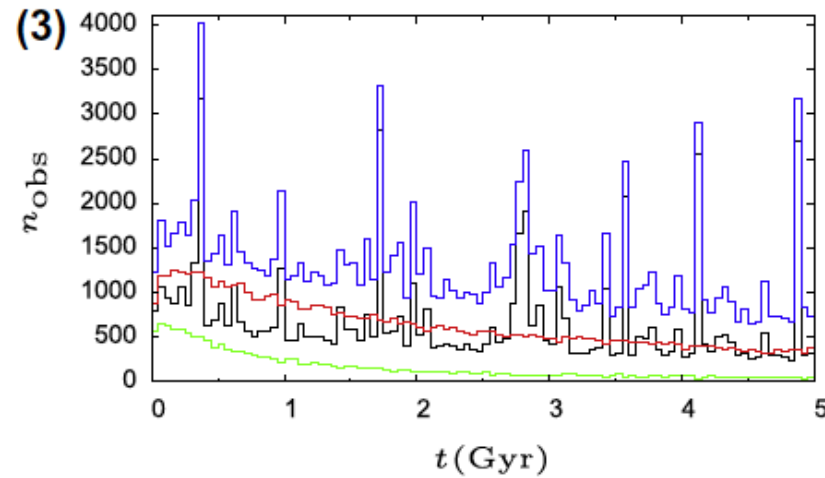
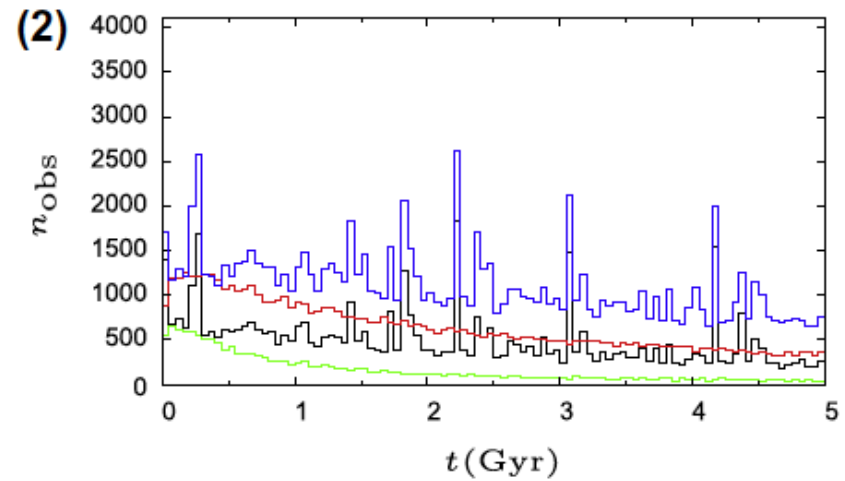
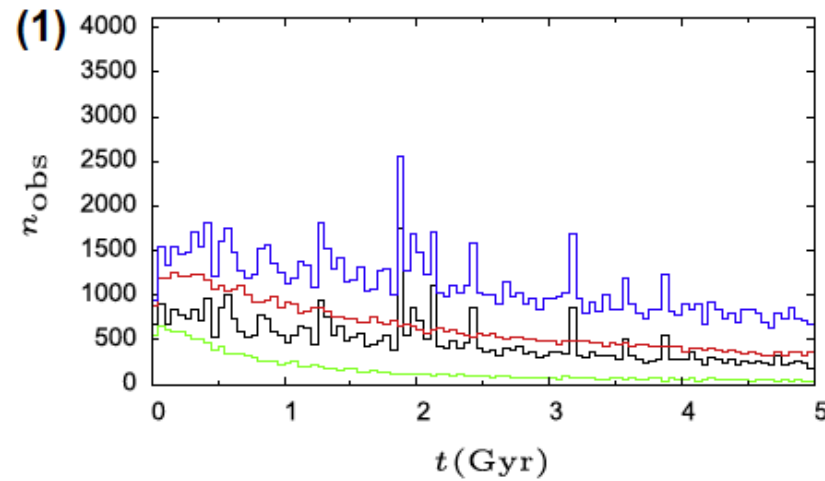
- *Stellar encounters randomize the phase space distribution of Oort Cloud comets*
- For an integrable disk tide ( $a < 40,000$  AU), there is a phase space domain, where  $q_{min}$  of the tidal cycle is  $< 5$  AU (observable). This is the ***Tidally Active Zone*** (Fouchard et al 2011)
- In the long-term evolution of the Oort Cloud, *the stellar encounters keep the TAZ population in steady state*

