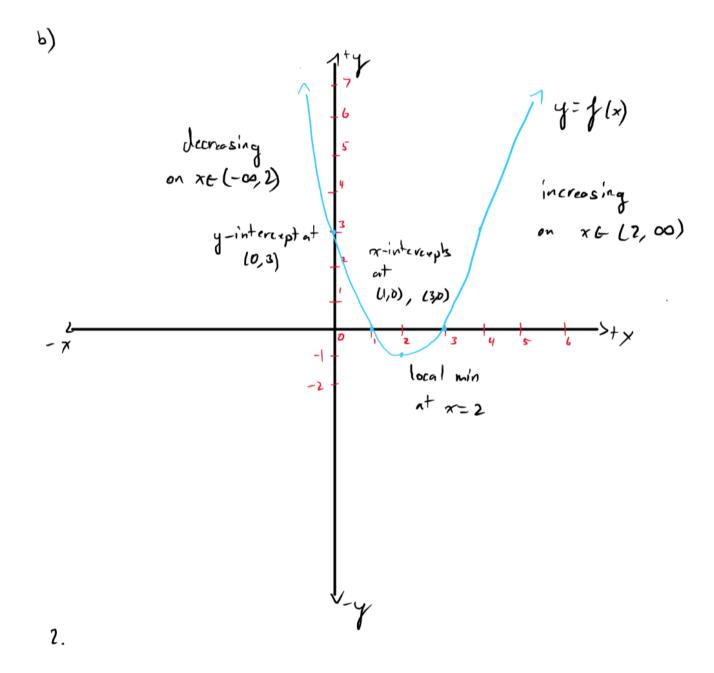
23 15.5 15 3

if $(x) \ L O \ on \ x \in (-\infty, 2)$, $f(x) \ \text{is decreasing on} \ \ \pi \in (-\infty, 2)$ $f(x) = 0 \ \text{at} \ \ x=7, \ f(x) \ \text{has a}$ $|ocal \ \max, |ocal \ \min, or \ \text{inflection point at } x=2.$

i f(1) = 0 and f(3) = 0, (1,0) and (3,0) are x-intercepts of f(x).

1. f(x) is decreasing on $x \in (-\infty, 2)$ but increasing on $x \in (2, \infty)$, f(x) has a local min at x=2. a y-intercept of f(x).



- f(x) is increasing when f'(x) is positive.

f'(x) is possitive when $x \in (-\infty,0)$ and $x \in (2,\infty)$ (From the graph)

- f(x) is decreasing when f'(x) is negative.

f'(x) is negative when $x \in (0,2)$ (From the graph)

- Local extrema of f(x) occur when f'(x)=0.

f'(x)=0 when x=0 and x=2, (Fromthe graph). flo) is a local max since f'(x)>0

- Points of inflection occur when 1"(x) = 0.

f''(x) corresponds to the instantaneous slope of f'(x). f''(x) = 0 at any maximal minima of

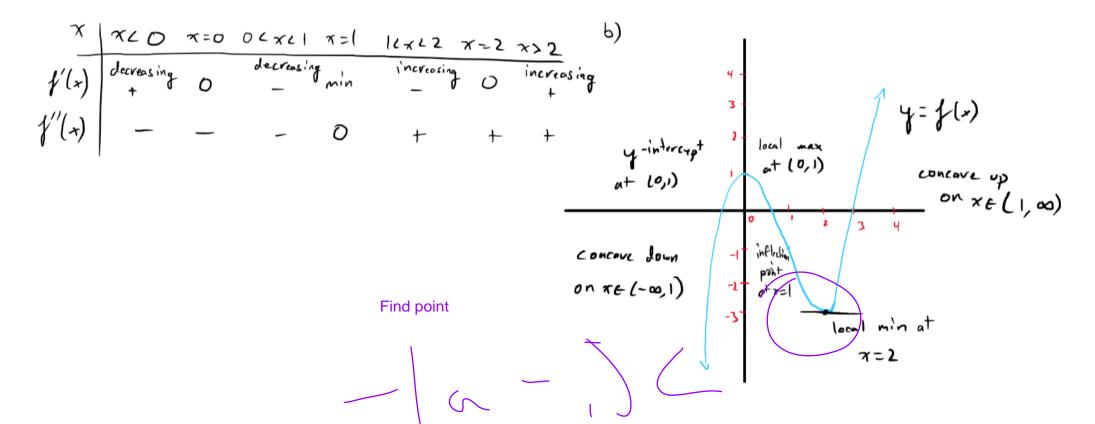
もりか.

