1.0) $f(x) = x^{3} \cos x$ Using the product rule,

Let $0 = x^{3}$ $g = \cos x$ $0' = 3x^{2}$ $g' = -\sin x$ f'(x) = 0'g + g'0 $= 3x^{2} \cos x - x^{3} \sin x$ I the derivative of $f(x) = x^{3} \cos x$ is $f'(x) = 3x^{2} \cos x - x^{3} \sin x$.

b) $h(x) = (x^2 - 1)^3 (x^2 + 1)^2$ For 1/2:

Use chain rule,

Let $f = (x^2 - 1)^3 (x^2 + 1)^2$ Use chain rule, $f' = b \times (x^2 - 1)^2 (x^2 + 1)^2$ Let $u = x^2 - 1$, $\frac{du}{dx} = \frac{1}{4}$ h'(x) = f'g + g'f $= b \times (x^2 - 1)^2 (x^2 + 1)^2 + 4y(x^2 + 1) = b \times (x^2 - 1)^2 (2x)$ $= b \times (x^2 - 1)^2 (x^2 + 1)^2 + 4y(x^2 + 1) = b \times (x^2 - 1)^2$ For g':

 $\begin{array}{l}
-1. \text{ The drive hive of} \\
h(a) = (x^2 - b)^3 (x^2 + 1)^2 \text{ is} \\
h'(x) = 6x (x^2 - 1)^2 (x^2 + 1)^2 + 4x (x^2 + 1)(x^2 - 1)^3
\end{array}$

5 (~ *

For 1/: 11 25.5 14.5 11.5 Use chain rule, Lut u= x2-1, du = dx (x2-1) .- 1(0) = U3 1'(v) = 35° $= 6x (x^2-)^2$ For g': Use chain rule, $| U + u = x^2 + 1$ i.glu)= v2 g'(v) = 20 :. of 12) = 2(x2+1)(1x) = 4x (x2+1)

Use Qualient rule:

... The dribable of
$$g(x) = \frac{x^2}{c^2}$$
 is $g'(x) = \frac{2xe^2 - x^2e^2}{c^2x}$.

2. The languant to the corne has slope
$$f'(1)$$

For $f'(x)$:

 $f(x) = (2x^2 - 1)^{-5}$

Use chain rule

Let $v = 2x^2 - 1$
 $f(v) = v^{-5}$
 $f(v) = -5v^{-6}$
 $f'(v) = -5(2x^2 - 1)^{-6}(14x)$
 $= -20x(2x^2 - 1)^{-6}$

At $x = 1$,

 $f'(1) = -70(1)(2(1)^2 - 1)^{-6}$

= -20 -. -20 is the slope of the languat line at x=1

=-20(1)-6

Find a point, Sub x=1 into f $f(1) = (2(1)^{2}-1)^{-5}$ $= (1)^{-5}$

i. (1,1) is appoint on the cone

Sub (1,1), m= -20

y= mx + b

1=-20(1)+6

6=21

:. The slope of the hongest to the come is y = -roxx21

```
Fory :
 y=ekx
Use chain whe
 Leto=kx do = de (kg)
 y = e V
y'= e'
iny'= Kekx
For y":
 Use chain role,
 Let u= Kx du = de lky
 y'= Ke
y"= ke"
·y"= k2enx
Solve:
 y +y'=y"
```

the ker = h2 mx

Use quadrabic bornula,

$$k = \frac{1 \pm \sqrt{1 + 4}}{2}$$

$$= \frac{1 \pm \sqrt{5}}{2}$$

.. K= 1- \square and K= 1+ \square sahishies He equation y+y'=y".

4.

Find T':

T=A+ (To-A)eht

7'= \$(A) - \$ (6-A) = K+

= 0 + (To-A) & (e 4.7)

= (16-A) Kent

1. T'= (To-A)Keks

SUL To= 88, A= 27, K= 0.033, J= 4,

T'= (68-27) (0.000) (0.083)4

2 1,297 °C/min

i. The temperature of the tea is cooling at 2.297 oc/min.