# TAZ filling efficiency



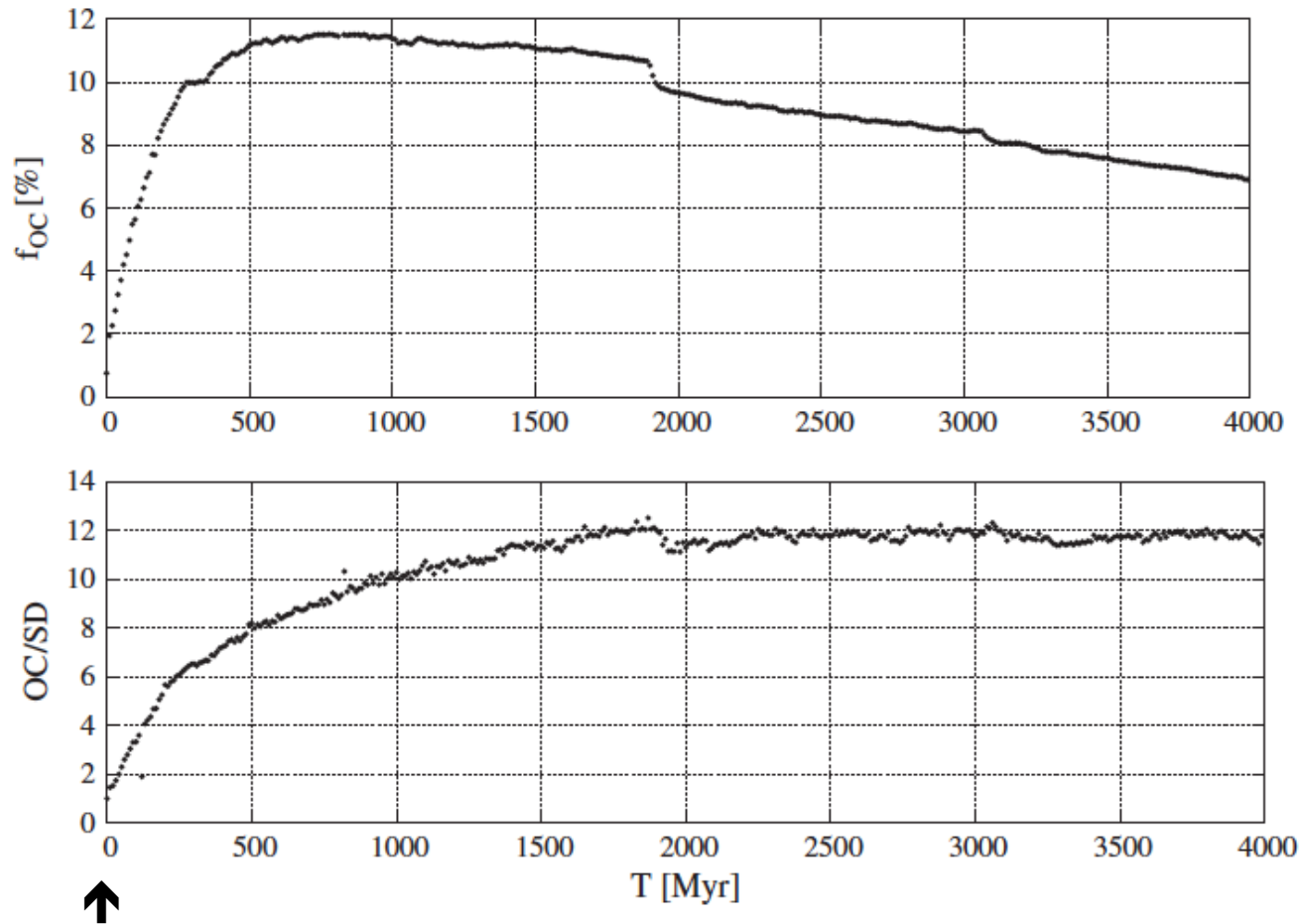
*Fouchard et al (2011)*

# Comet showers



*Fouchard et al (2014)*

# Brasser & Morbidelli (2013)

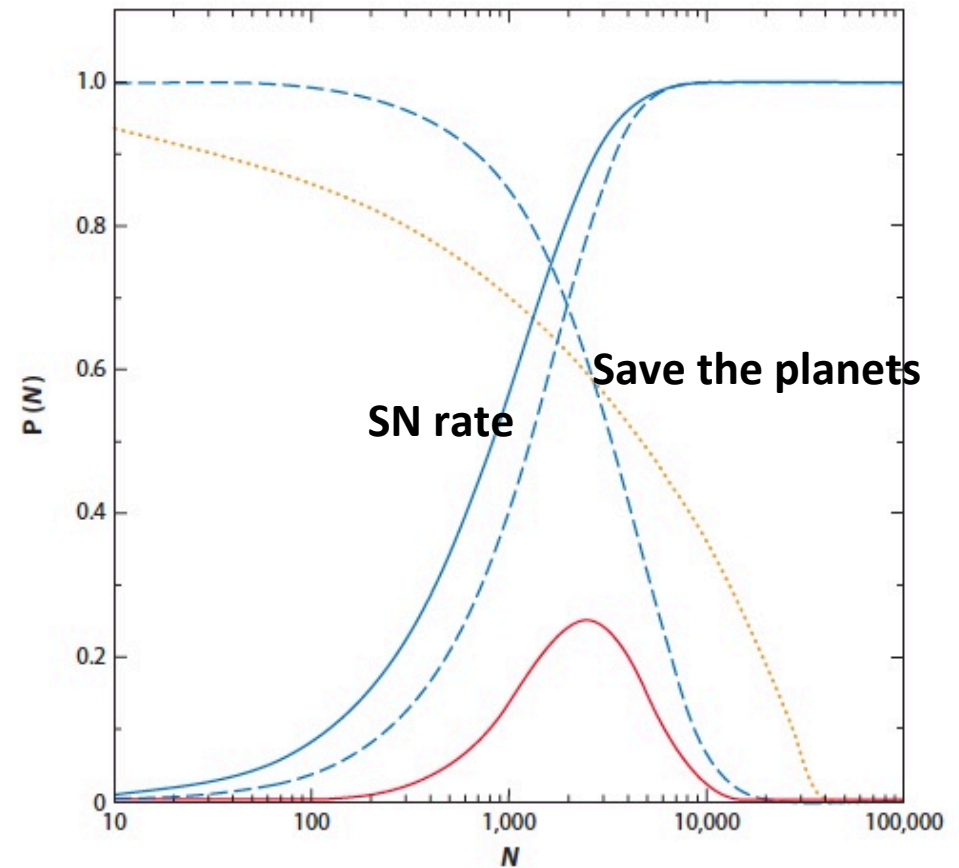


End of  
migration

Currently,  $M_{OC} \approx 7\%$  of  $M(\text{disk})$   
 $M_{SD}$  is 12 times less

# Solar birth cluster

- ***Solar-type stars are born in embedded clusters***
- ***About equal numbers of stars are born in clusters with  $10^2$ ,  $10^3$  and  $10^4$  members***  
(Lada & Lada 2003)



Adams (2010)

# Oort Cloud and Birth Cluster

- ***If the Oort Cloud was formed very early, and the solar birth cluster was long-lived, would the cloud survive or not?***
- This can be investigated by dynamical simulations!



# Nordlander et al (2017)

- *Assume very early OC formation in a long-lived birth cluster; find out if the cloud survives until the LHB*
- *High Mass (HM:  $N_0 = 24000$ ) or Intermediate Mass (IM:  $N_0 = 2000$ ) birth cluster assumed*
- *Trace  $10^3$  OC comets for 400 My* (100-500 My) *in a static cluster potential + random stellar encounters* (select the strongest)
- Perform  $10^3$  simulations per model (comets and cluster) for statistical robustness