· : 1'(x) has a local min at x=1, 1"(1)=0

:. f(x) has an inflection point at x=1.

- f(x) is concave down when f'(x) < 0 and is concave up who f'(x) >0.

f(0) is a local max since f'(x) > 0on $x \in (-\infty, 0)$ and f'(x) < 0 on $x \in (0,1)$ f(2) is a local min since $f'(x) \geq 0$ on $x \in (1,2)$ and f'(x) > 0 on $x \in (2, \infty)$ f''(x) corresponds to the instantaneous slope of f'(x). $f''(x) \ge 0$ when f'(x) is decreasing and $f''(x) \ge 0$ when f'(x) is increasing. From the graph, $f''(x) \ge 0$ on $x \in (L-\infty, 1)$ and $f''(x) \ge 0$ on $x \in (L, \infty)$



3.9 Domain: x + M, Ronge: x + M

$$\frac{x}{1} = 0$$

: 1(x) > 0 on x & (-00,0) and 1(x) >0 on xt (2,00),

.. f(x) is increasing on x & (-0,0) and on x + (2, 00)

: {(x) LO on x E (0,2)

.. flx) is decreasing on x 6 (0,2)

: f'(0) =0 and f'(x) > 0 on x ∈ (-0,0) and f'(x) < U on x & (0,1), if (x) has a local max at x=0.

: f'(2) =0 and f(x) > 0 on x ∈ (0,00) and f'(x) < U on x & (0,2),

- : flx) has a local min at x=2.

+ 0=(x)/f. x=0 and x=Z Test of (-1): 1'(-1) = 3(-1)2-6(-1) 1'1-0>0, . f'(x)>0 on xt (-0,0) Test { (1): f(1) = 3(1)2- 6(1) ·: f'(1) 20, : 11(x)<0 on xt (0,2) Test 1 (3):

 $f'(3) = 3(3)^2 - 6(3)$

1"(x)=6x-6 (Power role) Rule) Set 1"1x) to 0. D= 6x-6 x=1 - - f" (x) = 0 at オー Test 1"(0): 1"(0)=610)-6 · 1"(0) 20 : 1"(x) < D on x + (-0,0) Tes+ 1"(2): 1"(2) = 6(2) -6 · 1"(2) >0, f''(x) > 0 or $x \in (0, \infty)$

$$f''(1)=0,$$

$$f(x) \text{ has an inflection point}$$

$$at x=1.$$

if
$$|(x)| \leq 0$$
 on $x \in (-\infty, 1)$
if $|(x)| \leq 0$ on $x \in (-\infty, 1)$
or $x \in (-\infty, 1)$
if $|(x)| > 0$ on $x \in (1, \infty)$
if $|(x)| \leq 0$ concave up
or $x \in (1, \infty)$

For intercepts:

For
$$x-int$$
 ercept:
 $S+f(x) = 0$:
 $O=x^3-3x^2$
 $=x^2(x-3)$
 $f(x)=0$ if $x=0$

