$$y' = -12x^{2} + 30x + 18$$

$$= -6(7x^{2} - 5x + 3)$$

$$= -6(2x - 3)(x - 1)$$
Set  $y' = 0$ :
$$0 = -6(2x - 3)(x - 1)$$
if  $2x - 3 = 0$ 

$$x = \frac{3}{2}$$

$$x = 1$$

.. y is increasing on  $x \in (1, \frac{3}{2})$  and decreasing on  $x \in (-\infty, 1)$  and on  $x \in (\frac{3}{2}, \infty)$ 

$$1'(x) = \frac{1}{12} (3x^{4} - 16x^{2} + 24x^{2} - 9)$$

$$= 12x^{3} - 48x^{2} + 48x$$

$$= 12x (x^{2} - 4x + 4)$$

$$= 12x (x - 2)^{2}$$

$$1''(x) = \frac{1}{12} (12x^{3} - 98x^{2} + 48x)$$

$$= 36x^{2} - 96x + 48$$

$$= 12(3x^{2} - 8x + 4)$$

$$= 12(3x - 2)(x - 2)$$

$$x'$$
,  $x = \frac{2}{3}$   $x' = 2$ 

... f(x) is concave down on xE (3,2) and concave up on xE (-00, 3) and xe (2,00)

if 
$$(x-3)^2 = 0$$
 if  $2x+1=0$   
 $(x+3)^2 = 0$   $2x=-9$   
 $\therefore x=-3$   $x=-\frac{9}{2}$ 

$$(-3,8)$$
 is a critical point  $q(-\frac{9}{2})=(-\frac{9}{2}+3)^3(-\frac{9}{2}+5)$ 

$$g'(x) = 3(x+3)^{2}(x+5) + (1)(x+3)^{3}$$
 [Using product role)
$$= (x+3)^{2}(3x+15+x+3)$$

$$= (x+3)^{2}(4x+16)$$

$$g'(x) = 2(x+3)^{2}(2x+9)$$

$$g''(x) = 2\left(2(x+3)(2x+9) + (7)(x+3)^{2}\right)$$

$$= 4(x+3)(2x+9) + (7)(x+3)^{2}$$

$$= 4(x+3)(3x+12)$$

$$= 12(x+3)(x+4)$$
Sut  $g'(x) = 0$ :

Sub x=-3 and  $x=-\frac{9}{2}$  inb g''(x)g''(-3)=12(-3+3)(-3+4)

(-3,8) is a point of inflection

q"(-2)=12(-2+3)(-2+4)

=9

 $(1 - \frac{9}{2}, -1.688)$  is a minimum Set g''(x) to 0:

Sub x=-3 and r=-4 into g (x):

. (-3,0) is a POI (previously calculated)

. (-4, -1) is an inflection point

$$q(0) = (0+3)^3(0+5)$$
  
= 135

:. co, 130) is the y-intercept

i g is conone down on xtl-4,-3) and concavery on xtl-0,-4) and xt (-3,00)

For 
$$O_s$$
 to  $3_s$ :  
 $sl_{pe} = \frac{y_{1} - y_{1}}{x_{2} - x_{1}}$ 

$$= \frac{-5 - 10}{3 - 0}$$

$$= -5$$

... 
$$V(t) = -5t$$
 from  $t = 0s$  to  $t = 3s$ .  
...  $S(t) = -\frac{5}{2}t^2$  from  $t = 0s$  to  $t = 3s$ .

At 
$$t=0$$
,  $s(0)=0$  m  
At  $t>3$ ,  $s(0)=-\frac{5}{2}(0)^{7}$   
= -27.5 m

For 
$$36$$
 to  $45$   
 $6lope = \frac{4}{1} \cdot \frac{4}{1}$   
 $= \frac{-6 \cdot (-5)}{4 \cdot 3}$   
 $= 0$   
 $\therefore \sqrt{(4)} = 0 + -5$  from  $4 = 36$  to  $4 = 45$   
 $= -5$   
 $\therefore 5(4) = -5 + 6$  from  $4 = 35$  to  $4 = 45$   
At  $4 = 35$ ,  $5(3) = -27.5$  m  
At  $4 = 45$ ,  $5(4) = 5(3) + (-5(1))$   
 $= -27.5$  m  
 $\therefore (4, -27.8)$  is a key point

For t= 48 to t= 105

Slope = 
$$\frac{47-57}{x_2-x_1}$$
  
=  $\frac{5-(-5)}{10-4}$   
=  $\frac{5}{3}$ 

· · · (t) = = t from tous to to los

:. s(t)= { } from }=45 to to 105

At t= 41, s(4)= -27.5 m

At 7=105,5(10) = 5(4) + \(\frac{5}{6}(4)^2\)
= 47.5 M

·· (10, un.5) is a key point

(1. The displacement hundrion has Here key points:

$$f'(x) = 30x^{2} + 2bx + C$$

$$f''(x) = 60x + 2b$$

$$f'(x) = 0$$

$$O = 6a(0) + 2b$$

$$f'(x) = 0$$

$$A + x = 0, \quad f'(x) = 0 \quad (0,2)$$

$$O = 3a(0)^{2} + 2b(0) + C$$

$$C = 0$$

$$A + x = 2, \quad f'(x) = 0$$

$$O = 3a(2)^{2} + 2(0)(1) + C$$

$$O = 12a + C$$

$$6 = 8a + 2c + 2$$