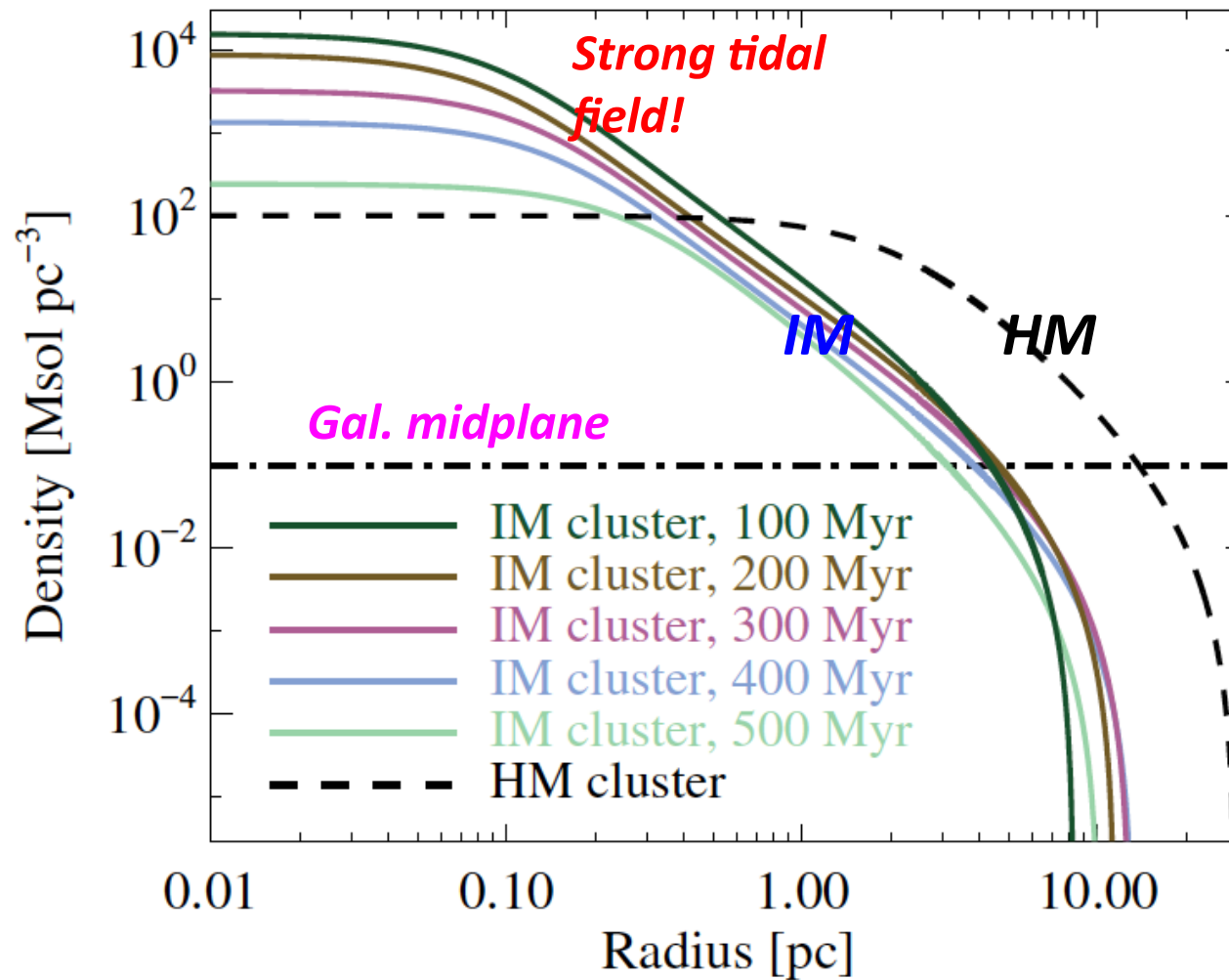
# Cluster model

- The most general distribution function for a relaxed stellar cluster with central symmetry is