For the min/max/inflection points:

$$f(x) \text{ has a local max at } x=0,$$

$$|ocal max \text{ at } L0, f(0)) = (0, 0^3 - 3(0)^2) = (0, 0)$$

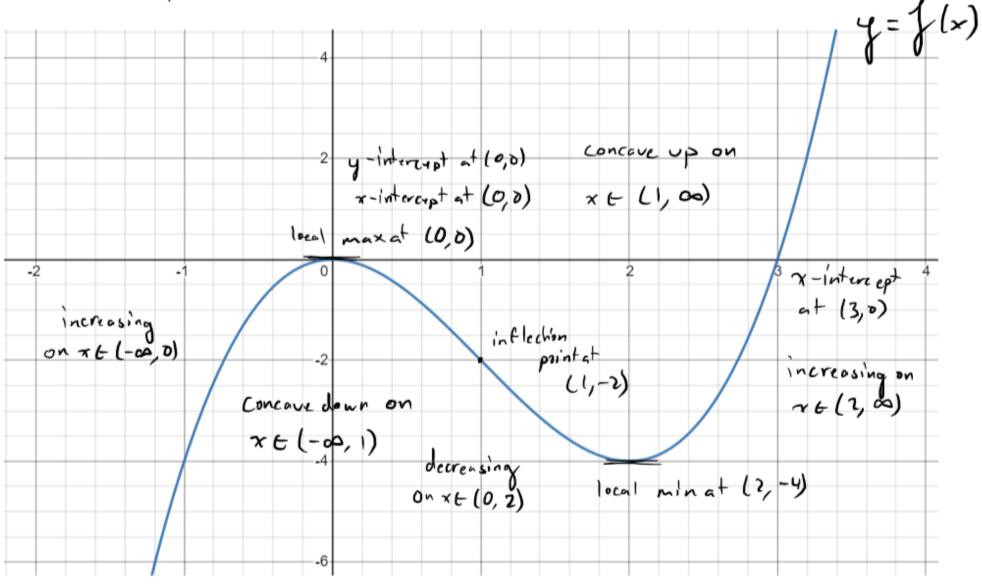
$$f(x) \text{ has a local min at } x=2,$$

$$|ocal min \text{ at } L^2, f(x)) = (2, 2^3 - 3(2)^2) = (2, -4)$$

$$f(x) \text{ has an inflection point at } x=1,$$

$$|offection \text{ at } (1, f(1)) = (1, 1^3 - 3(1)^2) = (0, -2)$$
For y-intercepts: point

. . (0,0) is the y-intercept



b) d=decreasing, i= increasing, POI = infliction point

$$x \mid x=2 \mid z=x=4 \mid x=x=5 \mid x=26 \mid x>6$$
 $g'(x) = \frac{1}{10001} = \frac{1}{100$

For Domain: X & M. Range: X & M. g'(x), Using product Let v= (x-2)3 v=(x-6) 0'=3(x-1)21) v'=1 ... q'(x)= u'v+ v'u $= (3(x-1)^2)(x-6)$ +(1)(2-2)3 $= (x-2)^2 (3(x-6)+1(x-1))$ = (x-2)2(4x-20) $=4(x-2)^{2}(x-5)$ Set q'lx lo 0. 0= 4(x-2)2(x-5) i.g'(x)=0 at x=2 and x=5

For
$$g''(x)$$
, Using product rule,

Let $u=4(x-2)^2$ $v=(x-5)$
 $v'=8(x-2)(1)$ $v'=1$
 $i=g'(x): v'v+ v'v$
 $=8(x-2)(x-5)+(1)(4(x-2)^2)$
 $=4(x-2)(2(x-5)+(x-2))$
 $=4(x-2)(3x-12)$
 $=12(x-2)(x-4)$

Set $g''(x)$ to 0.

