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## Bubble Sort

❑ Example 2:

|   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|
| 5 | 4 | 2 | 1 | 3 | 2 | 4 | 1 | 3 | 5 |
| 4 | 5 | 2 | 1 | 3 | 2 | 1 | 4 | 3 | 5 |
| 4 | 2 | 5 | 1 | 3 | 2 | 1 | 3 | 4 | 5 |
| 4 | 2 | 1 | 5 | 3 | 2 | 1 | 3 | 4 | 5 |
| 4 | 2 | 1 | 3 | 5 | 1 | 2 | 3 | 4 | 5 |
| 4 | 2 | 1 | 3 | 5 | 1 | 2 | 3 | 4 | 5 |

## Bubble Sort

❑ Time Complexity:  $O(n^2)$  as there are two nested loops

❑ Example of worst case

|   |   |   |   |   |
|---|---|---|---|---|
| 5 | 4 | 3 | 2 | 1 |
|---|---|---|---|---|

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## Selection Sort

❑ Example 2:

12	10	16	11	9	7
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12	10	16	11	9	7
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7	10	16	11	9	12
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7	9	16	11	10	12
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7	9	10	11	16	12
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7	9	10	11	16	12
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7	9	10	11	12	16
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## Selection Sort

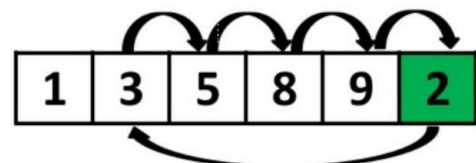
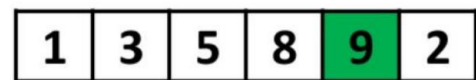
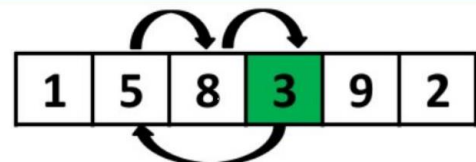
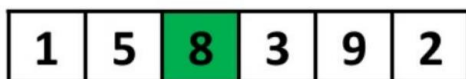
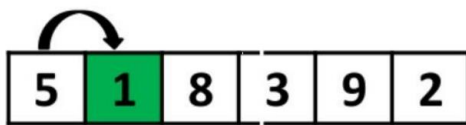
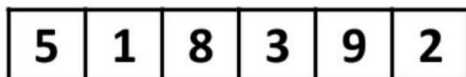
❑ **Time Complexity:**  $O(n^2)$  as there are two nested loops

❑ Example of worst case

2	3	4	5	1
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## Insertion Sort

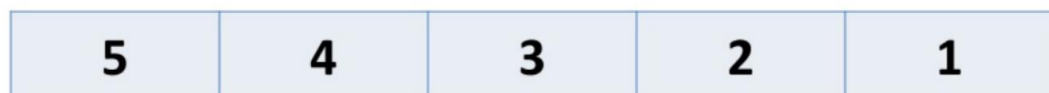
### □ Example 2:



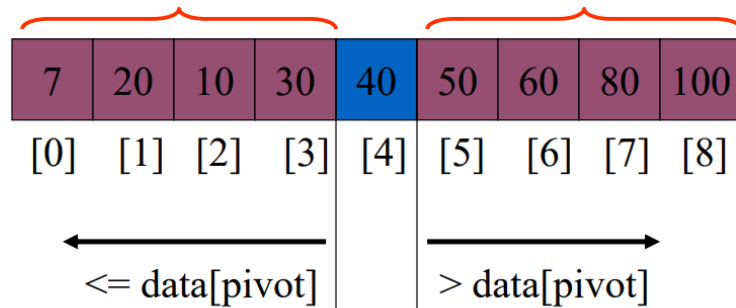
## Insertion Sort

□ Time Complexity:  $O(n^2)$

□ Example of worst case



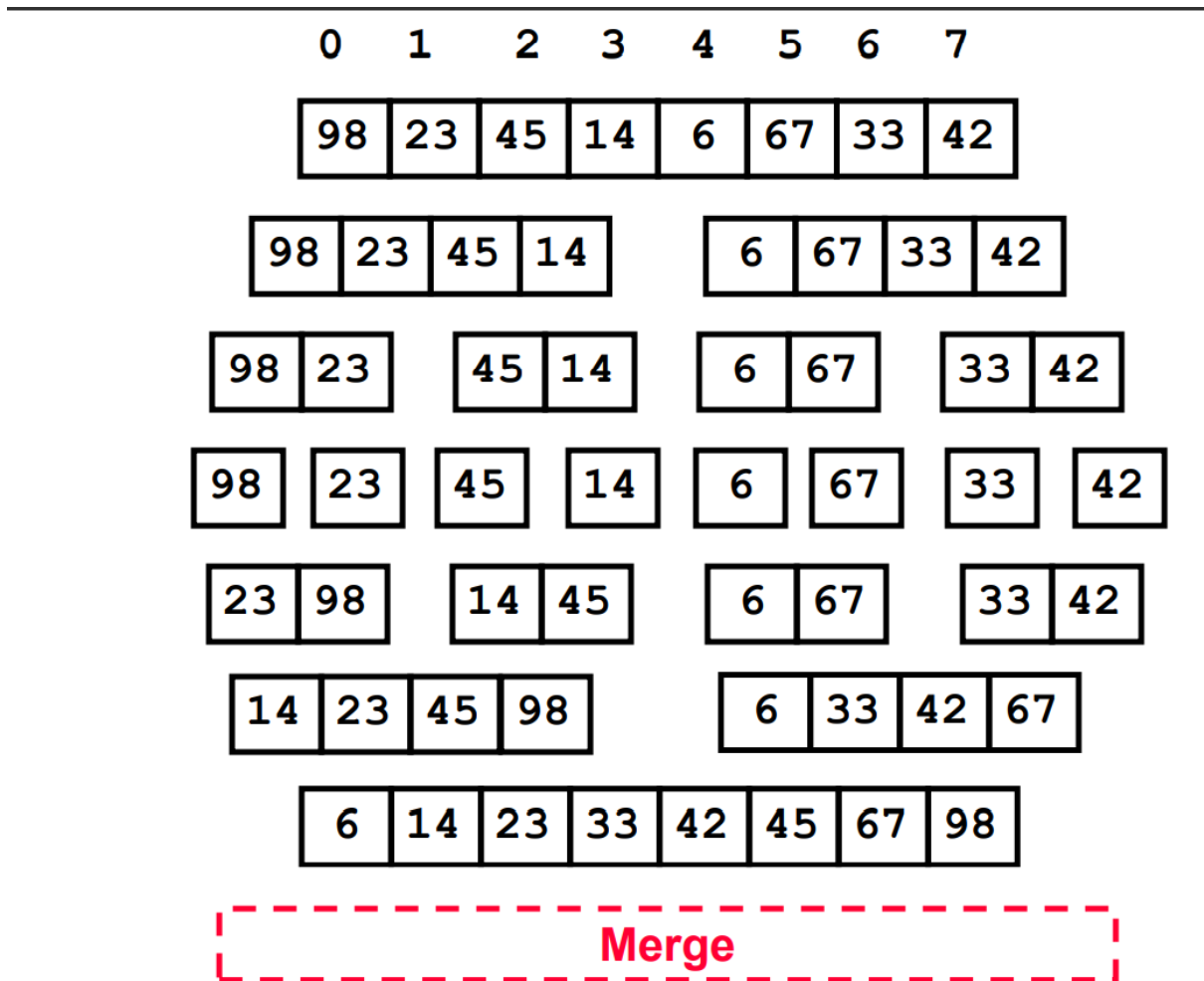
# Recursion: Quicksort Sub-arrays



## Quicksort Analysis

- Assume that keys are random, uniformly distributed.
- Best case running time:  $O(n \log n)$
- Worst case running time:  $O(n^2)!!!$

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running time:  $O(n \log n)$

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- **Bubble sort and Insertion sort -**

Average and worst case time complexity:  $n^2$

Best case time complexity:  $n$  when array is already sorted.

Worst case: when the array is reverse sorted.

- **Selection sort -**

Best, average and worst case time complexity:  $n^2$  which is independent of distribution of data.

- **Merge sort -**

Best, average and worst case time complexity:  $n \log n$  which is independent of distribution of data.

- **Heap sort -**

Best, average and worst case time complexity:  $n \log n$  which is independent of distribution of data.

- **Quick sort -**

It is a divide and conquer approach with recurrence relation:

$$T(n) = T(k) + T(n-k-1) + cn$$

Worst case: when the array is sorted or reverse sorted, the partition algorithm divides the array in two subarrays with 0 and  $n-1$  elements. Therefore,

$$T(n) = T(0) + T(n-1) + cn$$

Solving this we get,  $T(n) = O(n^2)$

Best case and Average case: On an average, the partition algorithm divides the array in two subarrays with equal size. Therefore,

$$T(n) = 2T(n/2) + cn$$

Solving this we get,  $T(n) = O(n \log n)$