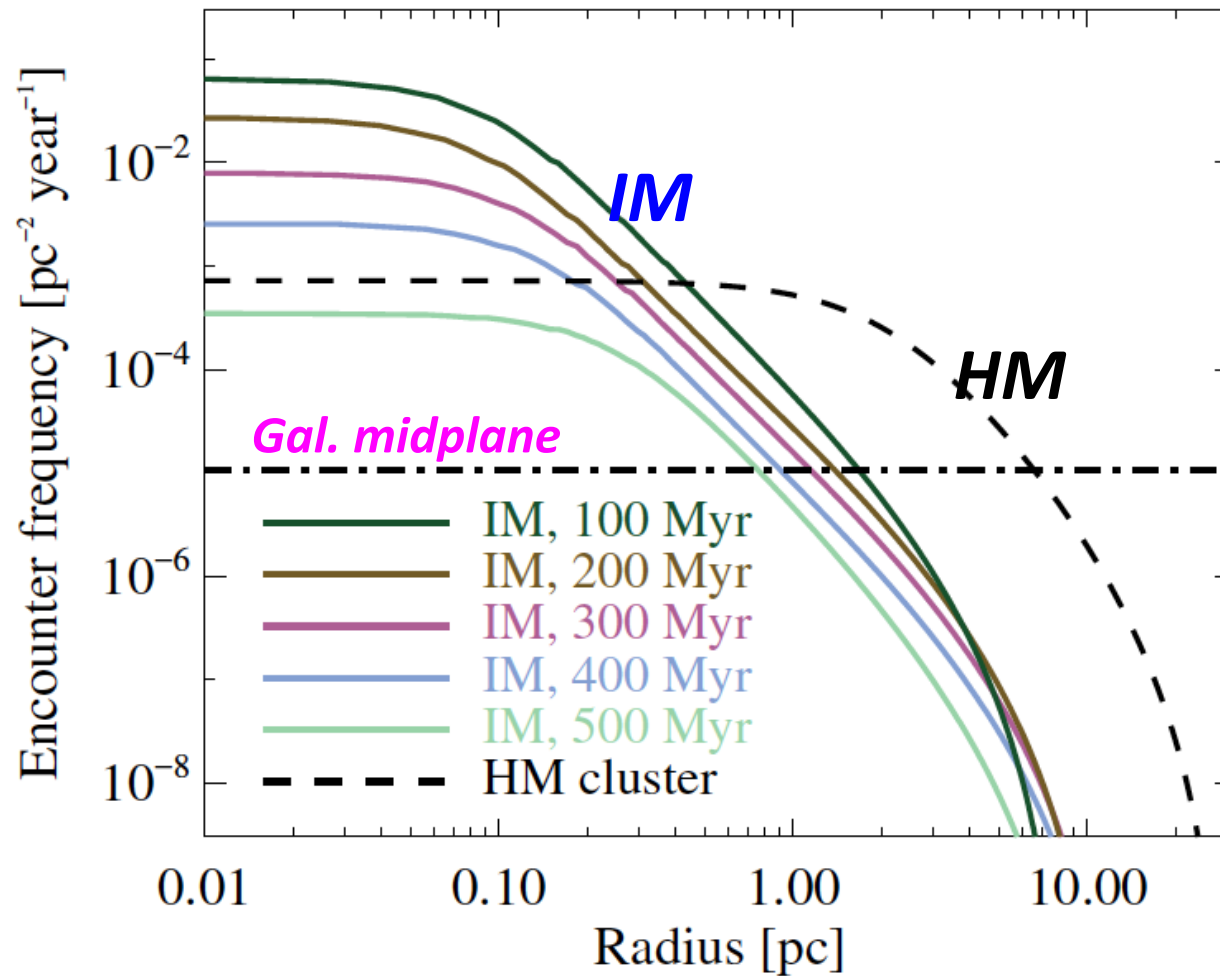
$$\varphi(E) = \begin{cases} a \{e^{b(E_t - E)} - 1\} & E < E_t \\ 0 & E \geq E_t \end{cases} \quad (\text{King 1966})$$

- ***No mass segregation; no binaries!***
- ***HM model:*** adapted to the young M67 (static)
- ***IM model:*** sequence of 16 static King models computed for evolving cluster ( $N = 1700 \rightarrow 300$ ) with constant mass distribution