 $0=12(x-2)(x-4)$

Test $g''(x)=0$ at $x=2$ and $x=4$

$$q'(\pi) < 0$$
 on $\pi < (2,5)$, $q''(2) = 0$, Test $q'(0)$
 $q(x)$ has an inflection point at $x = 2$. $q'(0) = 4$
 $q'(1) = 0$, $q'(1) =$

Test
$$g'(0)$$

 $g'(0) = 4(0-2)^{2}(0-5)$
 $= -80$
 $g'(x) \ge 0$ on $x \in (-\infty, 2)$
Test $g'(3)$:
 $g'(3) = 4(3-2)^{2}(3-5)$
 $= -8$
 $g'(3) \ge 0$ on $x \in (2,5)$
Test $g'(6)$:
 $g'(6) = 4(6-2)^{2}(6-5)$
 $= 16$
 $g'(6) \ge 0$
 $g'(8) \ge 0$
 $g'(8) \ge 0$
 $g'(8) \ge 0$
 $g'(8) \ge 0$

$$q''(0) = 12(0-2)(0-4)$$

 $= 96$
 $\therefore q''(0) > 0,$
 $\therefore q''(x) > 0 \text{ on } x \in (-\infty, 2)$
Test $q''(3)$:
 $q''(3) = 12(3-2)(3-4)$
 $= -12$
 $\therefore q''(3) < 0$
 $\therefore q''(3) < 0$
 $\therefore q''(3) < 0$
 $\therefore q''(5) = 12(5-2)(5-4)$
 $= 24$
 $\therefore q''(5) > 0$
 $\therefore q''(5) > 0$
 $\therefore q''(5) > 0$
 $\therefore q''(5) > 0$
 $\therefore q''(5) > 0$

For intercepts:

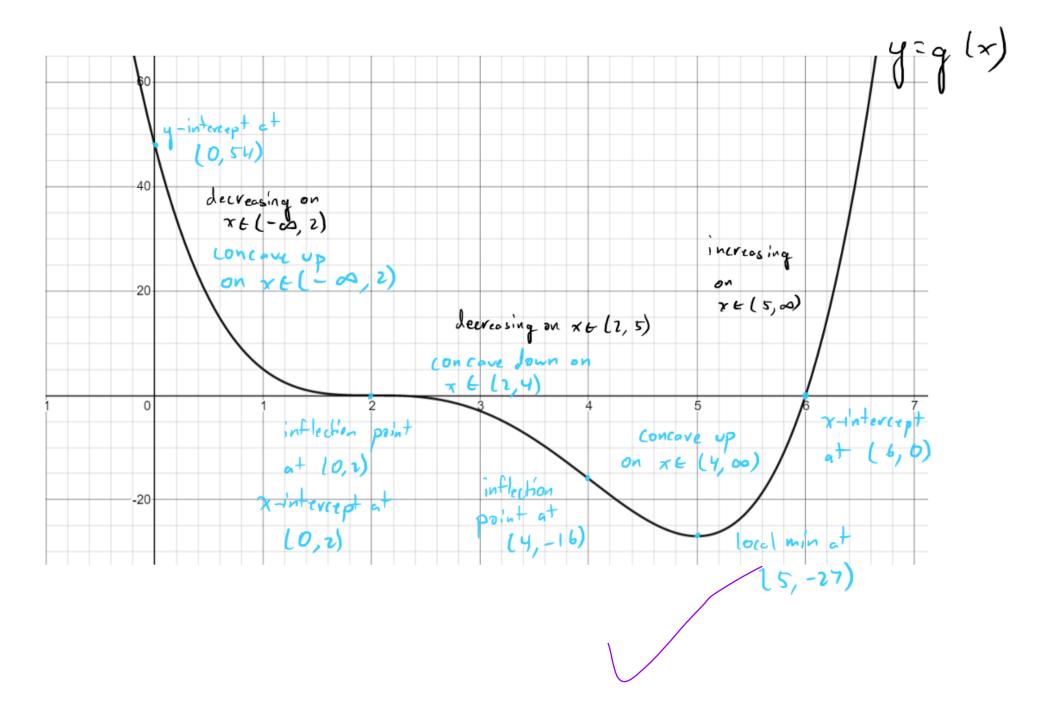
For x-int ercept: Set q(x) to 0: $0 = (x-2)^3(x-6)$ q(x) = 0 if x = 2and