5. Let: (290 + 10d) describes the price of the ipods, d = # of price increases. (30-d) describes the # of ipols sold permeck, d= # of price increases -110 (30-d) describes the total cost of the isods to the store, d= # of price increases. Revenue is given as the product, Let R be remove Lot R= (200 + 10 d) (30-d) - 11 0 (30-d) = (290 + 18d - 11 d) (30-d) = (100 + 101)(30-1) =5400-160 1+300d-1012 =-10d2+120 d+5400 For R': R'= 1/1 (-1022+120 d +5400)

```
= -201+120
```

Setn' 60:

0=-201+120

201 = 120 1=6 : 30-6=\$24 is the best price.

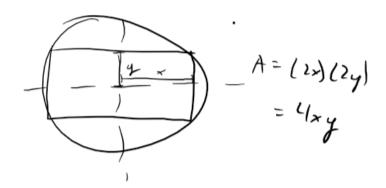
SJI d=6 , to R.

K(6)=(290+10(6)))(30-6) -120(30-6) = 5520

: Aprice of 30-6 = 824 yields the highert profit of \$5520.



Recorne



Total Area is giverby

$$A = (2-)(2y)$$

= 4xy
= 4x $\sqrt{25-x^2}$

= 4x J25-x2 (Only consider top half of

1. g'= -x(25-x)=

circle)

For A':

For 9 !:

Use chainne

Let $v = 2x - x^2$ $g = \sqrt{v}$ $g' = \frac{1}{2}v^{-\frac{1}{2}}$ = -2x $g' = \frac{1}{2}(-1x)(25 - x^2)^{-\frac{1}{2}}$

$$4 = \sqrt{2r - \frac{r}{2}}$$

$$= \frac{5}{\sqrt{2}}$$

.. The area of the largest reclarge in the circle is 25 g. units

$$L^{2} = \frac{1}{\ln 16} - \frac{1}{\ln \left(\frac{20.4n}{r^{2} + \ln n}\right)}$$

$$= -\frac{1}{\ln \left(\frac{10.4n}{r^{2} + \ln n}\right)}$$

$$=-\left(\frac{20.4(n^2+49)-2n(20.4n)}{(r^2+49)^2}\right)$$

$$= - \frac{20.4n^2 + 949.6 - 40.8n^2}{(n^2 + 49)^2}$$

$$= -\frac{-20.4n^2+999.6}{(n^2+49)^2}$$

i. The instrumencous rate of change in the pH of your mouth is changing at -0.159 pH lands. This value is the value at which the pH of your mouth changes. This most closely makes the rate instrumens at which the concentration of Ht long abanque in your mouth on a log scale.

Let b be the length of the base. Let h be the allitude, h'=1 Let A be the over, A = 2 A+ A=100 cm2, h= 101m, A= 64 100= 10 6 b=20cm U se product vde Let f=1, gsh 7'=b',g'=h' A===119+94) = 1 (b'h+ h'b) Sub h=10, h'=1, 4 =2, b= 20:

2== (6'(10) + (1)(20))

$$\frac{-16}{10} = 6'$$
 $\frac{1}{10} = \frac{8}{10}$ (m/min)

.. The base of the brimghe is changing at - \$ cu/min (it's shrinking by - \$ cu/min) when the allitude is 10 cm and the area is 100 cm².

S= Yerz

$$\frac{dV}{\lambda^{\frac{1}{2}}} = \frac{dV}{dr} \left(\frac{4}{3} \pi v^{3} \right) \left(\frac{dr}{dr} \right) \left(\frac{dr}{dr} \right) \left(\frac{dr}{dr} \right) = 4 \pi v^{2}$$

$$= (4ur^{2})(r')$$

$$\frac{dS}{dt} = \frac{dS}{dr} \left(4ur^{2} \right) \left(\frac{dr}{dt} \right) \quad Chairrell \qquad r = \frac{5\sqrt{3}}{2\sqrt{r}}$$

$$\frac{dV}{U} = \frac{1}{2} \left(\frac{5\sqrt{3}}{2\sqrt{n}} \right)$$

$$= \frac{5\sqrt{3}}{4\sqrt{n}} c_{m_{Ain}}^{3/3} \simeq 1.222 cm$$

... The balloon's volve is changing at a vote of 450 cm3/min or about 1.222 cm3/min with respect to its surface over when its our face area measures 75 cm2.