# Density profiles



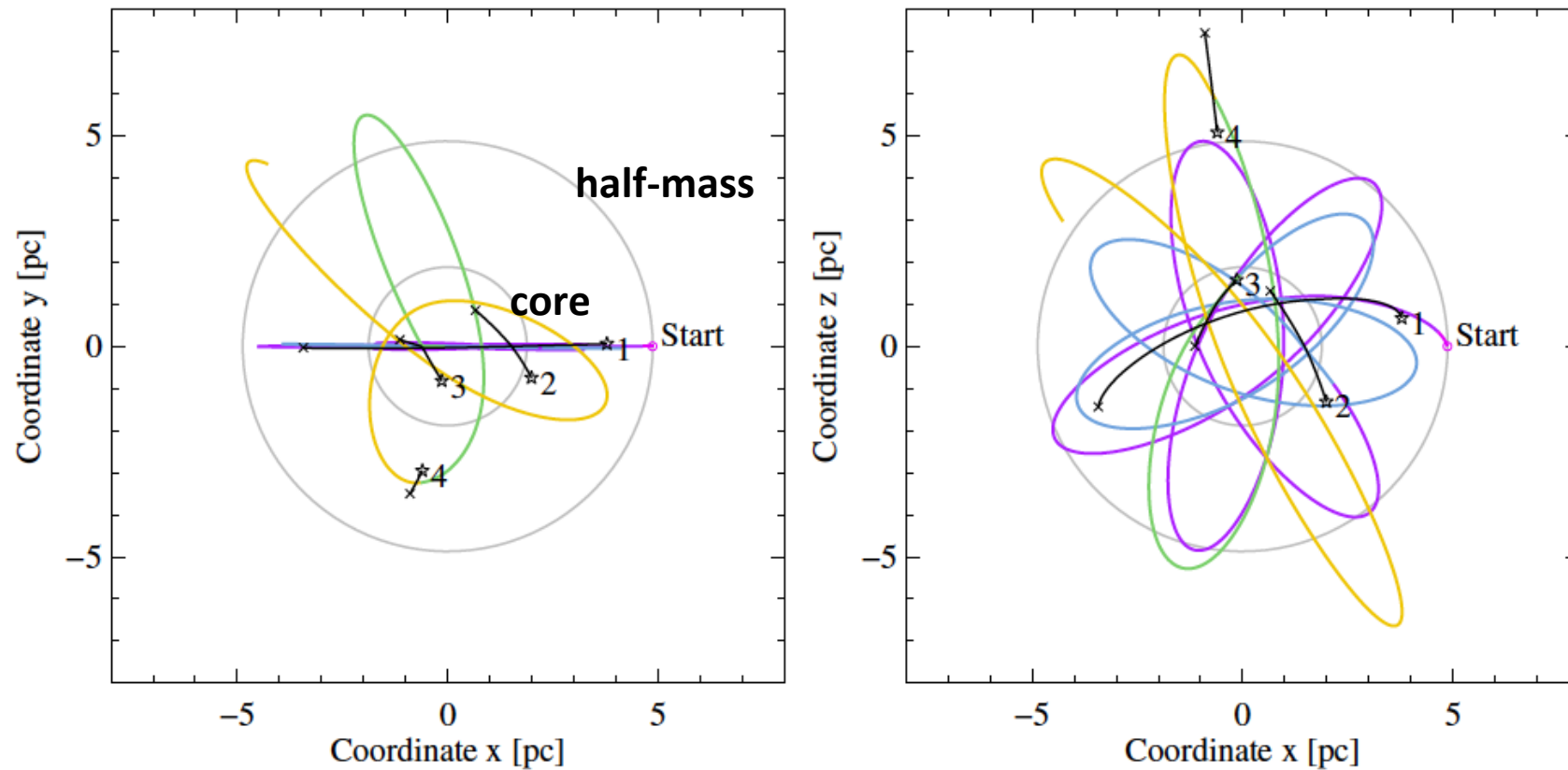
# Encounter frequency



# Simulations

- Initialize three groups of comets with  $a =$  **5000**, **10000** and **20000** AU and thermalized eccentricities
- Each group has *1000 comets*
- Start the Sun with random  $E$  and  $L$  defining the initial rosette orbit
- Integrate the effects of the  $\sim 20$  strongest ***stellar encounters*** on the Sun and comets, and the ***cluster tide*** all the time
- Derive statistical results for *1000 simulations*

# The solar orbit



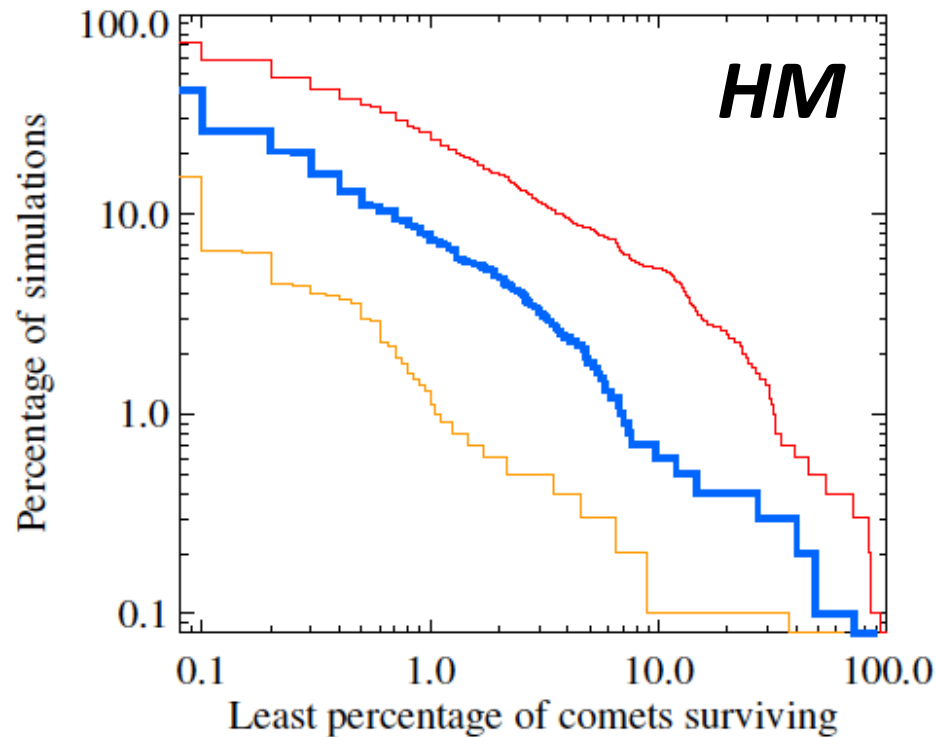
*HM cluster, first 80 Myr of one simulation*