if x= 6 -. (2,0) and (6,0) are the x-intercepts. For y-intercepts: Set x=0: $q(x)=(0-2)^3(0-6)$ =48(0,48) is the y-intercept For the min/max/inflection points:

if g(x) has a local min at x=5,

local min at $(5,q(5)) = (5,(5-2)^3(5-6)) = (5,-27)$ if g(x) has an inflection point at x=2,

inflection point at $(2, g(7)) = (2,(2-2)^3(2-6)) = (2,0)$ if g(x) has an inflection point at x=4inflection at $(4,g(4)) = (4,(4-2)^3(4-6)) = (4,-16)$ point



4. i=increasing, d=decreasing, DoI = point of inflection

$$\frac{1}{v(\pm)} + \frac{1}{v(\pm)} + \frac{1}{v(\pm)} = \frac{$$

Let s(t) be the displacement function, let a(t) be the acceleration function, s'(t) = v(t), v'(t) = a(t). v'(t) = a(t)

: U(5) LO on & & (10.5, 12), S(x) is decreasing on & & (10.5, 12)

+ t (10.5,12), there is a local max at t= 10.5.

· v(+) is limar on tt (0,3) and tt (3,12), s(t) is parabolic on

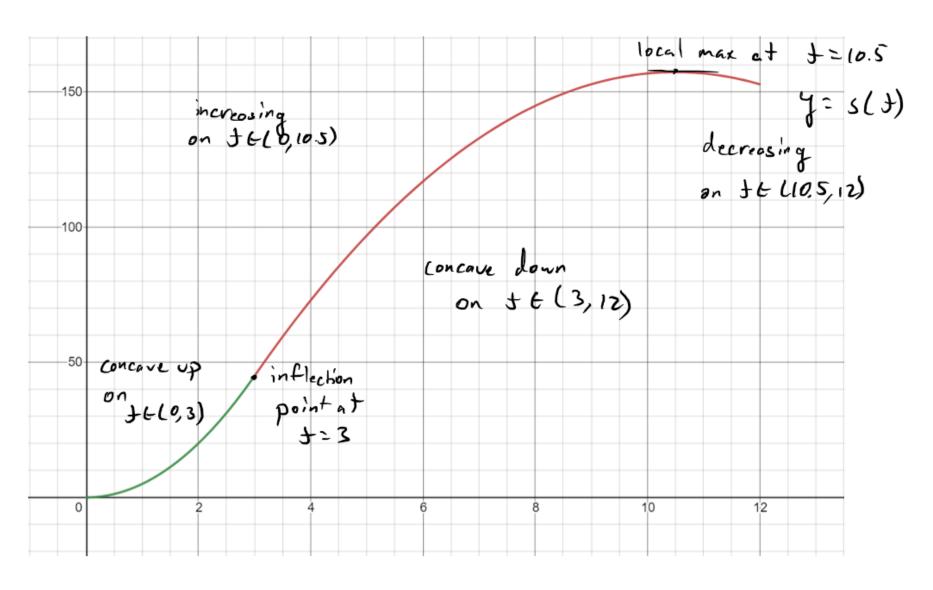
tt(0,3) and tt(3,12) (Power Rule).

: (3) is not differentiable, s(+) has an inflection point at +=3.

· alt >0 on t = (0,3), s(t) is concave up on t = (0,3)

Determine points with information

: a(+) <0 on f \(\)(3,12), \(\)(1) is concore down on f \(\)(3,12)



Critical points are points where the derivative is O or the Gunction is non-differentiable.

h(x) is a polynomial, h(x) is continuous on x e (-00, 00). ... all points on the h'(x) = 3x2+2bx

deniver are differentiable.

Sub x=2 , h'(x)=0

0=3(2)2+26(2)

0=12+46

· - b = -3

Sub b=-3, (2,-4) into h:

 $-4 = 2^3 + (-3)(2)^2 + d$

i - d= 0.

. The equation of h(x) is $h(x) = x^3 - 3x^2$.