# Comet escape

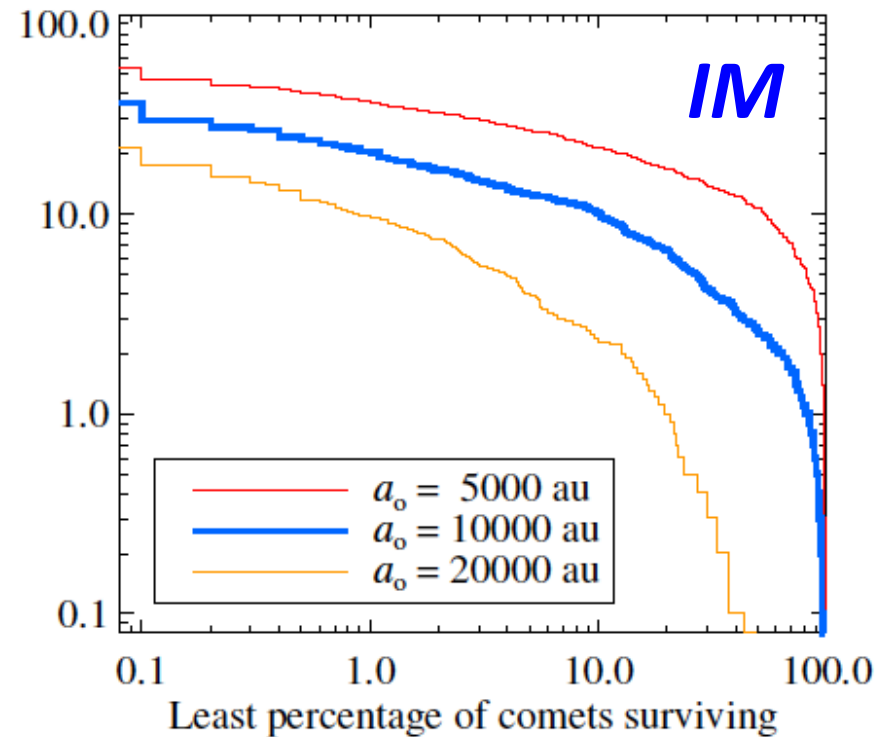
- **Unlinked** – *comets reach distances  $> 1$  pc from the Sun*
  - *Mechanism:* impulse imparted by a stellar encounter, or energy perturbation by a non-integrable cluster tide
- **Loss cone entry** – *comets enter within 5 AU of the Sun*
  - *Mechanism:* angular momentum drain by the cluster tide, or by impulse imparted by a stellar encounter

# Loss of comets

*Median survival probability of OC comets  $\sim 0.1\%$*



*Here, the inner group survives at 10% level in almost 10% of the simulations*

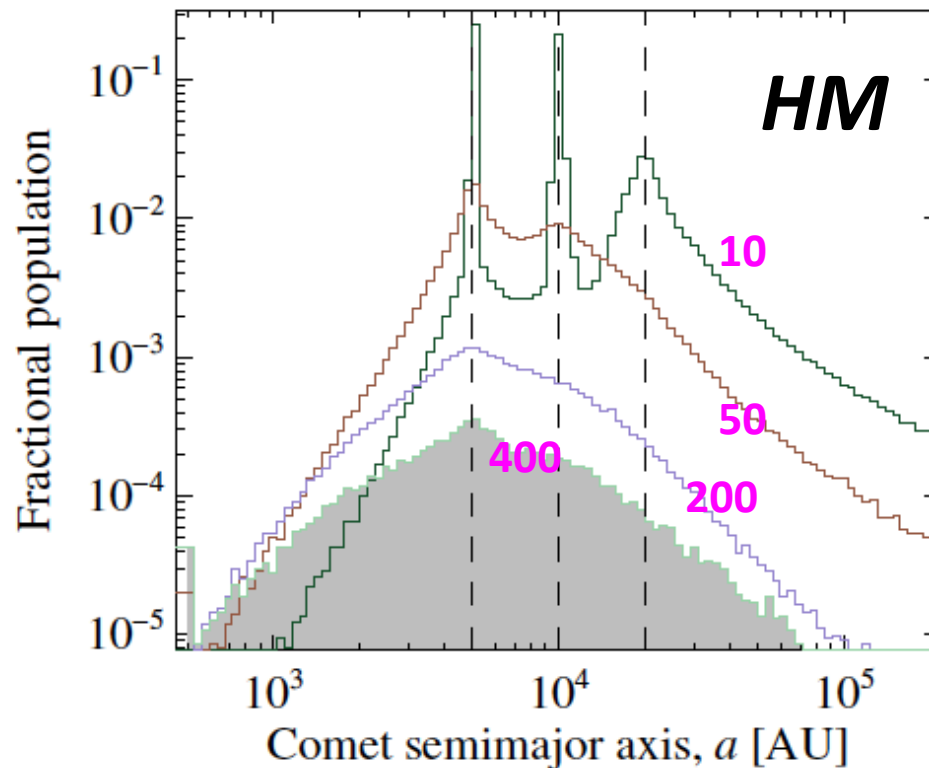


*Here, there is a chance of significant survival, if the Sun avoids the central core*

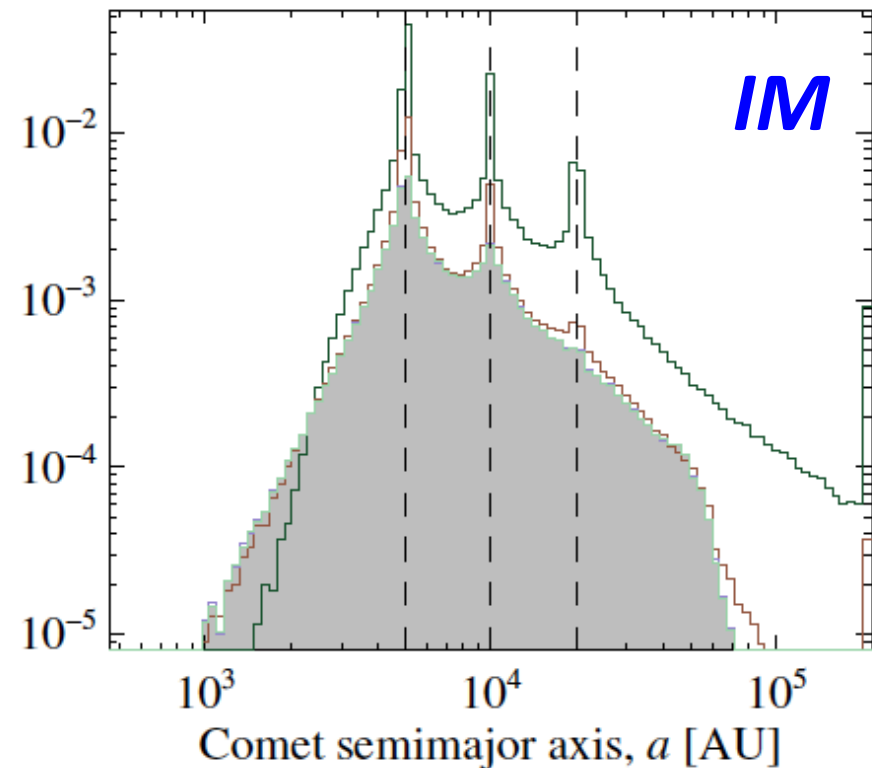


# OC energy distribution

*Four snapshots at times = X Myr, averaged*



***The Sun remains in the cluster: 94%***



***The Sun remains in the cluster: 5%***

*The OC gets fossilized, when the Sun leaves the cluster*